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State Finished

Completed on Wednesday, 16 March 2022, 3:00 PM

Time taken 43 mins 50 secs

Grade 16.00 out of 16.00 (100%)

Question **1**

Correct

Mark 2.00 out of 2.00

Consider an elastic wave

$$\xi(x, t) = \frac{1 \text{ nm}}{1 + (x - c_s t)^2}$$

propagating along a long rod of steel with density $\rho = 7.6 \times 10^3 \text{ kg m}^{-3}$ and Young's modulus $Y = 200 \times 10^9 \text{ N m}^{-2}$. Here c_s is the speed of the longitudinal elastic wave in steel. At what x do we have the maximum value of ξ for $t = 3.2$ milliseconds? Give your answer in meter units to at least one percent accuracy.

Answer: ✓

The correct answer is: 16.42

Question **2**

Correct

Mark 2.00 out of
2.00

For what value of s is the function

$$\xi(x, t) = \sin[x^2 + 2c_s xt + st^2]$$

a solution of the wave equation

$$\frac{\partial^2 \xi}{\partial x^2} - \frac{1}{c_s^2} \frac{\partial^2 \xi}{\partial t^2} = 0$$

where $c_s = 7 \text{ m/s}$. Give your answer in units of m/s to at least one percent accuracy.

Answer:



The correct answer is: 49.00

Question **3**

Correct

Mark 2.00 out of 2.00

An electromagnetic wave with

$$\vec{E}(z, t) = E_0[\hat{i} + 2\hat{j}] \cos(\omega t - kz)$$

is incident on a linear polarizer whose pass axis is along $\hat{n} = [\cos(\theta)\hat{i} + \sin(\theta)\hat{j}]$ where $\theta = 6$ degrees. If the intensity of the incident and transmitted waves be I_0 and the I_1 respectively, calculate $(I_1/I_0) \times 100$ to at least one percent accuracy.

Answer: ✓

The correct answer is: 28.97

Question **4**

Correct

Mark 2.00 out of 2.00

A birefringent crystal of thickness d has its optic axis parallel to the surface of the crystal. What is the minimum value of d (in μm) for the crystal is to be a quarter wave plate for light of wavelength $\lambda = 493 \text{ nm}$? ($n_e = 1.5334$, $n_o = 1.5443$). Give your answer to at least 1 percent accuracy.

Answer: ✓

The correct answer is: 11.31

Question **5**

Correct

Mark 2.00 out of 2.00

In a Compton effect experiment, incident light of wavelength 1.4×10^{-12} m is scattered at 180° to the incident direction,. The electron from which the scattering occurred was initially at rest. Calculate the final momentum of the electron. Give your answer in units of 10^{-23} kg m s⁻¹ to at least one percent accuracy. Compton wavelength $\lambda_c = 2.4 \times 10^{-12}$ m.

Answer: 58.10322 ✓

The correct answer is: 58.05

Question **6**

Correct

Mark 2.00 out of 2.00

The ground state energy of an electron in a 1-D infinite square potential well is 6.3 eV. Calculate the width of the well is in units of Angstroms. Write your answer to at least one percent accuracy. (Given, Planck constant $\hbar = 6.63 \times 10^{-34}$ J-s; mass of electron $m = 9.11 \times 10^{-31}$ kg; electronic charge is $e = 1.6 \times 10^{-19}$ C)

Answer: 2.446127 ✓

The correct answer is: 2.45

Question **7**

Correct

Mark 2.00 out of
2.00

Consider a quantum particle whose wavefunction is

$$\psi(x) = A x e^{-\alpha x} ; x \geq 0 \\ = 0 ; x < 0$$

with $\alpha = 9.3$. Calculate the magnitude of A so that the wavefunction is normalized. Give your answer to at least one percent accuracy.

Answer: ✓

The correct answer is: 56.72

Question **8**

Correct

Mark 2.00 out of
2.00

Find the uncertainty in x for a confined quantum particle in a 1-D infinite potential box of width $L = 9.5$ nm whose ground state wavefunction is given as

$$\psi(x) = A \sin \frac{\pi x}{L}.$$

Give your answer in Angstrom units to at least one percent accuracy.

Answer: ✓

The correct answer is: 17.20

