

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

**BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING
(Autonomous Institution under VTU)
BENGALURU-560019
Aug-2025 to Jan-2026**

**B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019**
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Sanjana Srinivas (1BM23CS301)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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Github Link:
<https://github.com/sanjanasrinivas22/BIS>

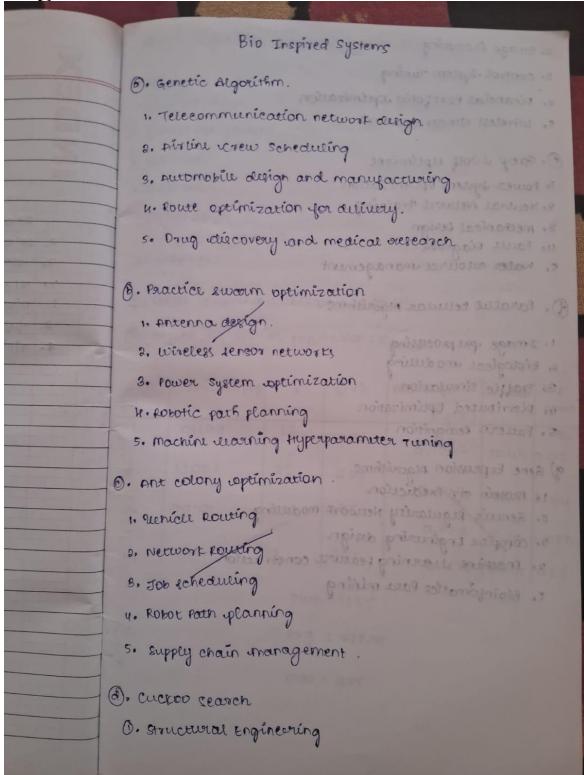
Program 1

Genetic Algorithm for Optimization Problems:

Problem Statement:

Genetic Algorithms (GA) are inspired by the principle of natural selection, where only the fittest individuals survive and reproduce. Implement a Genetic Algorithm in Python to solve an optimization problem in which the goal is to find the maximum value of a given mathematical function within a defined search space. The GA should include initialization of a population, fitness evaluation, selection, crossover, mutation, and generation-wise evolution until the optimal or near-optimal solution is found.

Algorithm:



Genetic algorithm for optimization problems

steps:-

- initialization
- fitness assignment
- selection
- crossover
- termination

$f(x) = x^2$

Iterations :-

1	0.100	12	144	0.1207	12.47	0.49
2	11001	25	625	0.5411	54.11	2.16
3.	00101	5	25	0.0216	2.16	0.086
4.	10011	19	361	0.3125	31.25	1.25

Sum : 1155

Avg : 288.75

Max = 625

④. select encoding technique : 0 to 31

⑤. select the initial population :

sn	Initial pop	x	f(x)	Prob: f(x)	% Prob	Exp count
1	01100	12	144	0.1207	12.47	0.49
2	11001	25	625	0.5411	54.11	2.16
3.	00101	5	25	0.0216	2.16	0.086
4.	10011	19	361	0.3125	31.25	1.25

⑥. selecting mating pool (Eliminate 3rd row)

sr	mating pool	Crossover point	offspring after crossover	x	fitness f(x)
1	01100	4	001101	13	169
2	11001		11000	24	576
3	111001	2	11011	27	729
4	101011		10001	17	289

Let's choose 1 and 2 max $\rightarrow 729$

⑦. mutation

srno	offspring after crossover	mutation chromosome for flipping	offspring	x
1	01101	10000	11101	29
2	11000	11000	11000	24
3	11011	11011	11011	27
4	10001	10100	10100	20

$f(y)$ Sum $\rightarrow 2546$
 841 Avg $\rightarrow 630.5$
 576 Max $\rightarrow 841$
 400

Actual count

1			
2	✓		
0			
4			

Iteration - 2

sn	Initial pop	x	f(x)	Prob	% Prob	EXP count
1	11101	29	841	0.33	33	
2	11000	24	576	0.22	22	
3	11011	27	729	0.28	88	
4	10100	20	400	0.157	15.7	

Algorithm

Start

⑧. Input

- fitness function $f(x)$ [we provide formula in terms of x , using numpy functions]
- population size (pop-size=4)

• no. of generation (generations = 5)
 • mutation rate (mutation - rate = 0.1)
 • crossover rate (crossover - rate = 0.7)
 • chromosome length in bit (chrom - length = 5)

a) Define Helper functions:-

- decode (binary - vector); convert binary chromosome to decimal integer.
- encode (value); convert decimal integer to binary chromosome.
- fitness (x); evaluate $f(x)$ safely using numpy.
- printable (title, population, bin_population, fitness - value, extra_info)
- Prints structured table with probabilities, fitness, expected count, actual count.

b) Initialize population:-

- generate random binary matrix of size [pop-size, chrom-length]
- decode to integer value

c) For each generation $g = 1 \rightarrow \text{generations}$

PRINT "Generation g"

- Fitness evaluation
 - decode population to integers

d) Selection (roulette wheel)

- evaluate $f(x)$ for each chromosome
- compute selection prob = fitness / total_fitness.
- form mating pool.

e) Crossover

- initialize empty offspring population
- for every pair of parents ($i, i+1$):
 - if (random < crossover_rate):
 - select random crossover point
 - split parents 1 and parent 2 at that point.
 - swap tails to produce child 1 and child 2

f) update:

- replace old population with mutated offspring.
- decode again for next iteration.

END LOOP

Output:-

```

Gen 1: Best individual = 11101 (x=29), fitness = 841
Gen 2: Best individual = 110111 (x=27), fitness = 729
Gen 3: Best individual = 11100 (x=28), fitness = 784
Gen 4: Best individual = 11100 (x=28), fitness = 784
Gen 5: Best individual = 11011 (x=27), fitness = 729
  
```

Code:

```
import random
```

```
POP = 6
BITS = 5
GEN = 5
CROSS = 0.7
MUT = 0.1
```

```
def fit(s):
    return int(s, 2)**2
```

```
def init_pop():
    return [".join(random.choice('01') for _ in range(BITS)) for _ in range(POP)]
```

```
def select(p):
    a, b = random.sample(p, 2)
    return a if fit(a) > fit(b) else b
```

```
def cross(a, b):
    if random.random() < CROSS:
```

```

pt = random.randint(1, BITS - 1)
    return a[:pt] + b[pt:], b[:pt] + a[pt:]
return a, b

def mutate(s):
    return ''.join('1' if c == '0' and random.random() < MUT else
                  '0' if c == '1' and random.random() < MUT else c
                  for c in s)

def run():
    pop = init_pop()
    best, best_fit = None, -1
    for g in range(1, GEN + 1):
        for x in pop:
            f = fit(x)
            if f > best_fit:
                best, best_fit = x, f
        print(f"Gen {g}: {best} (x={int(best,2)}), Fit={best_fit}")
        nxt = []
        while len(nxt) < POP:
            p1, p2 = select(pop), select(pop)
            c1, c2 = cross(p1, p2)
            nxt.extend([mutate(c1), mutate(c2)])
        pop = nxt[:POP]
        print(f"\nBest: {best} (x={int(best,2)}), Fit={best_fit}")

if __name__ == "__main__":
    run()

```

Output:

Gen 1: 11110 (x=30), Fit=900
 Gen 2: 11111 (x=31), Fit=961
 Gen 3: 11111 (x=31), Fit=961
 Gen 4: 11111 (x=31), Fit=961
 Gen 5: 11111 (x=31), Fit=961

Best: 11111 (x=31), Fit=961

Program 2

Particle Swarm Optimization for Function Optimization:

Problem Statement:

Particle Swarm Optimization (PSO) is modeled after the collective movement of birds or fish. Implement a PSO algorithm in Python to find the minimum or maximum of a mathematical function. Each particle should update its velocity and position based on personal best and global best positions. Evaluate how swarm behavior improves the algorithm's ability to converge to optimal solutions over time.

Algorithm:

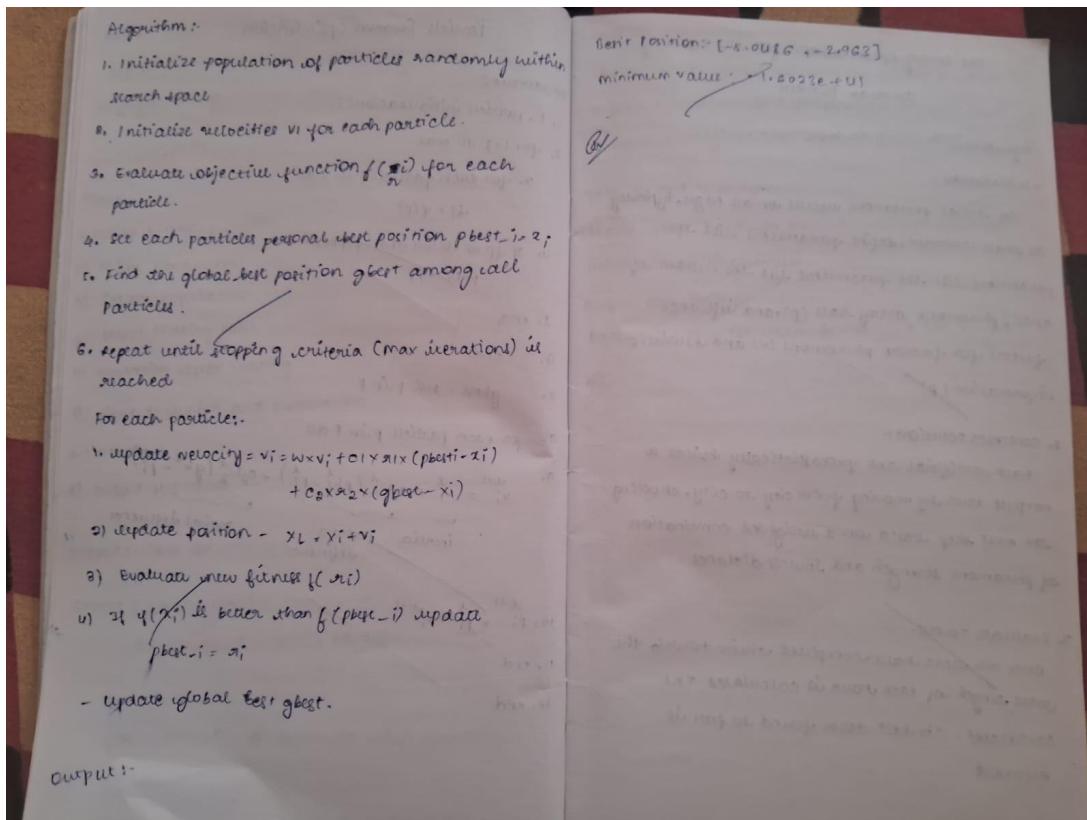
Particle Swarm Optimization

Pseudocode:-

1. $P = \text{particle initialization}()$
2. $\text{for } i = 1 \text{ to max}$
 3. $\text{for each particle } p \text{ in } P \text{ do}$
 4. $f_p = f(p)$
 5. $\text{if } f_p \text{ is better than } f(p_{best})$
 6. $p_{best} \leftarrow p$
 7. end
 8. $\text{if (end of run) condition satisfied then break}$
 9. $g_{best} = \text{best } p \text{ in } P$
 10. $\text{for each particle } p \text{ in } P \text{ do}$
 11. $v_i^{t+1} = (c_1 v_i^t + c_2 p_{best}^t - p_i^t) + c_3 U_2^t (g_{best}^t - p_i^t)$

$$v_i^{t+1} = v_i^t + c_1 v_i^t + c_2 p_{best}^t - p_i^t + c_3 U_2^t (g_{best}^t - p_i^t)$$

$\underbrace{v_i^t}_{\text{inertia influence}}$ $\underbrace{c_1 v_i^t}_{\text{personal influence}}$ $\underbrace{c_2 p_{best}^t - p_i^t}_{\text{social influence}}$
 12. $p_i^{t+1} = p_i^t + v_i^{t+1}$
 13. end
 14. end



Code:

```
import random
```

```
# Objective (fitness) function: De Jong function
```

```
def fitness_function(position):
```

```
    x, y = position
```

```
    return x**2 + y**2 # minimize this function
```

```
# PSO parameters
```

```
num_particles = 10
```

```
num_iterations = 50
```

```
W = 0.3 # inertia weight (from PDF)
```

```
C1 = 2 # cognitive coefficient
```

```
C2 = 2 # social coefficient
```

```
# Initialize particles and velocities
```

```
particles = [[random.uniform(-10, 10), random.uniform(-10, 10)] for _ in range(num_particles)]
```

```
velocities = [[0.0, 0.0] for _ in range(num_particles)]
```

```
# Initialize personal bests
```

```
pbest_positions = [p[:] for p in particles]
```

```
pbest_values = [fitness_function(p) for p in particles]
```

```
# Initialize global best
```

```

gbest_index = pbest_values.index(min(pbest_values))
gbest_position = pbest_positions[gbest_index][:]
gbest_value = pbest_values[gbest_index]

# PSO main loop
for iteration in range(num_iterations):
    for i in range(num_particles):
        r1, r2 = random.random(), random.random()

        # Update velocity
        velocities[i][0] = (W * velocities[i][0] +
                            C1 * r1 * (pbest_positions[i][0] - particles[i][0]) +
                            C2 * r2 * (gbest_position[0] - particles[i][0]))
        velocities[i][1] = (W * velocities[i][1] +
                            C1 * r1 * (pbest_positions[i][1] - particles[i][1]) +
                            C2 * r2 * (gbest_position[1] - particles[i][1]))

        # Update position
        particles[i][0] +== velocities[i][0]
        particles[i][1] +== velocities[i][1]

        # Evaluate fitness
        current_value = fitness_function(particles[i])

        # Update personal best
        if current_value < pbest_values[i]:
            pbest_positions[i] = particles[i][:]
            pbest_values[i] = current_value

        # Update global best
        if current_value < gbest_value:
            gbest_value = current_value
            gbest_position = particles[i][:]

    print(f'Iteration {iteration+1}/{num_iterations} | Best Value: {gbest_value:.6f} at {gbest_position}')

print("\nOptimal Solution Found:")
print(f'Best Position: {gbest_position}')
print(f'Minimum Value: {gbest_value}')

```

Output:

```

Iteration 1/50 | Best Value: -271.091815 at [-84.43244266546853, -51.11346474300606]
Iteration 2/50 | Best Value: -3147.519112 at [-990.3734271752983, -583.3861286613839]
Iteration 3/50 | Best Value: -8275.394058 at [-2605.963881015693, -1531.733147860558]
Iteration 4/50 | Best Value: -35826.154841 at [-11286.658966206636, -6626.41845422665]
Iteration 5/50 | Best Value: -69743.934634 at [-21972.964707857907, -12899.00260912271]
Iteration 6/50 | Best Value: -128492.226042 at [-40482.80512141413, -23763.307899605523]

```

Iteration 7/50 | Best Value: -2150898.767751 at [-677683.970780463, -397765.41309513245]
 Iteration 8/50 | Best Value: -15310298.854777 at [-4823827.139516395, -2831322.2878723536]
 Iteration 9/50 | Best Value: -49653453.407440 at [-15644353.385262355, -9182373.318457406]
 Iteration 10/50 | Best Value: -269516199.282408 at [-84916691.8396995, -49841407.80150427]
 Iteration 11/50 | Best Value: -2071103939.832669 at [-652544441.5664799, -383007528.3498548]
 Iteration 12/50 | Best Value: -16514265252.244366 at [-5203163304.138547, -3053969321.9836354]
 Iteration 13/50 | Best Value: -62522298877.396645 at [-19698952772.636093, -11562196666.06223]
 Iteration 14/50 | Best Value: -303452004697.334717 at [-95608875824.94115, -56117126523.72621]
 Iteration 15/50 | Best Value: -5479784825693.140625 at [-1726520368443.3489, -
 1013372044403.2217]
 Iteration 16/50 | Best Value: -97550626289445.703125 at [-30735357062486.24, -
 18039956082236.613]
 Iteration 17/50 | Best Value: -418935157142521.875000 at [-131994248838541.64, -
 77473329732719.31]
 Iteration 18/50 | Best Value: -5320521856026541.000000 at [-1676341251962195.2, -
 983919676051075.1]
 Iteration 19/50 | Best Value: -24428360527250232.000000 at [-7696663894585885.0, -
 4517516369039232.0]
 Iteration 20/50 | Best Value: -125188235202357312.000000 at [-3.9443161518517544e+16, -
 2.315095608266111e+16]
 Iteration 21/50 | Best Value: -667707656673289728.000000 at [-2.1037520743658112e+17, -
 1.2347862090006374e+17]
 Iteration 22/50 | Best Value: -1030904195610660736.000000 at [-3.248078434196429e+17, -
 1.906442543856875e+17]
 Iteration 23/50 | Best Value: -9356678590567034880.000000 at [-2.948016515513922e+18, -
 1.730322779769596e+18]
 Iteration 24/50 | Best Value: -122704432708514906112.000000 at [-3.866058779834038e+19, -
 2.269162855591707e+19]
 Iteration 25/50 | Best Value: -536066327314262261760.000000 at [-1.6889886416816262e+20, -
 9.91342994889685e+19]
 Iteration 26/50 | Best Value: -2046867967951136882688.000000 at [-6.449083952375761e+20, -
 3.7852558873799236e+20]
 Iteration 27/50 | Best Value: -18438479551870623809536.000000 at [-5.809427107465299e+21, -
 3.409812668470013e+21]
 Iteration 28/50 | Best Value: -91092058698079191171072.000000 at [-2.870045079295888e+22, -
 1.684557855608071e+22]
 Iteration 29/50 | Best Value: -586438393873119672532992.000000 at [-1.8476963312733012e+23, -
 1.0844956380922973e+23]
 Iteration 30/50 | Best Value: -3816864039219899427454976.000000 at [-1.2025825314161544e+24, -
 7.058494881937953e+23]
 Iteration 31/50 | Best Value: -40302670879267569381933056.000000 at [-1.2698196076883996e+25, -
 7.453139362749791e+24]
 Iteration 32/50 | Best Value: -497864892681195143961772032.000000 at [-
 1.5686270634522062e+26, -9.206973999537697e+25]
 Iteration 33/50 | Best Value: -8135214148890464247835787264.000000 at [-
 2.5631686966729733e+27, -1.504438377722588e+27]
 Iteration 34/50 | Best Value: -39795166729975694384902963200.000000 at [-
 1.253829632193114e+28, -7.359287043056707e+27]

Iteration 35/50 | Best Value: -257532895645339190122109730816.000000 at [-8.114110389727232e+28, -4.762534392539727e+28]
 Iteration 36/50 | Best Value: -1473074887175449488560115154944.000000 at [-4.641229314385222e+29, -2.7241451214920254e+29]
 Iteration 37/50 | Best Value: -11593580667625126840015144353792.000000 at [-3.6527991157629925e+30, -2.143991218049571e+30]
 Iteration 38/50 | Best Value: -42386731026256574797676353159168.000000 at [-1.3354822642943654e+31, -7.838542870184634e+30]
 Iteration 39/50 | Best Value: -126591157955093254888733420814336.000000 at [-3.988518155853745e+31, -2.3410397419009176e+31]
 Iteration 40/50 | Best Value: -717687757570118492131965238509568.000000 at [-2.2612247944819503e+32, -1.3272139933686418e+32]
 Iteration 41/50 | Best Value: -3311163212620019616185216680329216.000000 at [-1.043250950845624e+33, -6.1233065546438565e+32]
 Iteration 42/50 | Best Value: -12111965937081074979620964096016384.000000 at [-3.8161271943074396e+33, -2.2398557742330984e+33]
 Iteration 43/50 | Best Value: -130305771767680050386422002735906816.000000 at [-4.105554802589714e+34, -2.4097337857942887e+34]
 Iteration 44/50 | Best Value: -735450748758796362643242520135335936.000000 at [-2.3171907987454107e+35, -1.360062945048571e+35]
 Iteration 45/50 | Best Value: -2701395388393203478038978337378926592.000000 at [-8.511308946686484e+35, -4.995667995279534e+35]
 Iteration 46/50 | Best Value: -14748635214493649518168345315517661184.000000 at [-4.6468647792872993e+36, -2.727452827959526e+36]
 Iteration 47/50 | Best Value: -43310775725245935501677583787809046528.000000 at [-1.3645962175773178e+37, -8.009425686849791e+36]
 Iteration 48/50 | Best Value: -292179141730826441145694158762167762944.000000 at [-9.20571255038653e+37, -5.4032445361547915e+37]
 Iteration 49/50 | Best Value: -15396320896619782540270998692308851884032.000000 at [-4.8509316465295593e+39, -2.8472288017803326e+39]
 Iteration 50/50 | Best Value: -160237362078692376583522632064238981480448.000000 at [-5.0486119111390975e+40, -2.9632561927955213e+40]

Optimal Solution Found:

Best Position: [-5.0486119111390975e+40, -2.9632561927955213e+40]
 Minimum Value: -1.6023736207869238e+41

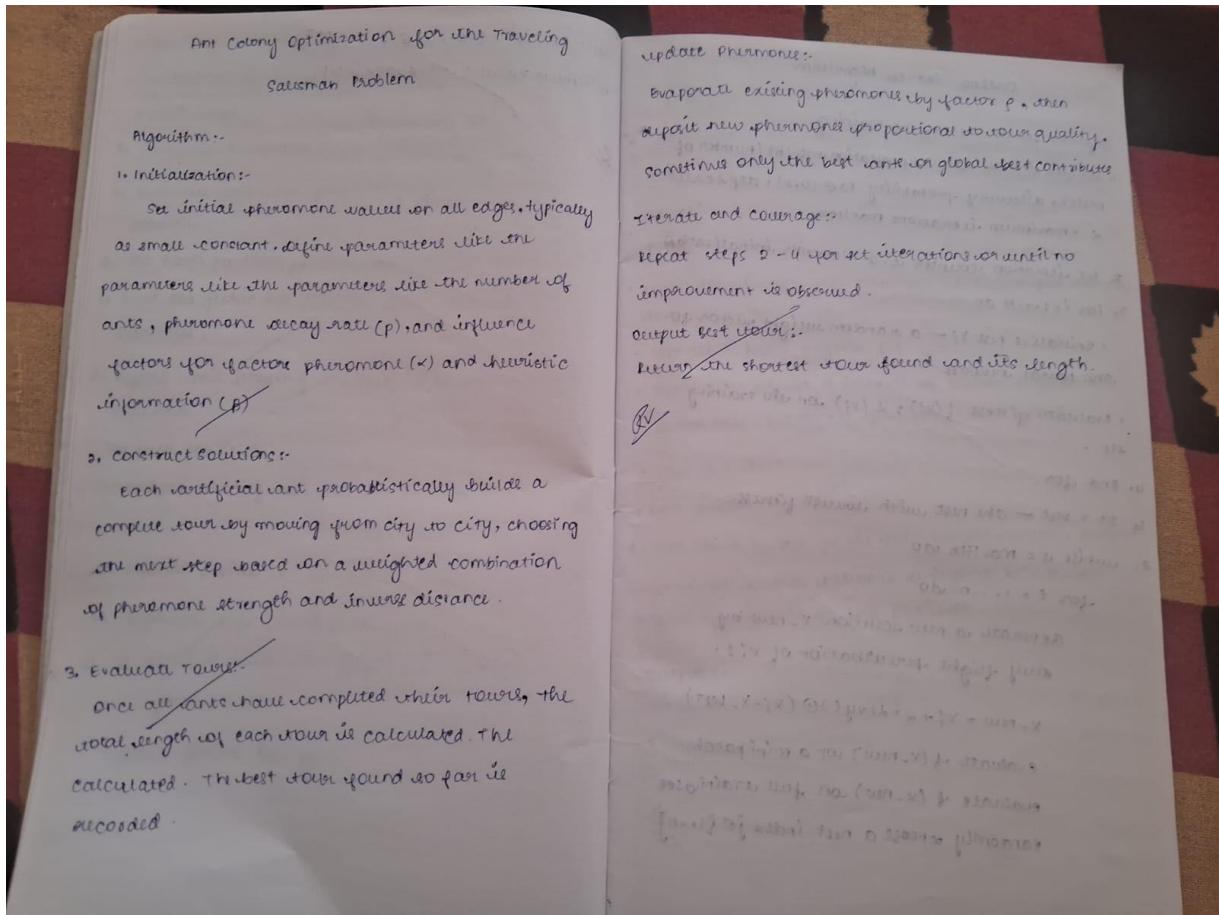
Program 3:

Ant Colony Optimization for the Traveling Salesman Problem:

Problem Statement:

Ant Colony Optimization (ACO) simulates the foraging behavior of ants to solve combinatorial optimization problems. Implement the ACO algorithm in Python to solve the Traveling Salesman Problem (TSP). Model pheromone deposition, evaporation, and probabilistic state transitions as ants traverse between cities. The objective is to identify the shortest possible Hamiltonian cycle that visits all cities exactly once and returns to the starting city.

Algorithm:



Code:

```

import random
import math

def dist(a, b):
    return math.sqrt((a[0]-b[0])**2 + (a[1]-b[1])**2)

def path_cost(route, pts):
    s = 0
    for i in range(len(route)):
        x = route[i]
        y = route[(i+1) % len(route)]
        s += dist(pts[x], pts[y])
    return s

def aco_tsp(pts, m=5, a=1, b=2, evap=0.5, it=20):
    n = len(pts)
    ph = [[1]*n for _ in range(n)]
    d = [[dist(pts[i], pts[j]) for j in range(n)] for i in range(n)]

    best_r = None

```

```

best_c = float('inf')

for _ in range(it):
    routes = []
    for _ in range(m):
        r = [random.randrange(n)]
        while len(r) < n:
            i = r[-1]
            opt = []
            for j in range(n):
                if j not in r:
                    t = ph[i][j]**a
                    h = (1/d[i][j])**b
                    opt.append((j, t*h))
            nxt = random.choices([x for x,_ in opt], weights=[w for _,w in opt])[0]
            r.append(nxt)
        routes.append(r)

    c = path_cost(r, pts)
    if c < best_c:
        best_c = c
        best_r = r[:]

for i in range(n):
    for j in range(n):
        ph[i][j] *= (1-evap)

for r in routes:
    c = path_cost(r, pts)
    add = 1/c
    for i in range(n):
        x = r[i]
        y = r[(i+1) % n]
        ph[x][y] += add

return best_r, best_c

```

```

cities = [(0,0), (1,5), (5,1), (3,4), (6,3)]
route, cost = aco_tsp(cities)
print("Best Route:", route)
print("Best Distance:", cost)

```

Output:

```

Best Route: [4, 2, 0, 1, 3]
Best Distance: 17.832452642353527

```

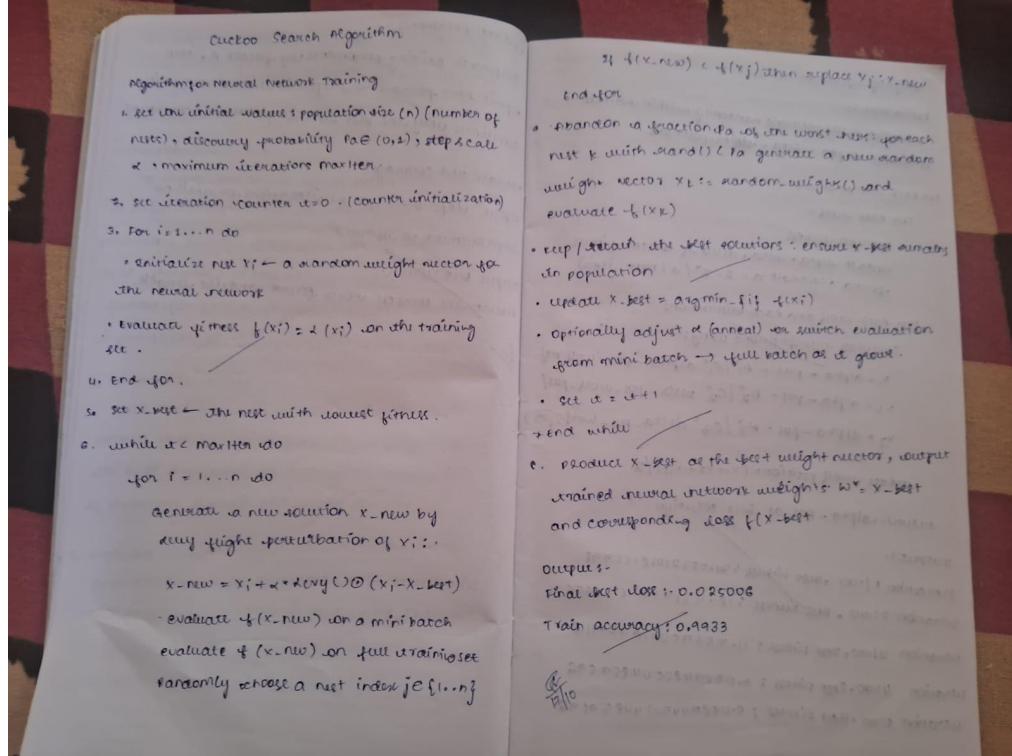
Program 4:

Cuckoo Search:

Problem Statement:

Cuckoo Search (CS) is inspired by the brood parasitism behavior of cuckoo birds. Implement the Cuckoo Search algorithm in Python using Lévy flight-based random walks to explore the global search space. Apply discovery probability to replace inferior solutions with new randomly generated nests. The objective is to apply CS to a continuous optimization problem and analyze its capability in avoiding local minima and locating optimal solutions.

Algorithm:



Code:

```

import numpy as np
import math

weights = np.array([12, 7, 11, 8, 9])
values = np.array([24, 13, 23, 15, 16])
capacity = 26
n = len(weights)

def fitness(sol):
    w = np.sum(sol * weights)
    v = np.sum(sol * values)
    return v if w <= capacity else 0

def levy_flight(l=1.5, d=n):
    a = (math.gamma(1+l) * math.sin(math.pi*l/2)) /
        (math.gamma((1+l)/2) * 1 * 2**((l-1)/2))) ** (1/l)
    u = np.random.normal(0, a, d)
    v = np.random.normal(0, 1, d)
    return u / (np.abs(v) ** (1/l))
  
```

```

def sig(x):
    return 1 / (1 + np.exp(-x))

def cuckoo(pop=20, pa=0.25, it=300):
    nests = np.random.randint(0, 2, (pop, n))
    fit_vals = np.array([fitness(s) for s in nests])

    best_idx = np.argmax(fit_vals)
    best_sol = nests[best_idx].copy()
    best_fit = fit_vals[best_idx]

    for _ in range(it):
        for i in range(pop):
            step = levy_flight()
            y = nests[i] + step
            p = sig(y)
            new = (np.random.rand(n) < p).astype(int)

            f = fitness(new)
            if f > fit_vals[i]:
                nests[i] = new
                fit_vals[i] = f
                if f > best_fit:
                    best_fit = f
                    best_sol = new.copy()

    idx = np.where(np.random.rand(pop) < pa)[0]
    for j in idx:
        nests[j] = np.random.randint(0, 2, n)
        fit_vals[j] = fitness(nests[j])
        if fit_vals[j] > best_fit:
            best_fit = fit_vals[j]
            best_sol = nests[j].copy()

    return best_sol, best_fit

sol, val = cuckoo()
print("Best solution:", sol)
print("Total value:", val)
print("Total weight:", np.sum(sol * weights))

```

Output:

Best solution: [0 1 1 1 0]
 Total value: 51
 Total weight: 26

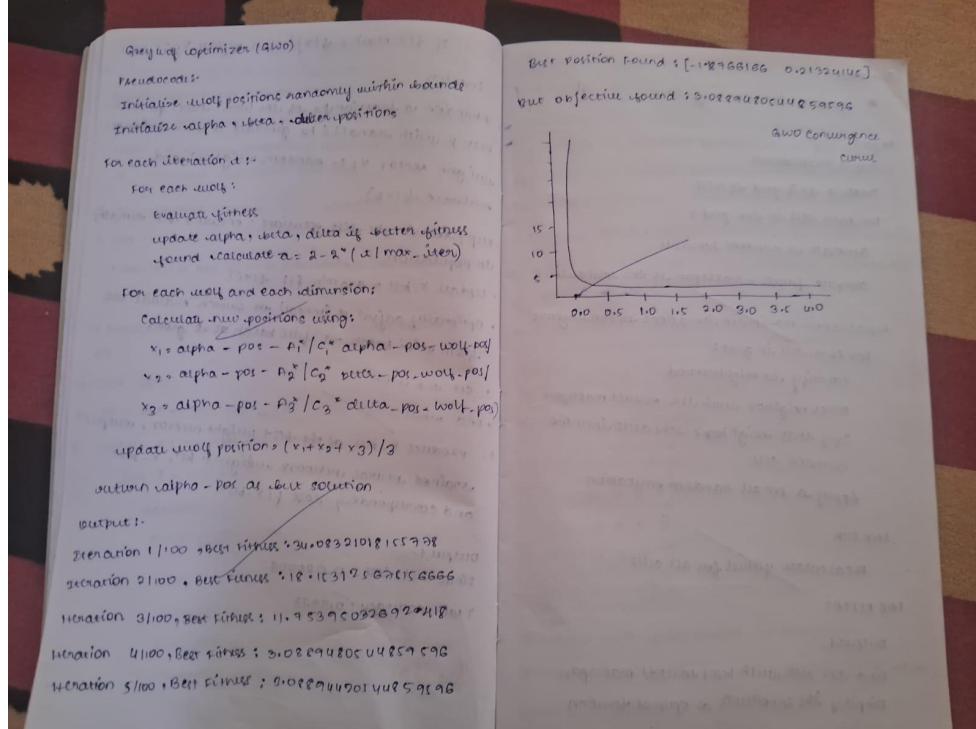
Program 5:

Grey Wolf Optimizer:

Problem Statement:

The Grey Wolf Optimizer (GWO) is inspired by the leadership hierarchy and hunting strategies of grey wolves. Implement the GWO algorithm in Python to solve a continuous optimization problem. Simulate the behaviors of alpha, beta, delta, and omega wolves during the encircling, hunting, and attacking phases. Evaluate the algorithm's ability to converge to the global minimum of a benchmark mathematical function.

Algorithm:



Code:

```
import numpy as np
```

```
def gwo(obj, dim, lb, ub, wolves=25, iters=80):
```

```
    lb = np.array(lb)
```

```
    ub = np.array(ub)
```

```
X = np.random.uniform(lb, ub, (wolves, dim))
```

```
a_pos = np.zeros(dim)
```

```
b_pos = np.zeros(dim)
```

```
d_pos = np.zeros(dim)
```

```
a_score = float('inf')
```

```
b_score = float('inf')
```

```
d_score = float('inf')
```

```
curve = []
```

```

for t in range(iters):
    for i in range(wolves):
        X[i] = np.clip(X[i], lb, ub)
        f = obj(X[i])

        if f < a_score:
            d_score, d_pos = b_score, b_pos.copy()
            b_score, b_pos = a_score, a_pos.copy()
            a_score, a_pos = f, X[i].copy()
        elif f < b_score:
            d_score, d_pos = b_score, b_pos.copy()
            b_score, b_pos = f, X[i].copy()
        elif f < d_score:
            d_score, d_pos = f, X[i].copy()

    A = 2 - 2 * (t / iters)

    for i in range(wolves):
        r1, r2 = np.random.rand(), np.random.rand()
        A1 = 2 * A * r1 - A
        C1 = 2 * r2

        r1, r2 = np.random.rand(), np.random.rand()
        A2 = 2 * A * r1 - A
        C2 = 2 * r2

        r1, r2 = np.random.rand(), np.random.rand()
        A3 = 2 * A * r1 - A
        C3 = 2 * r2

        D1 = abs(C1 * a_pos - X[i])
        D2 = abs(C2 * b_pos - X[i])
        D3 = abs(C3 * d_pos - X[i])

        X1 = a_pos - A1 * D1
        X2 = b_pos - A2 * D2
        X3 = d_pos - A3 * D3

        X[i] = (X1 + X2 + X3) / 3

        curve.append(a_score)
        print(f"Iter {t+1}/{iters} | Best = {a_score}")

    return a_pos, a_score, curve

```

```
def sphere(x):
```

```

return np.sum(x**2)

lb = [-10]*5
ub = [10]*5

best_x, best_f, curve = gwo(sphere, dim=5, lb=lb, ub=ub, wolves=20, iters=60)

print("\nBest position:", best_x)
print("Best fitness:", best_f)

```

Output:

```

Iter 1/60 | Best = 19.38453426344699
Iter 2/60 | Best = 12.847689101876695
Iter 3/60 | Best = 8.420193613082814
Iter 4/60 | Best = 1.3302224649909478
Iter 5/60 | Best = 1.3302224649909478
Iter 6/60 | Best = 0.8615491177497469
Iter 7/60 | Best = 0.4246542774007143
Iter 8/60 | Best = 0.3388244854477642
Iter 9/60 | Best = 0.18083224476768842
Iter 10/60 | Best = 0.07812973052449758
Iter 11/60 | Best = 0.03522460557660338
Iter 12/60 | Best = 0.03522460557660338
Iter 13/60 | Best = 0.012944899570136364
Iter 14/60 | Best = 0.012944899570136364
Iter 15/60 | Best = 0.006152950614212774
Iter 16/60 | Best = 0.0037310759775999102
Iter 17/60 | Best = 0.002735506845768878
Iter 18/60 | Best = 0.0011640701103155938
Iter 19/60 | Best = 0.0009104050542873242
Iter 20/60 | Best = 0.0006602536321871713
Iter 21/60 | Best = 0.00040667508175590506
Iter 22/60 | Best = 0.0002605017849749814
Iter 23/60 | Best = 0.00014268935347434156
Iter 24/60 | Best = 7.488484272466265e-05
Iter 25/60 | Best = 7.247094535557312e-05
Iter 26/60 | Best = 3.104607941020437e-05
Iter 27/60 | Best = 2.6829884971963454e-05
Iter 28/60 | Best = 1.1882729888824425e-05
Iter 29/60 | Best = 1.1229480621360995e-05
Iter 30/60 | Best = 4.845358846713108e-06
Iter 31/60 | Best = 4.65233486230689e-06
Iter 32/60 | Best = 3.3228272561699215e-06
Iter 33/60 | Best = 3.3181126472929255e-06
Iter 34/60 | Best = 2.455945937500936e-06
Iter 35/60 | Best = 1.7479393145140238e-06
Iter 36/60 | Best = 1.5948468972464486e-06

```

```
Iter 37/60 | Best = 1.3760549267731323e-06
Iter 38/60 | Best = 1.106879352926668e-06
Iter 39/60 | Best = 1.0341200387126218e-06
Iter 40/60 | Best = 9.679835810536737e-07
Iter 41/60 | Best = 7.270257902916992e-07
Iter 42/60 | Best = 7.270257902916992e-07
Iter 43/60 | Best = 6.234784775579161e-07
Iter 44/60 | Best = 5.832397928347616e-07
Iter 45/60 | Best = 5.584070849595501e-07
Iter 46/60 | Best = 4.911566777040607e-07
Iter 47/60 | Best = 4.533506668531795e-07
Iter 48/60 | Best = 4.0440339346248435e-07
Iter 49/60 | Best = 3.942344547235292e-07
Iter 50/60 | Best = 3.7470697488341257e-07
Iter 51/60 | Best = 3.5470071374662986e-07
Iter 52/60 | Best = 3.4764315127985757e-07
Iter 53/60 | Best = 3.3889763569838644e-07
Iter 54/60 | Best = 3.2487447793050615e-07
Iter 55/60 | Best = 3.205353914539447e-07
Iter 56/60 | Best = 3.189124599696688e-07
Iter 57/60 | Best = 3.171865169769369e-07
Iter 58/60 | Best = 3.1551459750944405e-07
Iter 59/60 | Best = 3.1361824113999946e-07
Iter 60/60 | Best = 3.1361824113999946e-07
```

Best position: [-0.000383 0.00029216 0.00010707 0.00023974 -0.00011242]

Best fitness: 3.1361824113999946e-07

Program 6:

Parallel Cellular Algorithms

Problem Statement:

Parallel Cellular Algorithms mimic the distributed behavior of biological cells, where each cell updates its state based on interactions with neighboring cells. Implement a Parallel Cellular Optimization Algorithm in Python using a 2D grid of cells, where each cell represents a candidate solution. Define neighbor interactions and update rules that allow the algorithm to iteratively improve solutions across the grid. The objective is to evaluate how local interactions support global optimization performance, particularly for solving a numerical optimization problem.

Algorithm:

7-11-2005

→ Parallel cellular algorithm

Begin:

Step 1: Initialization

Create a $G \times G$ grid of cells

For each cell in the grid:

- Generate a random schedule
- Compute fitness = makespan of the schedule.

Repeat until maximum iterations or convergence:

For each cell in grid:

- Identify its neighborhood
- Select neighbors with the lowest makespan
- Copy that neighbor's schedule into the current cell
- Apply a small random mutation

END FOR

Recalculate fitness for all cells

END REPEAT

Outputs:

Find one cell with best (lowest) makespan

Display its schedule as optimal solution

END

Applications: Network Routing - shortest path of communication in network

Algorithm:-

1. Define problem: represent network or a grid of cells
2. Initialize parameters: Define neighborhood, cost matrix
3. Initialize population: Assign initial path costs
4. Evaluate fitness: Compute routing cost per node
5. Update states: Update using neighbour minimum cost
6. Terminate: If no more convergence
7. Output result: Extract shortest path

Output:-

Converged after 10 iterations:

Final Routing cost grid

$\begin{bmatrix} 10 & 15 & 13 & 10 & 8 \\ 14 & 12 & 11 & 8 & 5 \\ 12 & 10 & 8 & 5 & 3 \\ 10 & 8 & 6 & 3 & 1 \\ 9 & 6 & 4 & 2 & 0 \end{bmatrix}$

Shortest path from source to destination

$(0,0) \rightarrow (1,0) \rightarrow (2,1) \rightarrow (3,2) \rightarrow (4,2) \rightarrow (4,4)$

Total path cost: 16.0

Code:

```
import numpy as np
```

```
GRID_SIZE = 5 # 5x5 network grid
```

```
MAX_ITER = 100
```

```
INF = 1e9
```

```
source = (0, 0)
```

```
destination = (4, 4)
```

```
np.random.seed(42)
```

```
cost_matrix = np.random.randint(1, 10, size=(GRID_SIZE, GRID_SIZE))
```

```
state = np.full((GRID_SIZE, GRID_SIZE), INF)
```

```
state[destination] = 0 # destination cost = 0
```

```
# Define 4-neighborhood (up, down, left, right)
```

```
neighbors = [(-1, 0), (1, 0), (0, -1), (0, 1)]
```

```
def get_neighbors(i, j):
```

```

"""Return valid neighboring cells"""
valid_neighbors = []
for dx, dy in neighbors:
    ni, nj = i + dx, j + dy
    if 0 <= ni < GRID_SIZE and 0 <= nj < GRID_SIZE:
        valid_neighbors.append((ni, nj))
return valid_neighbors

for iteration in range(MAX_ITER):
    new_state = state.copy()
    for i in range(GRID_SIZE):
        for j in range(GRID_SIZE):
            if (i, j) == destination:
                continue
            neighbor_costs = []
            for ni, nj in get_neighbors(i, j):
                # Update rule: min(cost to neighbor + neighbor's state)
                total_cost = cost_matrix[ni, nj] + state[ni, nj]
                neighbor_costs.append(total_cost)
            if neighbor_costs:
                new_state[i, j] = min(neighbor_costs)
    # Check for convergence
    if np.allclose(new_state, state):
        print(f"Converged after {iteration} iterations.")
        break
    state = new_state

path = [source]
current = source
while current != destination:
    i, j = current
    nbs = get_neighbors(i, j)
    next_cell = min(nbs, key=lambda n: state[n])
    path.append(next_cell)
    current = next_cell

print("Final Routing Cost Grid:")
print(np.round(state, 2))
print("\nShortest Path from Source to Destination:")
print(" → ".join([str(p) for p in path]))
print(f"\nTotal Path Cost: {state[source]}")

```

Output:

Converged after 8 iterations.

Final Routing Cost Grid:

```

[[33. 30. 22. 17. 17.]
 [30. 23. 15. 12. 13.]

```

[22. 15. 12. 6. 8.]

[20. 12. 6. 4. 3.]

[19. 13. 4. 3. 0.]]

Shortest Path from Source to Destination:

(0, 0) → (1, 0) → (2, 0) → (2, 1) → (3, 1) → (3, 2) → (4, 2) → (4, 3) → (4, 4)

Total Path Cost: 33.0

Program 7:

Optimization via Gene Expression Algorithms

Problem Statement:

Gene Expression Algorithms (GEA) mimic the biological mechanism of gene expression, where DNA sequences are translated into functional proteins. Implement a GEA in Python to solve a continuous optimization problem by encoding candidate solutions as gene-like sequences. Apply selection, crossover, mutation, and expression operators to evolve the population across generations. The objective is to determine the algorithm's effectiveness in discovering optimal or near-optimal solutions.

Algorithm:

The handwritten notes describe the GEA process and provide two tables for population management.

Flowchart:

```
graph TD; Start[Initial Population] --> Encoding[Encoding]; Encoding --> Selection[Selection]; Selection --> Crossover[Crossover]; Crossover --> Mutation[Mutation]; Mutation --> Expression(Expression); Expression --> Termination[Termination]; Termination --> End[End]
```

Initial Population Table:

Ind	Initial chromosome (Genotype)	Prototype expression	Value	Ritness	P
1	x x x	x 2	1.2	1.44	0.1244
2	x x x	2 x	2.5	6.25	0.541
3	x x	x	5	25	0.0216
4	-x x	x -2	1.9	3.61	0.3125

First Generation Table:

Ind	Initial chromosome (Genotype)	Prototype expression	Value	Ritness	P
1	x x x	x 2	1.2	1.44	0.1244
2	x x x	2 x	2.5	6.25	0.541
3	x x	x	5	25	0.0216
4	-x x	x -2	1.9	3.61	0.3125

③. selecting mating pool (Eliminate grow 3)

sr	mating pool	crossover point	offspring after crossover	x	fitness f(x)
1	01100	4	001101	13	169
2	110011		11000	24	576
3	111001	2	11011	27	729
4	101011	2	10001	17	289

will choose 4 and 2

max \rightarrow 729

④. mutation

sr no	offspring after crossover	mutation chromosome for flipping	offspring	x
1	01101	100.00	11101	29
2	11000	11000	11000	24
3	11011	11011	11011	27
4	10001	10100	10100	20

$$\begin{aligned} f(x) & \\ 841 & \text{sum} \rightarrow 2546 \\ 576 & \text{Avg} \rightarrow 630.5 \\ 729 & \text{Max} \rightarrow 841 \\ 289 & \\ 400 & \end{aligned}$$

sum \rightarrow 2546

Avg \rightarrow 630.5

Max \rightarrow 841

400

actual count

1

2 ✓

0

2

Iteration - 2

sr no	initial pop	x	f(x)	prob	% prob	Exp	Actual count
1	11101	29	841	0.33	33		
2	11000	24	576	0.22	22		
3	11011	27	729	0.28	28		
4	10100	20	400	0.157	15.7		

algorithm

start

①. input

• fitness function $f(x)$ [use provides formula in terms of x]

using numpy functions]

• population size (pop-size = 4)

Step 4:- iterate until convergence

repeat step 3 to 6 until fitness improvement is negligible or generation limit has reached.

Pseudocode

- Start
- 1) Define Fitness function
- 2) Define Parameter
- 3) Create Population
- 4) Select Mating pool
- 5) Mutation after mating
- 6) Gene expression and Evaluation
- 7) Iterate
- 8) Output best value

Output:- (ran for 1000 generations)

Genes: [29.53, 29.82, 29.34, 28.53, 15.09, 21.83,
23.53, 30.81, 28.51, 26.23]

$$x = 26.37$$

$$f(x) = 695.45 \quad \# \text{ Generation limit reached}$$

✓

Pseudocode

1. $P = P_0$

2. for

3.

4. if

5. end

6.

7.

8. for

9. x_i

vi

10. $P_i =$

11. end

12. end

Code:

```
import random, math

def fitness(x):
    return x * math.sin(10 * math.pi * x) + 2

def init_pop(size):
    return [random.uniform(-1, 2) for _ in range(size)]

def select(pop, fits):
    total = sum(fits)
    r = random.uniform(0, total)
    cum = 0
    for p, f in zip(pop, fits):
        cum += f
        if cum >= r:
            return p
    return random.choice(pop)

def crossover(a, b, rate):
    if random.random() < rate:
        alpha = random.random()
        return alpha*a + (1-alpha)*b, alpha*b + (1-alpha)*a
    return a, b

def mutate(x, rate):
    if random.random() < rate:
        return random.uniform(-1, 2)
    return x

def run():
    POP, GEN = 6, 20
    CROSS, MUT = 0.8, 0.05
    pop = init_pop(POP)
    best, best_fit = None, float("-inf")

    for g in range(1, GEN+1):
        fits = [fitness(x) for x in pop]
        for x, f in zip(pop, fits):
            if f > best_fit:
                best, best_fit = x, f
        print(f"Gen {g}: Best Fitness = {best_fit:.4f}, x = {best:.4f}")

        new_pop = []
        while len(new_pop) < POP:
            p1, p2 = select(pop, fits), select(pop, fits)
            c1, c2 = crossover(p1, p2, CROSS)
```

```

new_pop += [mutate(c1, MUT), mutate(c2, MUT)]
pop = new_pop[:POP]

print("\nBest solution found:")
print(f'x = {best:.4f}')
print(f'f(x) = {best_fit:.4f}')

if __name__ == "__main__":
    run()

```

Output:

Gen 1: Best Fitness = 3.0193, x = 1.0432
 Gen 2: Best Fitness = 3.0193, x = 1.0432
 Gen 3: Best Fitness = 3.0193, x = 1.0432
 Gen 4: Best Fitness = 3.1817, x = 1.2402
 Gen 5: Best Fitness = 3.1817, x = 1.2402
 Gen 6: Best Fitness = 3.1817, x = 1.2402
 Gen 7: Best Fitness = 3.1817, x = 1.2402
 Gen 8: Best Fitness = 3.1817, x = 1.2402
 Gen 9: Best Fitness = 3.1817, x = 1.2402
 Gen 10: Best Fitness = 3.1817, x = 1.2402
 Gen 11: Best Fitness = 3.1817, x = 1.2402
 Gen 12: Best Fitness = 3.1817, x = 1.2402
 Gen 13: Best Fitness = 3.1817, x = 1.2402
 Gen 14: Best Fitness = 3.1817, x = 1.2402
 Gen 15: Best Fitness = 3.1817, x = 1.2402
 Gen 16: Best Fitness = 3.1817, x = 1.2402
 Gen 17: Best Fitness = 3.1817, x = 1.2402
 Gen 18: Best Fitness = 3.1817, x = 1.2402
 Gen 19: Best Fitness = 3.1817, x = 1.2402
 Gen 20: Best Fitness = 3.1817, x = 1.2402

Best solution found:

x = 1.2402

f(x) = 3.1817