

Code : 1

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class A_Fibonaccidp {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int fib = Fib(n);
```

```
        System.out.println(fib);
```

```
        scn.close();
```

```
    }
```

```
    public static int Fib(int n) {
```

```
        if (n == 0 || n == 1) {
```

```
            return n;
```

```
        }
```

```
        int fibn1 = Fib(n - 1);
```

```
        int fibn2 = Fib(n - 2);
```

```
        int fibn = fibn1 + fibn2;
```

```
        return fibn;
```

```
    }
```

```
}
```

Code : 2

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class B_ClimbStairs {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int paths = countPathsTab(n);
```

```
        System.out.println(paths);
```

```
        scn.close();
```

```
    }
```

```
    public static int countPathsTab(int n) {
```

```
        if (n == 0) {
```

```
            return 1;
```

```
        } else if (n < 0) {
```

```
            return 0;
```

```
        }
```

```
        int[] dp = new int[n + 1];
```

```
        dp[0] = 1;
```

```
        for (int i = 1; i <= n; i++) {
```

```
            dp[i] = dp[i - 1];
```

```
            if (i >= 2)
```

```
                dp[i] += dp[i - 2];
```

```
            if (i >= 3)
```

```
                dp[i] += dp[i - 3];
```

```
        }
```

```
        return dp[n];
```

```
    }
```

```
}
```

Code : 3

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class C_ClimbStairsWithVariableJumps {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            arr[i] = scn.nextInt();
```

```
        }
```

```
        int[] dp = new int[n + 1];
```

```
        dp[n] = 1;
```

```
        for (int i = n - 1; i >= 0; i--) {
```

```
            for (int reach = i + 1; reach <= Math.min(n, i + arr[i]); reach++) {
```

```
                dp[i] += dp[reach];
```

```
            }
```

```
        }
```

```
        System.out.println(dp[0]);
```

```
        scn.close();
```

```
    }
```

```
}
```

Code : 4

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class D_ClimbStairsWithMinimumMoves {

    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        int n = scn.nextInt();
        int[] arr = new int[n];
        for (int i = 0; i < n; i++) {
            arr[i] = scn.nextInt();
        }
        Integer[] dp = new Integer[n + 1];
        dp[n] = 0;

        for (int i = n - 1; i >= 0; i--) {
            if (arr[i] == 0)
                continue;
            int min = Integer.MAX_VALUE;
            for (int j = 1; j <= arr[i] && i + j < dp.length; j++) {
                if (dp[i + j] != null) {
                    min = Math.min(min, dp[i + j]);
                }
            }
            if (min != Integer.MAX_VALUE)
                dp[i] = min + 1;
        }
        System.out.println(dp[0]);
        scn.close();
    }
}
```

Code : 5

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class E_MinCostInMazeTraversal {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int m = scn.nextInt();
```

```
        int[][] arr = new int[n][m];
```

```
        for (int i = 0; i < n; i++) {           //1
```

```
            for (int j = 0; j < m; j++) {
```

```
                arr[i][j] = scn.nextInt();
```

```
            }
```

```
        }
```

```
        int[][] dp = new int[n][m];           //2
```

```
        for (int i = n - 1; i >= 0; i--) {     //3
```

```
            for (int j = m - 1; j >= 0; j--) { //4
```

```
                if (i == n - 1 && j == m - 1) { //5
```

```
                    dp[i][j] = arr[i][j];
```

```
                } else if (i == n - 1) {        //6
```

```
                    dp[i][j] = arr[i][j] + dp[i][j + 1];
```

```
                } else if (j == m - 1) {        //7
```

```
                    dp[i][j] = arr[i][j] + dp[i + 1][j];
```

```
                } else {                        //8
```

```
                    int min = Math.min(dp[i + 1][j], dp[i][j + 1]);
```

```
                    dp[i][j] = arr[i][j] + min;
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[0][0]);         //9
```

```
    }
```

```
}
```

Code : 6

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class F_Goldmine {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int m = scn.nextInt();
```

```
        int[][] arr = new int[n][m];
```

```
        for (int i = 0; i < n; i++) {
```

```
            for (int j = 0; j < m; j++) {          //1
```

```
                arr[i][j] = scn.nextInt();
```

```
            }
```

```
        }
```

```
        int[][] dp = new int[n][m];              //2
```

```
        for (int j = m - 1; j >= 0; j--) {        //3
```

```
            for (int i = n - 1; i >= 0; i--) {    //4
```

```
                if (j == m - 1) {
```

```
                    dp[i][j] = arr[i][j];        //5
```

```
                } else if (i == 0) {              //6
```

```
                    dp[i][j] = arr[i][j] + Math.max(dp[i][j + 1], dp[i + 1][j + 1]);
```

```
                } else if (i == n - 1) {          //7
```

```
                    dp[i][j] = arr[i][j] + Math.max(dp[i][j + 1], dp[i - 1][j + 1]);
```

```
                } else {                          //8
```

```
                    dp[i][j] = arr[i][j] + Math.max(dp[i][j + 1], Math.max(dp[i + 1][j + 1],
```

```
                        dp[i - 1][j + 1]));
```

```
                }
```

```
            }
```

```
        }
```

```
        int max = dp[0][0];                      //9
```

```
        for (int i = 1; i < n; i++) {
```

```
            if (dp[i][0] > max)                  //10
```

```
                max = dp[i][0];
```

```
        }
```

```
        System.out.println(max);                //11
```

```
    }
```

```
}
```

Code : 7

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class G_TargetSumSubsetsDp {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int tar = Integer.parseInt(br.readLine());
```

```
        boolean[][] dp = new boolean[arr.length + 1][tar + 1];
```

```
        for (int i = 0; i < dp.length; i++) {
```

```
            for (int j = 0; j < dp[0].length; j++) {
```

```
                if (i == 0 && j == 0) {
```

```
                    dp[i][j] = true;
```

```
                } else if (i == 0) {
```

```
                    dp[i][j] = false;
```

```
                } else if (j == 0) {
```

```
                    dp[i][j] = true;
```

```
                } else {
```

```
                    if (dp[i - 1][j] == true) {
```

```
                        dp[i][j] = true;
```

```
                    } else {
```

```
                        int val = arr[i - 1];
```

```
                        if (j >= val
```

```
                            && dp[i - 1][j - val] == true) {
```

```
                            dp[i][j] = true;
```

```
                        }
```

```
                    }
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[dp.length - 1][tar]);
```

```
    }
```

```
}
```

Code : 8

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class H_CoinChangeCombination {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] coins = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            coins[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int amt = Integer.parseInt(br.readLine());
```

```
        int[] dp = new int[amt + 1];
```

```
        dp[0] = 1;
```

```
        for (int coin : coins) {
```

```
            for (int i = 1; i < dp.length; i++) {
```

```
                if (i >= coin) {
```

```
                    dp[i] += dp[i - coin];
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[amt]);
```

```
    }
```

```
}
```


Code : 9

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class I_CoinChangePermutations {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] coins = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            coins[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int amt = Integer.parseInt(br.readLine());
```

```
        int[] dp = new int[amt + 1];
```

```
        dp[0] = 1;
```

```
        for (int i = 1; i < dp.length; i++) {
```

```
            for (int coin : coins) {
```

```
                if (i >= coin) {
```

```
                    dp[i] += dp[i - coin];
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[amt]);
```

```
    }
```

```
}
```

Code : 10

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class J_ZeroOneKnapsack {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] price = new int[n];
```

```
        String str1 = br.readLine();
```

```
        for (int i = 0; i < n; i++) {
```

```
            price[i] = Integer.parseInt(str1.split(" ")[i]);
```

```
        }
```

```
        int[] weight = new int[n];
```

```
        String str2 = br.readLine();
```

```
        for (int i = 0; i < n; i++) {
```

```
            weight[i] = Integer.parseInt(str2.split(" ")[i]);
```

```
        }
```

```
        int cap = Integer.parseInt(br.readLine());
```

```
        int[][] dp = new int[n + 1][cap + 1];
```

```
        for (int i = 1; i < dp.length; i++) {
```

```
            for (int j = 1; j < dp[0].length; j++) {
```

```
                int val = price[i - 1];
```

```
                int wt = weight[i - 1];
```

```
                if (j >= wt) { //If the current capacity is greater than the weight of the current item
```

```
                    dp[i][j] = Math.max(dp[i - 1][j], dp[i - 1][j - wt] + val); // max cost will be max of cost before putting the item and
```

```
after putting it
```

```
                } else {
```

```
                    dp[i][j] = dp[i - 1][j]; //If current capacity is less than weight do not add item to the bag
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[n][cap]);
```

```
    }
```

```
}
```

Code : 11

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Arrays;
```

```
import java.util.Scanner;
```

```
public class K_FractionalKnapsackOfficial {
```

```
    static class Item implements Comparable<Item> {
```

```
        int val;
```

```
        int wt;
```

```
        double vwRatio;
```

```
        public int compareTo(Item o) {
```

```
            if (this.vwRatio < o.vwRatio) {
```

```
                return -1;
```

```
            } else if (this.vwRatio > o.vwRatio) {
```

```
                return +1;
```

```
            } else {
```

```
                return 0;
```

```
            }
```

```
        }
```

```
    }
```

```
    public static void main(String[] args) {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        Item[] items = new Item[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            items[i] = new Item();
```

```
            items[i].val = scn.nextInt();
```

```
        }
```

```
for (int i = 0; i < n; i++) {  
    items[i].wt = scn.nextInt();  
    items[i].vwRatio = items[i].val * 1.0 / items[i].wt;  
}  
  
Arrays.sort(items);  
  
double vib = 0;  
  
int space = scn.nextInt();  
  
int i = n - 1;  
  
while (space > 0 && i >= 0) {  
    if (space >= items[i].wt) {  
        vib = vib + items[i].val;  
        space = space - items[i].wt;  
    } else {  
        vib = vib + (space * items[i].val * 1.0) / items[i].wt;  
        space = 0;  
        break;  
    }  
    i--;  
}  
  
System.out.println(vib);  
}  
  
}
```

Code : 12

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class L_UnboundedKnapsack {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] values = new int[n];
```

```
        int[] wts = new int[n];
```

```
        for (int i = 0; i < n; i++) {  
            values[i] = scn.nextInt();  
        }
```

```
        for (int i = 0; i < n; i++) {  
            wts[i] = scn.nextInt();  
        }
```

```
        int cap = scn.nextInt();
```

```
        int[] dp = new int[cap + 1];
```

```
        dp[0] = 0;
```

```
        for (int bagc = 1; bagc <= cap; bagc++) {  
            int max = 0;  
            for (int i = 0; i < n; i++) {
```

```
                if (wts[i] <= bagc) {  
                    int rbagc = bagc - wts[i];  
                    int rbagv = dp[rbagc];  
                    int tbagv = rbagv + values[i];
```

```
                    if (tbagv > max) {  
                        max = tbagv;  
                    }  
                }
```

```
            }  
            dp[bagc] = max;
```

```
        }  
        System.out.println(dp[cap]);
```

```
    }  
}
```

Code : 13

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class M_CountBinaryStrings {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int zeroes = 1;
```

```
        int ones = 1;
```

```
        for (int i = 2; i <= n; i++) {
```

```
            int nzeroes = ones;
```

```
            int nones = ones + zeroes;
```

```
            zeroes = nzeroes;
```

```
            ones = nones;
```

```
        }
```

```
        System.out.println(zeroes + ones);
```

```
    }
```

```
}
```

Code : 14

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class N_CountEncodings {
    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        String str = scn.next();
        int[] dp = new int[str.length()];

        dp[0] = 1;
        for (int i = 1; i < str.length(); i++) {
            if (str.charAt(i - 1) == '0' && str.charAt(i) == '0') {
                dp[i] = 0;
            } else if (str.charAt(i - 1) == '0' && str.charAt(i) != '0') {
                dp[i] = dp[i - 1];
            } else if (str.charAt(i - 1) != '0' && str.charAt(i) == '0') {
                if (str.charAt(i - 1) == '1' || str.charAt(i - 1) == '2') {
                    dp[i] = (i >= 2 ? dp[i - 2] : 1);
                }
            } else {
                dp[i] = dp[i - 1];
                if (Integer.parseInt(str.substring(i - 1, i + 1)) <= 26) {
                    dp[i] += (i >= 2 ? dp[i - 2] : 1);
                }
            }
        }
        System.out.println(dp[str.length() - 1]);
        scn.close();
    }
}
```

Code : 15

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class O_Count_APlus_BPlus_CPlusSubsequences {  
    public static void main(String[] args) throws Exception {  
        Scanner scn = new Scanner(System.in);  
        String str = scn.next();  
        int a = 0;  
        int ab = 0;  
        int abc = 0;  
  
        for (int i = 0; i < str.length(); i++) {  
            char ch = str.charAt(i);  
  
            if (ch == 'a') {  
                a = 2 * a + 1;  
            } else if (ch == 'b') {  
                ab = 2 * ab + a;  
            } else if (ch == 'c') {  
                abc = 2 * abc + ab;  
            }  
        }  
        System.out.println(abc);  
        scn.close();  
    }  
}
```


Code : 16

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
// Java code to Count Palindromic Subsequence
```

```
// in a given String
```

```
public class P_CountPalindromicSubsequences {
```

```
    // Function return the total palindromic
```

```
    // subsequence
```

```
    static int countPS(String str) {
```

```
        int N = str.length();
```

```
        // create a 2D array to store the count
```

```
        // of palindromic subsequence
```

```
        int[][] cps = new int[N][N];
```

```
        // palindromic subsequence of length 1
```

```
        for (int i = 0; i < N; i++)
```

```
            cps[i][i] = 1;
```

```
        // check subsequence of length L is
```

```
        // palindrome or not
```

```
        for (int L = 2; L <= N; L++) {
```

```
            for (int i = 0; i <= N - L; i++) {
```

```
                int k = L + i - 1;
```

```
                if (str.charAt(i) == str.charAt(k)) {
```

```
                    cps[i][k] = cps[i][k - 1]
```

```
                        + cps[i + 1][k] + 1;
```

```
                } else {
```

```
                    cps[i][k] = cps[i][k - 1]
```

```
                        + cps[i + 1][k]
```

```
                        - cps[i + 1][k - 1];
```

```
                }
```

```
            }
```

```
        }
```

```
        // return total palindromic subsequence
```

```
        return cps[0][N - 1];
```

```
    }
```

```
    // Driver program
```

```
    public static void main(String args[]) {
```

```
        Scanner sc = new Scanner(System.in);
```

```
        String str = sc.nextLine();
```

```
        System.out.println(countPS(str));
```

```
    }
```

```
}
```

```
// This code is contributed by Sumit Ghosh
```

Code : 17

```
import java.util.Scanner;
```

```
public class Q_CountPalindromicSubstrings {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        String s = scn.nextLine();
```

```
        boolean[][] dp = new boolean[s.length()][s.length()];
```

```
        int count = 0;
```

```
        for (int g = 0; g < s.length(); g++) {
```

```
            for (int i = 0, j = g; j < dp.length; i++, j++) {
```

```
                if (g == 0) {
```

```
                    dp[i][j] = true;
```

```
                } else if (g == 1) {
```

```
                    if (s.charAt(i) == s.charAt(j)) {
```

```
                        dp[i][j] = true;
```

```
                    } else {
```

```
                        dp[i][j] = false;
```

```
                    }
```

```
                } else {
```

```
                    if (s.charAt(i) == s.charAt(j) && dp[i + 1][j - 1] == true) {
```

```
                        dp[i][j] = true;
```

```
                    } else {
```

```
                        dp[i][j] = false;
```

```
                    }
```

```
                }
```

```
                if (dp[i][j]) {
```

```
                    count++;
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(count);
```

```
    }
```

```
}
```

Code : 18

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class R_CountOfValleysAndMountains {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        long[] dp = new long[n + 1];
```

```
        dp[0] = 1;
```

```
        for (int i = 1; i < dp.length; i++) {
```

```
            for (int j = 0; j < i; j++) {
```

```
                dp[i] += dp[j] * dp[i - 1 - j];
```

```
            }
```

```
        }
```

```
        System.out.println(dp[n]);
```

```
    }
```

```
}
```

Code : 19

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class S_CountBrackets {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        long[] dp = new long[n + 1];
```

```
        dp[0] = 1;
```

```
        for (int i = 1; i < dp.length; i++) {
```

```
            for (int j = 0; j < i; j++) {
```

```
                dp[i] += dp[j] * dp[i - 1 - j];
```

```
            }
```

```
        }
```

```
        System.out.println(dp[n]);
```

```
    }
```

```
}
```

Code : 20

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class T_ArrangeBuildings {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        long n = scn.nextInt();
```

```
        long ob = 1;
```

```
        long os = 1;
```

```
        for (int i = 2; i <= n; i++) {
```

```
            long nb = os;
```

```
            long ns = os + ob;
```

```
            ob = nb;
```

```
            os = ns;
```

```
        }
```

```
        long total = ob + os;
```

```
        System.out.println(total * total);
```

```
    }
```

```
}
```

Code : 21

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class U_MaximumSumNonAdjacentElements {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            arr[i] = scn.nextInt();
```

```
        }
```

```
        int inc = arr[0];                //1
```

```
        int exc = 0;
```

```
        for (int i = 1; i < n; i++) {
```

```
            int ninc = exc + arr[i];      //2
```

```
            int nexc = Math.max(inc, exc);
```

```
            inc = ninc;                   //3
```

```
            exc = nexc;
```

```
        }
```

```
        System.out.println(Math.max(inc, exc));    //4
```

```
    }
```

```
}
```

Code : 22

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class V_MaximumSumIncreasingSubsequence {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int omax = Integer.MIN_VALUE;
```

```
        int[] dp = new int[arr.length];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            Integer max = null;
```

```
            for (int j = 0; j < i; j++) {
```

```
                if (arr[j] <= arr[i]) {
```

```
                    if (max == null || dp[j] > max) {
```

```
                        max = dp[j];
```

```
                    }
```

```
                }
```

```
            }
```

```
            if (max != null) {
```

```
                dp[i] = max + arr[i];
```

```
            } else {
```

```
                dp[i] = arr[i];
```

```
            }
```

```
            if (dp[i] > omax) {
```

```
                omax = dp[i];
```

```
            }
```

```
        }
```

```
        System.out.println(omax);
```

```
    }
```

```
}
```

Code : 23

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
import java.util.Arrays;
```

```
public class W_MaximumNonoverlappingBridges {
```

```
    public static class Bridge implements Comparable<Bridge> {
```

```
        int n;
```

```
        int s;
```

```
        @Override
```

```
        public int compareTo(Bridge o) {
```

```
            if (this.n != o.n) {
```

```
                return this.n - o.n;
```

```
            } else {
```

```
                return this.s - o.s;
```

```
            }
```

```
        }
```

```
    }
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        Bridge[] brdgs = new Bridge[n];
```

```
        for (int i = 0; i < brdgs.length; i++) {
```

```
            String str = br.readLine();
```

```
            brdgs[i] = new Bridge();
```

```
            brdgs[i].n = Integer.parseInt(str.split(" ")[0]);
```

```
            brdgs[i].s = Integer.parseInt(str.split(" ")[1]);
```

```
        }
```

```
        Arrays.sort(brdgs);
```

```
        int[] lis = new int[brdgs.length];
```

```
        for (int i = 0; i < brdgs.length; i++) {
```

```
            Integer max = null;
```

```
            for (int j = 0; j < i; j++) {
```

```
                if (brdgs[j].s <= brdgs[i].s) {
```

```
                    if (max == null || lis[j] > max) {
```

```
                        max = lis[j];
```

```
                    }
```

```
                }
```

```
            }
```

```
            if (max != null) {
```

```
                lis[i] = max + 1;
```

```
            } else {
```

```
                lis[i] = 1;
```

```
            }
```

```
        }
```

```
        int omax = 0;
```

```
        for (int i = 0; i < brdgs.length; i++) {
```

```
            if (lis[i] > omax) {
```



```
        omax = lis[i];
    }
}
System.out.println(omax);
}
}
```

Code : 24

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class X_PaintHouse {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[][] arr = new int[n][3];
```

```
        for (int i = 0; i < n; i++) {
```

```
            for (int j = 0; j < 3; j++) {          //1
```

```
                arr[i][j] = scn.nextInt();
```

```
            }
```

```
        }
```

```
        int[][] dp = new int[n][3];              //2
```

```
        dp[0][0] = arr[0][0];
```

```
        dp[0][1] = arr[0][1];                    //3
```

```
        dp[0][2] = arr[0][2];
```

```
        for (int i = 1; i < n; i++) {            //4
```

```
            dp[i][0] = Math.min(dp[i - 1][1], dp[i - 1][2]) + arr[i][0];
```

```
            dp[i][1] = Math.min(dp[i - 1][0], dp[i - 1][2]) + arr[i][1];
```

```
            dp[i][2] = Math.min(dp[i - 1][1], dp[i - 1][0]) + arr[i][2];
```

```
        }
```

```
        System.out.println(Math.min(dp[n - 1][0], (Math.min(dp[n - 1][1], dp[n - 1][2]))));
```

```
        //5
```

```
    }
```

```
}
```

Code : 25

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class YA_PaintHouseManyColors {

    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        int n = scn.nextInt();
        int c = scn.nextInt();

        int[][] arr = new int[n][c];
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < c; j++) {
                arr[i][j] = scn.nextInt();
            }
        }
        int[][] dp = new int[arr.length][arr[0].length];
        for (int j = 0; j < arr[0].length; j++) {
            dp[0][j] = arr[0][j];
        }

        int least = Integer.MAX_VALUE;
        int sleast = Integer.MAX_VALUE;
        for (int j = 0; j < arr[0].length; j++) {
            dp[0][j] = arr[0][j];
            if (arr[0][j] <= least) {
                sleast = least;
                least = arr[0][j];
            } else if (arr[0][j] <= sleast) {
                sleast = arr[0][j];
            }
        }
        for (int i = 1; i < dp.length; i++) {
            int nleast = Integer.MAX_VALUE;
            int nsleast = Integer.MAX_VALUE;
            for (int j = 0; j < dp[0].length; j++) {
                if (least == dp[i - 1][j]) {
                    dp[i][j] = sleast + arr[i][j];
                } else {
                    dp[i][j] = least + arr[i][j];
                }
                if (dp[i][j] <= nleast) {
                    nsleast = nleast;
                    nleast = dp[i][j];
                } else if (dp[i][j] <= nsleast) {
                    nsleast = dp[i][j];
                }
            }
            least = nleast;
            sleast = nsleast;
        }
        System.out.println(least);
    }
}
```


Code : 26

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class Y_PaintHouseManyColors {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int c = scn.nextInt();
```

```
        int[][] arr = new int[n][c];
```

```
        for (int i = 0; i < n; i++) {
```

```
            for (int j = 0; j < c; j++) {
```

```
                arr[i][j] = scn.nextInt();
```

```
            }
```

```
        }
```

```
        int[][] dp = new int[arr.length][arr[0].length];
```

```
        for (int j = 0; j < arr[0].length; j++) {
```

```
            dp[0][j] = arr[0][j];
```

```
        }
```

```
        for (int i = 1; i < dp.length; i++) {
```

```
            for (int j = 0; j < dp[0].length; j++) {
```

```
                int min = Integer.MAX_VALUE;
```

```
                for (int k = 0; k < dp[0].length; k++) {
```

```
                    if (k != j) {
```

```
                        if (dp[i - 1][k] < min) {
```

```
                            min = dp[i - 1][k];
```

```
                        }
```

```
                    }
```

```
                }
```

```
                dp[i][j] = arr[i][j] + min;
```

```
            }
```

```
        }
```

```
        int min = Integer.MAX_VALUE;
```

```
        for (int k = 0; k < dp[0].length; k++) {
```

```
            if (dp[n - 1][k] < min) {
```

```
                min = dp[n - 1][k];
```

```
            }
```

```
        }
```

```
        System.out.println(min);
```

```
    }  
}
```

Code : 27

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZA_TilingWith21Tiles {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] dp = new int[n + 1];
```

```
        dp[0] = 0;
```

```
        dp[1] = 1;
```

```
        dp[2] = 2;
```

```
        for (int i = 3; i < dp.length; i++) {
```

```
            dp[i] = dp[i - 1] + dp[i - 2];
```

```
        }
```

```
        System.out.println(dp[n]);
```

```
    }
```

```
}
```

Code : 28

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZB_TilingWithM1Tiles {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int m = Integer.parseInt(br.readLine());
```

```
        int[] dp = new int[n + 1];
```

```
        dp[1] = 1;
```

```
        for (int i = 2; i <= n; i++) {
```

```
            if (i < m) {
```

```
                dp[i] = 1;
```

```
            } else if (i == m) {
```

```
                dp[i] = 2;
```

```
            } else {
```

```
                dp[i] = dp[i - 1] + dp[i - m];
```

```
            }
```

```
        }
```

```
        System.out.println(dp[n]);
```

```
    }
```

```
}
```

Code : 29

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZC_FriendsPairing {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] dp = new int[n + 1];
```

```
        dp[0] = 1;
```

```
        dp[1] = 1;
```

```
        for (int i = 2; i <= n; i++) {
```

```
            dp[i] = dp[i - 1] + (i - 1) * dp[i - 2];
```

```
        }
```

```
        System.out.println(dp[n]);
```

```
        scn.close();
```

```
    }
```

```
}
```


Code : 30

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZD_PartitionIntoSubsets {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int k = scn.nextInt();
```

```
        if (n == 0 || k == 0 || n < k) {
```

```
            System.out.println(0);
```

```
            scn.close();
```

```
            return;
```

```
        }
```

```
        long[][] dp = new long[k + 1][n + 1];
```

```
        for (int t = 1; t <= k; t++) {
```

```
            for (int p = 1; p <= n; p++) {
```

```
                if (p == t)
```

```
                    dp[t][p] = 1;
```

```
                else if (p > t)
```

```
                    dp[t][p] = t * dp[t][p - 1] + dp[t - 1][p - 1];
```

```
            }
```

```
        }
```

```
        System.out.println(dp[k][n]);
```

```
        scn.close();
```

```
    }
```

```
}
```

Code : 31

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZE_BuyAndSellStocksOneTransactionAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int msf = arr[0];
```

```
        int op = 0;
```

```
        for (int i = 1; i < arr.length; i++) {
```

```
            if (arr[i] < msf) {
```

```
                msf = arr[i];
```

```
            }
```

```
            int cp = arr[i] - msf;
```

```
            if (cp > op) {
```

```
                op = cp;
```

```
            }
```

```
        }
```

```
        System.out.println(op);
```

```
    }
```

```
}
```

Code : 32

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZF_BuyAndSellStocksInfiniteTransactionsAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int bon = 0;
```

```
        int son = 0;
```

```
        int op = 0;
```

```
        for (int i = 1; i < arr.length; i++) {
```

```
            if (arr[i] < arr[i - 1]) {
```

```
                op += arr[son] - arr[bon];
```

```
                bon = son = i;
```

```
            } else {
```

```
                son++;
```

```
            }
```

```
        }
```

```
        op += arr[son] - arr[bon];
```

```
        System.out.println(op);
```

```
    }
```

```
}
```

Code : 33

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZG_BuyAndSellStocksWithTransactionFeeInfiniteTransactionsAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int fee = Integer.parseInt(br.readLine());
```

```
        int bstp = -arr[0];
```

```
        int sstp = 0;
```

```
        for (int i = 1; i < arr.length; i++) {
```

```
            int nsstp = 0;
```

```
            int nbstp = 0;
```

```
            if (sstp - arr[i] > bstp) {
```

```
                nbstp = sstp - arr[i];
```

```
            } else {
```

```
                nbstp = bstp;
```

```
            }
```

```
            if (bstp + arr[i] - fee > sstp) {
```

```
                nsstp = bstp + arr[i] - fee;
```

```
            } else {
```

```
                nsstp = sstp;
```

```
            }
```

```
            bstp = nbstp;
```

```
            sstp = nsstp;
```

```
        }
```

```
        System.out.println(sstp);
```

```
    }
```

```
}
```

Code : 34

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZH_BuyAndSellStocksWithCooldownInfiniteTransactionAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int bstp = -arr[0];
```

```
        int sstp = 0;
```

```
        int cstp = 0;
```

```
        for (int i = 1; i < arr.length; i++) {
```

```
            int nbstp = 0;
```

```
            int nsstp = 0;
```

```
            int ncstp = 0;
```

```
            if (cstp - arr[i] > bstp) {
```

```
                nbstp = cstp - arr[i];
```

```
            } else {
```

```
                nbstp = bstp;
```

```
            }
```

```
            if (bstp + arr[i] > sstp) {
```

```
                nsstp = bstp + arr[i];
```

```
            } else {
```

```
                nsstp = sstp;
```

```
            }
```

```
            if (sstp > cstp) {
```

```
                ncstp = sstp;
```

```
            } else {
```

```
                ncstp = cstp;
```

```
            }
```

```
            bstp = nbstp;
```

```
            sstp = nsstp;
```

```
            cstp = ncstp;
```

```
        }
```

```
        System.out.println(Math.max(sstp, cstp));
```

```
    }
```

```
}
```

Code : 35

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZI_BuyAndSellStocksTwoTransactionsAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        int n = Integer.parseInt(br.readLine());
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            arr[i] = Integer.parseInt(br.readLine());
```

```
        }
```

```
        int misf = arr[0];
```

```
        int[] ps = new int[arr.length];
```

```
        for (int i = 1; i < arr.length; i++) {
```

```
            if (arr[i] < misf) {
```

```
                misf = arr[i];
```

```
            }
```

```
            if (arr[i] - misf > ps[i - 1]) {
```

```
                ps[i] = arr[i] - misf;
```

```
            } else {
```

```
                ps[i] = ps[i - 1];
```

```
            }
```

```
        }
```

```
        int masf = arr[arr.length - 1];
```

```
        int[] pb = new int[arr.length];
```

```
        for (int i = arr.length - 2; i >= 0; i--) {
```

```
            if (arr[i] > masf) {
```

```
                masf = arr[i];
```

```
            }
```

```
            if (masf - arr[i] > pb[i + 1]) {
```

```
                pb[i] = masf - arr[i];
```

```
            } else {
```

```
                pb[i] = pb[i + 1];
```

```
            }
```

```
        }
```

```
        int mp = Integer.MIN_VALUE;
```

```
        for (int i = 0; i < arr.length; i++) {
```

```
            if (ps[i] + pb[i] > mp) {
```

```
                mp = ps[i] + pb[i];
```

```
            }
```

```
        }
```

```
        System.out.println(mp);
```

```
    }
```

```
}
```

Code : 36

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZJ_BuyAndSellStocksKTransactionsAllowed {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int[] arr = new int[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            arr[i] = scn.nextInt();
```

```
        }
```

```
        int k = scn.nextInt();
```

```
        int[][] dp = new int[k + 1][n];
```

```
        for (int t = 1; t <= k; t++) {
```

```
            for (int d = 1; d < arr.length; d++) {
```

```
                int max = dp[t][d - 1];
```

```
                for (int pd = 0; pd < d; pd++) {
```

```
                    int ptilltm1 = dp[t - 1][pd];
```

```
                    int ptth = arr[d] - arr[pd];
```

```
                    if (ptilltm1 + ptth > max) {
```

```
                        max = ptilltm1 + ptth;
```

```
                    }
```

```
                }
```

```
                dp[t][d] = max;
```

```
            }
```

```
        }
```

```
        System.out.println(dp[k][n - 1]);
```

```
    }
```

```
}
```

Code : 37

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZK_LongestIncreasingSubsequence {

    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        int n = scn.nextInt();
        int[] arr = new int[n];
        for (int i = 0; i < n; i++) {
            arr[i] = scn.nextInt();
        }
        int omax = 0;
        int[] dp = new int[n];
        for (int i = 0; i < dp.length; i++) {
            int max = 0;
            for (int j = 0; j < i; j++) {
                if (arr[j] < arr[i]) {
                    if (dp[j] > max) {
                        max = dp[j];
                    }
                }
            }
            dp[i] = max + 1;
            if (dp[i] > omax) {
                omax = dp[i];
            }
        }
        System.out.println(omax);
    }
}
```


Code : 38

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZL_LongestBitonicSubsequence {

    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        int n = scn.nextInt();
        int[] arr = new int[n];
        for (int i = 0; i < n; i++) {
            arr[i] = scn.nextInt();
        }
        int omax = 0;
        int[] dp = new int[n];
        for (int i = 0; i < dp.length; i++) {
            int max = 0;
            for (int j = 0; j < i; j++) {
                if (arr[j] < arr[i]) {
                    if (dp[j] > max) {
                        max = dp[j];
                    }
                }
            }
            dp[i] = max + 1;
            if (dp[i] > omax) {
                omax = dp[i];
            }
        }
        System.out.println(omax);
    }
}
```

Code : 39

```
package Topic_20_DynamicProgramming;
```

```
import java.io.BufferedReader;
```

```
import java.io.InputStreamReader;
```

```
public class ZM_LongestCommonSubsequence {
```

```
    public static void main(String[] args) throws Exception {
```

```
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
```

```
        String str1 = br.readLine();
```

```
        String str2 = br.readLine();
```

```
        int[][] dp = new int[str1.length() + 1][str2.length() + 1];
```

```
        for (int i = dp.length - 2; i >= 0; i--) {
```

```
            for (int j = dp[0].length - 2; j >= 0; j--) {
```

```
                if (str1.charAt(i) == str2.charAt(j)) {
```

```
                    dp[i][j] = 1 + dp[i + 1][j + 1];
```

```
                } else {
```

```
                    dp[i][j] = Math.max(dp[i + 1][j], dp[i][j + 1]);
```

```
                }
```

```
            }
```

```
        }
```

```
        System.out.println(dp[0][0]);
```

```
    }
```

```
}
```

Code : 40

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZN_LongestPalindromicSubsequences {
```

```
    // A utility function to get max of two integers
```

```
    static int max(int x, int y) {
```

```
        return (x > y) ? x : y;
```

```
    }
```

```
    // Returns the length of the longest
```

```
    // palindromic subsequence in seq
```

```
    static int lps(String seq) {
```

```
        int n = seq.length();
```

```
        int i, j, cl;
```

```
        // Create a table to store results of subproblems
```

```
        int L[][] = new int[n][n];
```

```
        // Strings of length 1 are palindrome of length 1
```

```
        for (i = 0; i < n; i++)
```

```
            L[i][i] = 1;
```

```
        // Build the table. Note that the lower
```

```
        // diagonal values of table are
```

```
        // useless and not filled in the process.
```

```
        // The values are filled in a manner similar
```

```
        // to Matrix Chain Multiplication DP solution (See
```

```
        // https://www.geeksforgeeks.org/matrix-chain-multiplication-dp-8/).
```

```
        // cl is length of substring
```

```
        for (cl = 2; cl <= n; cl++) {
```

```
            for (i = 0; i < n - cl + 1; i++) {
```

```
                j = i + cl - 1;
```

```
                if (seq.charAt(i) == seq.charAt(j) && cl == 2)
```

```
                    L[i][j] = 2;
```

```
                else if (seq.charAt(i) == seq.charAt(j))
```

```
                    L[i][j] = L[i + 1][j - 1] + 2;
```

```
                else
```

```
                    L[i][j] = max(L[i][j - 1], L[i + 1][j]);
```

```
            }
```

```
        }
```

```
        return L[0][n - 1];
```

```
    }
```

```
    /* Driver program to test above functions */
```

```
    public static void main(String args[]) {
```

```
        Scanner sc = new Scanner(System.in);
```

```
        String str = sc.nextLine();
```

```
        String seq = str;
```

```
        int n = seq.length();
```

```
        System.out.println(lps(seq));
```

```
    }
```

```
}
```

Code : 41

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZO_LongestPalindromicSubstring {
```

```
    public static void main(String[] args) throws Exception {
        Scanner scn = new Scanner(System.in);
        String str = scn.nextLine();
        boolean[][] dp = new boolean[str.length()][str.length()];
        int len = 0;
        for (int g = 0; g < str.length(); g++) {
            for (int i = 0, j = g; j < str.length(); i++, j++) {
                if (g == 0) {
                    dp[i][j] = true;
                } else if (g == 1) {
                    if (str.charAt(i) == str.charAt(j)) {
                        dp[i][j] = true;
                    } else {
                        dp[i][j] = false;
                    }
                } else {
                    if (str.charAt(i) == str.charAt(j) && dp[i + 1][j - 1] == true) {
                        dp[i][j] = true;
                    } else {
                        dp[i][j] = false;
                    }
                }
            }

            if (dp[i][j]) {
                len = g + 1;
            }
        }
    }
```

```
    System.out.println(len);
```

```
}
```

```
}
```

Code : 42

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Arrays;
```

```
import java.util.Scanner;
```

```
public class ZP_RussianDollEnvelopes {
```

```
    public static class Envelope implements Comparable<Envelope> { //1
```

```
        int w;
```

```
        int h;
```

```
        Envelope(int w, int h) {
```

```
            this.w = w;
```

```
            this.h = h;
```

```
        }
```

```
        public int compareTo(Envelope o) { //1
```

```
            return this.w - o.w;
```

```
        }
```

```
    }
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = Integer.parseInt(scn.nextLine()); //2
```

```
        Envelope[] envlps = new Envelope[n];
```

```
        for (int i = 0; i < n; i++) {
```

```
            String line = scn.nextLine();
```

```
            String[] parts = line.split(" ");
```

```
            int w = Integer.parseInt(parts[0]);
```

```
            int h = Integer.parseInt(parts[1]);
```

```
            envlps[i] = new Envelope(w, h);
```

```
        }
```

```
        Arrays.sort(envlps); //4
```

```
        int[] dp = new int[n]; //5
```

```
        int omax = 0; //omax=overall max
```

```
        for (int i = 0; i < dp.length; i++) {
```

```
            int max = 0;
```

```
            for (int j = 0; j < i; j++) {
```

```
                if (envlps[j].h < envlps[i].h && envlps[j].w < envlps[i].w) { //6
```

```
                    if (dp[j] > max) {
```

```
                        max = dp[j];
```

```
                    }
```

```
                }
```

```
            }
```

```
            dp[i] = max + 1;
```

```
            if (dp[i] > omax) { //7
```

```
                omax = dp[i];
```

```
            }
```

```
        }
```

```
        System.out.println(omax); //8
```

```
    }
```

```
}
```


Code : 43

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZQ_CatalanNumber {
```

```
    public static void main(String[] args) throws Exception {  
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        long[] dp = new long[n + 1];  
        dp[0] = 1; //since 0th Catalan number is 1
```

```
        dp[1] = 1; //since 1st Catalan number is also 1
```

```
        for (int i = 2; i < dp.length; i++) {  
            for (int j = 0; j < i; j++) {  
                dp[i] += dp[j] * dp[i - 1 - j];  
            }  
        }
```

```
        System.out.println(dp[n]); //nth Catalan number  
    }
```

```
}
```

Code : 44

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class ZR_NumberOfBsts {  
  
    public static void main(String[] args) throws Exception {  
        Scanner scn = new Scanner(System.in);  
  
        int n = scn.nextInt();  
  
        long[] dp = new long[n + 1];  
        dp[0] = 1; //since 0th Catalan number is 1  
  
        dp[1] = 1; //since 1st Catalan number is also 1  
  
        for (int i = 2; i < dp.length; i++) {  
            for (int j = 0; j < i; j++) {  
                dp[i] += dp[j] * dp[i - 1 - j];  
            }  
        }  
  
        System.out.println(dp[n]); //nth Catalan number  
    }  
}
```


Code : 45

```
package Topic_20_DynamicProgramming;
```

```
import java.util.Scanner;
```

```
public class Z_PaintFence {
```

```
    public static void main(String[] args) throws Exception {
```

```
        Scanner scn = new Scanner(System.in);
```

```
        int n = scn.nextInt();
```

```
        int k = scn.nextInt();
```

```
        long[] dp = new long[n + 1];
```

```
        long same = k * 1;
```

```
        long diff = k * (k - 1);
```

```
        long total = same + diff;
```

```
        for (int i = 3; i <= n; i++) {
```

```
            same = diff * 1;
```

```
            diff = total * (k - 1);
```

```
            total = same + diff;
```

```
        }
```

```
        System.out.println(total);
```

```
    }
```

```
}
```

