

# Hardware Implementation of an Invariant Observer



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## **Declaration**

I hereby declare that except where specific reference is made to the work of others, the contents of this dissertation are original and have not been submitted in whole or in part for consideration for any other degree or qualification in this, or any other University. This dissertation is the result of my own work and includes nothing which is the outcome of work done in collaboration, except where specifically indicated in the text. This dissertation contains less than 65,000 words including appendices, bibliography, footnotes, tables and equations and has less than 150 figures.

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## Abstract

The Invariant Observer is an approach to implement an alternative hardware realization of the invariant operation published in the paper **Runtime Verification of Embedded Real Time Systems**. The Invariant Observer is a Runtime Verification Unit monitoring a signal  $\phi$  from a System under Test in real time and determining whether the signal was in an active state and had been active up to  $\tau$  clock cycles before. If this is the case then signal  $\phi$  is observed as being invariant in the past within the time interval  $[0, \tau]$ .



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# Chapter 1

## Introduction

### 1.1 Overview of the Bachelor Thesis

In embedded real time systems it is necessary to make efforts to verify a system design. A system design can be formalized by a mathematical specification for a dynamic system model. One approach to system design verification is a deduction, which shows that the design implies the requirements.

In critical Real Time Systems (RTS) timing constraints have to be considered in the requirement engineering. Such Real Time Systems are modelled by states changing over time. Time constraints can be formulated as constraints on the duration of critical states. A real time logic should be able to specify that real time constraints. Generally it seems that two main classes of real time logic are present, explicit or implicit temporal logic.[1]

Explicit temporal logic is an expression of a time variable. The time variable can be the representation of a time interval or a variable in temporal logic. Implicit temporal logic (for example MTL - Metric Temporal Logic) is using temporal operators that constrain the extend of a state. It is based on interval temporal logic and the duration concept. Implicit temporal logic can be very useful to express before/after relations between concurrent actions. For further details [1] can be a good source of information. In runtime verification a monitor evaluates executions of a **System under Test (SUT)** [2]. The evaluation is formalised from a formal specification described in temporal logic.

For ultra critical systems it is important to meet four major requirements:

1. Functionality : cannot change target's behaviour
2. Certifiability: must avoid re-certification
3. Timing : must not interfere with the target's timing
4. Swap : must not exhaust size, weight and power tolerance

A **Runtime Verification Unit (RVU)** is a verification monitor that meets these four major requirements. As part of this requirements, the RVU must be separated from SUT. In fact it is a synthesized hardware that monitors the execution of a SUT.

The topic of my thesis “Hardware Implementation of an Invariant Observer” can also be considered as a RVU, it evaluates the execution of a SUT and checks it for invariance conditions. My observer is an alternative implementation of the invariant observer INVARIANT-SYMBOL published in [2], that bypasses the problem of resource limitation and makes use of the significant advantages of a highly parallel **Field Programmable Gate Array(FPGA)** hardware implementation. The most important difference is that my observer is not bounded to a specific  $\tau$ , but the observer in [2] are bounded. This feature will be explained in the next section.

In the publication “**Real-Time Runtime Verification on Chip** ” [2] the concept of a RVU and the principles of that Verification Framework are described in great detail.

A survey about the functionality of the invariant observer in the following sections.

## 1.2 The Invariant Observer

This section is a survey about the invariant observer and how it works. More details about the observer algorithm are presented in the next chapter.

The Invariant Observer acts like the temporal (invariant previously) operator  $\Box_{\tau}\phi$  of the Metric Temporal Logic (MTL) and is certainly restricted on the past (ptMTL). Such a temporal operator takes an input  $\phi$ , the calculation of a propositional formula, and evaluates if  $\phi$  holds for the past  $\tau$  execution times, including the current execution time in a discrete time setting. For example the logical consequence  $e^n \models \Box_3\phi$  expresses that the current execution  $e^n$  (with  $n$  as the discrete execution time,  $n \in \mathbb{N}$ ) is true iff (if and only if) the evaluation of  $\phi$  is true now and was also true the last  $\tau = 3$  execution times. In fact the  $\Box_{\tau}\phi$  is a specialization of the  $\Box_{[0,\tau]}\phi$  ptMTL operator which restricts the range of the invariance qualification.

Figure 1.1 and Figure 1.2 show an example for such a temporal operator.

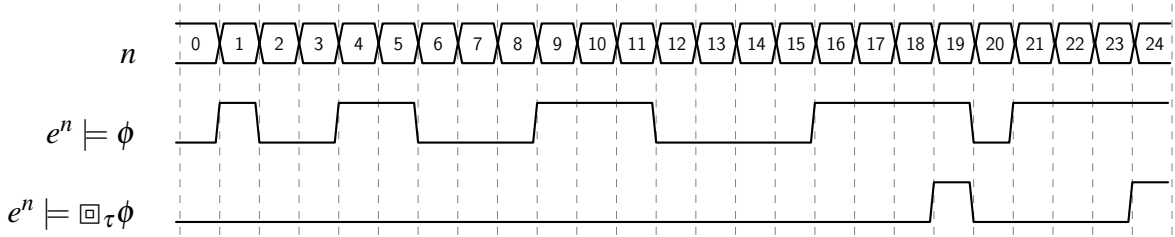


Fig. 1.1 Example for Invariant Operator  $\Box_{\tau}\phi$  with  $\tau=3$

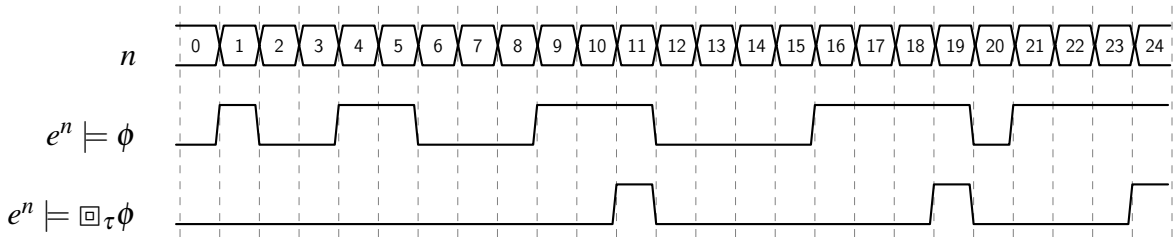


Fig. 1.2 Example for Invariant Operator  $\Box_{\tau}\phi$  with  $\tau=2$

My approach of the invariant observer is based on some certain requirements. The following subsections will discuss these requirements.

### 1.2.1 Arbitrary calculation time of logical proposition formulas

To introduce the first requirement we begin with the discussion of the problem that the calculation of a propositional formula  $\phi$  could take several clock cycles (execution times). This means that an observer has to wait until the calculation of the proposition is finished. In [2] the observer needs to guarantee that it finishes evaluation of atomic propositions within a tight time bound. In our case, if we start calculation of a propositional formula  $\phi$  at every clock cycle and the calculation itself needs  $y$  clock cycles, then we need at least  $y$  observer stages to cover finished calculations at every clock cycle. These observer stages are part of the whole observer. After  $y$  clock cycles, at every following clock cycle, a calculation of  $\phi$  will be available. At least one observer stage will be ready, too, to evaluate a calculation  $\phi$  at any time. In other words, we are implementing temporal pipeline stages that represent components of the invariant operator and these components together are evaluating the invariance qualification of the proposition  $\phi$ . We don't have one observer, in fact the observer is composed from several observer stages. As a matter of fact, the calculation of a logical proposition  $\phi$  can take as long as necessary.

Propositional formulas can be composed from several other complex propositional subformulas or atomic propositions. In some cases a subformula is waiting for the resolution of an another subformula. In [2] this balance is achieved by the restriction of the atomic proposition class in sense of the abstract domain of logahedron.

### 1.2.2 Pipelined Observer Stages

Consider every finished calculation of a propositional formula  $\phi$  as a signal value of the signal  $W(\phi)$ , every value in that signal is timely ordered just in the order it was calculated. Obviously, every represented execution time of  $W(\phi)$  is the same as the execution time of the Observer. This means, at every execution time (clock cycle) an observer stage is evaluating a signal  $W(\phi)$  at that time. In our case, signal  $W(\phi)$  is apparently shifted by  $y$  clock cycles to the right. This view is encouraged by the fact, that at the beginning of the monitoring, the observer stages have to wait, until the first value of the signal  $W(\phi)$  is available which means that the first observer stage evaluates, at execution time  $e^y$ , the first value of  $W(\phi)$ . The second observer stage evaluates, at execution time  $e^{y+1}$ , the second value of  $W(\phi)$ , and so on and so forth. Remember also, that an evaluation  $W(\phi)$  relates to a propositional formula  $\phi$ , which was relevant  $y$  clock cycles before.



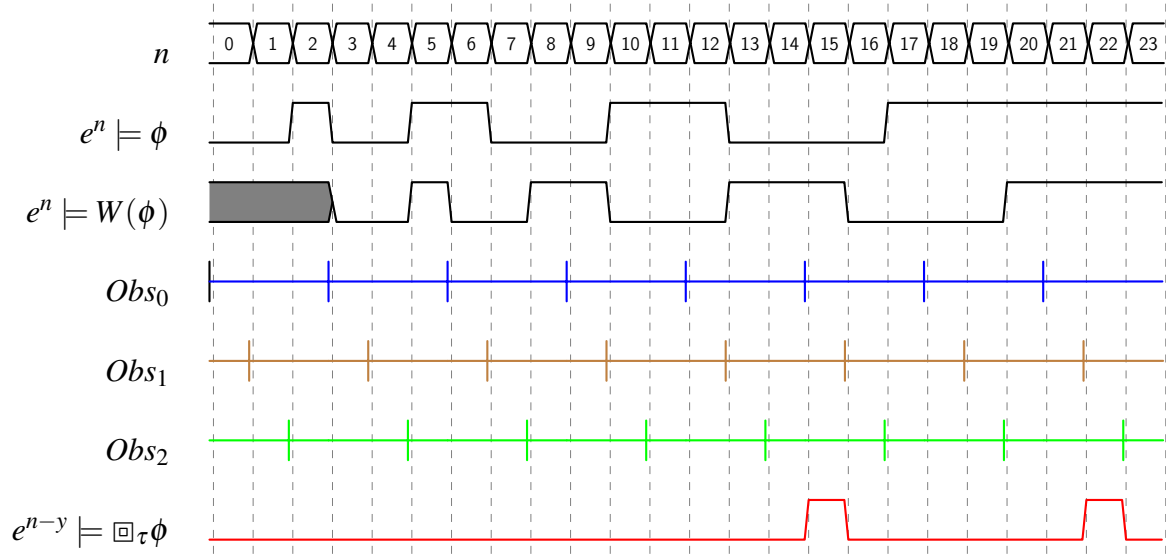


Fig. 1.3 Example for 3 observer stages monitoring a signal  $W(\phi)$ ,  $\tau=2$

The example in Figure 1.3 shows us that the calculation of the first value from  $W(\phi)$  needs  $y$  execution times. So no value is defined in the cycles before. If we take the view only from the proposition  $\phi$  as a signal, then we calculate at every execution time  $e^n$ , from the latest inputs and subformulas at that time, exactly the proposition  $\phi$  at that moment. But this holds under the assumption that the result of such a calculation is available immediately. The signal  $W(\phi)$  shows us, what happens if calculations of proposition  $\phi$  need some time, in that case  $y=3$  clock cycles. As mentioned,  $W(\phi)$  is like signal  $\phi$  shifted to the right. In Figure 1.3 we also see at which execution time the observer stages evaluate the signal  $W(\phi)$ . But this is only a preview about these observer stages. The algorithm about their real behaviour will be explained in the next chapter. The most important thing here is that these observers are working delayed. Every new observer stage starts its work after the observer stage before. This is important, because every clock cycle must be covered as long as the calculation of  $W(\phi)$  takes. The last signal shows us the invariance qualification  $e^{n-y} \models \boxplus_{\tau} \phi$  for  $\tau=2$ , which holds at execution time  $e^{15}$  and  $e^{22}$ , but either for one cycle only.

The invariance qualification will be resolved if we connect every observer stage in a binary "and" operation. In Figure 1.3 the result is simply calculated with:

$$\boxplus_2 \phi = Obs_0 \text{ and } Obs_1 \text{ and } Obs_2$$

Summarized, every observer stage is included in a binary "and" operation as the and all these observer stages together are computing at every execution time  $e^n$ , if the logical consequence  $e^{n-y} \models \Box_{\tau}\phi$  holds. If we consider all these observer stages together as one temporal (invariance before) operator, then this operator checks at every execution time  $e^n$ , the invariance qualification of the proposition  $\phi$ ,  $y$  clock cycles before. Regarding Figure 1.3, it is true now if the proposition  $\phi$ ,  $y$  clock cycles before, was invariant with  $\tau=2$ .

### 1.2.3 System Settings of the Invariant Observer Stages

This was a briefly introduction about the specific behaviour of the invariant observer as a whole, but what's about the parameter settings. It starts with the question of how many observer stages do we actually need? We already know that at least  $y$  are necessary. If we have to define a number of observer stages with variable "m" then following condition must hold:  $m \geq y$ . Depending on how long the calculation of a proposition  $\phi$  needs, a minimum of  $y$  observer stages are necessary, but upwards can be chosen arbitrarily. This shows us also the possibility to apply the Observer with his observer stages on different evaluations of system inputs despite the time they need and it works in real time. If we define only one observer stage (means immediate evaluation of  $\phi$ ), then it works as a native invariant operator.

The next interesting aspect, and maybe the most powerful argument of this design way, is the invariance parameter  $\tau$ . The number of observer stages "m" stays in no relation to the invariance parameter  $\tau$ . Following conditions are possible:  $m \geq \tau$  or  $m < \tau$ . As long as the observer is configured to cover the computation time of  $W(\phi)$ , it can be used for every arbitrary choice of  $\tau$ . In [2] this setting is fixed. My implementation of an invariant observer is able to change that parameter during run-time, but this feature is not specified in the requirements, and should be treated as such.

The next chapter shows the algorithm of the observer stages and how every observer stage works. Also a representation of the software implementation will be explained in great detail.

## Chapter 2

# Software Implementation and Algorithm

### 2.1 Algorithm of the Invariant Observer Stages

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**Algorithm 1** Pseudo Code of an Observer Stage

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**Require:** Precondition:  $m \geq y$

```
1: Initialize: count = 0
2: if m clock cycle passed then
3:   if  $W(\phi) = 0$  then
4:     /*evaluates finished calculation of  $\phi$  after m clock cycles*/
5:     count = 0
6:   else
7:     /*do nothing*/
8:   end if
9: end if
10: /*Following code executes every clock cycle*/
11: if count =  $\tau + 1$  then
12:   output = 1
13: else
14:   output = 0
15: end if
16: count = min(count + 1,  $\tau + 1$ )
```

---



## **Chapter 3**

# **Hardware Impelementation**



## **Chapter 4**

# **Experiments and Testing**





# References

- [1] A.P. Ravn, H. Rischel, and K.M. Hansen. Specifying and verifying requirements of real-time systems. *Software Engineering, IEEE Transactions on*, 19(1):41–55, Jan 1993. ISSN 0098-5589. doi: 10.1109/32.210306.
- [2] Thomas Reinbacher, Matthias Függer, and Jörg Brauer. Real-time runtime verification on chip. In Shaz Qadeer and Serdar Tasiran, editors, *Runtime Verification*, volume 7687 of *Lecture Notes in Computer Science*, pages 110–125. Springer Berlin Heidelberg, 2013.



# Appendix A

## How to install L<sup>A</sup>T<sub>E</sub>X

### Windows OS

#### TeXLive package - full version

1. Download the TeXLive ISO (2.2GB) from <https://www.tug.org/texlive/>
2. Download WinCDEmu (if you don't have a virtual drive) from <http://wincdemu.sysprogs.org/download/>
3. To install Windows CD Emulator follow the instructions at <http://wincdemu.sysprogs.org/tutorials/install/>
4. Right click the iso and mount it using the WinCDEmu as shown in <http://wincdemu.sysprogs.org/tutorials/mount/>
5. Open your virtual drive and run setup.pl

or

#### Basic MikTeX - TeX distribution

1. Download Basic-MiK<sub>T</sub>E<sub>X</sub>(32bit or 64bit) from <http://miktex.org/download>
2. Run the installer

3. To add a new package go to Start » All Programs » MikTeX » Maintenance (Admin) and choose Package Manager
4. Select or search for packages to install

## **TexStudio - Tex Editor**

1. Download TexStudio from  
<http://texstudio.sourceforge.net/#downloads>
2. Run the installer

## **Mac OS X**

### **MacTeX - TeX distribution**

1. Download the file from  
<https://www.tug.org/mactex/>
2. Extract and double click to run the installer. It does the entire configuration, sit back and relax.

### **TexStudio - Tex Editor**

1. Download TexStudio from  
<http://texstudio.sourceforge.net/#downloads>
2. Extract and Start

## **Unix/Linux**

### **TeXLive - TeX distribution**

#### **Getting the distribution:**

1. TeXLive can be downloaded from  
<http://www.tug.org/texlive/acquire-netinstall.html>.

2. TexLive is provided by most operating system you can use (rpm,apt-get or yum) to get TexLive distributions

## Installation

1. Mount the ISO file in the mnt directory

```
mount -t iso9660 -o ro,loop,noauto /your/texlive####.iso /mnt
```

2. Install wget on your OS (use rpm, apt-get or yum install)
3. Run the installer script install-tl.

```
cd /your/download/directory  
./install-tl
```

4. Enter command 'i' for installation
5. Post-Installation configuration:  
<http://www.tug.org/texlive/doc/texlive-en/texlive-en.html#x1-320003.4.1>
6. Set the path for the directory of TexLive binaries in your .bashrc file

## For 32Bit OS

For Bourne-compatible shells such as bash, and using Intel x86 GNU/Linux and a default directory setup as an example, the file to edit might be

```
edit ~/.bashrc file and add following lines  
PATH=/usr/local/texlive/2011/bin/i386-linux:$PATH;  
export PATH  
MANPATH=/usr/local/texlive/2011/texmf/doc/man:$MANPATH;  
export MANPATH  
INFOPATH=/usr/local/texlive/2011/texmf/doc/info:$INFOPATH;  
export INFOPATH
```

**For 64Bit**

```
edit ~/.bashrc file and add following lines
PATH=/usr/local/texlive/2011/bin/x86_64-linux:$PATH;
export PATH
MANPATH=/usr/local/texlive/2011/texmf/doc/man:$MANPATH;
export MANPATH
INFOPATH=/usr/local/texlive/2011/texmf/doc/info:$INFOPATH;
export INFOPATH
```

**Fedora/RedHat/CENTOS:**

```
sudo yum install texlive
sudo yum install psutils
```

**SUSE:**

```
sudo zypper install texlive
```

**Debian/Ubuntu:**

```
sudo apt-get install texlive texlive-latex-extra
sudo apt-get install psutils
```

## Appendix B

### Installing the CUED Class file

$\text{\LaTeX}$ .cls files can be accessed system-wide when they are placed in the  $\langle\text{texmf}\rangle/\text{tex}/\text{latex}$  directory, where  $\langle\text{texmf}\rangle$  is the root directory of the user's  $\text{\TeX}$  installation. On systems that have a local texmf tree ( $\langle\text{texmflocal}\rangle$ ), which may be named “texmf-local” or “localtexmf”, it may be advisable to install packages in  $\langle\text{texmflocal}\rangle$ , rather than  $\langle\text{texmf}\rangle$  as the contents of the former, unlike that of the latter, are preserved after the  $\text{\LaTeX}$  system is reinstalled and/or upgraded.

It is recommended that the user create a subdirectory  $\langle\text{texmf}\rangle/\text{tex}/\text{latex}/\text{CUED}$  for all CUED related  $\text{\LaTeX}$  class and package files. On some  $\text{\LaTeX}$  systems, the directory look-up tables will need to be refreshed after making additions or deletions to the system files. For  $\text{\TeX}$ Live systems this is accomplished via executing “texhash” as root.  $\text{\TeX}$  users can run “initexmf -u” to accomplish the same thing.

Users not willing or able to install the files system-wide can install them in their personal directories, but will then have to provide the path (full or relative) in addition to the filename when referring to them in  $\text{\LaTeX}$ .

