

# Inflation Targeting and Financial Stability

very very preliminary

Nicolas Caramp <sup>1</sup>    Sanjay R. Singh <sup>2</sup>    Alan M. Taylor <sup>3</sup>

<sup>1</sup>UC Davis

<sup>2</sup>Federal Reserve Bank of San Francisco and UC Davis

<sup>3</sup>Columbia University and NBER and CEPR

September 2024

Liquidity in Macroeconomics Workshop, UC Davis

The views expressed herein are those of the author and not necessarily those of the Bank of England, the Federal Reserve Bank of San Francisco, or the Federal Reserve System.

develop a connection between some secular trends in macro and finance

- inflation targeting regime since the 90s
- decline in natural rate of interest measured on nominal bonds
- increase in debt to GDP ratio (Schularick and Taylor 2012)

Q1: Can inflation targeting monetary policy regime be a plausible explanation?

Q2: When does inflation targeting pose financial stability risks

- under supply shocks, nominal interest rates are countercyclical
- under demand shocks, nominal interest rates are low when demand is low
- more likely to hit ZLB in a low  $r^*$  environment when
  1. demand shocks dominate
  2. central bank aggressive in fighting inflation

monetary policy and financial instability: in the short and the medium run

- Borio & White (2004), Woodford (2012), Gourio Kashyap & Sim (2018), Borio Disyatat and Rungcharoenkitkul (2019), Cairo & Sim (2023), Boissay Collard Gali & Manea (2024)

macro-finance trends

- Del Negro Giannone Giannoni Tambalotti (2017), Farhi & Gourio (2020), Eggertsson Robbins & Wold (2023)
- Jorda Schularick & Taylor (2016), Mian Straub & Sufi (2023), Laudati (2024)
- Campbell Pflueger Viceira (2020), Miller Paron & Wachter (2023), Gourio & Ngo (2024)

zero lower bound and financial crises

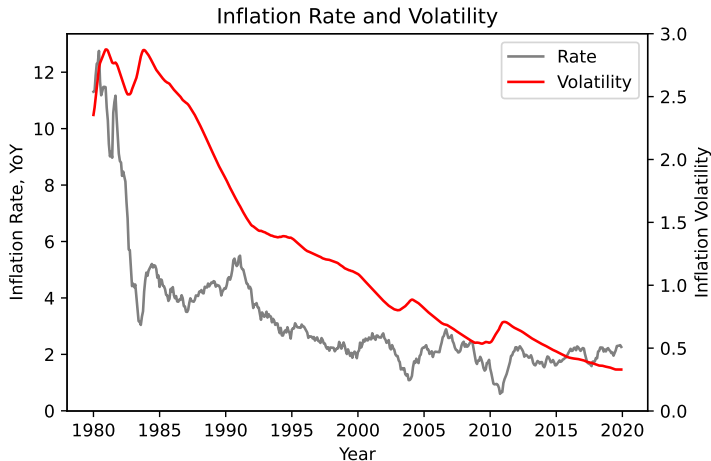
- Eggertsson & Krugman (2012), Korinek & Simsek (2016), Del Negro Eggertsson Ferrero Kiyotaki (2017), Guerrieri & Lorenzoni (2017), Caballero & Farhi (2018), Caramp & Singh (2023)
- Schularick & Taylor (2012), Kumhof Ranciere & Winant (2015), Mian Sufi Verner (2017)

1. Stylized facts, connect  $r^*$  to inflation targeting
2. Simple macro-finance model
3. Analytical results: representative agent
4. Analytical results: endogenous debt
5. Conclusion

## Fact 1: Inflation targeting

---

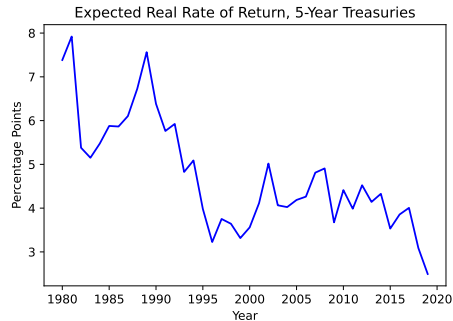
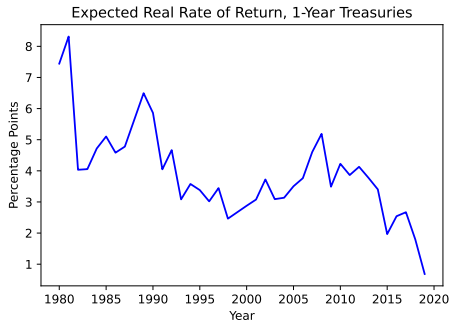
Post Volcker, central banks adopted inflation targeting in the early 90s.



## Fact 2: Decline in real rate and $r^*$

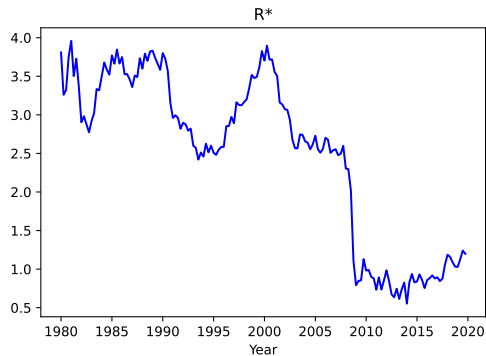
---

### Secular decline in real rates



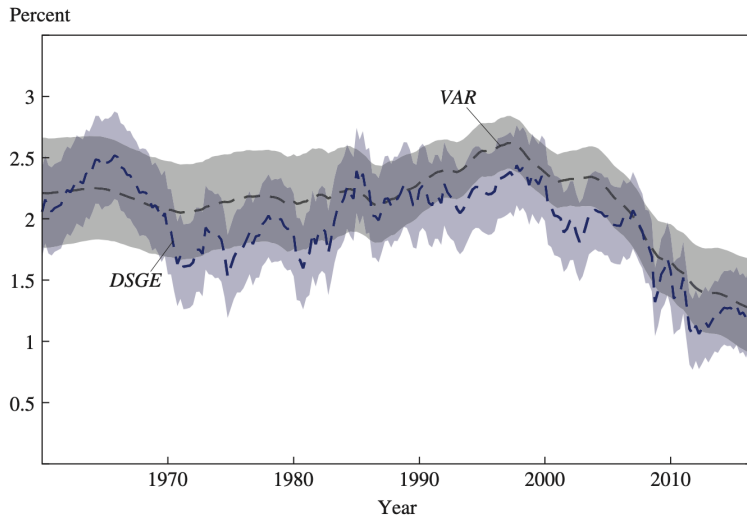
## Fact 2: Decline in real rate and $r^*$

---



Source: Holston, Laubach and Williams (2017) estimate from FRBNY

## Fact 2: Decline in real rate and $r^*$



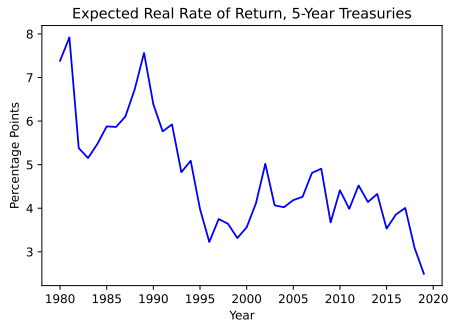
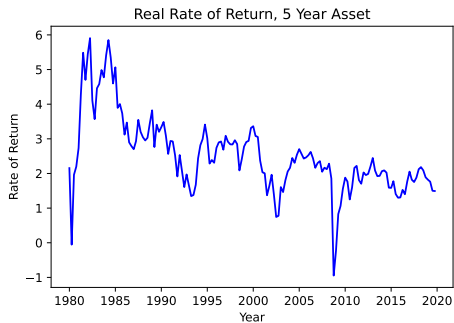
Source: Del Negro, Giannone, Giannone & Tambalotti (2017)



## Fact 2: Decline in real rate and $r^*$

---

### Real return on a counterfactual real asset

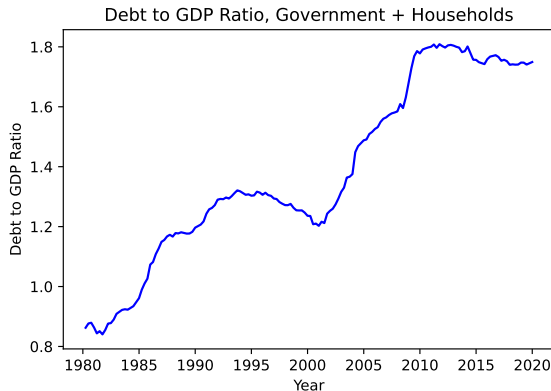


Source: Chernov & Mueller (2012) until 2002 and TIPS 5-year after on left panel

### Fact 3: Rise in debt

---

Debt owed by households in the US increased since 1980

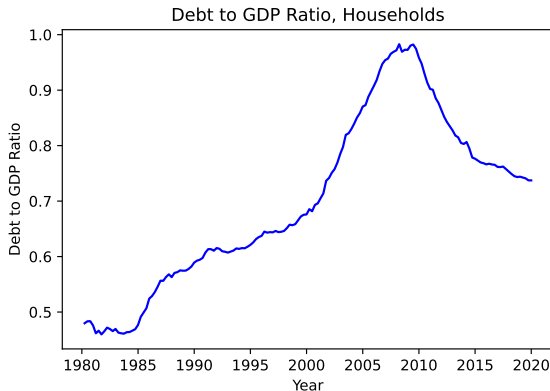


Source: Mian Sufi & Straub (2023)

### Fact 3: Rise in household debt

---

Debt owed by households in the US increased since 1980



Source: Our calculations based on Mian Sufi & Straub (2023)

## Step 1: estimate inflation targeting coefficient

---

Estimate Taylor rule coefficient using OLS (Carvalho and Nechio 2021)

$$r_t = \alpha_{aux} + \rho_{1,aux}r_{t-1} + \rho_{2,aux}r_{t-2} + \beta_{aux}\pi_t + \gamma_{aux}X_t + \epsilon_t$$

$$\hat{\rho} = \rho_{1,aux} + \rho_{2,aux}; \quad \hat{\phi}_{\pi} = \frac{\beta_{aux}}{1 - \hat{\rho}}$$

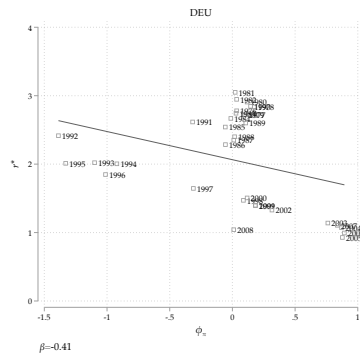
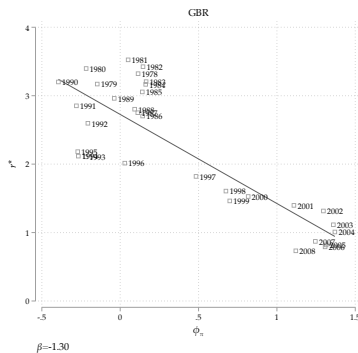
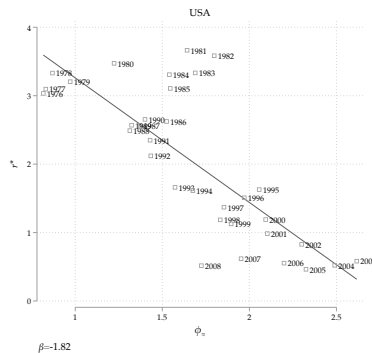
Data over 1976–2008

USA, GBR, DEU

20-year rolling window

## Step 2: Connecting $r^*$ and Inflation targeting

Scatter plot of  $\hat{\phi}_\pi$  and Laubach-Williams one-sided  $r^*$  estimate



## A Stylized model: Environment

---

Eggertsson & Krugman (2012) with aggregate risk

- endowment, cashless economy
- Three dates: 0, 1, and 2
- Two agents: Savers (s) and Borrowers (b)
- One assets: one-period nominal bond
- borrowers constrained by a debt limit
- shocks: discount factor (demand) and endowment (supply) realized at date 1
- date 1 central bank policy with a Taylor rule targeting inflation
- Price level is price of consumption basket in units of the cashless numeraire
- policy regimes: low or high inflation targeting coefficient  $\phi_\pi$

## Households

---

Unit mass of households (borrowers, b, or savers, s)

$$\max \mathbb{E}_0 \sum_{t=0}^{\infty} \beta_j^t \xi_{j,t} \log C_{j,t}; \quad j = \{b, s\}; \quad \beta_b < \beta_s \equiv \beta$$

preference shock only for savers

$$\xi_{s,t} = \xi_t = \xi_{t-1}^{\rho} e^{\epsilon_{d,t}}, \quad \epsilon_{d,t} \sim N\left(-\frac{\sigma_d^2}{2}, \sigma_d^2\right), \quad \xi_0 = \xi_{b,t} = 1.$$

Save/borrow in a one-period nominal bond with net nominal return  $i_t$  subject to a borrowing constraint:

$$\mathbb{E}_t \left[ \frac{(1 + i_t) B_{j,t+1}}{P_{t+1}} \right] \geq -\bar{d}_t.$$

Gross inflation rate  $\Pi_t \equiv \frac{P_t}{P_{t-1}}$ , and date-0 ex-ante natural rate:  $R_0^* \equiv \mathbb{E}_t \left[ \frac{1+i_0}{\Pi_1} \right]$

## Households' budget and endowments

---

Assuming that households' start with no debt, their budget constraints are given by

$$\begin{aligned}P_0 C_{j,0} + B_{j,1} &\leq P_0 Y_0 \\P_1 C_{j,1} + B_{j,2} &\leq P_1 Y_1 + (1 + i_0) B_{j,1} \\P_2 C_{j,2} &\leq P_2 Y_2 + (1 + i_1) B_{j,2}\end{aligned}$$

Date 1 and 2 endowment  $Y_t$  depends on realization of  $\epsilon_{s,1}$

$$Y_t = Y_{t-1}^\rho e^{\epsilon_{s,t}}, \quad \epsilon_{s,t} \sim N\left(-\frac{\sigma_s^2}{2}, \sigma_s^2\right), \quad Y_0 = 1$$

Assume borrowers sufficiently impatient that their borrowing constraint is always binding.



date-1 interest rate rule:

$$1 + i_1 = R_1^* \left( \frac{\Pi_1}{\bar{\Pi}} \right)^{\phi_\pi}$$

with  $\phi_\pi > 1$ , and  $\bar{\Pi} = 1$  is central bank's inflation target.

As in Eggertsson & Krugman,

assume that  $\Pi_2 = \bar{\Pi}$  since there are no shocks in  $t = 2$

normalize  $P_0 = 1$

Policy regime characterized by  $\phi_\pi$ .

Savers are on their Euler equation at dates 0 and 1

$$1 = \beta \mathbb{E}_t \left[ \frac{\xi_{t+1}}{\xi_t} \frac{C_{s,t}}{C_{s,t+1}} \frac{1 + i_t}{\Pi_{t+1}} \right]$$

Budget (and borrowing) constraints of all agents are satisfied at all dates

bond market clears:

$$B_{s,t} = -B_{b,t}, \quad \forall t = \{1, 2\}$$

and given central bank policy as discussed above.

## Zero debt equilibrium (representative agent limit)

---

Assume  $\bar{d}_0 = \bar{d}_1 = 0 \implies$  effectively a representative agent model:

$$1 = \beta \mathbb{E}_t \left[ \underbrace{\frac{\xi_{t+1}}{\xi_t} \frac{Y_t}{Y_{t+1}}}_{M_{t+1}} \frac{1 + i_t}{\Pi_{t+1}} \right]$$

$$1 + i_1 = R_1^* \Pi_1^{\phi_\pi}; \quad \Pi_2 = 1 \quad P_0 = 1$$

$$R_0^* = \mathbb{E}_0 \left[ \frac{1 + i_0}{\Pi_1} \right]$$

where  $R_1^*$  is an exogenous deterministic constant known at time 0.

## Zero debt equilibrium: solution

---

Date-1 and Date-2 pricing kernels/ SDFs:

$$M_1 = \frac{\xi_1}{Y_1} = e^{\epsilon_d - \epsilon_s}; \quad M_2 = \left( \frac{Y_1}{\xi_1} \right)^{1-\rho} = e^{(\epsilon_s - \epsilon_d)(1-\rho)}$$

Date -1 inflation and nominal interest rate:

$$\Pi_1 = \left( \frac{1}{\beta R_1^*} \right)^{\frac{1}{\phi\pi}} \times e^{\frac{1-\rho}{\phi\pi}\epsilon_d} \times e^{-\frac{1-\rho}{\phi\pi}\epsilon_s}; \quad 1 + i_1 = R_1^* \Pi_1^{\phi\pi}$$

## Zero debt equilibrium: solution

---

Expected real return on a nominal bond:

$$R_0^* = \frac{1}{\beta} \times e^{\frac{1-\rho}{\phi\pi}\sigma_d^2} \times e^{\left(\frac{1-\rho}{\phi\pi}-1\right)\sigma_s^2}$$

Expected return on a hypothetical real bond

$$R_{0,real}^* = \frac{1}{\beta} \times e^{-\sigma_s^2}$$

Inflation premium:

$$\frac{R_0^*}{R_{0,real}^*} = e^{\frac{1-\rho}{\phi\pi}\sigma_d^2} \times e^{\frac{1-\rho}{\phi\pi}\sigma_s^2}$$

## Zero debt equilibrium

---

Only **demand** shocks ( $\sigma_s = 0$ ):

$$R_0^* = \frac{1}{\beta} \times e^{\frac{1-\rho}{\phi\pi}\sigma_d^2}; \quad R_{0,real}^* = \frac{1}{\beta}$$

$$\Pi_1 = \left( \frac{1}{\beta R_1^*} \right)^{\frac{1}{\phi\pi}} \times e^{\frac{1-\rho}{\phi\pi}\epsilon_d}; \quad M_1 = e^{\epsilon_d}; \quad M_2 = e^{-\epsilon_d(1-\rho)}$$

- $\uparrow \sigma_d \implies \uparrow R_0^*$  (higher compensation for inflation risk)
- $\uparrow \phi_\pi \implies \downarrow R_0^*$  (lower compensation for inflation risk)
- Date 1 inflation is “pro-cyclical” with respect to the date-1 SDF
- Date 1 nominal rate is “counter-cyclical” with respect to the date-2 SDF

## Zero debt equilibrium

---

Only **supply** shocks ( $\sigma_d = 0$ ):

$$R_0^* = \frac{1}{\beta} \times e^{(\frac{1-\rho}{\phi\pi}-1)\sigma_s^2}; \quad R_{0,real}^* = \frac{1}{\beta} \times e^{-\sigma_s^2}$$

$$\Pi_1 = \left( \frac{1}{\beta R_1^*} \right)^{\frac{1}{\phi\pi}} \times e^{-\frac{1-\rho}{\phi\pi}\epsilon_s}; \quad M_1 = e^{-\epsilon_s}; \quad M_2 = e^{\epsilon_s(1-\rho)}$$

- $\uparrow \sigma_s \implies$ 
  1.  $\downarrow$  return on real bond (safety premium against aggregate risk)
  2.  $\downarrow R_0^*$  (falls less than real bond return)
  3.  $\uparrow \frac{R_0^*}{R_{0,real}^*}$  (compensation for inflation risk)
- $\uparrow \phi_\pi \implies \downarrow R_0^*$  (lower compensation for inflation risk)
- Date 1 inflation is “pro-cyclical” with respect to the date-1 SDF.
- Date 1 nominal rate is “counter-cyclical” with respect to the date-2 SDF

## Zero debt equilibrium: date-1 interest rate cyclical

---

Date 1 nominal rate is “counter-cyclical” with respect to the date-2 SDF

when supply shocks drive inflation volatility, aggressive inflation targeting (higher  $\phi_{pi}$ )

- reduces inflation volatility
- lower inflation risk premia
- hence lower  $R_0^*$
- counter-cyclical of date-1 interest rates  $\implies$  date 1 nominal rates go up when date-1 endowment falls.  $\implies$  not a potential ZLB type risk scenario



## Zero debt equilibrium: date-1 interest rate cyclical

---

Date 1 nominal rate is “counter-cyclical” with respect to the date-2 SDF

when demand shocks drive inflation volatility, aggressive inflation targeting (higher  $\phi_{pi}$ )

- reduces inflation volatility
- lower inflation risk premia
- hence lower  $R_0^*$
- counter-cyclical of date-1 interest rates  $\implies$  date 1 nominal rates go up when agents are patient to postpone consumption to date 2 from date 1.  $\implies$  a potential ZLB type risk scenario (Eggertsson & Woodford for example)

## Back to the General Case: Equilibrium

---

Savers are on their Euler equation at dates 0 and 1

$$1 = \beta \mathbb{E}_t \left[ \frac{\xi_{t+1}}{\xi_t} \frac{C_{s,t}}{C_{s,t+1}} \frac{1 + i_t}{\Pi_{t+1}} \right]$$

$$\begin{aligned} \forall j = \{b, s\}, \quad P_0 C_{j,0} + B_{j,1} &= P_0 Y_0 \\ P_1 C_{j,1} + B_{j,2} &= P_1 Y_1 + (1 + i_0) B_{j,1} \\ P_2 C_{j,2} &= P_2 Y_2 + (1 + i_1) B_{j,2} \end{aligned}$$

borrower's borrowing constraint binds

$$\mathbb{E}_t \left[ \frac{(1 + i_t) B_{bt+1}}{P_{t+1}} \right] = -\bar{d}_t, \quad \forall t = \{0, 1\}$$

and bond market clears:

$$B_{s,t} = -B_{b,t}, \quad \forall t = \{1, 2\}$$

Now, let's assume that  $\bar{d}_0 > 0$  but  $\bar{d}_1 = 0$ . Then, the Euler equations simplify to

$$1 = \beta \mathbb{E}_0 \left[ \xi_1 \frac{Y_0 - b_{s,1}}{Y_1 + \frac{1+i_0}{\Pi_1} b_{s,1}} \frac{1+i_0}{\Pi_1} \right]$$

$$1 = \beta \mathbb{E}_1 \left[ \frac{\xi_2}{\xi_1} \frac{Y_1 + \frac{1+i_0}{\Pi_1} b_{s,1}}{Y_2} \frac{1+i_1}{\bar{\Pi}} \right]$$

Plugging in the monetary rule in the Euler equation in  $t = 1$ , we get

$$\xi_1^{1-\rho} = \beta R_1^* \frac{Y_1 \Pi_1^{\phi_\pi} + \Pi_1^{\phi_\pi-1} (1+i_0) b_{s,1}}{Y_2}$$

The saver's Euler equation in  $t = 0$  implies

$$1 = \beta \left( 1 - \frac{b_{s,1}}{Y_0} \right) Y_0 \mathbb{E}_0 \left[ \frac{\xi_1}{Y_1 \Pi_1 + (1+i_0) b_{s,1}} \right] (1+i_0)$$

## Log-linear approximation results: demand shocks

---

Log-linearize the system with  $\bar{d}_1 = 0$  around zero debt equilibrium ( $\bar{d}_0 = \bar{d}_1 = 0$ )

$$\hat{b}_{s,1} = \beta e^{-\frac{\phi_\pi - 1}{\phi_\pi^2} \frac{\sigma_d^2}{2} \hat{d}_0}$$

Note that

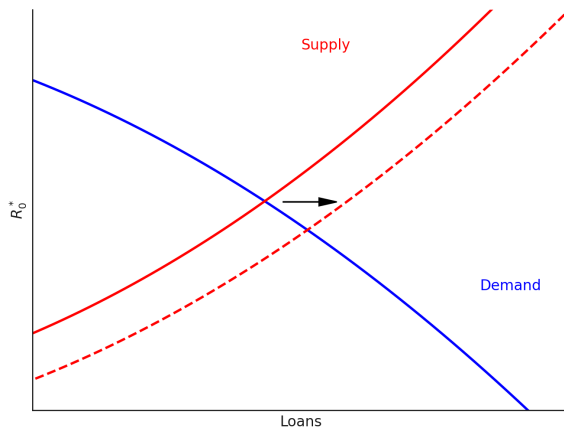
$$\frac{\partial \hat{b}_{s,1}}{\partial \phi_\pi} = \frac{\phi_\pi + 2}{\phi_\pi^3} \frac{\sigma_d^2}{2} \beta e^{-\frac{\phi_\pi - 1}{\phi_\pi^2} \frac{\sigma_d^2}{2} \hat{d}_0} > 0$$

## Intuition

---

Aggressive inflation targeting regime features lower inflation risk premium.

⇒ increases supply of nominal debt by savers



- quantitative effects are somewhat small now
- production economy with nominal rigidities for ZLB to matter
- add other channels such as inequality, non-homotheticity, exogenous risk premia
- add capital to connect to Farhi Gourio macro-finance trends on investment
- long list...

## Conclusion

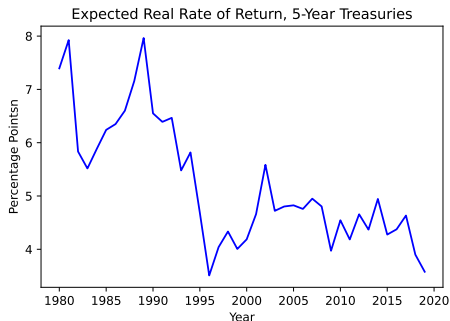
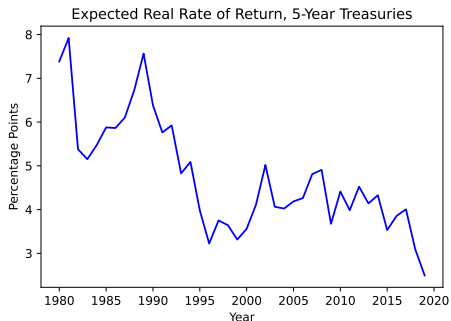
---

- Connect secular trends in macro-finance with a monetary policy regime explanation
- A simple macro finance model seems to get the qualitative patterns

## Fact 2: Decline in real rate and $r^*$

---

### Secular decline in real rates



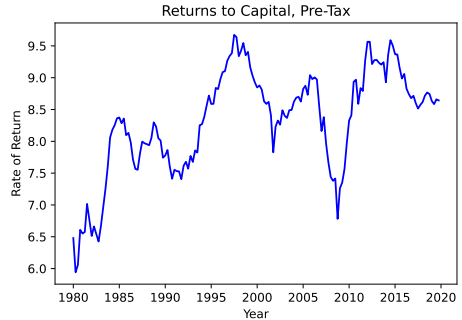
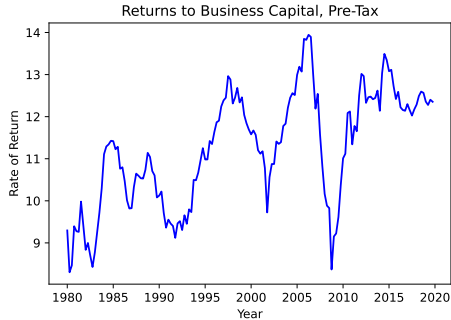
Source: 5 year and 10-yr zero coupon Treasury rates minus expected 5 year ahead and 10 year ahead inflation from Cleveland Fed



## Fact 4: Return to capital

---

Real return to capital stable

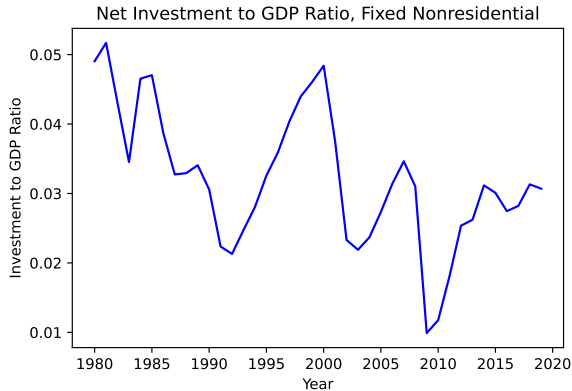


Source: Gomme, Ravikumar, & Rupert (2019)

## Fact 5: Investment/GDP

---

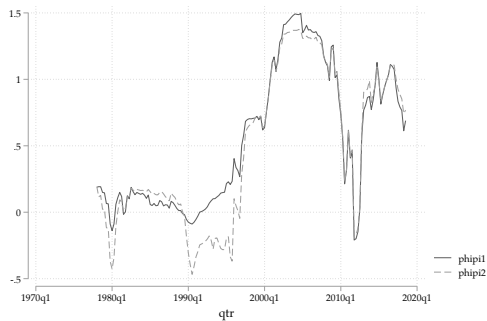
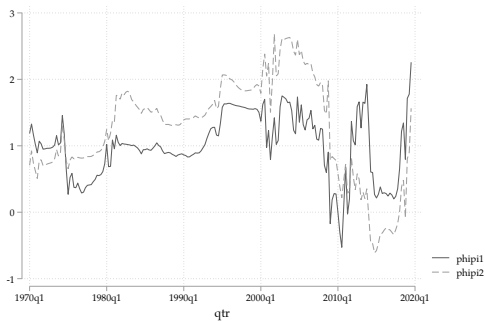
Investment to GDP declined



Source: our calculations

## Taylor rule estimated coefficients

---



Source: USA on the left and GBR on the right