



Decision Trees

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Predicting potential loan defaults

What makes a loan risky?



Credit history explained

Did I pay previous loans on time?

Example: excellent, good, or fair

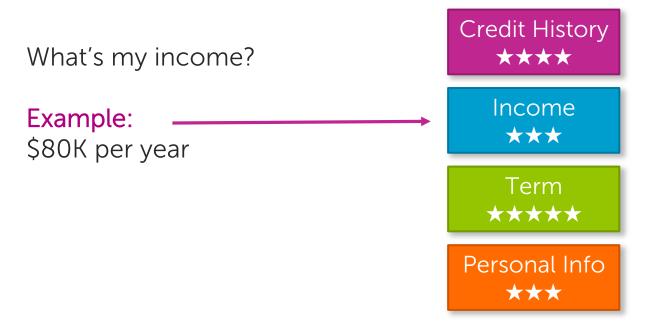
Credit History

Income

Term

Personal Info

Income



Loan terms

How soon do I need to pay the loan?

Example: 3 years,

5 years,...









Personal information

Age, reason for the loan, marital status,...

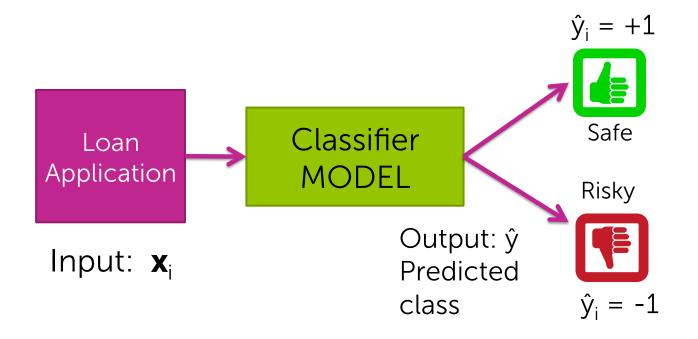
Example: Home loan for a married couple



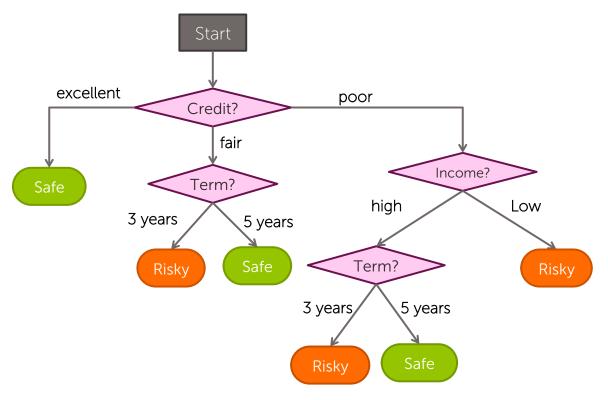
Intelligent application



Classifier review

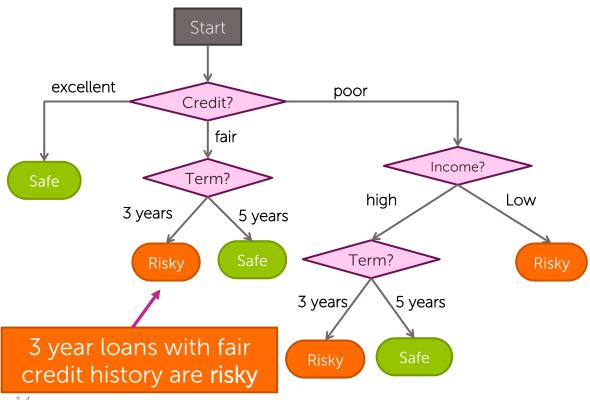


This module ... decision trees

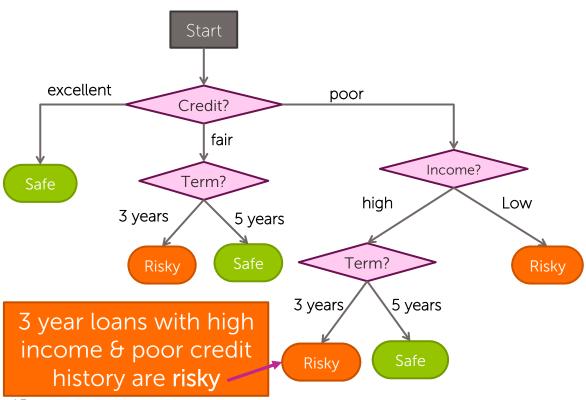


Decision trees: Intuition

What does a decision tree represent?



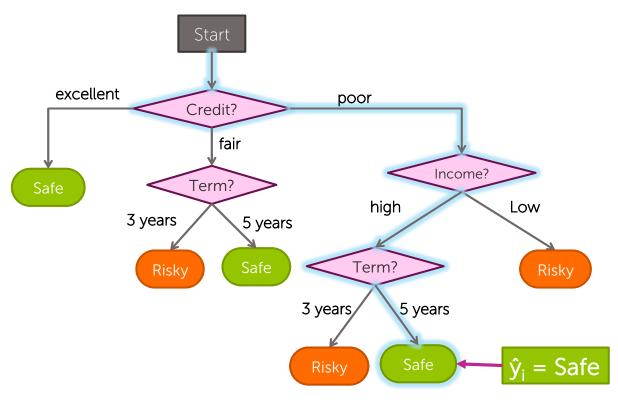
What does a decision tree represent?



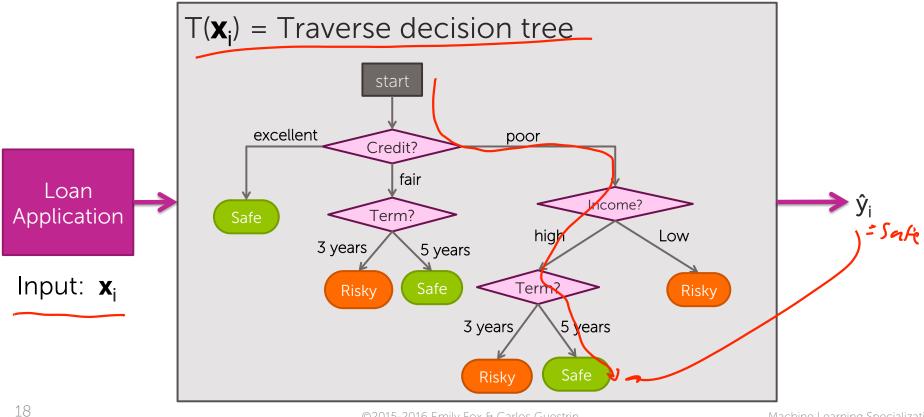
15

Scoring a loan application

 \mathbf{x}_{i} = (Credit = poor, Income = high, Term = 5 years)



Decision tree model

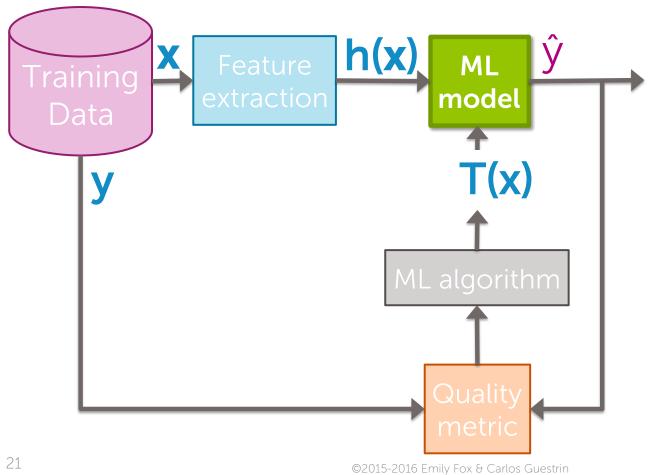


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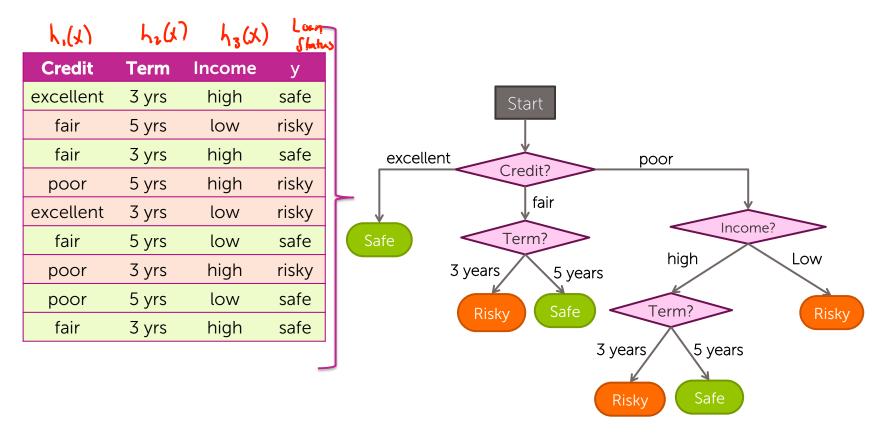
Decision tree learning task

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Carlos Guestrin Machine Learning Specialization

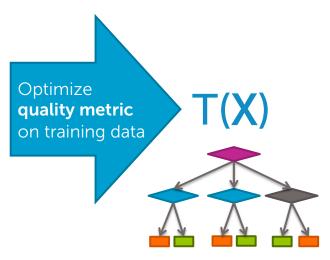
Learn decision tree from data?



Decision tree learning problem

Training data: N observations (\mathbf{x}_i, y_i)

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



Quality metric: Classification error

Error measures fraction of mistakes

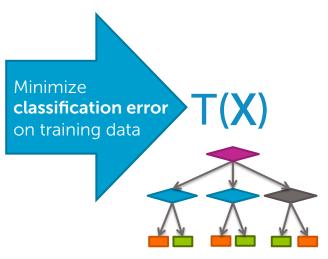
```
Error = # incorrect predictions # examples
```

- Best possible value : 0.0

- Worst possible value: 1.0

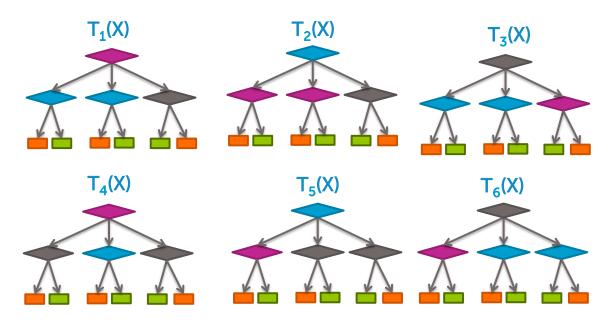
Find the tree with lowest classification error

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



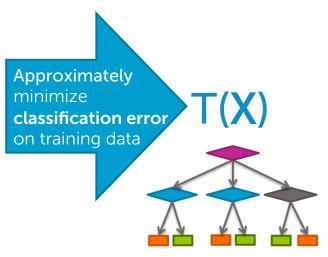
How do we find the best tree?

Exponentially large number of possible trees makes decision tree learning hard! (NP-hard problem)



Simple (greedy) algorithm finds "good" tree

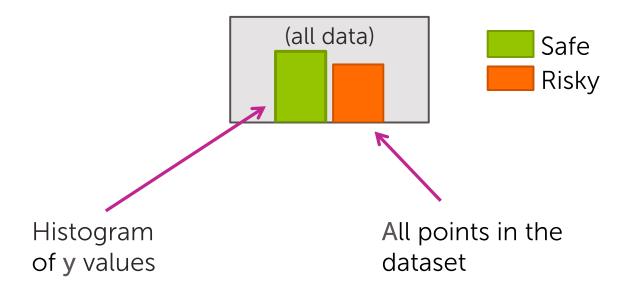
Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



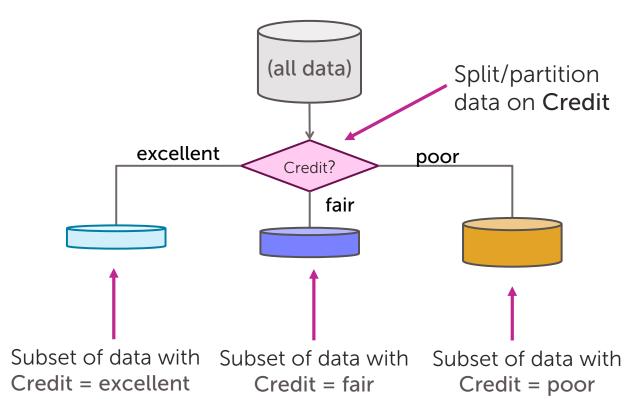
Greedy decision tree learning: *Algorithm outline*

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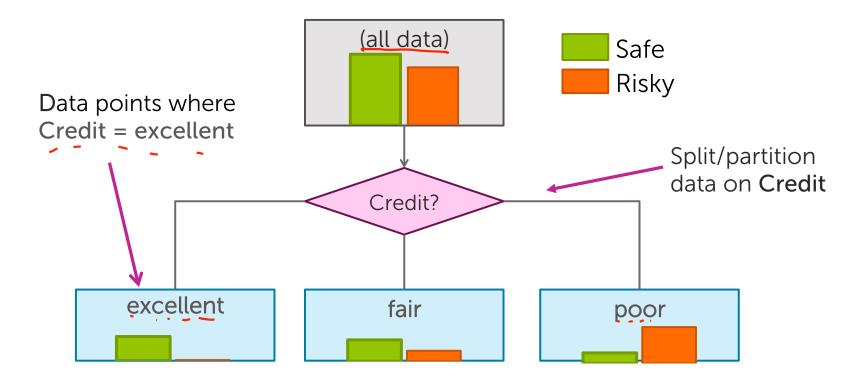
Step 1: Start with an empty tree



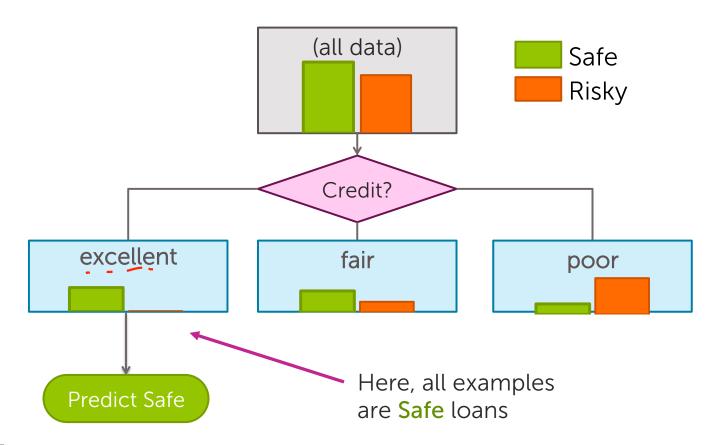
Step 2: Split on a feature



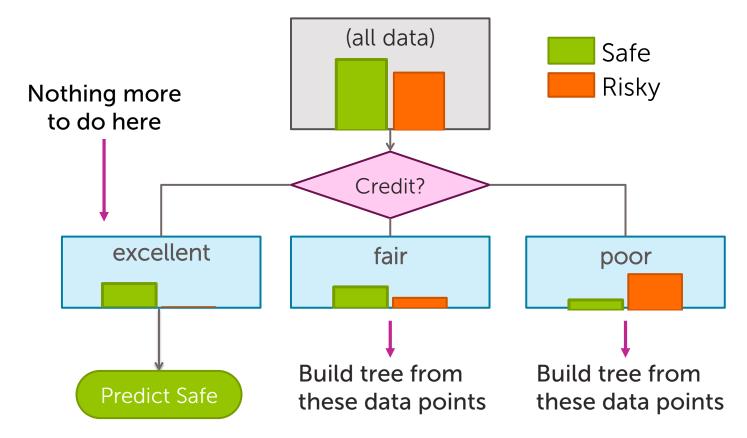
Feature split explained



Step 3: Making predictions



Step 4: Recursion



Greedy decision tree learning

- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
 - Step 3: If nothing more to, make predictions
 - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Problem 1: Feature split selection

Problem 2: Stopping condition

Recursion

Feature split learning

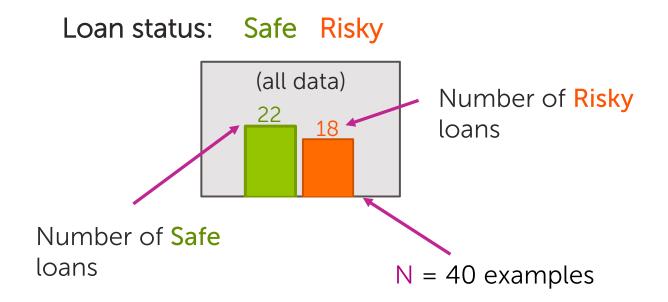
Decision stump learning

Start with the data

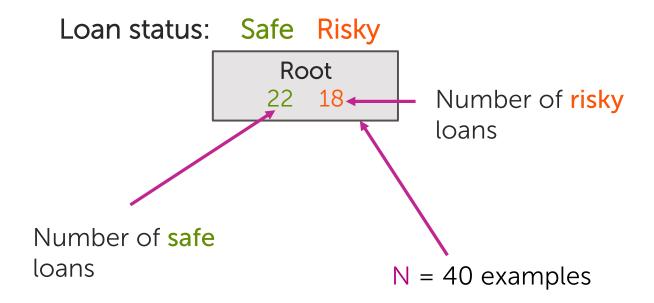
Assume N = 40, 3 features

Credit	Term	Income	У
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

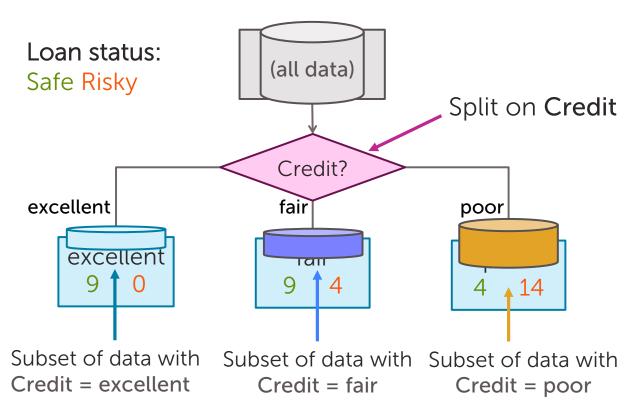
Start with all the data



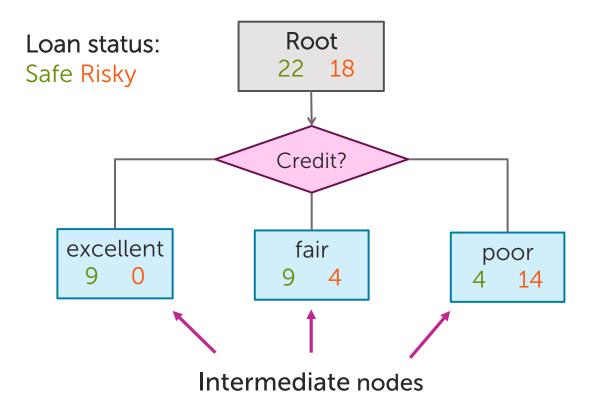
Compact visual notation: Root node



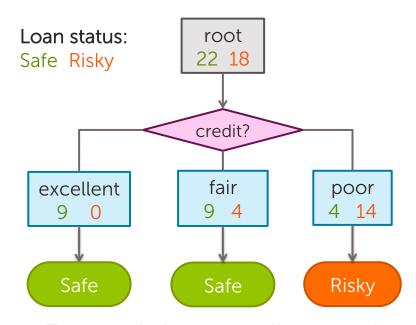
Decision stump: Single level tree



Visual Notation: Intermediate nodes



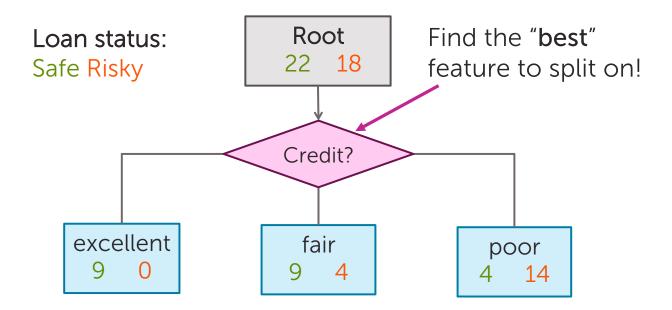
Making predictions with a decision stump



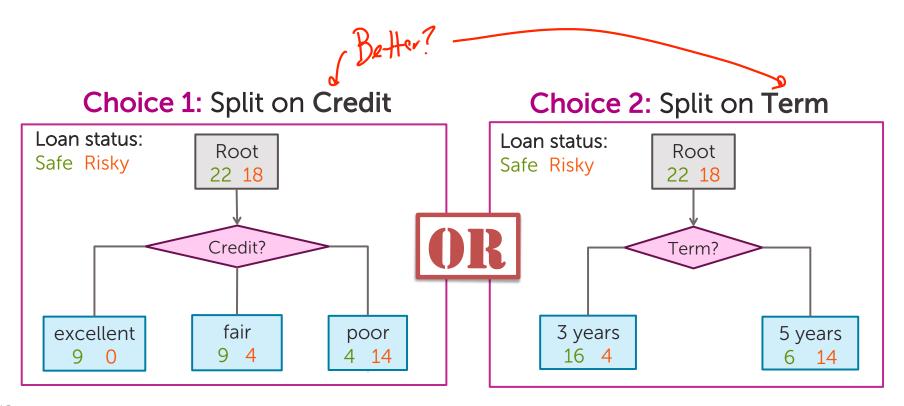
For each intermediate node, set $\hat{y} = majority value$

Selecting best feature to split on

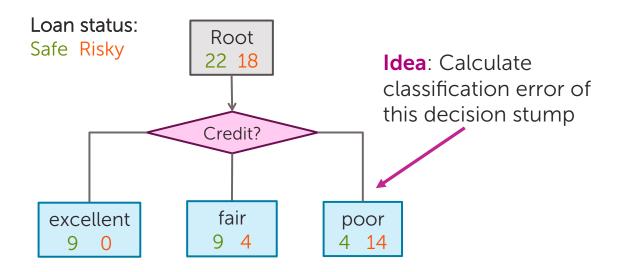
How do we learn a decision stump?



How do we select the best feature?



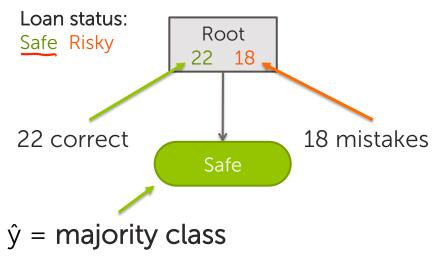
How do we measure effectiveness of a split?



Error = # mistakes # data points

Calculating classification error

- Step 1: \hat{y} = class of majority of data in node
- Step 2: Calculate classification error of predicting ŷ for this data

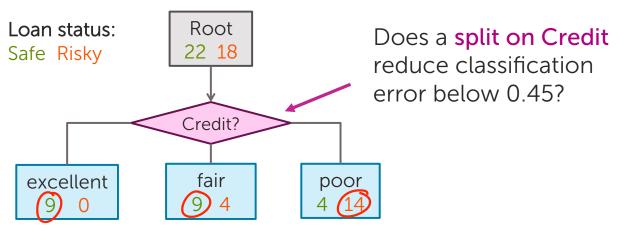


Error =	18
=	

Tree	Classification error	
(root)	0.45	

Choice 1: Split on credit history?

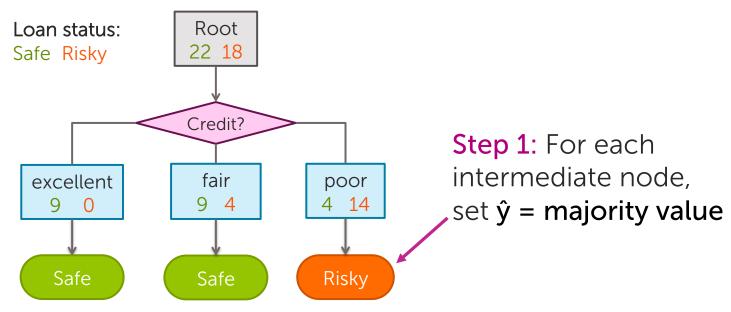
Choice 1: Split on Credit



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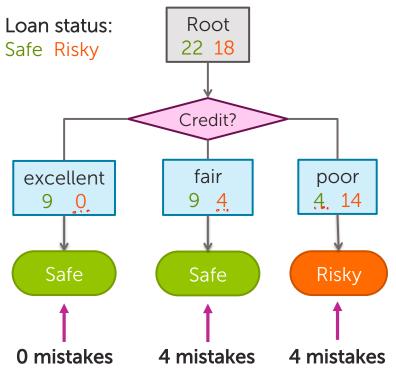
How good is the split on Credit?

Choice 1: Split on Credit



Split on Credit: Classification error

Choice 1: Split on Credit



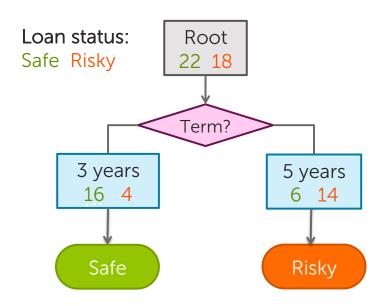
$$Error = \underbrace{4+4}_{40}$$

$$= 0.20$$

Tree	Classification error	
(root)	0.45	
Split on credit	0.2	

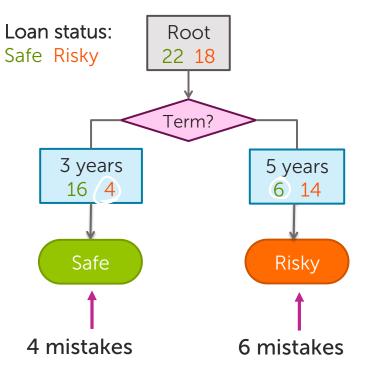
Choice 2: Split on Term?

Choice 2: Split on Term



Evaluating the split on Term

Choice 2: Split on Term



$$Error = \frac{4+6}{40}$$
$$= 0.25$$

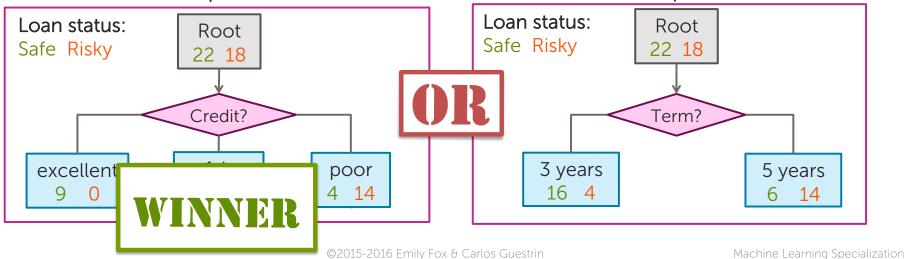
Tree	Classification error	
(root)	0.45	
Split on credit	0.2	
Split on term	0.25	

Choice 1 vs Choice 2

Tree	Classification error	
(root)	0.45	
split on credit	0.2	-First
split on loan term	0.25	35

Choice 1: Split on Credit

Choice 2: Split on Term



57

Feature split selection algorithm

- Given a subset of data M (a node in a tree)
- For each feature $h_i(x)$: < credit, ten, income
 - 1. Split data of M according to feature $h_i(x)$
 - 2. Compute classification error split
- Chose feature $h^*(x)$ with lowest classification error f

Greedy decision tree learning

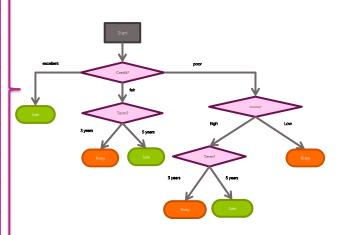
- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
 - Step 3: If nothing more to, make predictions
 - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Pick feature split leading to lowest classification error

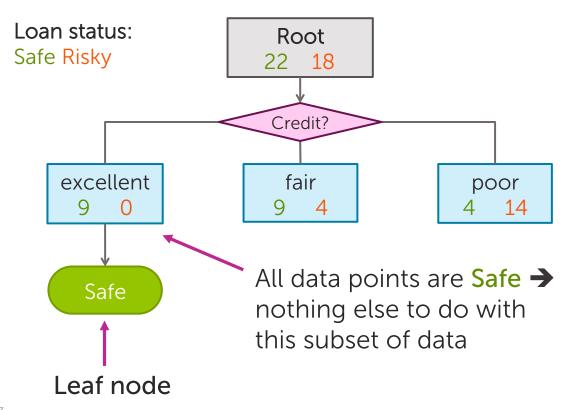
Decision Tree Learning: Recursion & Stopping conditions

Learn decision tree from data?

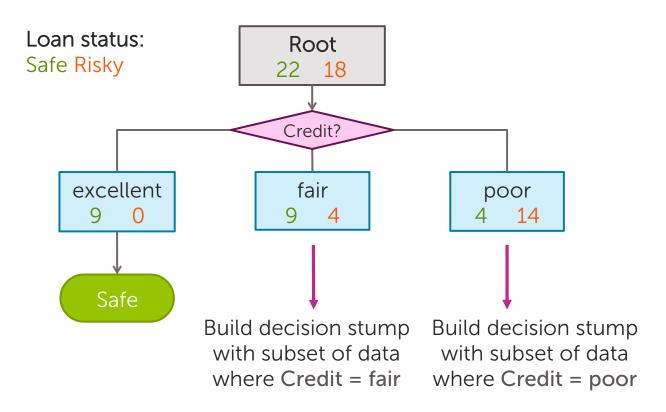
Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
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poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



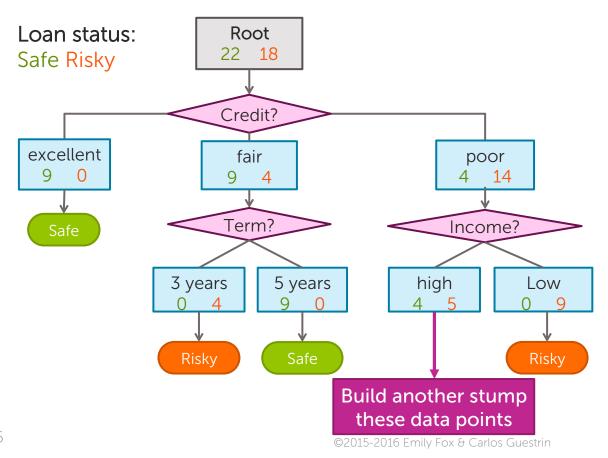
We've learned a decision stump, what next?



Tree learning = Recursive stump learning

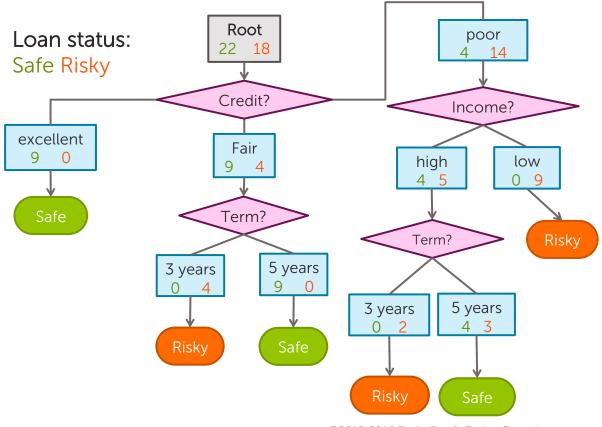


Second level



65

Final decision tree



66

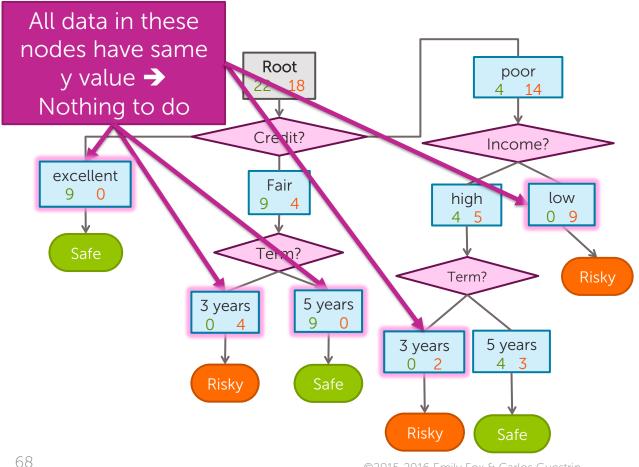
Simple greedy decision tree learning

Pick best feature to split on Learn decision stump with this split For each leaf of decision stump, recurse When do we stop??? 67

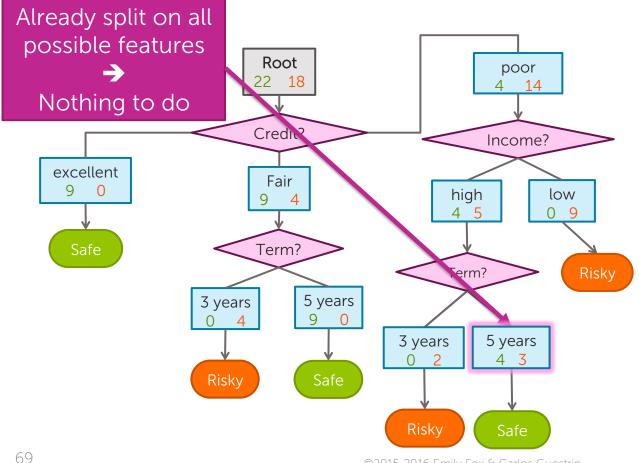
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Stopping condition 1: All data agrees on y



Stopping condition 2: Already split on all features



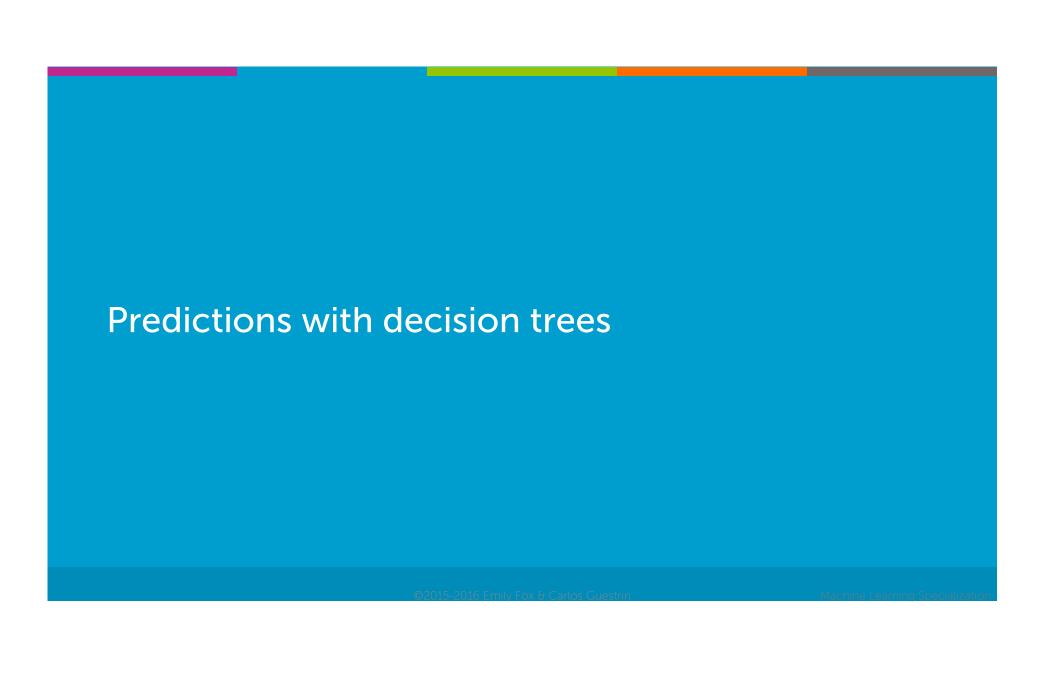
Greedy decision tree learning

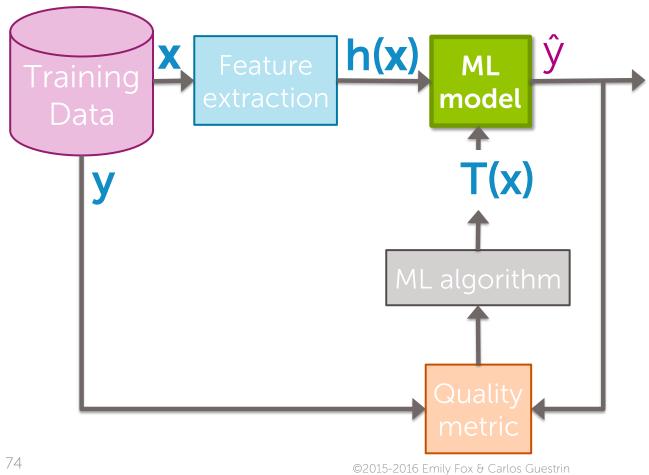
- Step 1: Start with an empty tree
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Pick feature split leading to lowest classification error

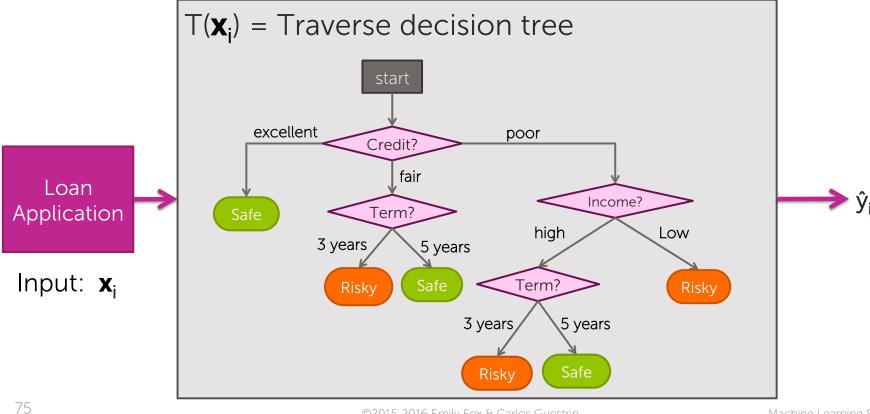
Stopping conditions 1 & 2

Recursion



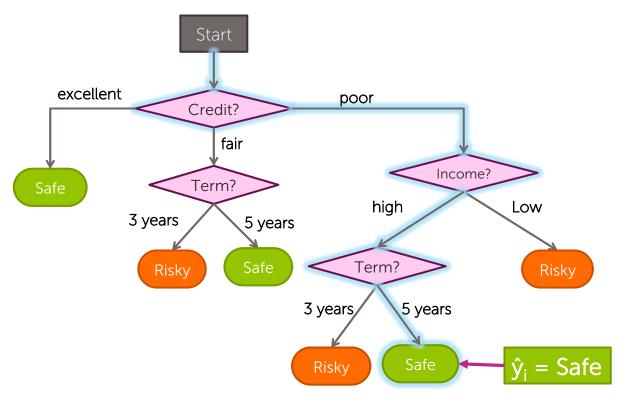


Decision tree model



Traversing a decision tree

 \mathbf{x}_{i} = (Credit = poor, Income = high, Term = 5 years)



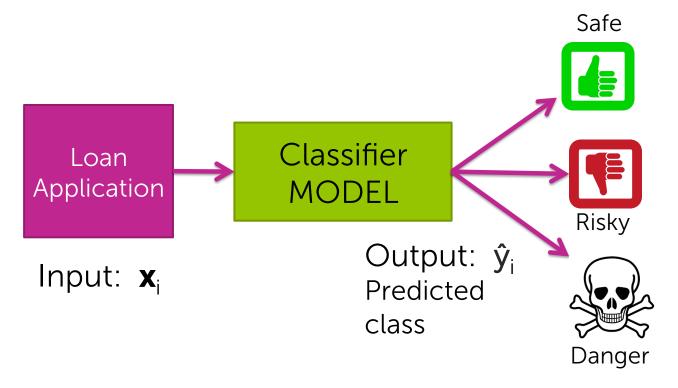
Decision tree prediction algorithm

predict(tree_node, input)

- If current tree_node is a leaf:
 - return majority class of data points in leaf
- else:
 - next_note = child node of tree_node whose feature value agrees with input
 - return predict(next_note, input)

Multiclass classification & predicting probabilities

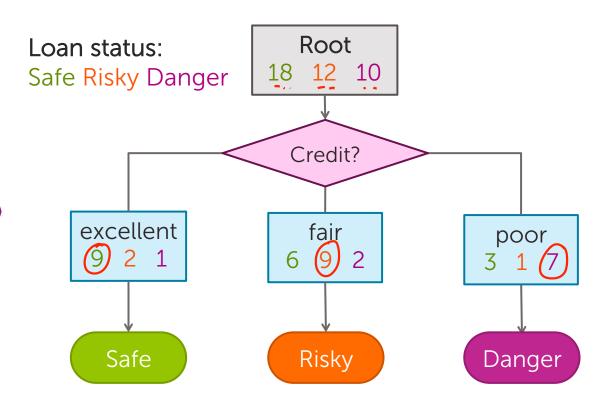
Multiclass prediction



Multiclass decision stump

N = 40, 1 feature, 3 classes

Credit	у	
excellent	safe	
fair	risky	
fair	safe	
poor	danger	
excellent	risky	
fair	safe	
poor	danger	
poor	safe	
fair	ir safe	

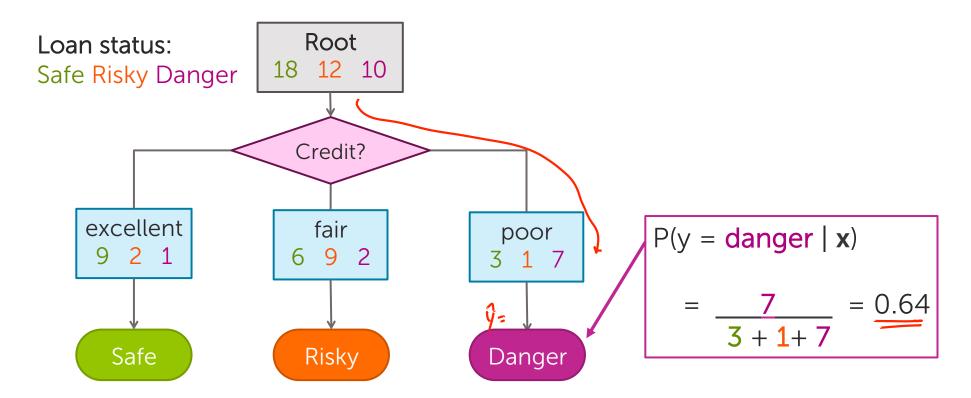


81

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Predicting probabilities with decision trees

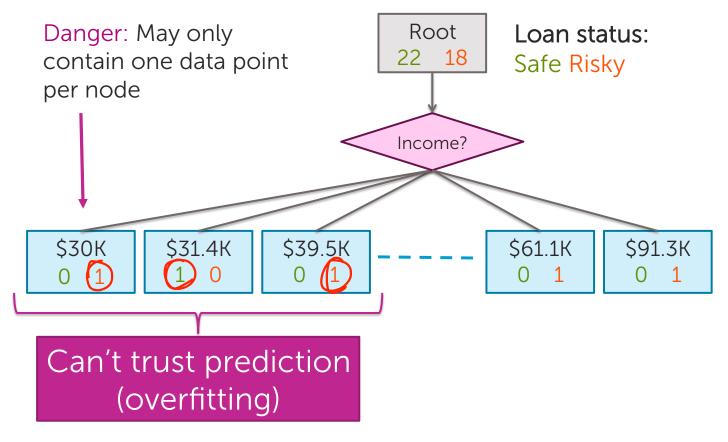


Decision tree learning: *Real valued features*

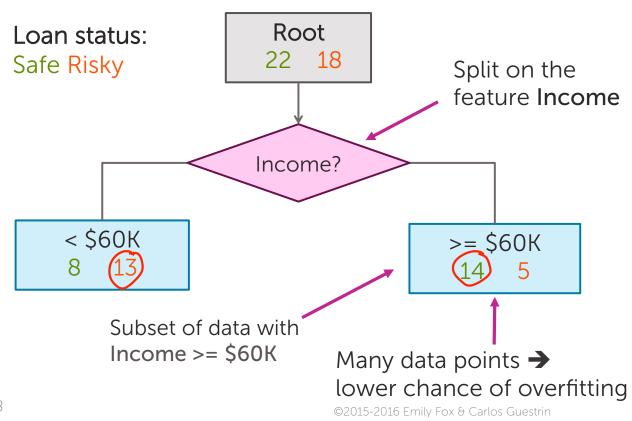
How do we use real values inputs?

Income	Credit	Term	у
\$105 K	excellent	3 yrs	Safe
\$112 K	good	5 yrs	Risky
\$73 K	fair	3 yrs	Safe
\$69 K	excellent	5 yrs	Safe
\$217 K	excellent	3 yrs	Risky
\$120 K	good	5 yrs	Safe
\$64 K	fair	3 yrs	Risky
\$340 K	excellent	5 yrs	Safe
\$60 K	good	3 yrs	Risky

Split on each numeric value?

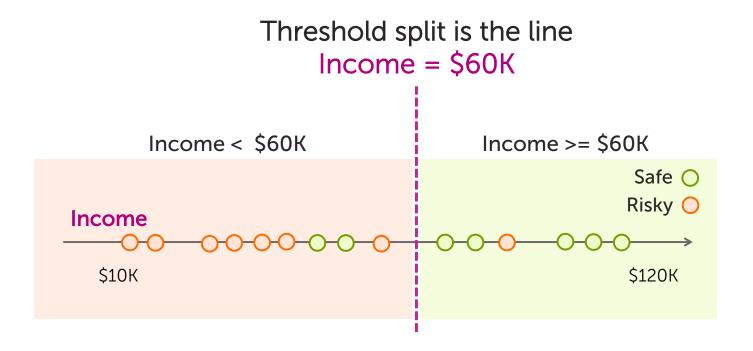


Alternative: Threshold split

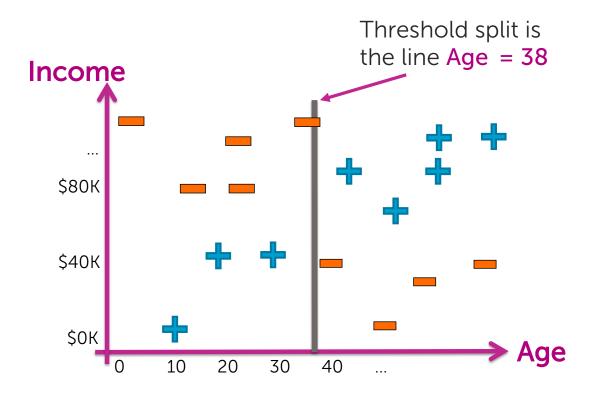


88

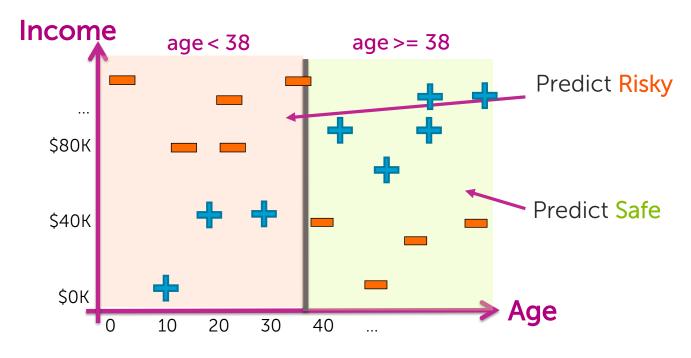
Threshold splits in 1-D



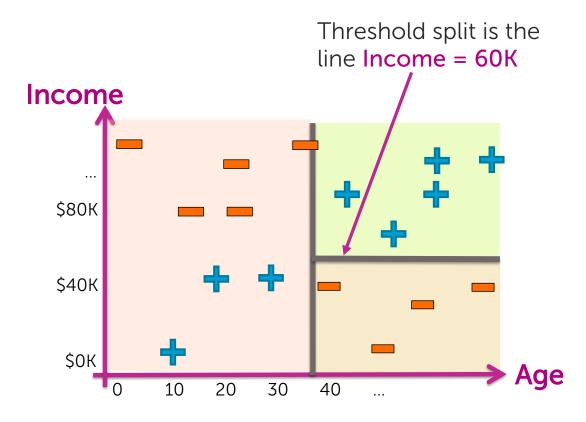
Visualizing the threshold split



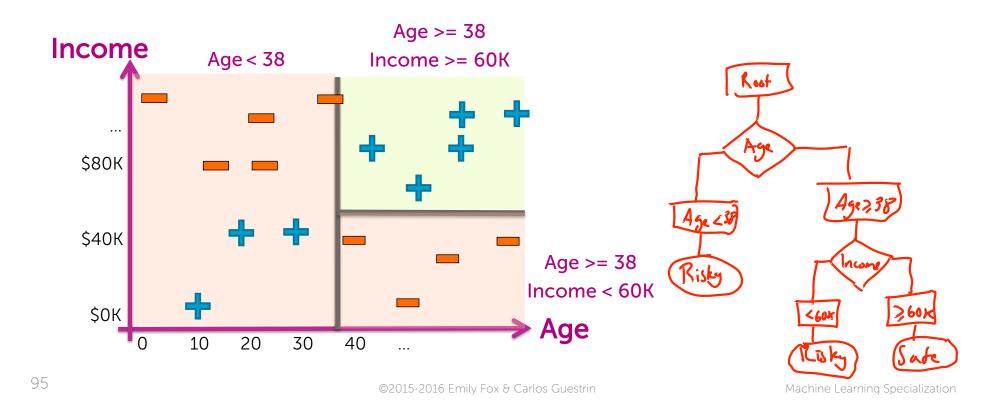
Split on Age >= 38



Depth 2: Split on Income >= \$60K



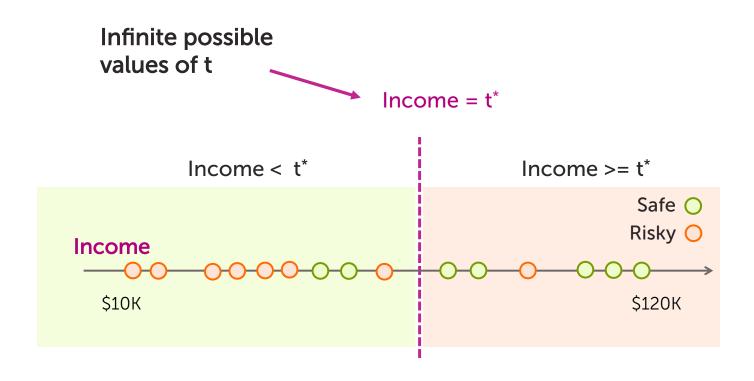
Each split partitions the 2-D space



Finding the best threshold split

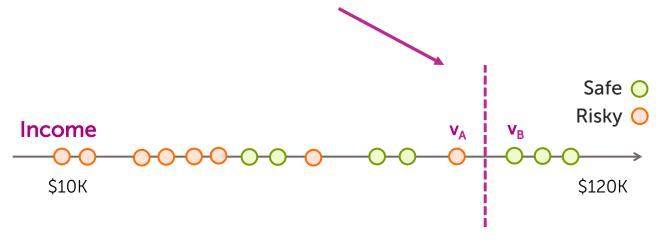


Finding the best threshold split

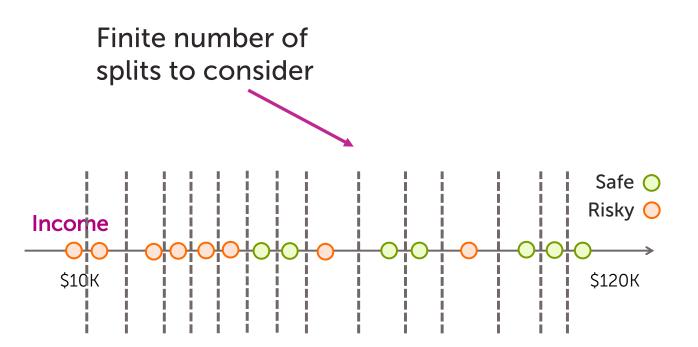


Consider a threshold between points

Same classification error for any threshold split between v_A and v_B



Only need to consider mid-points



Threshold split selection algorithm

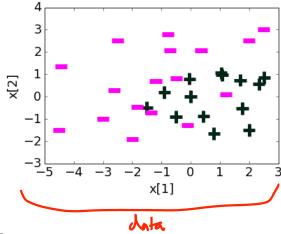
/ Income

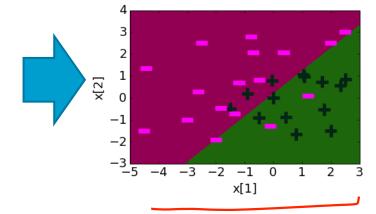
- Step 1: Sort the values of a feature $h_j(\mathbf{x})$: Let $\{\mathbf{v_1}, \mathbf{v_2}, \mathbf{v_3}, ... \mathbf{v_N}\}$ denote sorted values
- Step 2:
 - -Fori = 1 ... N-1
 - Consider split $t_i = (v_i + v_{i+1}) / 2$
 - Compute classification error for treshold split $h_j(\mathbf{x}) >= \mathbf{t}_i$
 - Chose the t with the lowest classification error



Logistic regression

Feature	Value	Weight Learned
h ₀ (x)	1	0.22
h ₁ (x)	x [1]	1.12
h ₂ (x)	x [2]	-1.07



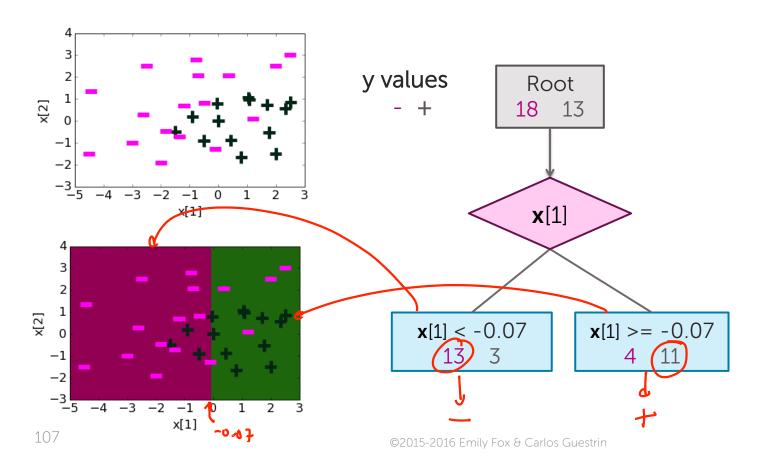


106

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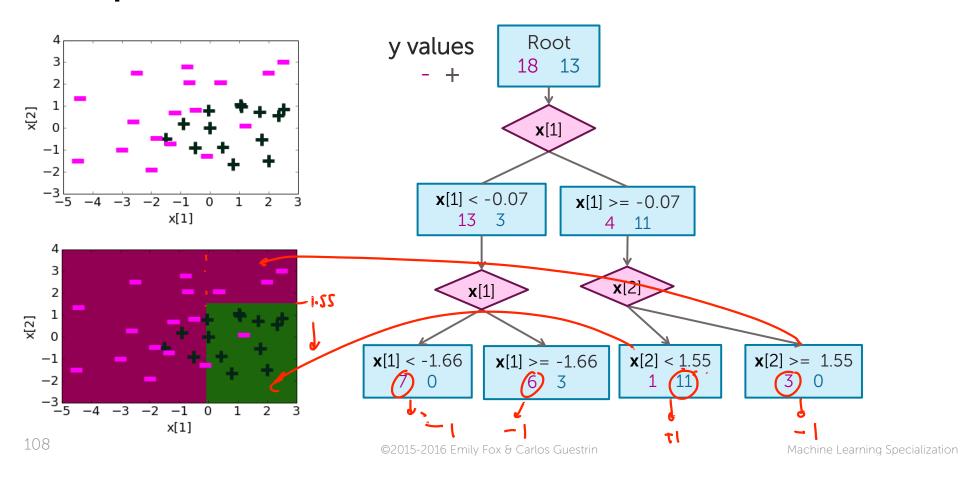
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Depth 1: Split on x[1]

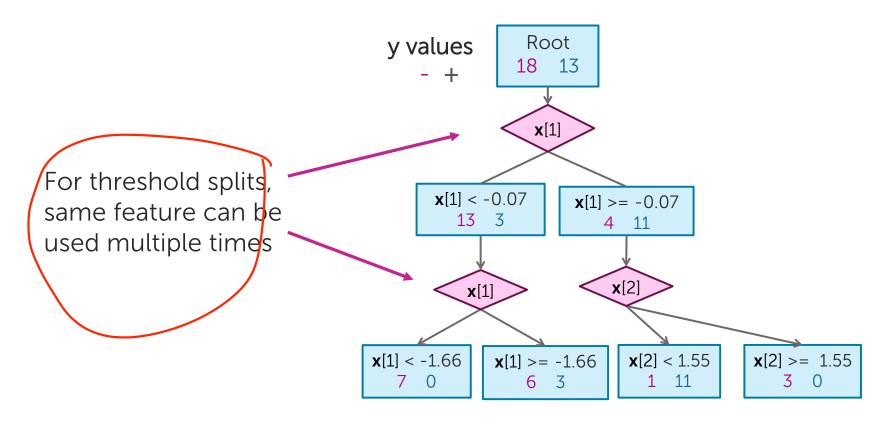


Machine Learning Specialization

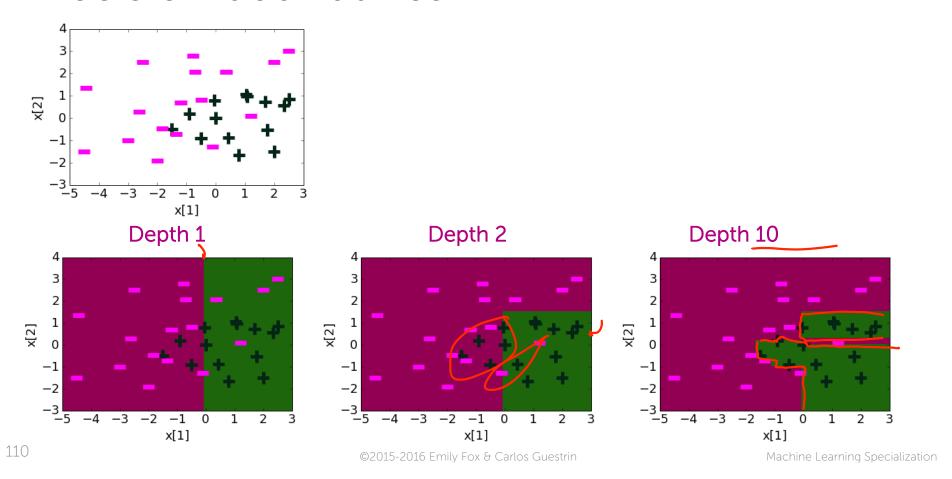
Depth 2



Threshold split caveat

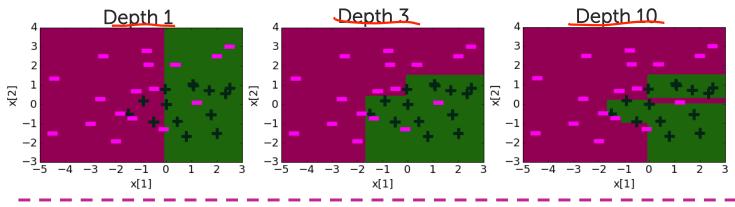


Decision boundaries

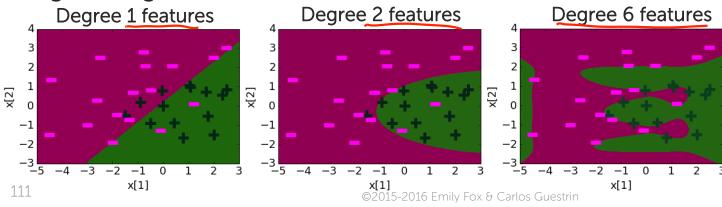


Comparing decision boundaries

Decision Tree



Logistic Regression



Machine Learning Specialization

Summary of decision trees

What you can do now

- Define a decision tree classifier
- Interpret the output of a decision trees
- Learn a decision tree classifier using greedy algorithm
- Traverse a decision tree to make predictions
 - Majority class predictions
 - Probability predictions
 - Multiclass classification

Thank you to Dr. Krishna Sridhar



Dr. Krishna Sridhar Staff Data Scientist, Dato, Inc.