

Project report: Nussinov Folding Algorithm for RNA Secondary Structure Prediction

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Algorithm:

Nussinov's algorithm compares given sequence of RNA to itself in order to predict the secondary structure. Dynamic programming is used to calculate the maximum number of matching pairs in the sequence and predict the structure which will be 2D representation of RNA.

Allowed pairs: **A – U & G – C**

Objective:

Identify maximum number of non-crossing pairs in a given RNA sequence and trace back the sequence to predict the secondary structure of RNA (folding of a RNA sequence)

Dynamic Programming:

Let S be a given RNA sequence consisting characters A, C, G, U

Let $\delta(i, j) = 1$ if x_i and x_j are complementary i.e. they form a pair
= 0 otherwise

Initialization:

$dp(i, i-1) = 0$ for $i = 2$ to N
 $dp(i, i) = 0$ for $i = 1$ to N

Recursion:

$$dp(i, j) = \max \left\{ \begin{array}{l} dp(i+1, j), \\ dp(i, j-1), \\ dp(i+1, j-1) + \delta(i, j) \\ \max(dp(i, k) + dp(k+1, j)) \text{ where } i < k < j \end{array} \right\}$$

Result:

$dp(1, N)$ gives the maximum number of paired bases in the given RNA sequence.

Backtracking:

We backtrack from $dp(1, N)$ position till we get diagonal position at which $dp(i, i)$ is zero. $Backtrack(1, N)$ will give the secondary structure of RNA sequence.

Backtrack(i, j):

```
if i == j
    return S(i)
if i > j
    return ""

if dp(i, j) == dp(i + 1, j)
    return S(i) + Backtrack(i + 1, j)

if dp(i, j) == dp(i, j - 1)
    return Backtrack(i, j - 1) + S(j)

if S(i) == S(j) && dp(i, j) == dp(i + 1, j - 1) +  $\delta(i, j)$ 
    return "(" S(i) + Backtrack(i + 1, j - 1) + S(j) + ")"

if (dp(i, j) == dp(i, k) + dp(k + 1, j)) for every  $i < k < j$ 
    return Backtrack(i, k) + Backtrack(k + 1, j);

return "Backtracking failed"
```

Example

1. Input RNA sequence: GGGAAAUCC
Output: Matched pairs: 3
Secondary Structure after folding: G(G(GAA(AU)C)C)
2. Input RNA sequence: AAUCCCAGGA
Output: Matched pairs: 3
Secondary Structure after folding: AAA(UC(C(CAG)G)A)
3. Input RNA sequence: AAUCCCAGGAU
Output: Matched pairs: 4
Secondary Structure after folding: AA(A(UC(C(CAG)G)A)U)

Run Instructions:

Compile: `javac -cp . Nussinov.java`

Run: `java -cp . Nussinov AAAUCCCAGGA`

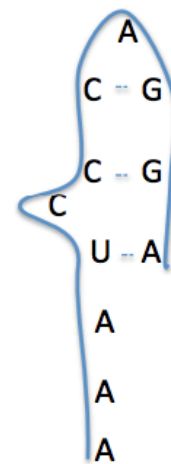
Output:

Matched pairs: 3

Secondary Structure after folding: AAA(UC(C(CAG)G)A)

Visualization of above example:

	A	A	A	U	C	C	C	A	G	G	A
A	0	0	0	1	1	1	1	1	2	3	3
A	0	0	0	1	1	1	1	1	2	3	3
A		0	0	1	1	1	1	1	2	3	3
U			0	0	0	0	0	1	1	2	3
C				0	0	0	0	0	1	2	2
C					0	0	0	0	1	2	2
C						0	0	0	1	1	1
A							0	0	0	0	0
G								0	0	0	0
G									0	0	0
A										0	0



Complexity:

Space complexity: $O(n^2)$

Time complexity along with backtrack: $O(n^2)$