

**Hindi Vidya Prachar Samiti's  
Ramniranjan Jhunhunwala College of Arts, Science and  
Commerce(Autonomous)**

**Programme: MSc. (Statistics)**

**Part-1**

**Semester-1**

**Practical- 2.4.3**

**Branching Process**

1. A branching process has offspring distribution  $a = (1/4, 1/4, 1/2)$  where a discrete r.v.  $X$  takes values  $\{0,1,2\}$ . Find the following :

- i. Mean of offspring distribution.
- ii.  $P(s)$ , probability generating function of offspring distribution.
- iii. The probability of ultimate extinction. Verify graphically.

2. A branching process has offspring distribution  $a = (1/6, 1/2, 1/3)$  where a discrete r.v.  $X$  takes values  $\{0,1,2\}$ . Find the following –

- i. Mean of offspring distribution.
- ii.  $P(s)$ , probability generating function of offspring distribution.
- iii. The probability of ultimate extinction. Verify graphically.

3. Assume the offspring distribution is uniform on  $\{0,1,2,3,4\}$ . Find the probability of ultimate extinction.

4. Find probability of ultimate extinction whose offspring distribution is Poisson with parameter  $\lambda = 0.80, 2$ .

5. Find probability of ultimate extinction whose offspring distribution is geometric with parameter  $p = 0.7, 0.2$ .