

Plate notation

In Bayesian inference, **plate notation** is a method of representing variables that repeat in a graphical model. Instead of drawing each repeated variable individually, a plate or rectangle is used to group variables into a subgraph that repeat together, and a number is drawn on the plate to represent the number of repetitions of the subgraph in the plate.^[1] The assumptions are that the subgraph is duplicated that many times, the variables in the subgraph are indexed by the repetition number, and any links that cross a plate boundary are replicated once for each subgraph repetition.^[2]

Contents

Example

Extensions

Software implementation

References

Example

In this example, we consider Latent Dirichlet allocation, a Bayesian network that models how documents in a corpus are topically related. There are two variables not in any plate; α is the parameter of the uniform Dirichlet prior on the per-document topic distributions, and β is the parameter of the uniform Dirichlet prior on the per-topic word distribution.

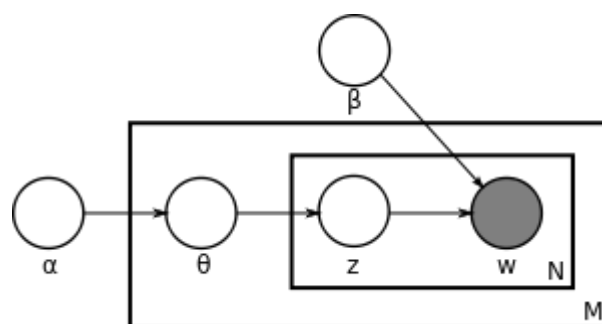


Plate notation for Latent Dirichlet allocation

The outermost plate represents all the variables related to a specific document, including θ_i , the topic distribution for document i . The M in the corner of the plate indicates that the variables inside are repeated M times, once for each document. The inner plate represents the variables associated with each of the N_i words in document i : z_{ij} is the topic distribution for the j th word in document i , and w_{ij} is the actual word used.

The N in the corner represents the repetition of the variables in the inner plate N_i times, once for each word in document i . The circle representing the

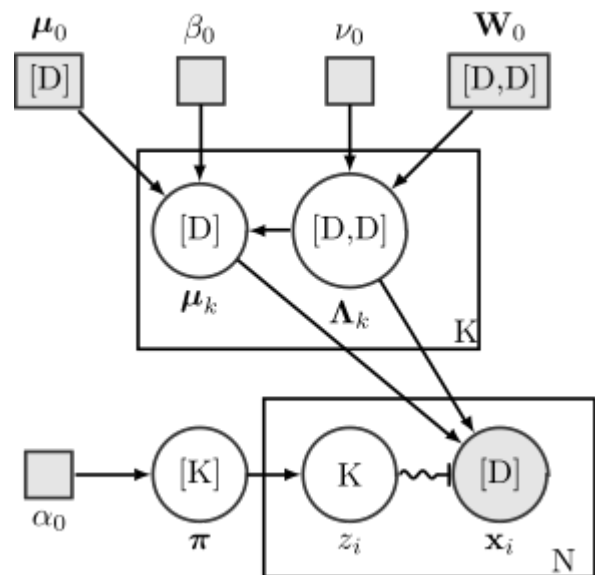
individual words is shaded, indicating that each w_{ij} is observable, and the other circles are empty, indicating that the other variables are latent variables. The directed edges between variables indicate dependencies between the variables: for example, each w_{ij} depends on z_{ij} and β .

Extensions

A number of extensions have been created by various authors to express more information than simply the conditional relationships. However, few of these have become standard. Perhaps the most commonly used extension is to use rectangles in place of circles to indicate non-random variables—either parameters to be computed, hyperparameters given a fixed value (or computed through empirical Bayes), or variables whose values are computed deterministically from a random variable.

The diagram on the right shows a few more non-standard conventions used in some articles in Wikipedia (e.g. variational Bayes):

- Variables that are actually random vectors are indicated by putting the vector size in brackets in the middle of the node.
- Variables that are actually random matrices are similarly indicated by putting the matrix size in brackets in the middle of the node, with commas separating row size from column size.
- Categorical variables are indicated by placing their size (without a bracket) in the middle of the node.
- Categorical variables that act as "switches", and which pick one or more other random variables to condition on from a large set of such variables (e.g. mixture components), are indicated with a special type of arrow containing a squiggly line and ending in a T junction.
- Boldface is consistently used for vector or matrix nodes (but not categorical nodes).



Bayesian multivariate Gaussian mixture model using plate notation. Smaller squares indicate fixed parameters; larger circles indicate random variables. Filled-in shapes indicate known values. The indication $[K]$ means a vector of size K ; $[D,D]$ means a matrix of size $D \times D$; K alone means a categorical variable with K outcomes. The squiggly line coming from z ending in a crossbar indicates a *switch* — the value of this variable selects, for the other incoming variables, which value to use out of the size- K array of possible values.

Software implementation

Plate notation has been implemented in various [TeX/LaTeX](#) drawing packages, but also as part of graphical user interfaces to [Bayesian](#) statistics programs such as [BUGS](#) and [BayesiaLab](#).

References

1. Ghahramani, Zoubin (August 2007). *Graphical models* (http://videolectures.net/mlss07_ghahramani_grafm/) (Speech). Tübingen, Germany. Retrieved 21 February 2008.
2. Buntine, Wray L. (December 1994). "Operations for Learning with Graphical Models" (<https://www.cs.cmu.edu/afs/cs/project/jair/pub/volume2/buntine94a.pdf>) (PDF). *Journal of Artificial Intelligence Research*. AI Access Foundation. **2**: 159–225. ISSN 1076-9757 (<https://www.worldcat.org/issn/1076-9757>). Retrieved 21 February 2008.

Retrieved from "https://en.wikipedia.org/w/index.php?title=Plate_notation&oldid=913090516"

This page was last edited on 29 August 2019, at 20:29 (UTC).

Text is available under the [Creative Commons Attribution-ShareAlike License](#); additional terms may apply. By using this site, you agree to the [Terms of Use](#) and [Privacy Policy](#). Wikipedia® is a registered trademark of the [Wikimedia Foundation, Inc.](#), a non-profit organization.