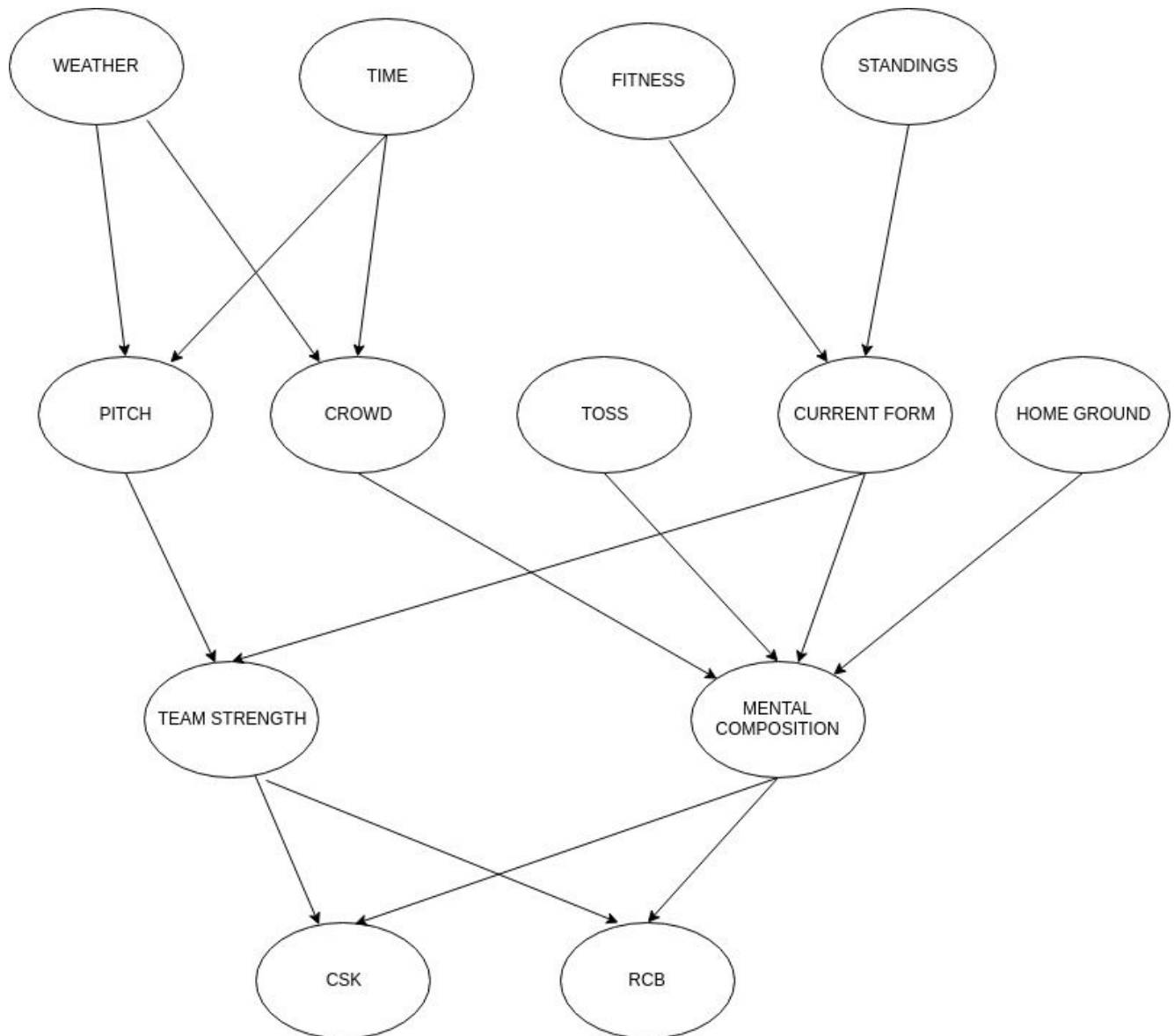


AI Assignment 3 : Bayesian Networks

Team Members:

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Flow Diagram :



Key:

W	Weather	Sunny, Rainy, Other
Tm	Time	Day, Night
H	Home Ground	RCB
F	Fitness	Fit, Unfit
S	Standings	Top, Bottom, Middle
P	Pitch	Batting, Bowling
C	Crowd	High, Low
T	Toss	CSK, RCB
CF	Current Form	Good, Bad
TS	Team Strength	High, Low, Average
MC	Mental Composition	Good, Bad

Conditional Probability Tables :-**Home(given the ground is chinnaswamy):**

H	CSK	RCB
P(H)	0	1

Time:

Tm	Day	Night
P(T)	0.2	0.8

Weather:

W	Sunny	Rainy	Other
P(W)	0.7	0.1	0.2

Standings:

S	Top	Bottom	Middle
P(S)	0.6	0.1	0.3

Fitness:

F	Fit	Unfit
P(F)	0.8	0.2

Toss:

T	yes	no
P(T)	0.5	0.5

Home:

H	yes	no
P(H CSK)	0	1
P(H RCB)	1	0

Pitch:

Tm	W	P.Batting	P.Bowling
Day	Sunny	0.8	0.2
Day	Rainy	0.6	0.4
Day	Other	0.7	0.3

Night	Sunny	0.85	0.15
Night	Rainy	0.65	0.35
Night	Other	0.75	0.25

Crowd:

Tm	W	C.High	C.Low
Day	Sunny	0.4	0.6
Day	Rainy	0.3	0.7
Day	Other	0.5	0.5
Night	Sunny	0.8	0.2
Night	Rainy	0.6	0.4
Night	Other	0.9	0.1

Current Form:

F	S	CF.Good	CF.Bad
Fit	Top	0.95	0.05
Fit	Bottom	0.2	0.8
Fit	Middle	0.6	0.4
Unfit	Top	0.75	0.25
Unfit	Bottom	0.1	0.9
Unfit	Middle	0.4	0.6

Team Strength:

P	CF	TS.High	TS.Low	TS.Average
Batting	Good	0.7	0.1	0.2

Batting	Bad	0.5	0.25	0.25
Bowling	Good	0.8	0.1	0.1
Bowling	Bad	0.4	0.4	0.2

Mental Composition:

C	T	CF	H	MC.Good	MC.Bad
High	yes	Good	yes	0.95	0.05
High	yes	Good	no	0.8	0.2
High	yes	Bad	yes	0.6	0.4
High	yes	Bad	no	0.4	0.6
High	no	Good	yes	0.8	0.2
High	no	Good	no	0.95	0.05
High	no	Bad	yes	0.3	0.7
High	no	Bad	no	0.6	0.4
Low	yes	Good	yes	0.9	0.1
Low	yes	Good	no	0.7	0.3
Low	yes	Bad	yes	0.4	0.6
Low	yes	Bad	no	0.3	0.7
Low	no	Good	yes	0.8	0.2
Low	no	Good	no	0.65	0.35
Low	no	Bad	yes	0.3	0.7
Low	no	Bad	no	0.2	0.8

CSK:

TS	MC	CSK.win	CSK.lose
High	Good	0.9	0.1
High	Bad	0.6	0.4
Low	Good	0.55	0.45
Low	Bad	0.3	0.7
Average	Good	0.75	0.25
Average	Bad	0.4	0.6

RCB:

TS	MC	RCB.win	RCB.lose
High	Good	0.8	0.2
High	Bad	0.5	0.5
Low	Good	0.45	0.55
Low	Bad	0.2	0.8
Average	Good	0.6	0.4
Average	Bad	0.3	0.7

Justifications:-

1. The pitch is usually prepared to keep the home team's needs in mind. So the home team has a definite advantage here.
2. The time of the match and the weather greatly impact the pitch conditions and thus the outcome of the game.
3. The crowd will be more if the weather is pleasant and the match is in the evening(night) as most people have jobs/classes in the morning.
4. The team which has won more matches before and is more fit definitely is in the better form.
5. The pitch conditions are hugely dependent on weather and time(dew factor comes into play).
6. The team/player form and crowd support can increase the mental composition of the team.
7. The team having the right combinations (team strength), with confident players, has a higher chance of winning.
8. Given the ground in Chinnaswamy so the probability of CSK playing on their home ground is 0 and the probability of RCB playing on their home ground is 1.

QUERY :-

Form - $P(X | p(X), p(p(X)))$

where $p(X)$ refers to the parent of X .

Query - $P(\text{CSK} = \text{win} | \text{MC} = \text{Good}, \text{CF} = \text{Good})$

$$\begin{aligned} P(\text{CSK} = \text{win} | \text{MC} = \text{Good}, \text{CF} = \text{Good}) &= P(\text{CSK} = \text{win} | \text{MC} = \text{Good}, \text{TS} = \text{High}) * \\ &\quad P(\text{TS} = \text{High} | \text{CF} = \text{Good}) + \\ &\quad P(\text{CSK} = \text{win} | \text{MC} = \text{Good}, \text{TS} = \text{Avg}) * \\ &\quad P(\text{TS} = \text{Avg} | \text{CF} = \text{Good}) + \\ &\quad P(\text{CSK} = \text{win} | \text{MC} = \text{Good}, \text{TS} = \text{Low}) * \\ &\quad P(\text{TS} = \text{Low} | \text{CF} = \text{Good}) \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Batting} \mid W = \text{Sunny}) &= P(P = \text{Batting} \mid W = \text{Sunny}, T_m = \text{Day}) * P(T_m = \text{Day}) \\
 &+ \\
 &\quad P(P = \text{Batting} \mid W = \text{Sunny}, T_m = \text{Night}) * P(T_m = \\
 \text{Night}) \\
 &= 0.8 * 0.2 + 0.85 * 0.8 \\
 &= \mathbf{0.84}
 \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Batting} \mid W = \text{Rainy}) &= P(P = \text{Batting} \mid W = \text{Rainy}, T_m = \text{Day}) * P(T_m = \text{Day}) \\
 &+ \\
 &\quad P(P = \text{Batting} \mid W = \text{Rainy}, T_m = \text{Night}) * P(T_m = \\
 \text{Night}) \\
 &= 0.6 * 0.2 + 0.65 * 0.8 \\
 &= \mathbf{0.64}
 \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Batting} \mid W = \text{Other}) &= P(P = \text{Batting} \mid W = \text{Other}, T_m = \text{Day}) * P(T_m = \text{Day}) + \\
 &\quad P(P = \text{Batting} \mid W = \text{Other}, T_m = \text{Night}) * P(T_m = \\
 \text{Night}) \\
 &= 0.7 * 0.2 + 0.75 * 0.8 \\
 &= \mathbf{0.74}
 \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Bowling} \mid W = \text{Sunny}) &= P(P = \text{Bowling} \mid W = \text{Sunny}, T_m = \text{Day}) * P(T_m = \text{Day}) \\
 &+ \\
 &\quad P(P = \text{Bowling} \mid W = \text{Sunny}, T_m = \text{Night}) * P(T_m = \\
 \text{Night}) \\
 &= 0.2 * 0.2 + 0.15 * 0.8 \\
 &= \mathbf{0.16}
 \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Bowling} \mid W = \text{Rainy}) &= P(P = \text{Bowling} \mid W = \text{Rainy}, T_m = \text{Day}) * P(T_m = \text{Day}) \\
 &+ \\
 &\quad P(P = \text{Bowling} \mid W = \text{Rainy}, T_m = \text{Night}) * P(T_m = \\
 \text{Night}) \\
 &= 0.4 * 0.2 + 0.35 * 0.8 \\
 &= \mathbf{0.36}
 \end{aligned}$$

$$\begin{aligned}
 P(P = \text{Bowling} \mid W = \text{Other}) &= P(P = \text{Bowling} \mid W = \text{Other}, T_m = \text{Day}) * P(T_m = \text{Day}) \\
 &+ \\
 &\quad P(P = \text{Bowling} \mid W = \text{Other}, T_m = \text{Night}) * P(T_m = \\
 \text{Night})
 \end{aligned}$$

$$= 0.3*0.2 + 0.25*0.8$$

$$= \mathbf{0.26}$$

$$P(P = \text{Batting}) = P(P = \text{Batting} \mid W = \text{Sunny}) * P(W = \text{Sunny}) + P(P = \text{Batting} \mid W = \text{Rainy}) * P(W = \text{Rainy}) + P(P = \text{Batting} \mid W = \text{Other}) * P(W = \text{Other})$$

$$= 0.84*0.7 + 0.64*0.1 + 0.74*0.2$$

$$= \mathbf{0.8}$$

$$P(P = \text{Bowling}) = P(P = \text{Bowling} \mid W = \text{Sunny}) * P(W = \text{Sunny}) + P(P = \text{Bowling} \mid W = \text{Rainy}) * P(W = \text{Rainy}) + P(P = \text{Bowling} \mid W = \text{Other}) * P(W = \text{Other})$$

$$= 0.16*0.7 + 0.36*0.1 + 0.26*0.2$$

$$= \mathbf{0.2}$$

$$P(\text{TS} = \text{High} \mid \text{CF} = \text{Good}) = P(\text{TS} = \text{High} \mid \text{CF} = \text{Good}, P = \text{Batting}) * P(P = \text{Batting}) + P(\text{TS} = \text{High} \mid \text{CF} = \text{Good}, P = \text{Bowling}) * P(P = \text{Bowling})$$

$$= 0.7 * 0.8 + 0.8*0.2$$

$$= \mathbf{0.72}$$

$$P(\text{TS} = \text{Avg} \mid \text{CF} = \text{Good}) = P(\text{TS} = \text{Avg} \mid \text{CF} = \text{Good}, P = \text{Batting}) * P(P = \text{Batting}) + P(\text{TS} = \text{Avg} \mid \text{CF} = \text{Good}, P = \text{Bowling}) * P(P = \text{Bowling})$$

$$= 0.2*0.8 + 0.1*0.2$$

$$= \mathbf{0.18}$$

$$P(\text{TS} = \text{Low} \mid \text{CF} = \text{Good}) = P(\text{TS} = \text{Low} \mid \text{CF} = \text{Good}, P = \text{Batting}) * P(P = \text{Batting}) + P(\text{TS} = \text{Low} \mid \text{CF} = \text{Good}, P = \text{Bowling}) * P(P = \text{Bowling})$$

$$= 0.1*0.8 + 0.1*0.2$$

$$= \mathbf{0.1}$$

$$P(\text{CSK} = \text{win} \mid \text{MC} = \text{Good}, \text{CF} = \text{Good}) = P(\text{CSK} = \text{win} \mid \text{MC} = \text{Good}, \text{TS} = \text{High}) * P(\text{TS} = \text{High} \mid \text{CF} = \text{Good}) +$$

$$\begin{aligned}
 &P(\text{CSK} = \text{win} \mid \text{MC} = \text{Good}, \text{TS} = \text{Avg}) * \\
 &P(\text{TS} = \text{Avg} \mid \text{CF} = \text{Good}) + \\
 &P(\text{CSK} = \text{win} \mid \text{MC} = \text{Good}, \text{TS} = \text{Low}) * \\
 &P(\text{TS} = \text{Low} \mid \text{CF} = \text{Good}) . \\
 &= 0.9 * 0.72 + 0.75 * 0.18 + 0.55 * 0.1 \\
 &= \mathbf{0.838}
 \end{aligned}$$