

# Hardware Implementation of an Invariant Observer



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## **Declaration**

I hereby declare that except where specific reference is made to the work of others, the contents of this thesis are original and have not been submitted in whole or in part for consideration for any other degree or qualification in this, or any other University. This thesis is the result of my own work and includes nothing which is the outcome of work done in collaboration, except where specifically indicated in the text.

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## Abstract

The Invariant Observer is a Runtime Verification Unit monitoring a signal  $\phi$  from a System under Test in real time and determining whether the signal was in an active state and had been active up to  $\tau$  clock cycles before. If this is the case then signal  $\phi$  is observed as being invariant in the past within the time interval  $[0, \tau]$ .

In their paper „Runtime Verification of Embedded Real Time Systems“, Reinbacher et al. [4] presented a hardware implementation of an Invariant Observer. In this thesis a different hardware implementation is shown, that allows for parallel execution of several instances, leading to significant performance improvements if the time required for determining whether  $\phi$  holds, is not neglectable.



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# Chapter 1

## Introduction

### 1.1 Overview of the Bachelor Thesis

In embedded real time systems it is necessary to make efforts to verify a system design. A system design can be formalized by a mathematical specification within a properly chosen dynamic system model. One approach to system design verification is a deduction, which shows that the design implies the requirements.

In critical Real Time Systems (RTS) timing constraints have to be considered in the requirement engineering. Such Real Time Systems are modelled by states changing over time. Time constraints can be formulated as constraints on the duration of critical states. A real time logic should be able to specify that real time constraints. Generally it seems that two main classes of real time logic are present, explicit or implicit temporal logic.[3]

Explicit temporal logic makes use of explicit expressions of time variables. The time variable can be the representation of a time interval or a variable in temporal logic. Implicit temporal logic (for example MTL - Metric Temporal Logic) is using temporal operators that constrain the extent of a state. It is based on interval temporal logic and the duration concept. Implicit temporal logic can be very useful to express before/after relations between concurrent actions. For further details [3] can be a good source of information. In run-time verification a monitor evaluates executions of a **System under Test (SUT)** [4]. The evaluation is formalised from a formal specification described in temporal logic.

For ultra critical systems it is important to meet four major requirements:

1. Functionality: cannot change target's behaviour
2. Certifiability: must avoid re-certification
3. Timing: must not interfere with the target's timing
4. Swap: must not exhaust size, weight and power tolerance

A **Runtime Verification Unit (RVU)** is a verification monitor that meets these four major requirements. As part of this requirements, the RVU must be separated from SUT. In fact it is a synthesized hardware that monitors the execution of a SUT.

The topic of my thesis “Hardware Implementation of an Invariant Observer” can also be considered as a RVU, it evaluates the execution of a SUT and checks it for invariance conditions. My observer is an alternative implementation of the invariant observer INVARIANT-SYMBOL published in [4], that bypasses the problem of resource limitation and makes use of the significant advantages of a highly parallel **Field Programmable Gate Array (FPGA)** hardware implementation. The most important difference is that my observer is not bounded to a specific  $\tau$ , but the observers in [4] are bounded. This feature will be explained in the next section.

In the publication “**Real-Time Runtime Verification on Chip**” [4] the concept of a RVU and the principles of that Verification Framework are described in greater detail.

A survey about the functionality of the invariant observer is given in the following sections.

## 1.2 The Invariant Observer

This section is a survey about the invariant observer and how it works. More details about the observer algorithm are presented in the next chapter.

The Invariant Observer acts like the temporal (invariant previously) operator  $\Box_{\tau}\phi$  of the Metric Temporal Logic (MTL) and is certainly restricted to the past (ptMTL). Such a temporal operator takes an input  $\phi$ , the calculation of a propositional formula, and evaluates if  $\phi$  holds for the past  $\tau$  execution times, including the current execution time in a discrete time setting. For example the logical consequence  $e^n \models \Box_3\phi$  expresses that the operator  $\Box_3\phi$  is true at current time  $n$  iff (if and only if) the evaluation of  $\phi$  is true now and was also true the last  $\tau = 3$  execution times. In fact the  $\Box_{\tau}\phi$  is a specialization of the  $\Box_{[0,\tau]}\phi$  ptMTL operator which restricts the range of the invariance qualification.

Figure 1.1 and Figure 1.2 show an example for such a temporal operator.

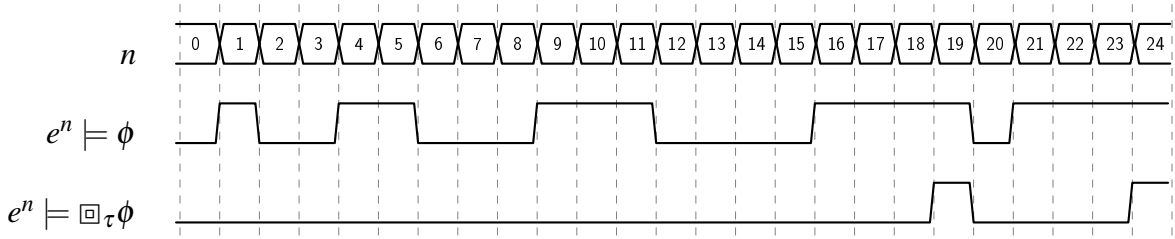


Fig. 1.1 Example for Invariant Operator  $\Box_{\tau}\phi$  with  $\tau=3$

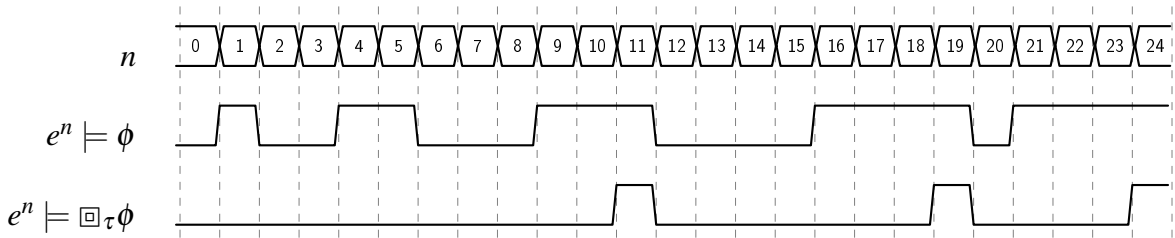


Fig. 1.2 Example for Invariant Operator  $\Box_{\tau}\phi$  with  $\tau=2$

My approach of the invariant observer is based on some certain requirements. The following subsections will discuss these requirements.

### 1.2.1 Arbitrary calculation time of logical propositions

To introduce the first requirement we begin with the discussion of the problem that the calculation of a propositional formula  $\phi$  could take several clock cycles (execution times). This means that an observer has to wait until the calculation of the proposition is finished. In [4] the observer needs to guarantee that it finishes evaluation of atomic propositions within a tight time bound. In our case, if we start calculation of a propositional formula  $\phi$  at every clock cycle and the calculation itself needs  $y$  clock cycles, then we need at least  $y$  observer stages to cover finished calculations at every clock cycle. These observer stages are part of the whole observer. After  $y$  clock cycles, at every following clock cycle, a calculation of  $\phi$  will be available. At least one observer stage will be ready, too, to evaluate a calculation  $\phi$  at any time. In other words, we are implementing temporal pipeline stages that represent components of the invariant operator and these components together are evaluating the invariance qualification of the proposition  $\phi$ . We don't have one observer, in fact the observer is composed from several observer stages. As a matter of fact, this solution only requires the calculation time of a proposition  $\phi$  to be bounded by some previously known time  $y$ .

Propositional formulas can be composed from several other complex propositional subformulas or atomic propositions. In some cases a subformula is waiting for the resolution of an another subformula. In [4] this balance is achieved by the restriction of the atomic proposition class in sense of the abstract domain of logahedron.

### 1.2.2 Pipelined Observer Stages

Consider every finished calculation of a propositional formula  $\phi$  as a signal value of the signal  $W(\phi)$ , every value in that signal is timely ordered just in the order it was calculated. Obviously, every represented execution time of  $W(\phi)$  is the same as the execution time of the Observer. This means, at every execution time (clock cycle) an observer stage is evaluating a signal  $W(\phi)$  at that time. In our case, signal  $W(\phi)$  is apparently shifted by  $y$  clock cycles to the right. This view is encouraged by the fact, that at the beginning of the monitoring, the observer stages have to wait, until the first valid value of the signal  $W(\phi)$  is available for evaluation of any observer stage which is duly put at disposal. The following observer stage evaluates, at execution time  $n = y + 1$ , the second valid value of  $W(\phi)$ , and so on and so forth. It should be considered, that the evaluation of a signal value from  $W(\phi)$  relates to a propositional formula  $\phi$ , which was relevant  $y$  clock cycles before. But it should also be mentioned that the signal values between execution time  $n = 0$  and  $n = y - 1$  are evaluated



as well, but obviously with a negative result, because no calculation can be started before any input is available.

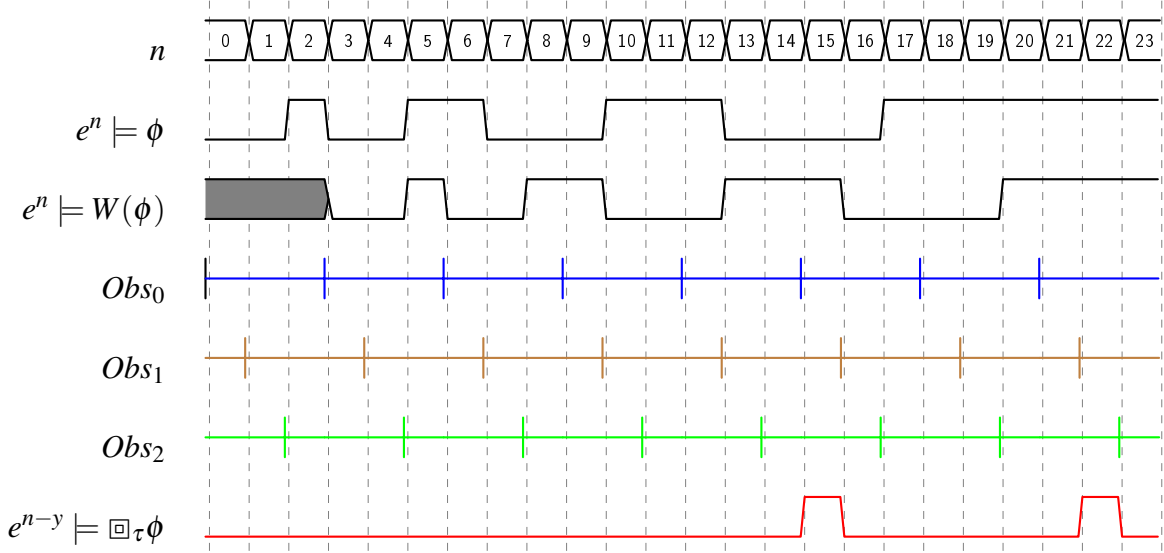


Fig. 1.3 Example for  $m=3$  observer stages monitoring a signal  $W(\phi)$ ,  $\tau=2$

The example in Figure 1.3 shows that the calculation of the first value from  $W(\phi)$  needs  $y$  execution times. So no value is defined in the cycles before. If we take the view only from the proposition  $\phi$  as a signal, then we calculate at every execution time  $n$ , from the latest inputs and subformulas at that time, exactly the proposition  $\phi$  at that moment. But this holds under the assumption that the result of such a calculation is available immediately. The signal  $W(\phi)$  shows us, what happens if calculations of proposition  $\phi$  need some time, here we assume  $y=3$  clock cycles. As mentioned,  $W(\phi)$  is like signal  $\phi$  shifted to the right. In Figure 1.3 we also see at which execution time the observer stages evaluate the signal  $W(\phi)$ . But this is only a preview about these observer stages. The algorithm about their real behaviour will be explained in the next chapter. The most important thing here is that these observers are working delayed. Every new observer stage starts its work after the observer stage before. This is important, because every clock cycle must be covered as long as the calculation of  $W(\phi)$  takes. The last signal shows us the invariance qualification  $e^{n-m} \models \boxplus_{\tau} \phi$  for  $\tau=2$ , which holds at execution time  $n = 15$  and  $n = 22$ , but either for one cycle only.

The invariance qualification will be resolved if we connect every observer stage in a binary “and” operation. In Figure 1.3 the result is simply calculated with:

$$\boxplus_2 \phi = Obs_0 \text{ and } Obs_1 \text{ and } Obs_2$$

Summarized, every observer stage is included in a binary "and" operation and all these observer stages together are computing at every execution time  $n$ , if the logical consequence  $e^{n-m} \models \Box_{\tau}\phi$  holds. If we consider all these observer stages together as one temporal (invariance before) operator, than this operator checks at every execution time  $n$ , the invariance qualification of the proposition  $\phi$ ,  $m$  clock cycles before. Regarding Figure 1.3, it is true now if the proposition  $\phi$ ,  $m$  clock cycles before, was invariant with  $\tau=2$ .

### 1.2.3 System Settings of the Invariant Observer Stages

This was a brief introduction about the specific behaviour of the invariant observer as a whole. We will next detail on the parameter settings. It starts with the question of how many observer stages do we actually need? We already know that at least  $y$  are necessary. If we have to define a number of observer stages with variable "m" then the following condition must be hold:  $m \geq y$ . Depending on how long the calculation of a proposition  $\phi$  needs, a minimum of  $y$  observer stages are necessary, but upwards can be chosen arbitrarily. This shows us also the possibility to apply the Observer with his observer stages on different evaluations of system inputs despite the time they need and it works in real time. If we use only one observer stage (means immediate evaluation of  $\phi$ ), then it works as a native invariant operator.

The next interesting aspect, and maybe the most powerful argument of this design way, is the invariance parameter  $\tau$ . The number of observer stages "m" stays in no relation to the invariance parameter  $\tau$ . Following conditions are possible:  $m \geq \tau$  or  $m < \tau$ . As long as the observer is configured to cover the computation time of  $W(\phi)$ , it can be used for every arbitrary choice of  $\tau$ . In [4] this setting is fixed. My implementation of an invariant observer is able to change that parameter during run-time, but this feature is not specified in the requirements, and should be treated as such.

The next chapter shows the algorithm of the observer stages and how every observer stage works. Also a representation of the software implementation will be explained in great detail.

# Chapter 2

## Software Implementation and Algorithm

### 2.1 Algorithm of the Invariant Observer Stages

The following algorithm shows the proper behaviour of an observer stage.

---

**Algorithm 1** Pseudo Code of an Observer Stage

---

**Require:** Precondition:  $m \geq y$

```
1: Initialize: count = 0
2: if (clock mod m) = 0 then
3:   if  $W(\phi) = 0$  then
4:     /*evaluates finished calculation of  $\phi$  after m clock cycles*/
5:     count = 0
6:   else
7:     /*do nothing*/
8:   end if
9: end if
10: /*Following code executes every clock cycle*/
11: if count =  $\tau + 1$  then
12:   output = 1
13: else
14:   output = 0
15: end if
16: count = min(count + 1,  $\tau + 1$ )
17: return output
```

---

As shown in Algorithm 1 the algorithm is split in two main parts. From the start of the observer stage, and periodically every  $m$  clock cycles, the upper part checks the status of the current signal value  $W(\phi)$ . If  $W(\phi)$  has an active state (e.g.  $W(\phi)=1$ ), the counter keeps his

old value, otherwise it will be set to zero. It is important that one observer stage recognizes, that the invariance qualification was not satisfied at this time. When the conjunction of all observer stages is computed, at any arbitrary execution time  $n$ , and at least one stage does not have an active output, then the result is false. This means, that at the execution time  $n$ , the invariance qualification is not fulfilled. The bottom part is executed at every clock cycle and increments the counter value up to the maximum value of the invariance qualification's range. If the counter reaches the maximum value, the respective observer stage activates its output to an active state. In fact, the counter represents the invariance qualification of length ' $\tau$ '. The term ' $\tau + 1$ ' indicates that the present value must also be involved in the invariance qualification. The counter value will be initialized with zero at the beginning of the algorithm. Hypothetically, if the counter is initialized with ' $\tau + 1$ ' the output is activated immediately, because of the bottom algorithm. But this is a contradiction to the assumption that  $W(\phi)=0$  for all execution times  $n$  before zero.

It should be mentioned that this current design does not implement or handle the calculations of the truth value of propositions  $\phi$ , which is indicated with  $W(\phi)$ . On the other hand, the observers from [4] are responsible for taking the necessary inputs, calculate the atomic propositions (with ATCheckers) and immediately evaluate the ptMTL-operator qualifications. These steps have to be done in a tight time bound. In our case,  $W(\phi)$  must be updated from another entity in such a way, that at every clock cycle an observer stage must have a consistent value for evaluation. The following subsection is an overview about the implementation of the Algorithm 1 in VHDL.

## 2.2 VHDL Implementation of the Algorithm

In Appendix A.2, there is an implementation in VHDL which follows the meaning of Algorithm 1. We will discuss the different process entities and the relations with Algorithm 1. Finally, we get an overview about the improvements which are significant for a faster design. This VHDL design of an observer stage has got the following inputs and outputs:

(a) inputs:

- **invariance\_tau** is a signal variable which gets the value for  $\tau$
- **enable\_in** signal activates the observer stage
- **signal\_phi** is the signal state of  $W(\phi)$

(b) output:

- **enable\_out** is a signal whose state is set to active after the activation of the current observer stage, but delayed for exact one clock cycle.
- **output signal** is simply the output state of the observer stage.

The Observer Stage is split in a synchronous and an asynchronous design, in terms of a Moore State Machine. The process labelled “sync” (at line 83 of the VDHL-Code A.2) represents the synchronous part of that design where the register states are changed at every clock cycle. The synchronous process is only executed if the combined signal **enable\_logic** has been activated, indicating a specific behaviour of the observer stages. (VDHL-Code A.2, line 22) The observer stages are linked to each other through cascade connections. The first stage activates the next observer stage through the signal **enable\_out** after being activated through **enable\_input**. If the signal **enable\_input** of an observer stage is being activated, in a clock cycle, then the signal **enable\_out** will be activated in the clock cycle afterwards.

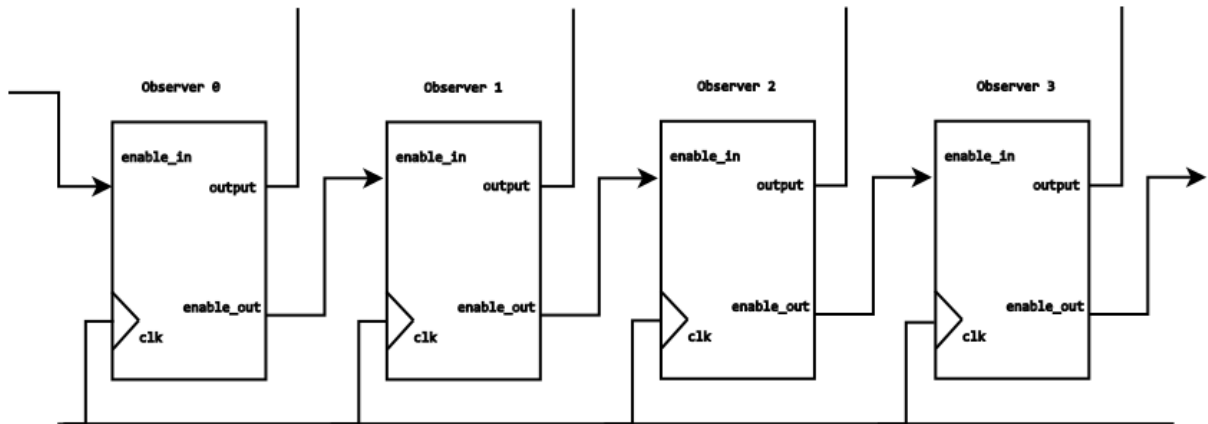


Fig. 2.1 Example for  $m=4$  Invariant Observer Stages concatenated in cascade.

This ensures, that these observers are starting delayed, each 1 clock cycle after its predecessor.

Signal **inc\_tau**(VDHL-Code A.2, line 21) increments the input signal **invariance\_tau**, which represents  $\tau + 1$  at every execution time. The asynchronous part works immediately after every change of the system state. (VDHL-Code A.2, line 25 and line 51) In the following descriptions of the asynchronous parts, only temporary signals are changed, but

these signals transfer their values inside the synchronous part at every clock cycle, except **inc\_tau** and **enable\_logic**. Every of these signals are indicated with “\_next” at the end of their names, but in the following descriptions only their register counterparts will be mentioned.

The process entity **comb\_cycle**(VDHL-Code A.2, line 25) is the description of an internal clock counter which only counts up and down between values 0 and  $m$ . The signal **cycle** is significant for checking the condition “(clock mod  $m$ ) = 0” from Algorithm 1.

The process entity **comb\_logic** implements the main part of the algorithm. Signal **count\_p** will be incremented in each clock cycle until it reaches  $\tau + 1$ . The counter should be initialised to zero (as indicated in the algorithm), but is incremented immediately at every clock cycle. (VDHL-Code A.2, line 55) Or in other words, if **count\_p** is reset to zero in a clock cycle, it will be incremented immediately in the “same” clock cycle. To demonstrate this fact we have an additional signal **count**, initialised with 1. But this signal is only for reasoning and will be reduced by the syntheses tool. The synchronous design is cumbersome in a way, which is due to the way of how the states change. If the counter is supposed to be incremented after evaluating some conditions, this does not imply an immediate change of the counter. To overcome this handicap the counter **count\_p** is initialised to 2(VDHL-Code A.2, line 56) which means, that at every clock cycle we check if the counter **count\_p** will reach a maximum at the next clock cycle. This enables us to change things on time. According to the Algorithm 1 at line 5, **count\_p** will only be reset if signal  $W(\phi)$  has been evaluated as being not active in **comb\_cycle**. (VDHL-Code A.2, line 56)

The first if-branch at line 53 of the VDHL-Code A.2 checks two cases. At first it will be checked if the clock passed  $m$  cycles or not and second if the signal **enable\_logic** is supposed to be active. The first question is in term of Algorithm 1, line 2. The second question concerns the signal **enable\_logic**. This signal combines **enable\_in** and **reset** in one signal. If signal **enable\_logic** is active, means that the observer stage is active and no reset condition happens. The else-branch of the first if-branch at line 67 of the VDHL-Code A.2 checks the condition in terms of Algorithm 1, line 11. The content of the if-branch (line 53) and the else-branch (67) are nearly the same, but there are two exceptions. Inside the if-branch, beginning at line 54, the status of signal  $W(\phi)$  will be checked, according to Algorithm 1, line 3. And inside the else-branch at line 75, if  $m$  cycles are no yet passed and signal **count\_p** is already at the maximum, then signals **count\_p**, **count** and **output** keep their old values. The

other parts of **comb\_cycle** are straightforward, if you compare it with the algorithm. In case the counter **count\_p** reaches the maximum, the **output** of the observer stage is activated.

The current design has been made optimizing for throughput. Besides from design decisions like using `count_p` instead of `count`, this led to the following general design rules:

It is very important that no Latches are built by the syntheses tool, so every if-branch must contain the same changes on the same signals. A further point is to reduce the number of if-branches to a minimum. If-branches inside of an If branch extends signal paths and reduce the maximum clock design of the whole design. In the next chapter we get an overview of the hardware realisation of the current design, which shows us a more visual view on that.





# Chapter 3

## Hardware Implementation

The following sections show an overview about the hardware implementation of the Invariant Observer Design. It starts with a description about the hardware platform on which the observer runs and some details about the synthesis tools. At the end of this chapter, there comes a design view about the synthesized hardware and a discussion about the design steps.

### 3.1 Hardware Platform for a Prototype

The Invariant Observer is synthesized on a Field Programmable Gate Array(FPGA), on this platform it is possible to get an insight about the runtime behaviour and to see the observer in action. The FPGA board, that was used for the simulations, is a **DE2-115** modell from ALTERA[1]. That board is ideal to illustrate fundamental concepts and advanced designs, and it gives a possibility to meet necessary real-time requirements. The DE2-115 is equipped with a **Cyclone IV EP4CE115F29** FPGA Chip and it is powerful enough to emulate a CPU(ex. Nios from Altera). In [4] this FPGA board was used for performance studies, besides other FPGA's, so it was logical to use a similar environment. The **DE2-115** has an on-board oscillator of 50 Mhz and in combination with a Phase Locked Loop(PLL) it is possible to increase the operating frequency for advanced tests. In the following section it will be shown, how enhanced frequencies can change the design on the Register Transfer level(RTL) and why bad design decisions can influence the maximal speed of a design. In Appendix D there is a schema illustration about the components of the **DE2-115** FPGA board.

## 3.2 Synthesis and Design

This section gives an overview about the synthesis tool and details about the Register Transfer Level design view. An interesting part in this section is to see how the synthesis tool creates hardware structures based on the code of the Observer VHDL implementation.

For synthesis and compilation of the observer VHDL code, the **Altera Quartus II Version 12.1 Build 177 Full Version** was used.

### 3.2.1 Design View of the Register Transfer Level

In Quartus II, after compilation of the design and after creation of the netlists, you can use a tool named **RTL Viewer**, which shows how the components of the design will be created on a Hardware Platform. It is an abstract view on the **Register Transfer Level**. This tool can be very handy if someone want to see how the hardware should look like. Based on the illustration of the hardware, some decisions can be reconsidered in terms of the performance.

Figure 3.1 is the hardware schematic view of a single observer stage ( $m=1$ ), which is modelled as a single observer with input frequency of 50Mhz. In which way, this test cases was modelled, will be discussed in the next chapter. The next Figure 3.2 shows exact the same design case like Figure 3.1 but with the difference that the operating frequency is 150Mhz. In Figure 3.2, it is illustrated how the syntheses tool reorientates the hardware design, to meet the requirements of that clock speed. The worst case path determines the maximum frequency, which is allowed for that design. A more detailed description about the timing model is in the next subsection.

### 3.2.2 Timing Model of the Design

One important thing that have to be considered is that the signal path from the beginning of the observer entity to the end should be as short as possible, this concludes to some important design facts. The maximum frequency of the whole system is limited by the longest path of the design, which means that the performance of a system is expressed by the maximum frequency at which it may be operated. So it should be logical for every entity in the netlist, to keep the signal path as short as possible. The performance maximum can be computed by the Quartus Tool named **TimeQuest Timing Analyzer**, which gives estimations about the maximum frequency of the design. The longest signal path of a design is indicated by the **worst case path** in the tool.

The first version of the observer stage had a low performance level, a illustration of this version is shown in the Appendix C.2. The TimeQuest Timing Analyzer consider some uncertainties for the performance estimations. From [2] it is known how the Quartus Tool creates timing models. These are created in the TimeQuest Timing Analyzer after building the netlist, as part of the compilation process of a design. A FPGA has to operate in a continuum of conditions. These conditions include the die junction temperature which can vary among specific ranges, for example commercial parts have a range of 0°C to 85°C and industrials a bigger range. A further condition is the voltage supply level with regard to critical voltages for maintaining FPGA performance( $V_{cc}$  and the various I/O supplies).

The timing analyzer shows estimations for three cases

1. Slow 1200mv 85°C model
2. Slow 1200mv 0°C model
3. Fast 1200mv 0°C model

These are operating-condition corners which are usually end point combinations of the ranges in temperature, voltage and manufacturing processes. Each operating-condition is used to model the timing delays under specific end points of temperature, voltage, and manufacturing process conditions. The first case with “Slow 1200mv 85°C model” seems natural and was more considered for test cases, because it shows frequencies under long term operating conditions. A lot of tests about estimations of the maximum frequency of different design cases have been exercised(shown in the next chapter), and only the estimations from “Slow 1200mv 85°C model” were significant for further discussions. In the next chapter there is a summary of these tests.

### 3.2.3 Design Decisions based on Register Transfer level

At the first time, where the VHDL Code of the observer stage was behavioural correct, some performance and optimization decisions had to be reconsidered. The most important thing is to separate synchronous and asynchronous design. So, it was necessary to split the first version of a completely synchronous design, where every action is only triggered after every clock cycle. A more parallel approach was necessary where only state changes are done synchronously, but other actions should be triggered immediately after any change of the state. And a asynchronous system part can be separated in several independent asynchronous components, which achieves more system parallelism and a better performance. As already mentioned in chapter 2, this system design is similar to a Moore State Machine,

where the logic is separated in a transition logic, an output logic and a state memory. And only the state memory should be changed on every clock cycle. The design approach of the invariant observer is similar, but with the difference that the output logic and transition logic components are merged together. The hardware schemas from the Register Transfer Level illustrations were beneficial, because they showed how the components were created with its VHDL background. For example If-statements should be created in a way, that allow no Latches. This means that every else-branch should contain the same components like the if-branch. Following that rule, muxes will be created which are shown here in the example of Figure 3.1. Every mux has two inputs(according to if, else), which are selected depending on the third input(MUX21). At the beginning of the entity there are several adders and these are representations for the different addition operations which has to be done according to the behaviour of the observer. **Add2** emulates “ $cycle\_next = cycle + 1$ ”, **Add1** emulates “ $cycle\_next = cycle - 1$ ” and **Add3** emulates “ $count\_p = count\_p + 1$ ” according to the sourcecode of the Observer Stages in Appendix A.2. In Figure 3.1, the MUX 21 Mux at the beginning, indicated by **cycle\_next[15..0]**, is the if-branch, according to the sourcecode in Appendix A.2, which decides if “ $cycle = 0$ ” or not. The **MUX21[cycle\_next[31..16]]** below stands for the branch “if  $cycle = observernumber$ ”. **MUX21[cycle\_next[15..0]]** decrements  $cycle\_next$  in normal case, but increments it only once if the value of  $cycle\_next$  reaches the bottom limit. **MUX21[cycle\_next[31..16]]** works the opposite way. As you can see, the tool enhanced  $cycle\_next$  up to 48bit to reserve memory for intermediate results. In the middle of the hardware scheme, there are two another **MUX21[cycle\_next[15..0]]**, the first(left to right) decides between “ $cycle\_next = cycle + 1$ ” or “ $cycle\_next = cycle - 1$ ” and the second between the result from first Mux before and the reset value. **MUX21[cycle\_next[47..32]]** decides between keeping the old value “ $cycle\_next = cycle$ ” or taking over the value from **MUX21[cycle\_next[31..16]]**. The overview regarding  $count\_p$  is similar, but a deeper insight about that Quartus translation behaviour would exceed that subsection. As you can see in the hardware schema, there are 5 registers( $cycle$ ,  $count\_p$ ,  $direction$ ,  $output$ ,  $enable\_out$ ) and these representates the state of the Invariant Observer and they may only change their values after every clock\_cycle. The dimensions of the registers are conform to the dimensions of the input conditions. For example if  $inc\_tau$  has a value with only 5 bits, then  $count\_p$  is accordingly large-dimensioned to 6 Bit. This is only a cut-out, about how the Quartus II translates VHDL Code. A lot of other hardware representations are shown in Appendix C, actually they have the same components but another orientations. The next subsection shows something about problems during the progress of that development.

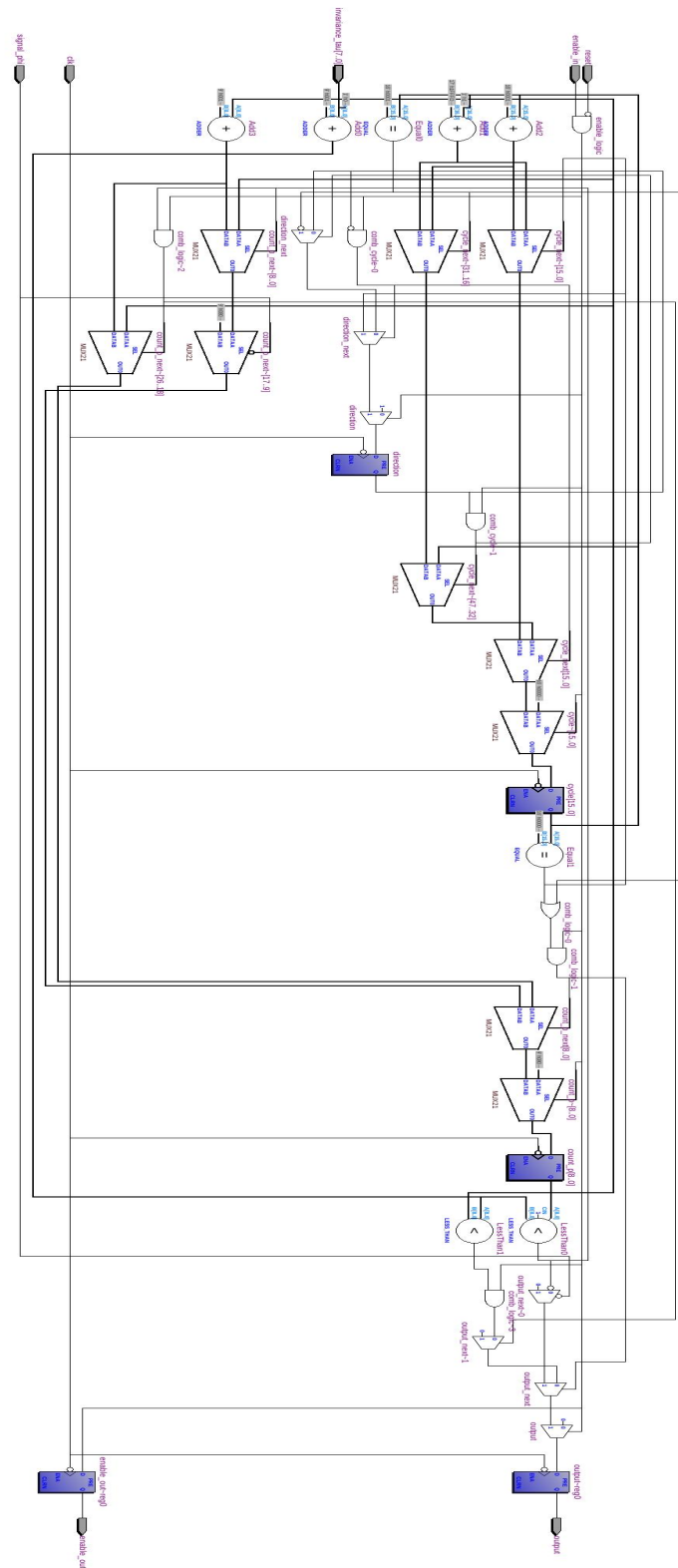


Fig. 3.1 Shows a RTL View of a single observer stage with input clock of 50Mhz

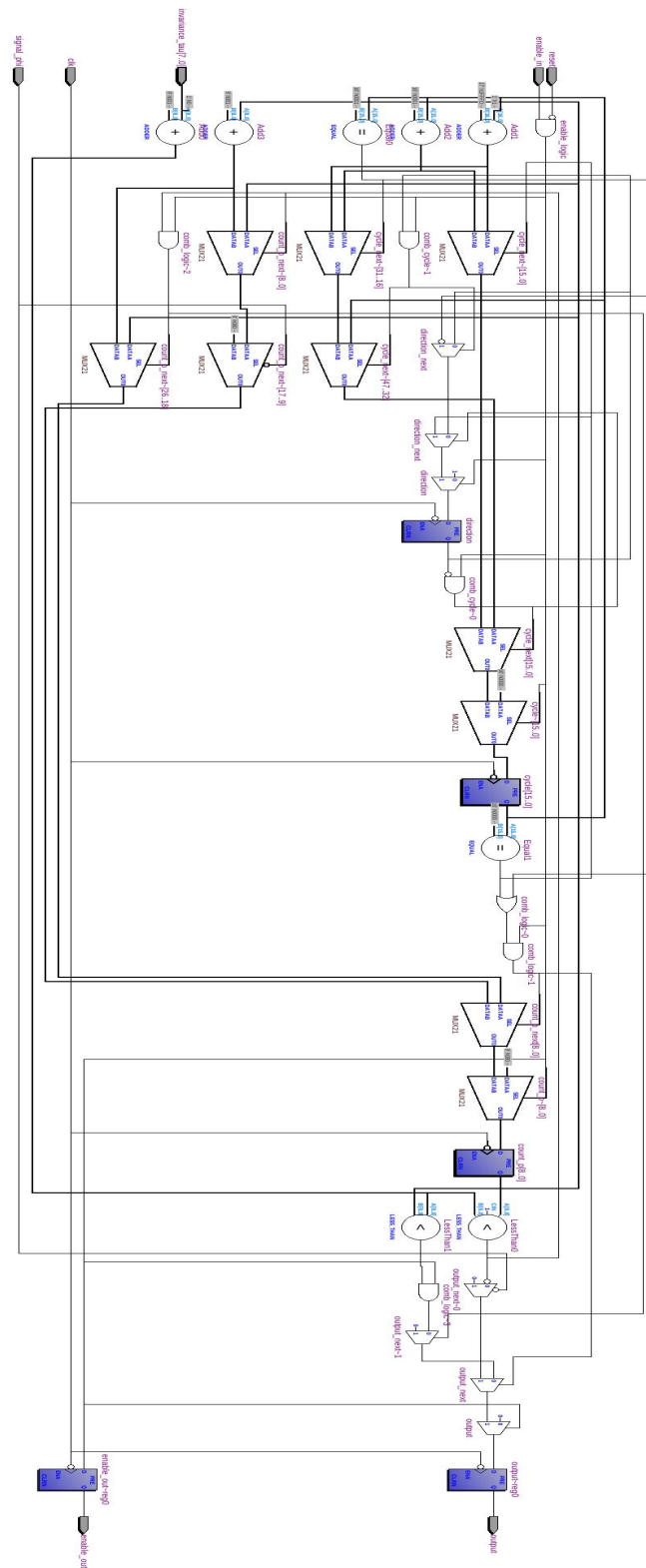


Fig. 3.2 Shows a RTL View of a single observer stage with input clock of 150Mhz

### 3.3 Design problems in the development

This subsection is only a kind of a protocol about problems during the development.

1. The starting condition of the Algorithm 1 was uncertain, the question was, should variable count be initialised with 0 or with  $(\tau + 1)$ . If  $\text{count} = (\tau + 1)$  then the output is immediately switched on, which correspond to an invariance qualification. From the specification of an observer in [4], it is known from the proof of Theorem 1 (in [4]) that  $\forall i : (i \in [\max(0, n - \tau), n] \rightarrow e^i \models \phi)$  which follows that at the beginning of an execution if  $n - \tau$  exceeds the bottom border, but the signal  $\phi$  is true, the invariance qualification is fulfilled by that specification. This condition only holds if signal  $\phi$  is known at that time, in our case the status of signal  $\phi$  is always (if  $m \geq 1$ ) taken from the past. So it is not known which status the signal  $\phi$  has before execution time  $e^0$ . Hence, the Algorithm 1 was initialised in a manner, that no decisions can be made about invariance qualifications.
2. The Invariance Observer was tested with a self-made signal generator which imitates input  $\phi$ . As a result, two clock domains were created, although the clock signals came from the same PLL (Phase Locked Loop). If the observer's clock is an "even" multiple of the second clock frequency (signal generator), there was no problem, but if the clock frequencies are choosed in a different way, then it comes to clock drifts.
3. The file (\*.sdc file) for timings has to be adjusted every time, if there are changes in one of the clock domains. The PLL output timings have to be analyzed separately by the TimeQuest Timing Analyzer. If this does not happen, false estimations are created for "Slow 1200mv 85°C model" maximum frequencies and worst case paths.
4. The first download of the compiled design to the FPGA was not successful, because the Quartus Tool was not correctly adjusted to that platform. Following points had to be changed:
  - The correct architecture must be set
  - the voltage level must be set for all inputs and outputs
5. It should be always considered what is the active state of an input component or output component, for example input KEY is low active and it was used to reset the FPGA board.





# Chapter 4

## Experiments and Testing

This Chapter is a detailed description about the simulations and experiments of the Invariant Observer. The first section introduce a survey about the test environment and their different configurations. The second section shows something about the simulations and their conclusions. The third section is a detailed description about the test cases and experiments, even something about the performance studies which were discussed in the chapter before.

### 4.1 Reasoning and Environment of Experiments

This section should be considered as a description about the questions “Which result do we gain from these experiments?” and “How are the experiments done?”.

#### 4.1.1 Reasoning and Meaning

The Invariant Observer will interact in an environment where at least soft real-time, but rather hard real-time conditions, should be fulfilled. The first step, to show correct behaviour of the algorithm and the resulting VHDL Implementation, are simulations. But it should be mentioned that no clear assertions can be made about correct timings. This question relies on the part of experiments. How the simulations and experiments were done, and which insights they produced, will be discussed in the next subsection. To present a first proof about correct principle of the Invariant Observer it was necessary to synthesize the VHDL Implementation to get a prototype. A FPGA was the best solution, besides other possibilities like ASIC's or a Microcontroller. An ASIC (Application-specific integrated circuit) is the most performant solution, but that solution is hardwired and any change of the

design is very expensive. But it could be considered as the final product implementation. A Microcontroller would never reach the performance of a FPGA and FPGA's are more cost effective and nearly performant like hardwired solutions. Any change of the design can be easily downloaded on a FPGA Board, so it seems logical to use FPGA's as prototyping platform. One important aspect of the experiments was to show the timings of the design. for example to show the maximum performance on a FPGA board like the DE2-115, which was used for the experiments, as already mentioned. But other FPGA's with stronger abilities could reach better performance goals. In [4] several FPGA models were used to show that aspect. A further aspect was to show the ability of handling any propositional formula  $\phi$ , which is composed of several possible input signals. The evaluation of  $\phi$  takes time, maybe several clock cycles. That circumstance was not exactly tested, but a different approach was tried to show the same way. A more exact test could be done if this work will be continued. The next subsection will explain the actual investigations of the experiments in great detail.

#### 4.1.2 Build-up of Experiments

At first some facts about the Invariant Observer will be repeated, to give a better understanding about the tests that were made. The Invariant Observer consist of several Observer Stages. Every Observer Stage hast to wait, at least the time needed to evalaute a proposition  $\phi$ , until th evaluation finished. To cover every clock cycle  $e^n$ , where a finished computation of a proposition  $W(\phi)$  will be evaluated, we need least as many Observer Stages, as the computation (m clock cycles) needs. To remind, the observer stages are not responsible for the computation of the propositions(like in [4] ), but for the final evaluation of the status of the computation. So it seems logical to create a signal  $\phi$  which gives, at every clock cycle, a pseudo evaluation of an proposition  $\phi$ . After that it was easy to show the correct beahviour of the Invariant Observer. For example we have m=3 Observer (means theoretical that the evaluation needs 3 clock cycles), and want to show the invariance of signal  $\phi$ , actually the finished computation  $W(\phi)$ , with  $\tau = 10$ . That 3 Observer Stages shows whether the  $W(\phi)$  was invariant 10 clock cycles before and the current clock cycle. The experiments have been exercised with a plain implementation of a signal  $W(\phi)$  and with a more complex implementation of  $W(\phi)$ , which gives a stronger argument of the correct behaviour. More about that in the simulation section and experiment section. That two versions of simulating the input signal of the observer are justified with the fact, that the Quartus synthesis tool could create distinct implementations of the Observer Design, because it must match the correct timing behaviours. This will be discussed in the experiment section The experiments con-

sists of a plain Observer Stage with different configurations with the plain input and the complex input. The same with several Observer Stages. The next section gives us an insight about the simulations.

## 4.2 Simulations

To simulate the VHDL Design of the Observer Stages the simulation tool **ModelSim (Version 10.1d)** from **MentorGraphics** was used. A testbench created for simulations in Modelsim gives a good overview about the intended behaviour of the implemented algorithm and it is usefull for debugging and error detection. At the beginning, only one Observer Stage was simulated, because it demonstrates the simplest case. After error corrections and succesfull simulation of one Observer Stage, which behaves like an native Invariance Observer, simulations were proceed with more Observer Stages.

In Figure 4.1 there is illustrated a simulation with  $m=5$  Observer, where every observer stage monitors the yellow-colored input signal  $\phi$  for Invariance  $\tau = 3$ . The most left column shows the names of the illustrated signals. For every Observer (OBS1 to OBS5), signals cycle,  $count_p$  and their outputs (add1 to add5) are shown to overlook their behaviour on input signal  $phi\_s (= \phi)$ . Signals cycle and  $count_p$  are already descibed in Chapter 3, so there is nothing additional. Signals add1 to add5 are the outputs of the different Observer Stages, which are linked together in a binary add operation. The result of that operation is illustrated as the red-colored signal  $output_s$  which shows the final result of the Invariance Observer. Signal  $phi\_s$  is generated by a complex signalgenerator to get a nearly universal test signal. The green-colored signal at the top indicates the system clock which drives the signalgenerator with his output  $phi\_s$  and all the observer stages at the same time. But the signalgenerator is driven on the rising edge, the Oberver Stages on falling edge. This fact is important to understand one further explanations of the simulation. The most important thing that is shown in that illustration is that the observer stages activate the final  $output_s$  exactly  $\tau + 1$  clock cycles after signal  $phi\_s$  still holds his active state. This case is indicated between the two big vertical lines. This shows that the Invariance Observer monitored an Invariance Situation of signal  $phi\_s$ , according to the behaviour described in Chapter 2. The Invariance Situation continues three clock cycles until signal  $phi\_s$  goes into a non active state.

As mentioned, signal  $phi\_s$  changes his states on every rising edge, whereas a Observer Stage checks the state of signal  $phi\_s$  on every falling edge. This explains the delayed reac-

tion of the Observer Stages on changes of the input signal. This handicap could be enhanced by driving the Observers clock a multiple faster. The signalgenerator is designed to increase the invariance of his active state continuously, so it was reasonable to see how the final red-colored output works. To make it clear, signal `phi_s` which is created by the signalgenerator only delivers a pseudo input for the Observer Stages which can be understood like as, at every clock cycle, a computation of  $W(\phi)$  is finished and the result of that computation is illustrated as true (active state) or false (low state). This means, that the number of Observer Stages in Figure 2.1 has no intended meaning. There could be also only one Observer Stage or more than five, the simulation would behaves he same.

Finally, it should be discussed how the Observer Stages are initialised. The fourth signal from the top `enable_s` activates the first Observer Stage which is located at the beginning of the Observer Cascade. This principle is shown in Figure 2.1. After one clock cycle the following Observer Stage will be activated by signal `en_1`, and after one clock cycle again signal `en_2` activates the next Observer Stage and so on. In Figure 4.1 this bahaviour is illustrated at the beginning by signal `enable_s`, signals `en_1` till `en_4` and the last output in the cascade by signal `next_obs`.

A further more detailed illustration is shown in Appendix B with  $m=10$  Observer. Simulations with different configurations were made, with different numbers of Observer Stages and different Invariance Qualifications. Automated Testing was necessary to have a stronger error check in case of changes in the design. Assertions as part of th VHDL language were inserted in to the Code to have a possibility to check if the behaviour of the Observer Stages is still the same. Modelsim gives also the possibilty of scripting, which is very helpful when a lot of simulation parameters have to be handled.

The last section introduces the experiments, which were exercised after simulations.

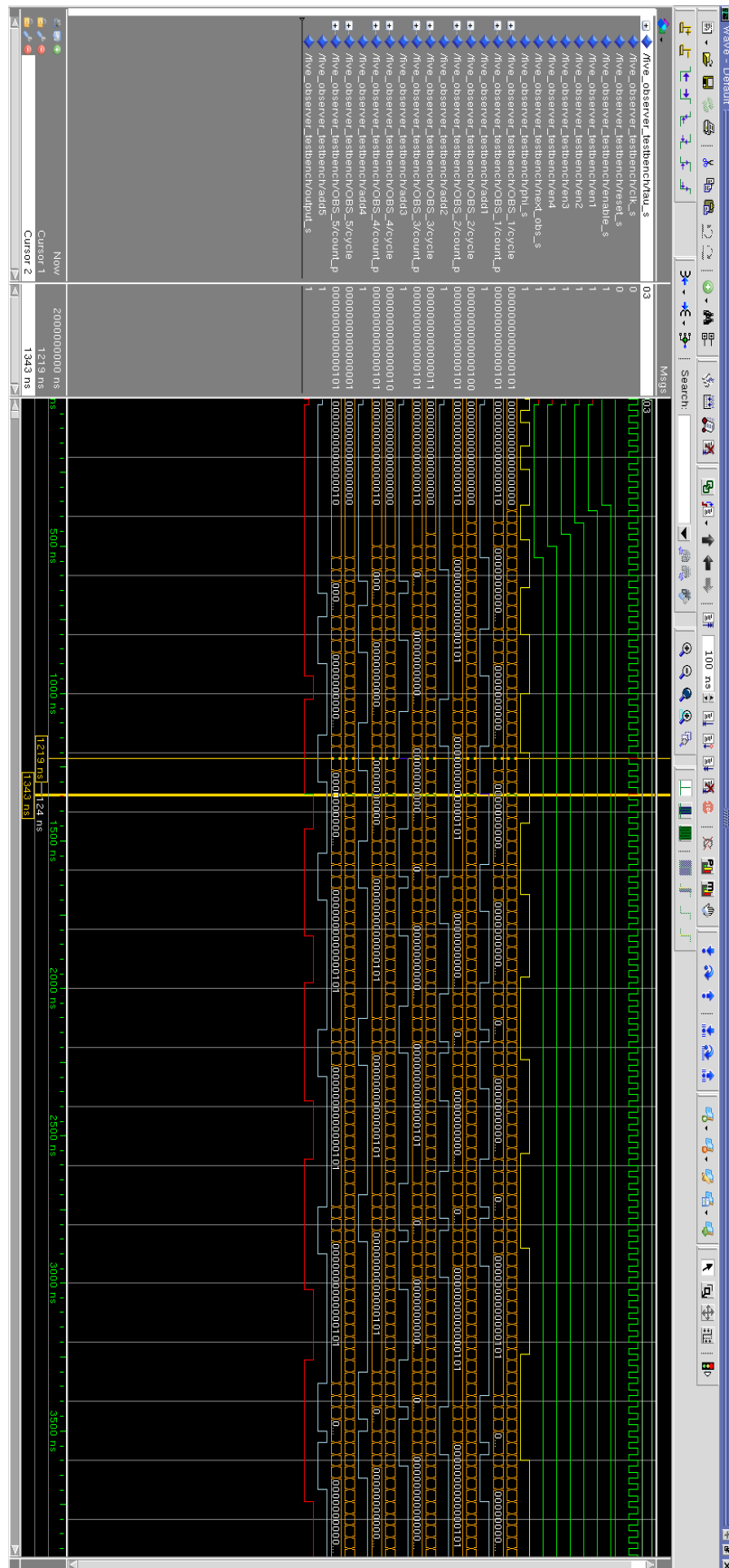


Fig. 4.1 Illustration of a Simulation with  $m=5$  Observer and Invariance  $\tau = 3$

## 4.3 Experiments

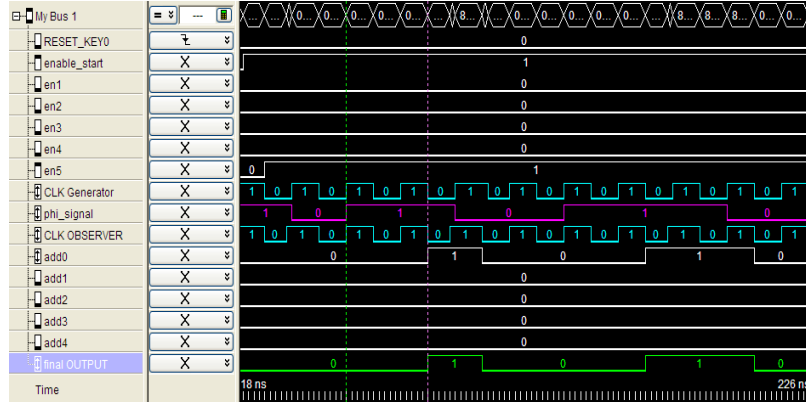
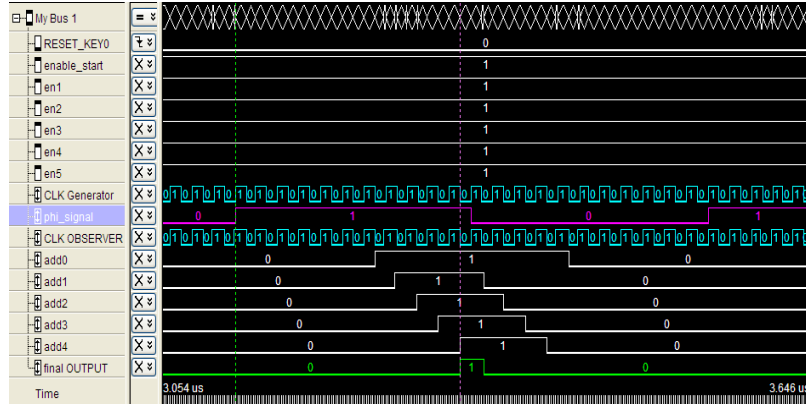
This section treats the experiments done for the Invariance Observer Design. The main part of the experiments were dedicated for testing of the behaviour of the Invariant Observer Stages. Other experiments were justified by the reason to figure out the maximum performance of these Observer Stages. It is decent to present only the edge cases of the experiments, which have reasonable arguments, but it is clear that a lot of more test cases were exercised. At first it was important that the correct behaviour of the Invariant Observer Stages was tested and demonstrated on the FPGA Board.

The correct behaviour of the Invariant Observer Design, synthesized on a DE2-115 FPGA board, will be shown by following pictures made with the Logic Analyzer (Agilent 16803A). The logic analyzer was used to monitor the output pins GPIO(0) to GPIO(34) of the FPGA Board. A example of a TOP VHDL file which embeds the Invariant Observer Design inside a Test Environment is shown in Appendix A. A lot of TOP files with different configurations were created, but this one example should only show how the experiments work. The output of every Observer Stage is connected to a GPIO output pin, and every of these GPIO pins can be measured and displayed on the logic analyzer.

The pictures shown for up to 5 Observers show only the outputs from GPIO(0) to GPIO(14) in the left side of every these pictures. For 10 Observers, the examples in Figure 4.4 and Figure 4.4 illustrate the output pins from GPIO(0) to GPIO(31). For example the first signal GPIO(0) is always the reset\_s signal similar to the arrangement in Figure 4.1. The names of the signals in the following picture are also the same like in the simulation, so it should be clear what the signals in the appropriate line means.

### 4.3.1 Testing the Behaviour

The experiments in this subsection are realized with a signalgenerator which was build individually to simulate a continuously increasing invariance signal. This is only the case, because we want to see the correct behaviour of the Observer Stages indicated by add0 to addn and final\_output. The signalgenerator and the observer stages are driven with the same input clock of 50Mhz, only for demonstrations. A indicated  $f_{max}$  means the maximum frequency estimation from the Quartus Tool for the whole design according to the Slow 1200mv 85°C model, which was described in subsection Chapter 3.2.2. But that will be more considered in the next subsection regarding the performance, whereas this section has no significant arguments regarding the performance of the Observer Stages, because  $f_{max}$  also depends on the included signalgenerator. The pictures in that subsection are very simi-

Fig. 4.2 Illustration from the Logic,only one Observer Stage with  $m=1, \tau = 1$ Fig. 4.3 Illustration from the Logic analyzer which shows the  $m=5, \tau = 10$ 

lar to the explanations in Section 4.2, so no additional explanation will be added. Every picture contains two clock signals, one for the signalgenerator and one for the Observer Stages, this was introduced only for the possibility that the frequency of **CLK\_OBSERVER** is a multiple of **CLK\_Generator**, but that idea was declined because of some irregular behaviours which will be discussed in the Conclusion of that Thesis. In principle **CLK\_Generator** and **CLK\_OBSERVER** should be the same.

The simplest case as the first picture Figure 4.2 shows, is one Observer  $m = 1$  and  $\tau = 1$ . Like in the simulation explained the vertical lines indicates the start of an Invariance Condition and the start of active signal  $\phi_s$  itself.

- $\tau = 1$  with  $f_{max} = 91,41 \text{ Mhz}$  (shown in Figure 4.2)
- $\tau = 10$  with  $f_{max} = 87,61 \text{ Mhz}$

Figure 4.3 shows 5 Observer ( $m=5$ ) with observing Invariance of 10 clock cycles

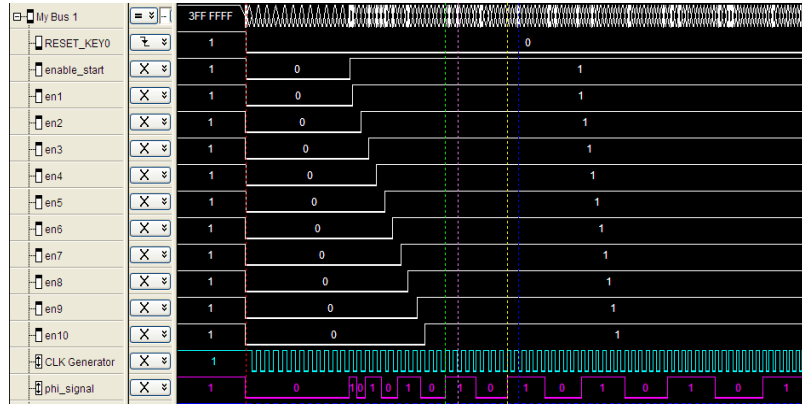


Fig. 4.4 Illustration from the Logic analyzer which shows the  $m=1, \tau = 1$

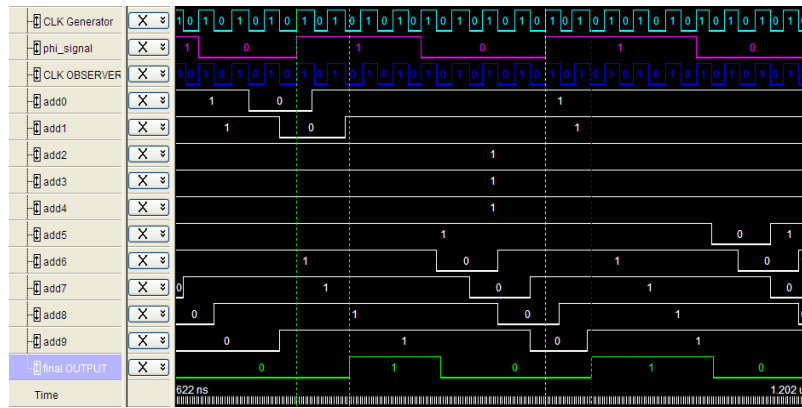


Fig. 4.5 Illustration from the Logic analyzer which shows the  $m=10, \tau = 1$

Signal **final\_OUTPUT** is the binary conjunction from add0 to add4. The vertical lines indicates the beginning of the observation by the Observer Stages ( $\phi_s$  in active state) and the Invariance Condition  $\tau = 10$  fulfilled at the right vertical line. If every falling edge of signal **CLK\_OBSERVER** is counted between both vertical lines, it should be equal to  $\tau + 1 = 11$ . Same principle should hold for further pictures.

Figure 4.4 and Figure 4.5 show the same experiment (illustration from logic analyzer sperated in two pictures) with 10 Observer ( $m=10$ ) which are observing Invariance of  $\tau = 1$  on signal  $\phi_s$ . Figure 4.5 illustrates the same behaviour like the pictures before.

Figure 4.5 also shows how the Observer Stages are switched on, one by one. Signal **enable\_start** shows the start of that start-up sequence, important to see the behaviour as part of the Algorithm 1 that every Observer Stage turns on the next following Observer Stage after one clock cycle as illustrated by Figure 2.1.

The next subsection shows a chain of experiments which could be argued as “What is



the maximum possible clock frequency that can drive the Observer Stages?”

### **4.3.2 Maximum Performance**

This subsection discuss the maximum possible performance of the Observer Stage Design under involvement of the limitation by the DE2-115 FPGA Board.



# References

- [1] Altera de2-115 fpga-board description. <http://www.altera.com/education/univ/materials/boards/de2-115/unv-de2-115-board.html>, . Accessed: 2014-04-24.
- [2] Altera timing model. <http://www.altera.com/literature/wp/wp-01139-timing-model.pdf>, . Accessed: 2014-04-24.
- [3] A.P. Ravn, H. Rischel, and K.M. Hansen. Specifying and verifying requirements of real-time systems. *Software Engineering, IEEE Transactions on*, 19(1):41–55, Jan 1993. ISSN 0098-5589. doi: 10.1109/32.210306.
- [4] Thomas Reinbacher, Matthias Függer, and Jörg Brauer. Real-time runtime verification on chip. In Shaz Qadeer and Serdar Tasiran, editors, *Runtime Verification*, volume 7687 of *Lecture Notes in Computer Science*, pages 110–125. Springer Berlin Heidelberg, 2013.



# **Appendix A**

## **Source Implementation in VHDL**

The following source Codes in this Appendix A shows the implementation of the Invariant Observer. The Source Codes are written in VHDL 1993 and shows a description about the Behavioural Specification of the design.

Observer.vhd is the entity specification of an Observer Stage and shows specifications about the input and outputs. Figure 2.1 shows us an excerpt of the input and output but at most how the several observer stages interact together.

Observer\_behave.vhd describes the exact behaviour of an observer stage. A detailed description of this behaviour is shown in Chapter 2.2.

```
1  LIBRARY ieee;
2  USE ieee.std_logic_1164.all;
3  use IEEE.NUMERIC_STD.ALL;
4
5
6  entity observer is
7  generic (
8      observernumber: unsigned(15 downto 0) := x"0001" -- how many observer are instan
9      tiated
10     );
11  port (
12      clk          :in   std_logic;
13      reset        :in   std_logic;
14      enable_in    :in   std_logic;
15      invariance_tau :in   std_logic_vector(7 downto 0);
16      signal_phi   :in   std_logic;
17      output       :out  std_logic;
18      enable_out   :out  std_logic
19  );
20
21  end entity;
```

Fig. A.1 Code of Observer Entity Design

```

71  elsif(count_p > inc_tau and enable_logic = '1') then
72    count_next <= count;
73    count_p_next <= count_p;
74    output_next <= '1';
75  else
76    count_next <= count;
77    count_p_next <= count_p;
78    output_next <= '0';
79  end if;
80  end process comb_logic;
81  --the synchronisation logic
82  sync: process(clk,enable_logic)
83  begin
84    if(clk'event and clk = '0') then
85      if(enable_logic = '1') then
86        cycle <= cycle_next;
87        direction <= direction_next;
88        count <= count_next;
89        count_p <= count_p_next;
90        output <= output_next;
91        enable_out <= '1';
92      else
93        cycle <= x"0000";
94        direction <= '1';
95        count <= x"0001";
96        count_p <= x"0002";
97        output <= '0';
98        enable_out <= '0';
99      end if;
100    end if;
101  end process sync;
102
103  end architecture; --END ARCHITECTURE

```

```

1  LIBRARY ieee;
2  USE ieee.std_logic_1164.all;
3  use IEEE.NUMERIC_STD.ALL;
4
5
6  architecture Behavioural of observer is
7
8    signal inc_tau      : unsigned(8 downto 0) := "000000000";
9    signal count_next   : unsigned(15 downto 0) := x"0001";
10   signal count_p_next  : unsigned(15 downto 0) := x"0002";
11   signal cycle,cycle_next : unsigned(15 downto 0) := x"0000";
12   signal direction,direction_next : std_logic := '1';
13
14
15   signal enable_logic : std_logic := '0';
16   signal output_next : std_logic := '0';
17   begin --BEGIN ARCHITECTURE
18
19   -- parallel logic
20   inc_tau <= unsigned(invariance_tau) + to_unsigned(1,9) ;
21   enable_logic <= enable_in and not reset;
22
23   -- changes cycle up from 0 to observernumber and down back to 0
24   comb_cycle: process(cycle,direction,enable_logic)
25   begin --changes cycle_next, direction, changeDirection
26     if(direction = '0' and enable_logic = '1') then
27       if(cycle = 0) then
28         direction_next <= '1';
29         cycle_next <= cycle + 1;
30       else
31         direction_next <= '0';
32         cycle_next <= cycle - 1;
33       end if;
34     elsif(direction = '1' and enable_logic = '1') then
35       if(cycle = observernumber) then
36         direction_next <= '0';
37         cycle_next <= cycle - 1;
38       else
39         direction_next <= '1';
40         cycle_next <= cycle + 1;
41       end if;
42     else
43       direction_next <= direction;
44       cycle_next <= cycle;
45     end if;
46   end process comb_cycle;
47
48
49   -- main logic of the observer
50   comb_logic: process(inc_tau,count,cycle,signal_phi,enable_logic)
51   begin
52     if ( cycle = observernumber or cycle = 0) and enable_logic = '1' then -- m
53       cycles_passed
54         if(signal_phi = '0') then -- w(phi) = 0
55           count_next <= x"0001";
56           count_p_next <= x"0002";
57           output_next <= '0';
58         elsif(count_p <= inc_tau) then
59           count_next <= count + 1; --every clock cycle
60           count_p_next <= count_p + 1 ;
61           output_next <= '0';
62         else
63           count_next <= count;
64           count_p_next <= count_p;
65           output_next <= '1';
66         end if;
67       elsif(count_p <= inc_tau and enable_logic = '1') then
68         count_next <= count + 1; --every clock cycle
69         count_p_next <= count_p + 1 ;
70         output_next <= '0';

```

Fig. A.2 Code of the Behavioural Design of an Invariant Observer

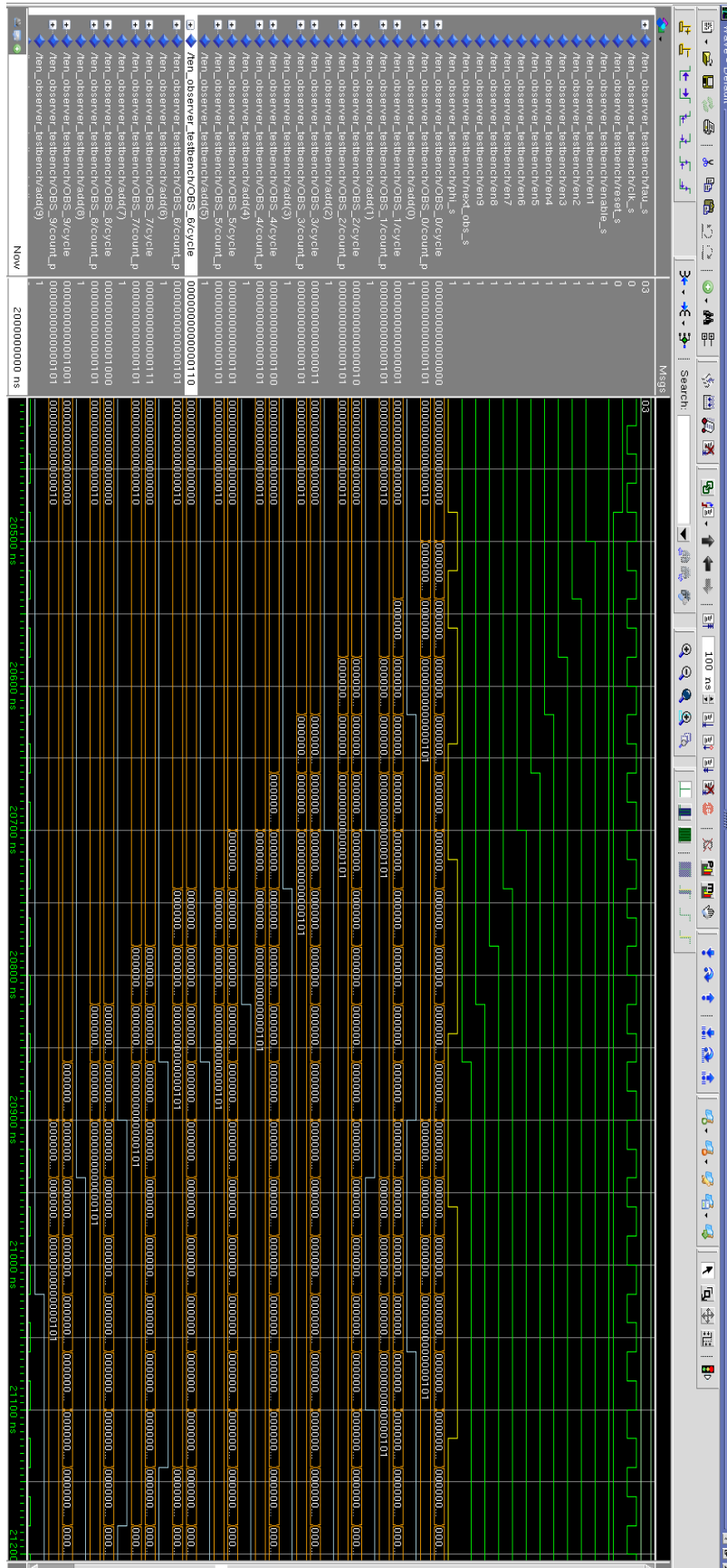




# **Appendix B**

## **Modelsim Simulations**

### **B.1 Simulations with 10 Observer**

Fig. B.1  $m=10$  Observer and  $\tau = 3$  with view about cascade activation of the observer

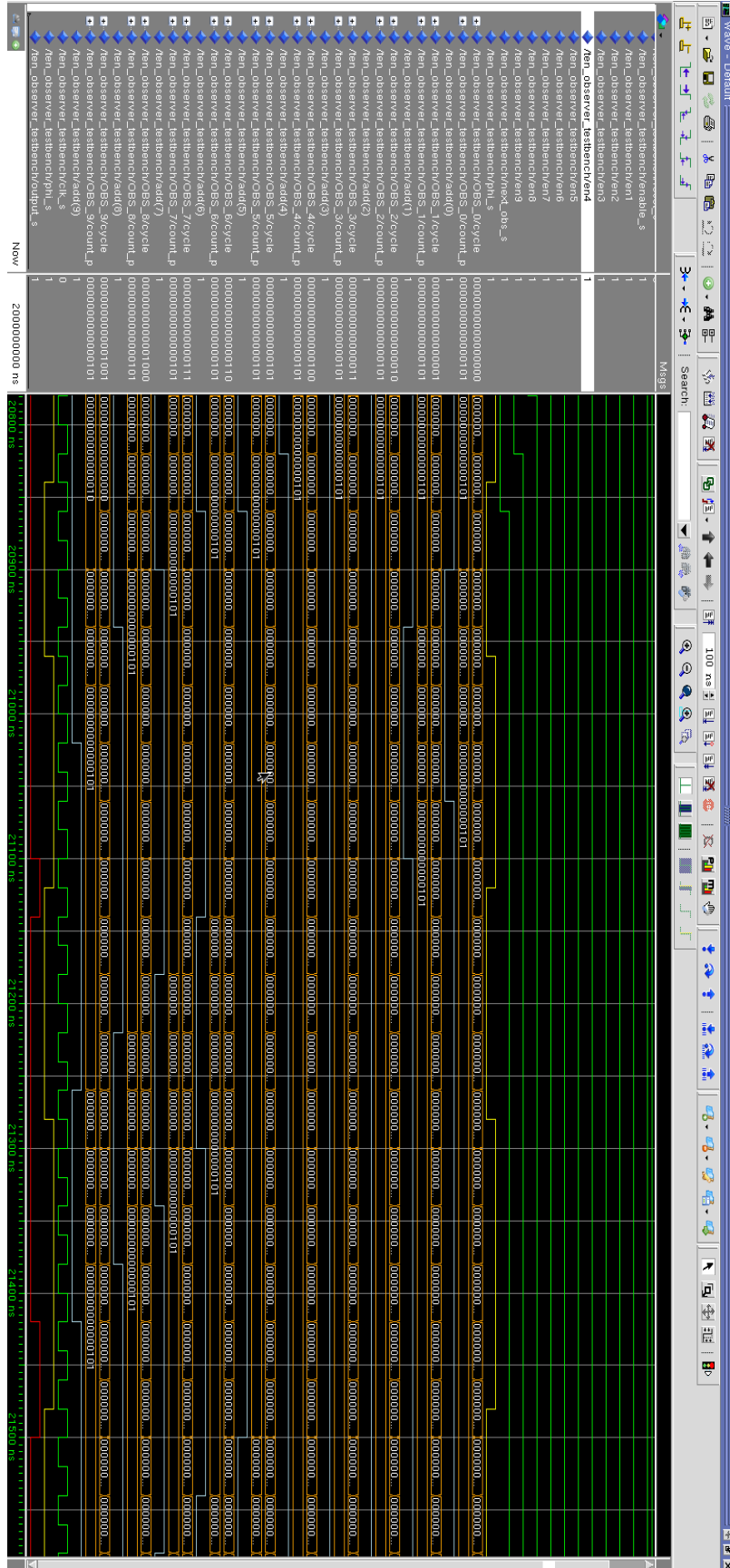
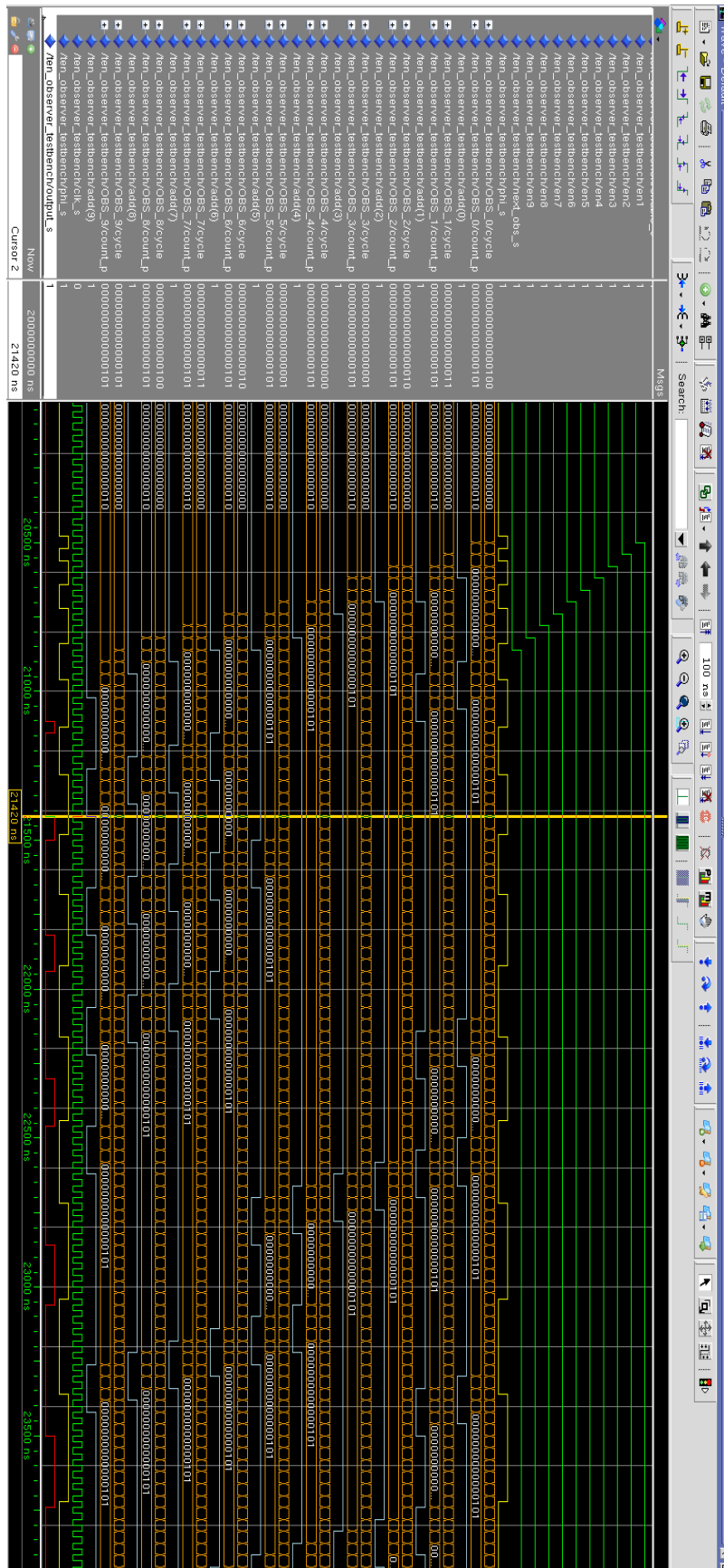


Fig. B.2  $m=10$  Observer and  $\tau = 3$  with view about the output of the Observer Stages and final red-colored output

Fig. B.3  $m=10$  Observer and  $\tau = 3$  with an overall view

# **Appendix C**

## **Register Transfer Level Design View**

### **C.1 Design of the First Version**

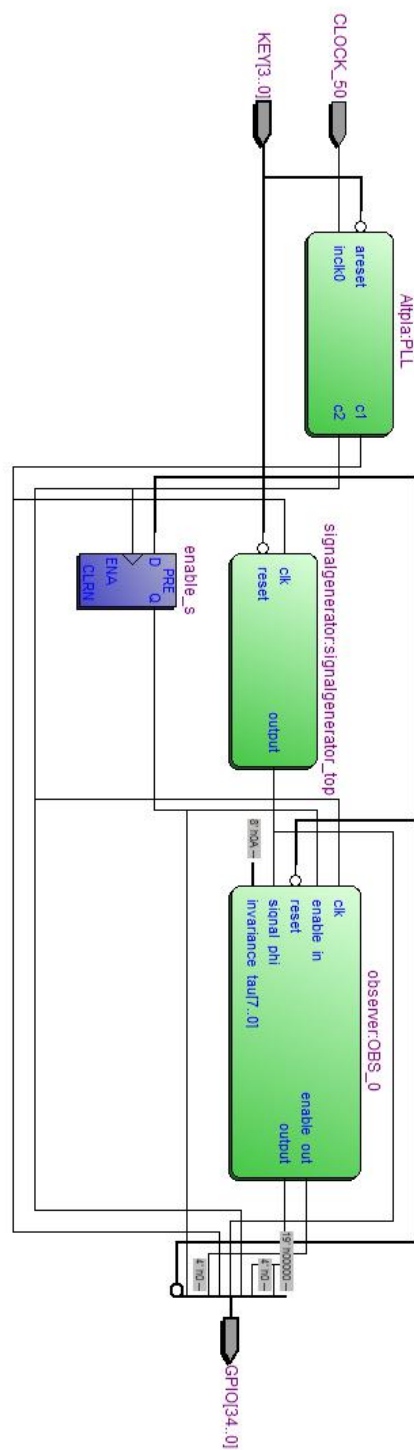


Fig. C.1 Illustration of the TOP Design of the first correct version, but without improvements

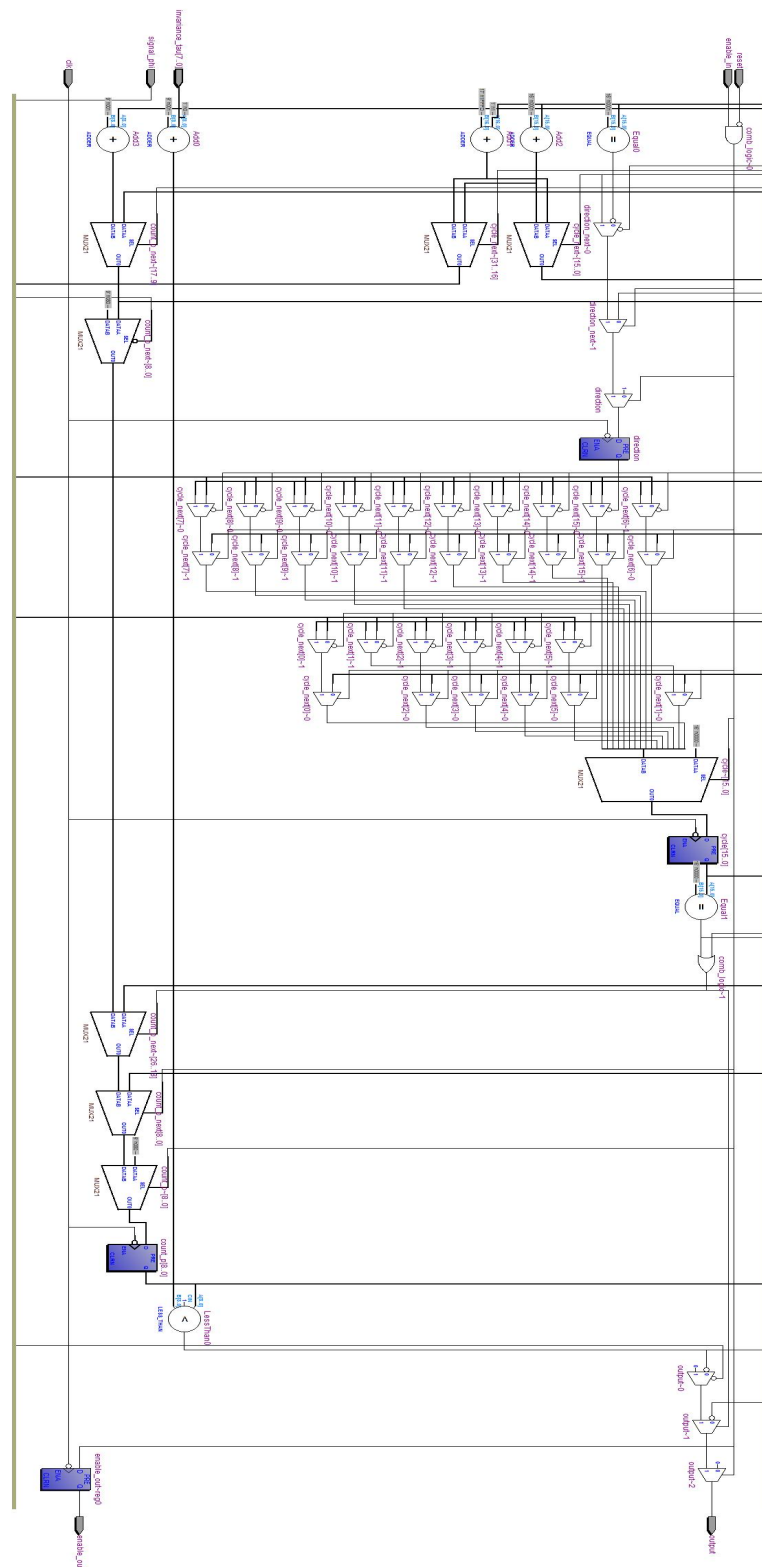


Fig. C.2 Illustration of the Observer Design of the first correct version, but without improvements

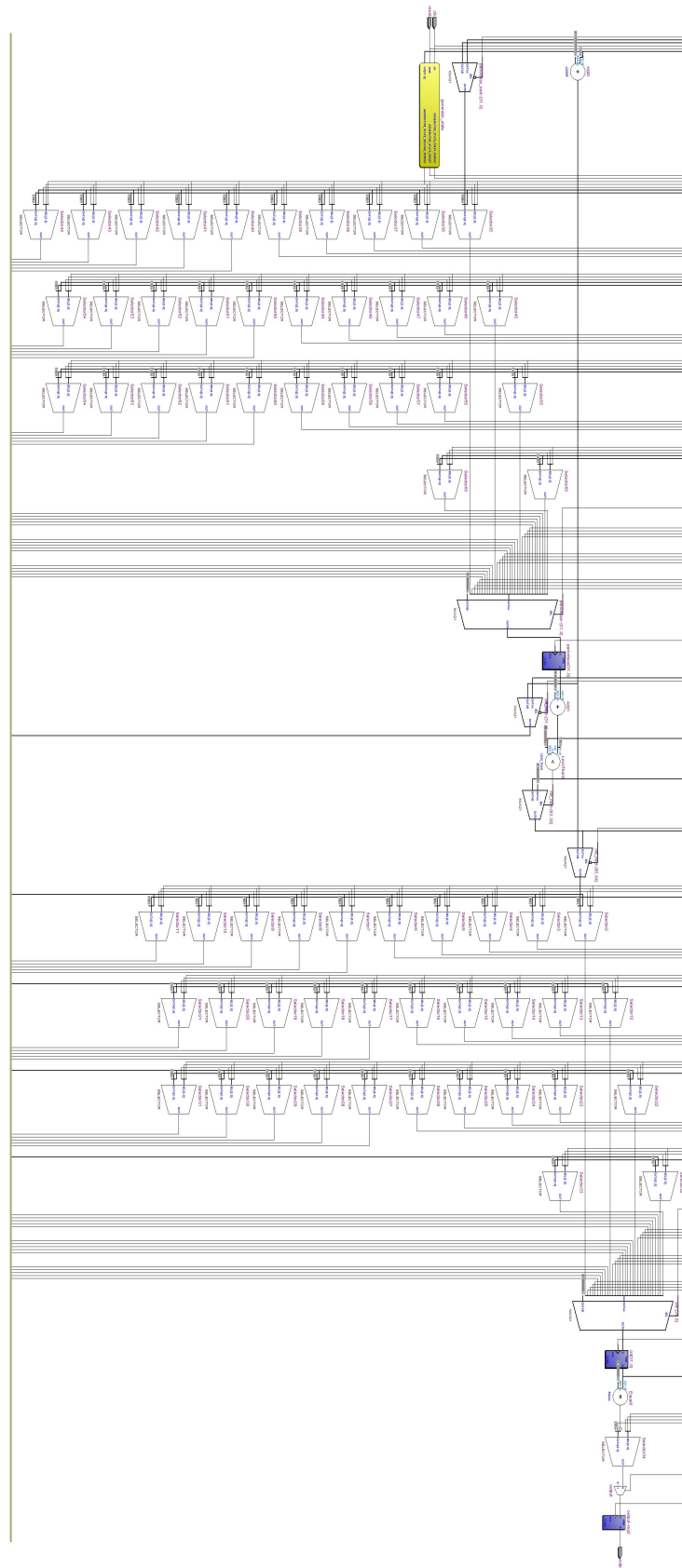


Fig. C.3 Illustration of the Signalgenerator of the first correct version, but without improvements



## **Appendix D**

### **Datasheets and Descriptions**

