

# COMS 4701 Artificial Intelligence

## Homework 3: Coding - CSPs

Due Date: November 4, 2021

Please read all the sections carefully:

- I. Introduction
- II. Backtracking Algorithm
- III. Important Information
- IV. What You Need To Submit
- V. Before You Submit

### I. Introduction

	1	2	3	4	5	6	7	8	9
A	8		9	5		1	7	3	6
B	2		7		6	3			
C	1	6							
D					9		4		7
E		9		3		7		2	
F	7		6		8				
G								6	3
H				9	3		5		2
I	5	3	2	6		4	8		9

	1	2	3	4	5	6	7	8	9
A	8	4	9	5	2	1	7	3	6
B	2	5	7	8	6	3	9	1	4
C	1	6	3	7	4	9	2	5	8
D	3	2	5	1	9	6	4	8	7
E	4	9	8	3	5	7	6	2	1
F	7	1	6	4	8	2	3	9	5
G	9	8	4	2	7	5	1	6	3
H	6	7	1	9	3	8	5	4	2
I	5	3	2	6	1	4	8	7	9

The objective of Sudoku is to fill a 9x9 grid with the numbers 1-9 so that each column, row, and 3x3 sub-grid (or box) contains one of each digit. You may try out the game here: [sudoku.com](https://sudoku.com). Sudoku has 81 **variables**, i.e. 81 tiles. The variables are named by **row** and **column**, and are **valued** from 1 to 9 subject to the constraints that no two cells in the same row, column, or box may be the same.

Frame your problem in terms of **variables**, **domains**, and **constraints**. We suggest representing a Sudoku board with a Python dictionary, where each key is a variable name based on location, and value of the tile placed there. Using variable names **A1... A9... I1... I9**, the board above has:

- `sudoku_dict["B1"] = 2`, and
- `sudoku_dict["E2"] = 9`.

We give value **zero** to a tile that has not yet been filled.

### Executing your program

Your program will be executed as follows:

```
$ python3 sudoku.py <input_string>
```

In the starter zip, `sudokus.start.txt`, contains hundreds of sample unsolved Sudoku boards, and `sudokus.finish.txt` the corresponding solutions. Each board is represented as a single line of text, starting from the top-left corner of the board, and listed left-to-right, top-to-bottom.

The first board in `sudokus.start.txt` is represented as the string:

003020600900305001001806400008102900700000008006708200002609500800203009005010300

Which is equivalent to:

```
0 0 3 0 2 0 6 0 0
9 0 0 3 0 5 0 0 1
0 0 1 8 0 6 4 0 0
0 0 8 1 0 2 9 0 0
7 0 0 0 0 0 0 0 8
0 0 6 7 0 8 2 0 0
0 0 2 6 0 9 5 0 0
8 0 0 2 0 3 0 0 9
0 0 5 0 1 0 3 0 0
```

Your program will generate `output.txt`, containing a single line of text representing the finished Sudoku board. E.g.:

483921657967345821251876493548132976729564138136798245372689514814253769695417382

Test your program using `sudokus.finish.txt`, which contains the solved versions of all of the same puzzles.

### III. Backtracking Algorithm

Implement **backtracking** search using the **minimum remaining value heuristic**. Pick your own order of values to try for each variable, and apply **forward checking** to reduce variables domains.

- Test your program on `sudokus.start.txt`.
- Report the number of puzzles you can solve and the mean, standard deviation, min, and max of the runtime over all puzzles in `sudokus.start.txt`.

### IV. Important Information

#### 1. Test-Run Your Code

Test, test, test. Make sure you produce an output file with the **exact format** of the example given.

#### 2. Grading Submissions

We test your final program on **20 boards**. Each board is worth **5 points** if solved, and zero otherwise. These boards are similar to those in your starter zip, so if you solve all those, you'll get full credit.

#### 3. Time Limit

No brute-force! Your program should solve puzzles in **well under a minute** per board. Programs with much longer running times will be killed.

#### 4. Just for fun

Try your code on the world's hardest Sudokus! There's nothing to submit here, just for fun. For example:

**Sudoku:**

800000000003600000070090200050007000000045700000100030001000068008500010090000400

**Solution:**

812753649943682175675491283154237896369845721287169534521974368438526917796318452

## IV. What You Need To Submit

1. Your `sudoku.py` file (and any other python code dependency)
2. A `README.txt` with your results, including the:
  - number of boards you could solve from `sudokus_start.txt`,
  - running time statistics: min, max, mean, and standard deviation.

## V. Before You Submit

- Ensure that your file is named `sudoku.py`
- Ensure that your file compiles and runs.