

Practice problems aimed to improve your coding skills.

- PRACTICE-02\_SCAN-PRINT
- PRACTICE-03\_TYPES
- LAB-PRAC-02\_SCAN-PRINT
- LAB-PRAC-01
- PRACTICE-04\_COND
- **BONUS-PRAC-02**
- LAB-PRAC-03\_TYPES
- PRACTICE-05 COND-LOOPS
- LAB-PRAC-04 COND
- LAB-PRAC-05\_CONDLOOPS
- PRACTICE-07\_LOOPS-ARR
- LAB-PRAC-06\_LOOPS
- LAB-PRAC-07\_LOOPS-ARR
- LABEXAM-PRAC-01 MIDSEM
- PRACTICE-09 PTR-MAT
- LAB-PRAC-08 ARR-STR
- PRACTICE-10 MAT-FUN
- LAB-PRAC-09 PTR-MAT
- LAB-PRAC-10\_MAT-FUN
- PRACTICE-11 FUN-PTR
- LAB-PRAC-11\_FUN-PTR
- LAB-PRAC-12 FUN-STRUC
- LABEXAM-PRAC-02 ENDSEM
- LAB-PRAC-13\_STRUC-NUM
  - Too tired to create a story part I
  - 2 Too tired to create a story part II
  - 2 Too tired to create a story part III
  - Point Proximity
  - The Bisection Method
  - The pace is too fast
  - A Question on Quadrilaterals
  - 2 The Trapezoidal Technique
  - Constrained Candy Crush
  - Major Mobile Madness
  - The Newton Raphson Method
  - The Palindrome Decomposition
- LAB-PRAC-14\_SORT-MISC

## The Newton Raphson Method

LAB-PRAC-13\_STRUC-NUM

## The Newton Raphson Method [20 marks]

-----

## **Problem Statement**

The Newton-Raphson method is a popular method for finding the roots of functions. It is a precursor to the Newton method for optimizing non-linear functions. Given a real-valued function  $f:\mathbb{R}\to\mathbb{R}$ , and an initial guess of the root  $x_0$ , the NR method iteratively improves this guess using the following update rule

$$x_1=x_0-rac{f(x_0)}{f'(x_0)}$$

Then, using  $x_1$ , it obtains a (hopefully) better estimate of the root  $x_2$  as

$$x_2 = x_1 - rac{f(x_1)}{f'(x_1)}$$

Thus, you can get  $x_{t+1}$  using  $x_t$ . You have to stop updating when  $abs(x_t - x_{t+1}) < eps$  i.e. the absolute difference between two successive estimates is strictly smaller than eps where eps will be given to you. When the above happens, simply output  $x_{t+1}$  as your output.

The first line will contain n, a strictly positive number indicating the degree of the polynomial, followed by a space, followed by eps a floating point number (store it as a double). The second line will contain n+1 integers (may be zero or negative or positive), containing the coefficients of the polynomial from zero degree to max degree i.e. if the polynomial is a cubic (i.e. n = 3)

$$f(x) = a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

then we will give you the coefficients as

dcba

The last line will contain  $x_0$  the initial guess you should use.  $x_0$  will not be an integer and you should store it as a double. Run the NR algorithm as shown above and give your output correct to 2 decimal places, using the %0.2lf flag in printf.

## Caution

- 1. All coefficients of the polynomial will be integers but they may be zero or negative too.
- 2. You may use the fabs() function from math.h to compute the absolute value of a non-integral number.
- 3. The roots and intermediate values in your computations may be non-integral. Use double variables for all your computations.
- 4. Be careful while computing the derivative polynomial.
- 5. We assure you that if you follow the above rules correctly, you will never run into a divide-by-zero situation.
- 6. Be careful about extra/missing lines and extra/missing spaces in your output.

-----

EXAMPLE:
INPUT
2 0.01
1 -2 1
3.00
OUTPUT: 1.01

Grading Scheme:

Total marks: [20 Points]

There will be no partial grading in this question. An exact match will receive full marks whereas an incomplete match will receive 0 points. Please be careful of missing/extra spaces and missing/lines (take help of visible test cases). Each visible test case is worth 1 point and each hidden test case is worth 2 points. There are 2 visible and 4 hidden test cases.

**¥**¶ Start Solving! (/editor/practice/6265)