

# Competitive Programming Team: AB IdeaLab at Fall Activities Fair

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## 1 Description

Hello prospective IdeaLab **Competitive Programming Team** (CPT) member!

This year is AB's first year competing in the **American Computer Science League** (ACSL) competition! As you will see with the three samples on the back page, the problems are an interesting mix between Math and Computer Science and cover topics such as:

- Recursion (see Figure 1 and Problems 2 and 4)
- Graph Theory (see Figure 2)
- Computer Number Systems (see Problem 3)
- Data Structures

If you would like to collaborate with others, learn how to solve these and similar problems, and enter the world of Competitive Programming, come to IdeaLab's first meeting, **September 21, 2018 in the SYSCO lab<sup>1</sup> at 3:00 PM.**

The only pre-requisites are a **love for solving problems and an open mind**. We value these **more** than prior experience coding (as we'll be teaching basic coding skills on an ad-hoc basis).

**Represent AB, join an inclusive and caring team, and learn a ton in our first year competing in ACSL!**

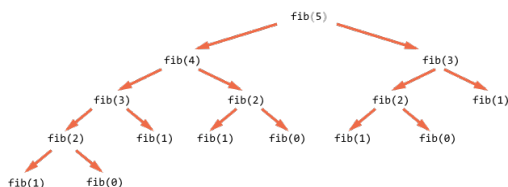


Figure 1: A tree representing the recursive calls made to the Fibonacci function.

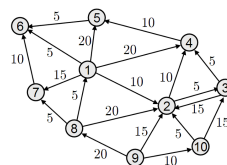


Figure 2: A graph theoretic representation of nodes, directed edges, and weights.

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<sup>1</sup>Location: Upper West, near math department center

## 2 Easy Problem

Find  $f(-1)$ :

$$f(x) = \begin{cases} x - f(x+1) & \text{if } x < 3 \\ f(2x) & \text{if } 3 \leq x < 5 \\ x + 1 & \text{otherwise} \end{cases}$$

Your Answer:
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## 3 Medium Problem

Let  $n$  be any positive base 10 integer from 1 to  $2^{12}$  inclusive. Let  $S(n)$  be the number of 1's in the binary representation of  $n$ . Find the number of possible  $n$ 's such that  $S(n) - S(n+1) = 3$ .

Your Answer:
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## 4 Hard Problem

Ackerman's function is defined as:

$$A(x, y) = \begin{cases} y + 1 & \text{if } x = 0 \\ A(x - 1, 1) & \text{if } x \neq 0 \text{ and } y = 0 \\ A(x - 1, A(x, y - 1)) & \text{if } x \neq 0 \text{ and } y \neq 0 \end{cases}$$

Find  $A(3, 4)$ .

Your Answer:
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