

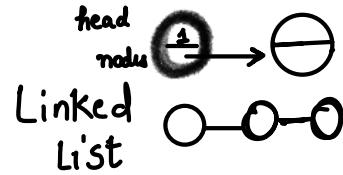
Trees - 1

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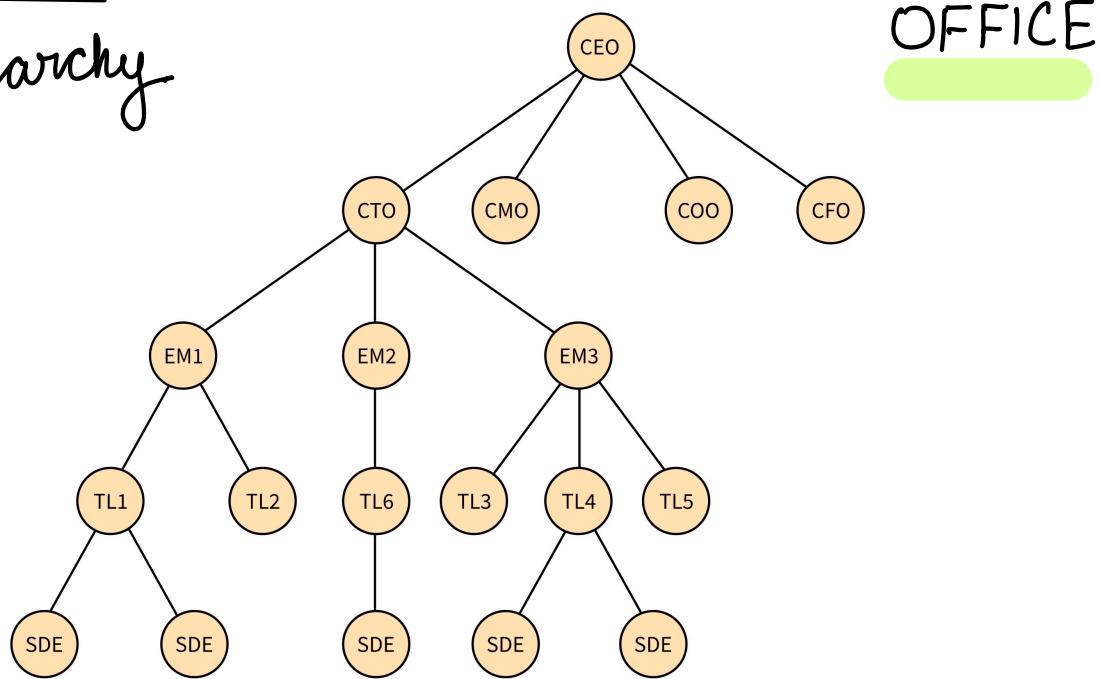
<p>For normal people</p>	<p>A diagram of a tree with a thick trunk and many branches extending upwards towards the top left. The roots are visible at the top of the trunk. Below the tree, the text "Root at top" is written.</p>
<p>For program - mers</p>	



Trees

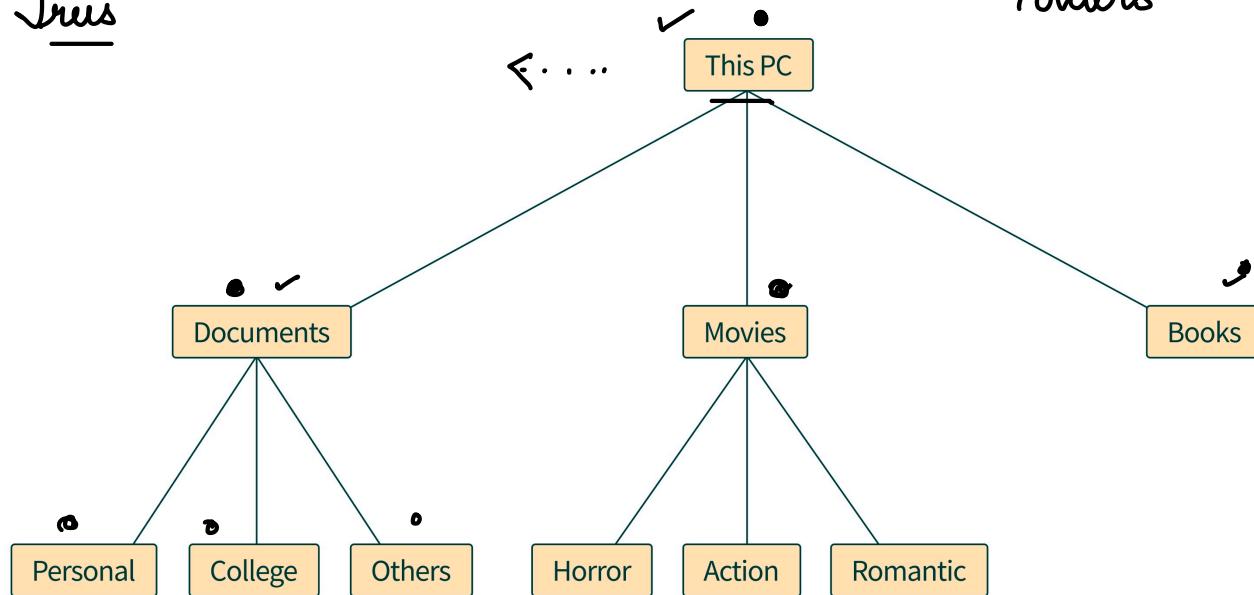
NonLinear

hierarchy

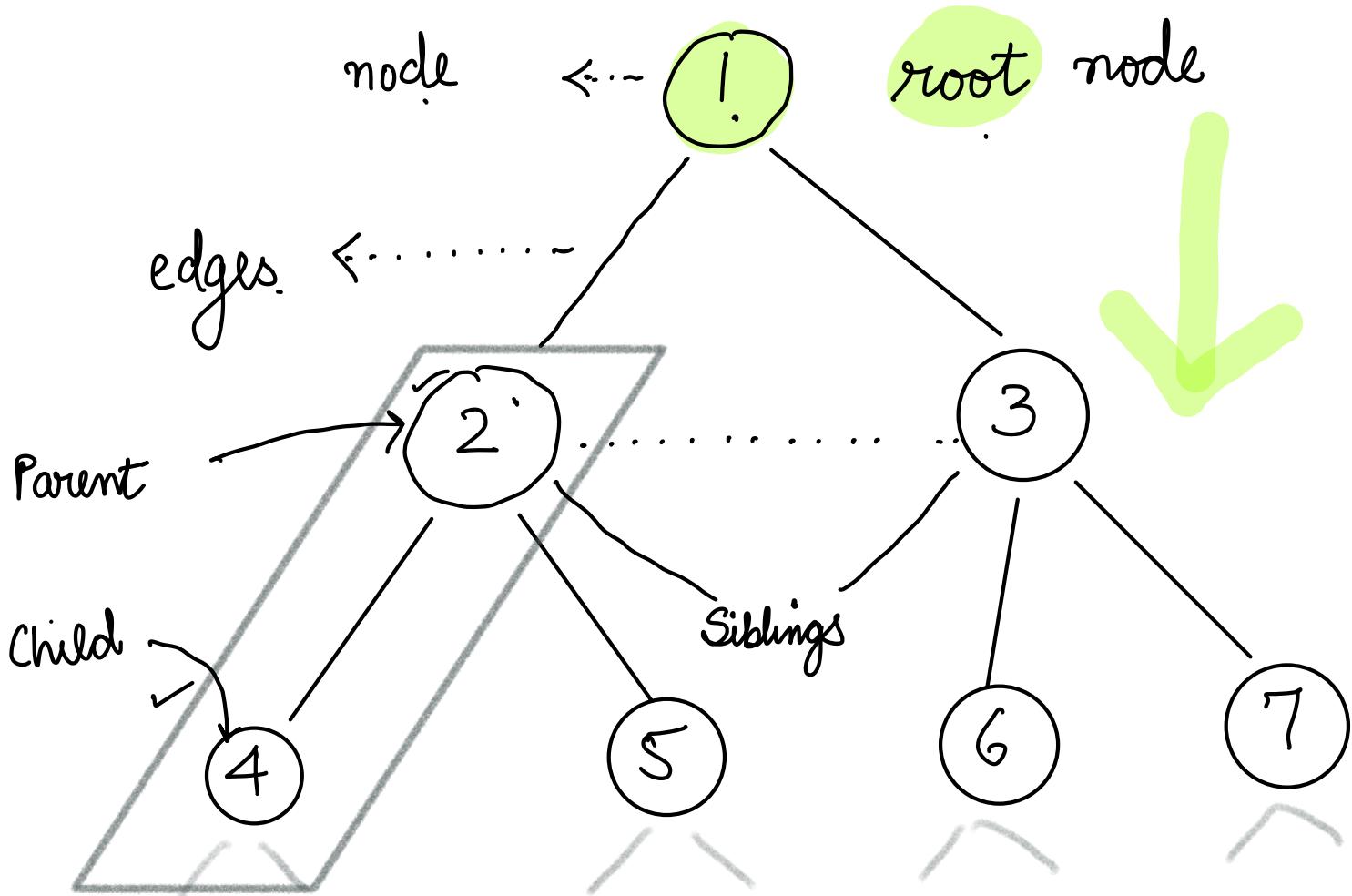


Trees

Folders



height &
depth

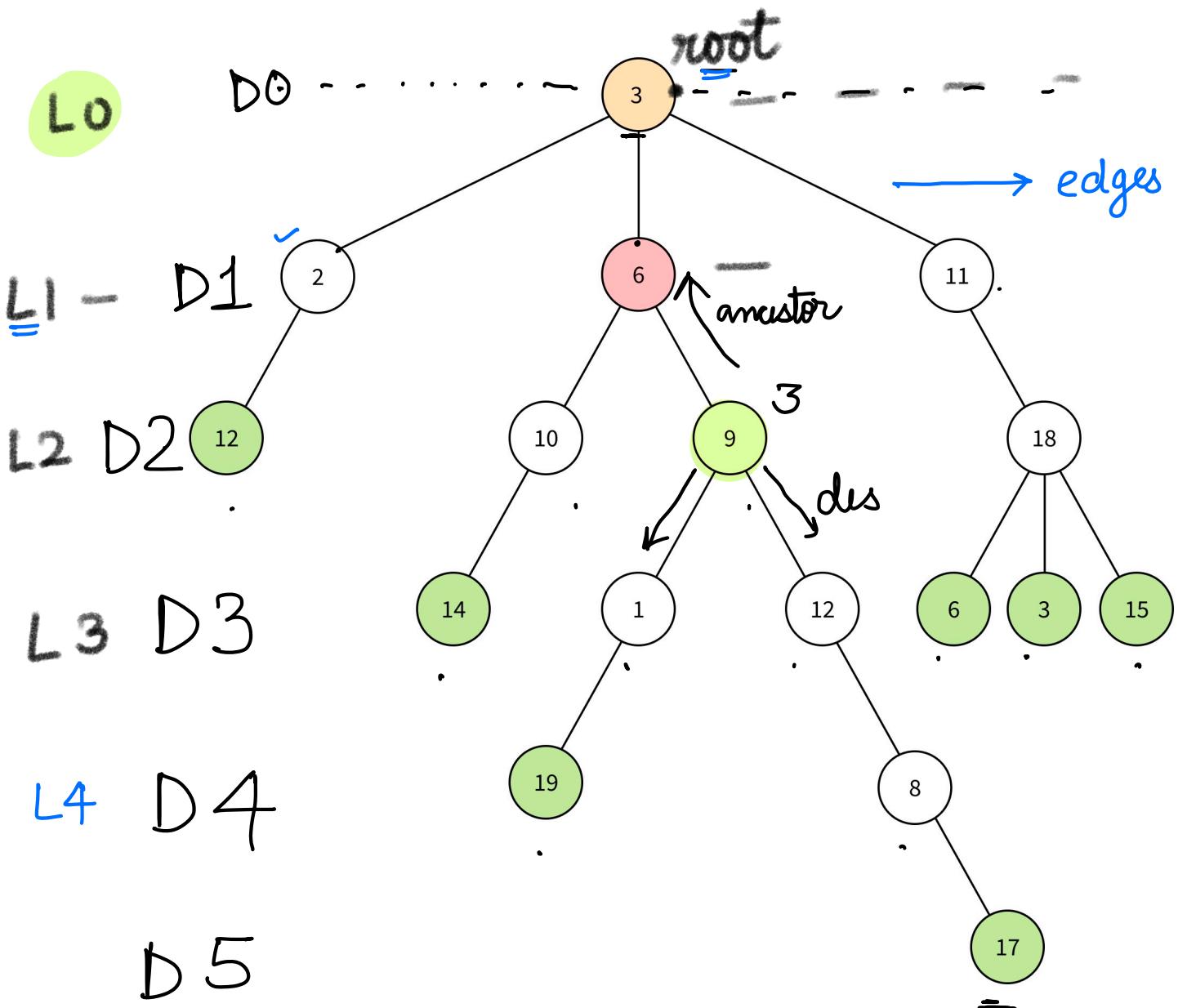


Leaf nodes = 0 children

Sibling



data - int

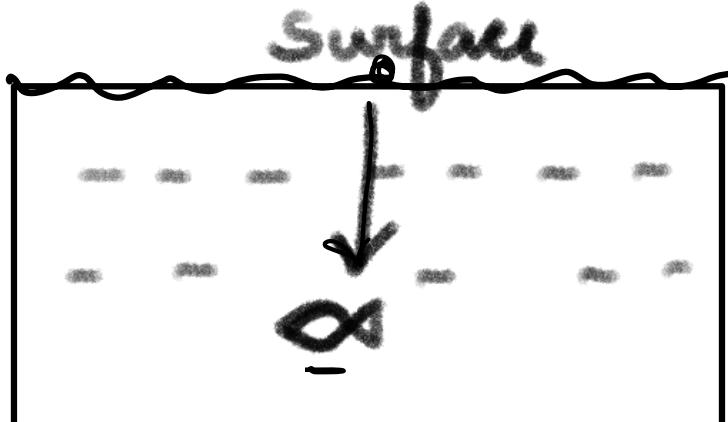


11 - Parent

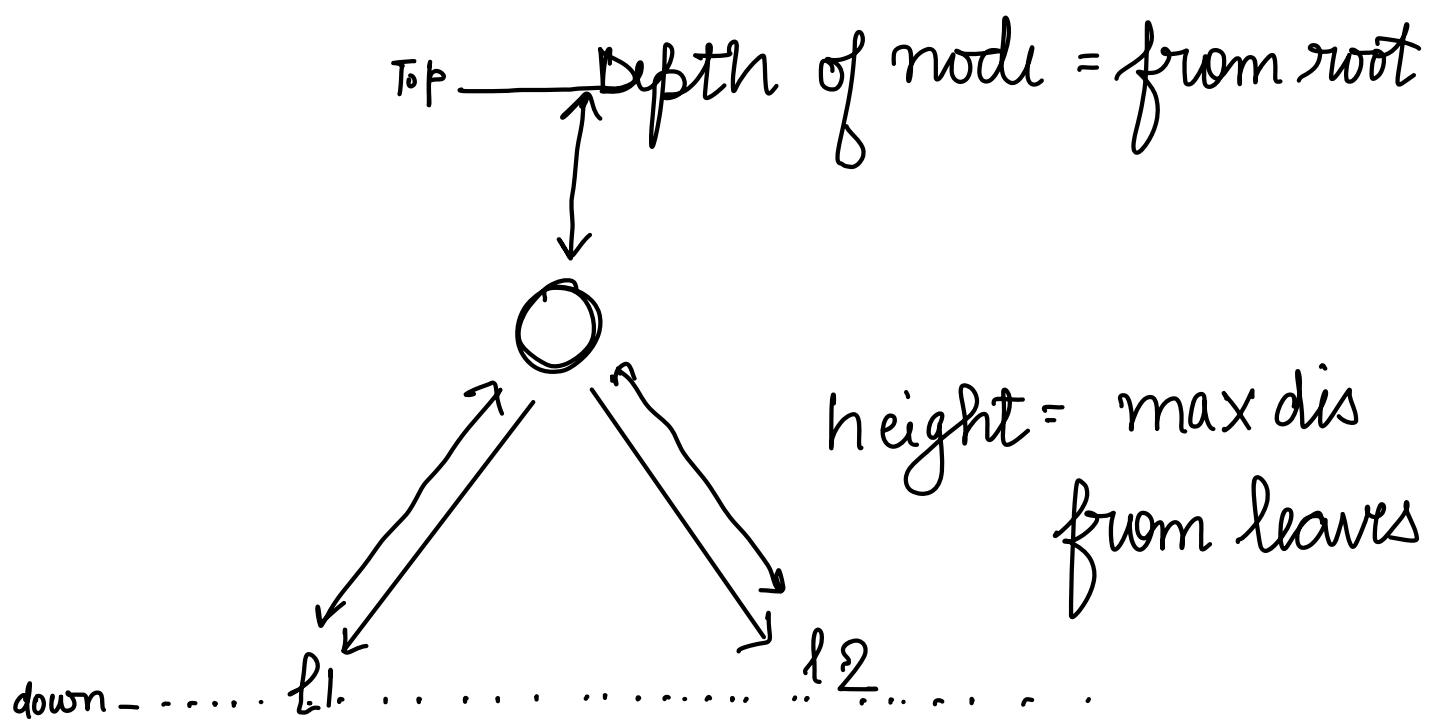
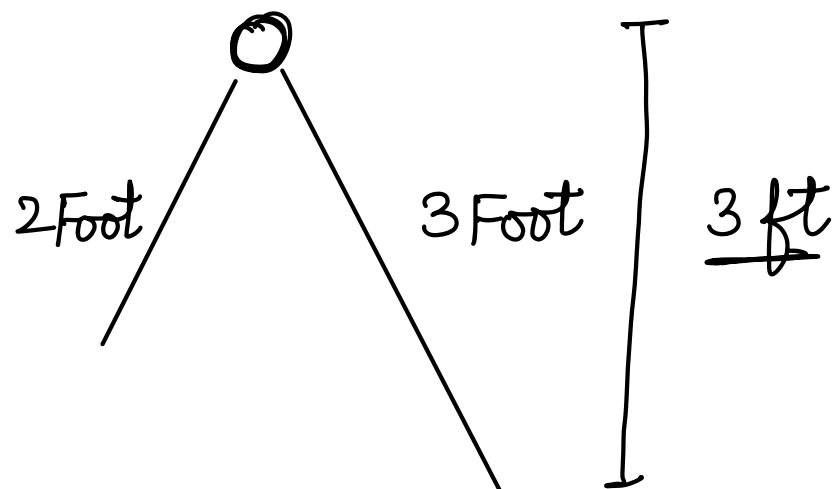
18 - child node

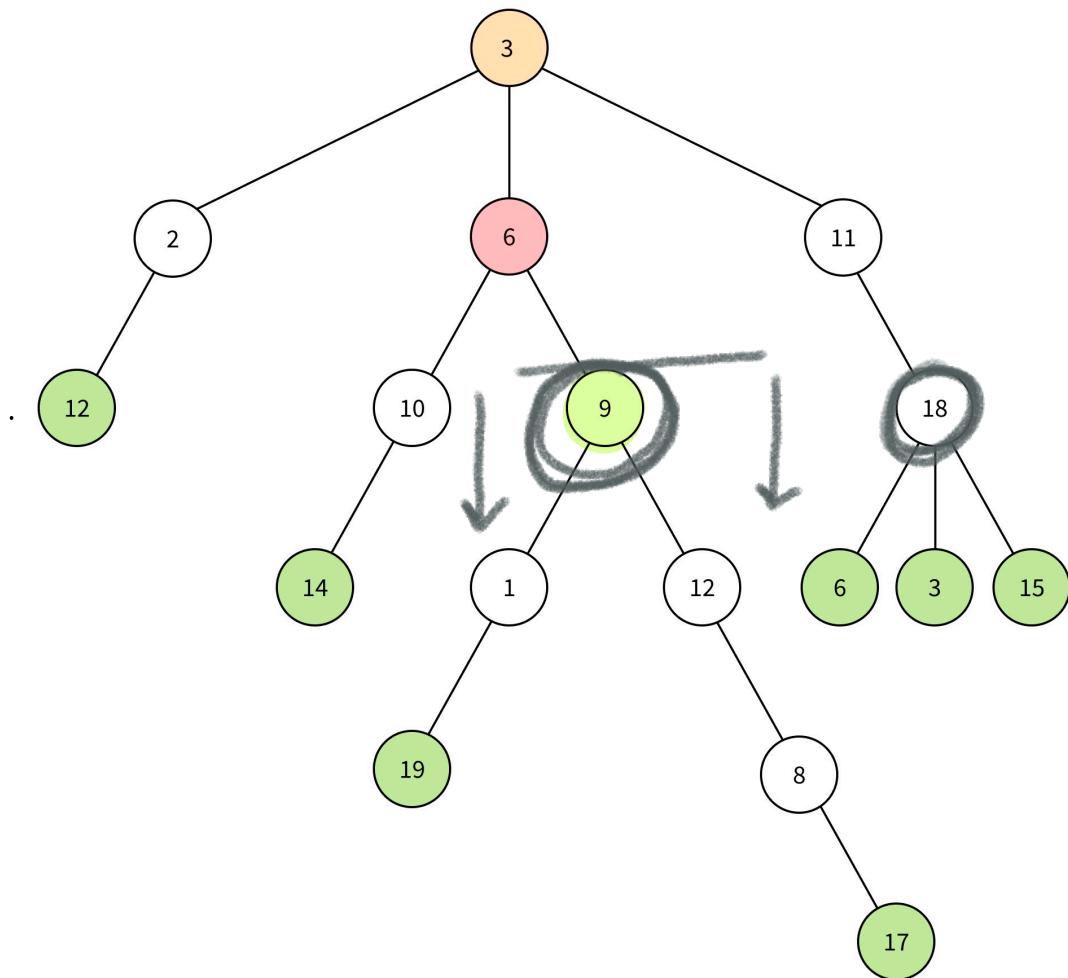
10 - 9 - 18
- Siblings -

Depth



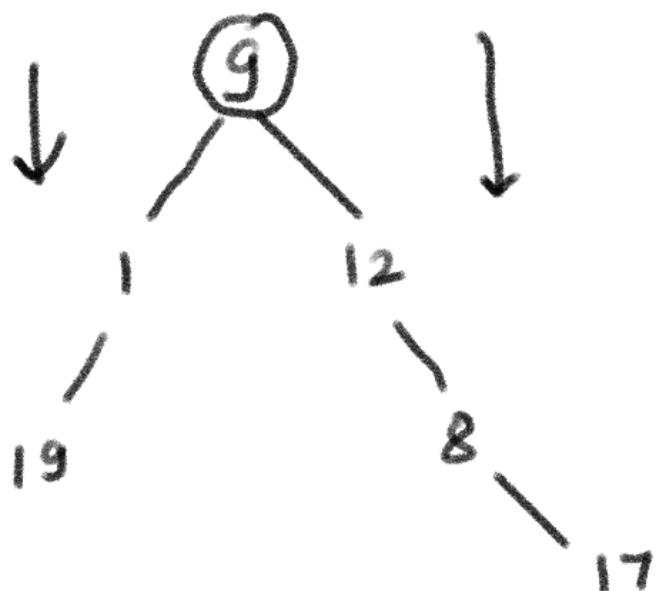
height :





Subtree at 9

any part of tree



Can leaf be a subtree?

Yes

Do all nodes have parent node? No.

Who is root's parent? — No parent

\Rightarrow Depth of root node = 0

\Rightarrow height of leaf node = 0

— L

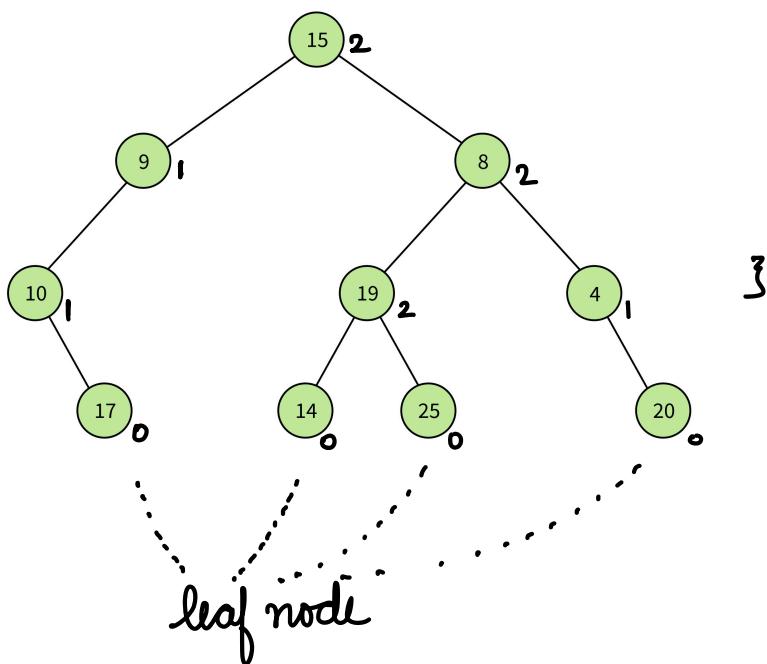
$\therefore 2 \rightarrow l, r$
 $\therefore 1$ either l or r



$2, 1, 0 \dots \cdot l = \text{null}$
 $r_2 = \text{null}$

Binary Tree

2

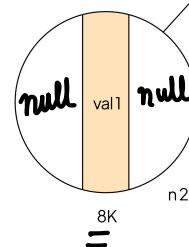
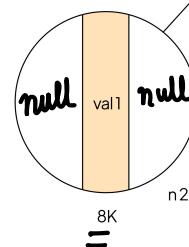
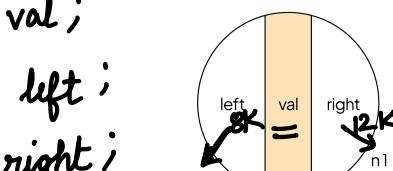


✓ class Node {

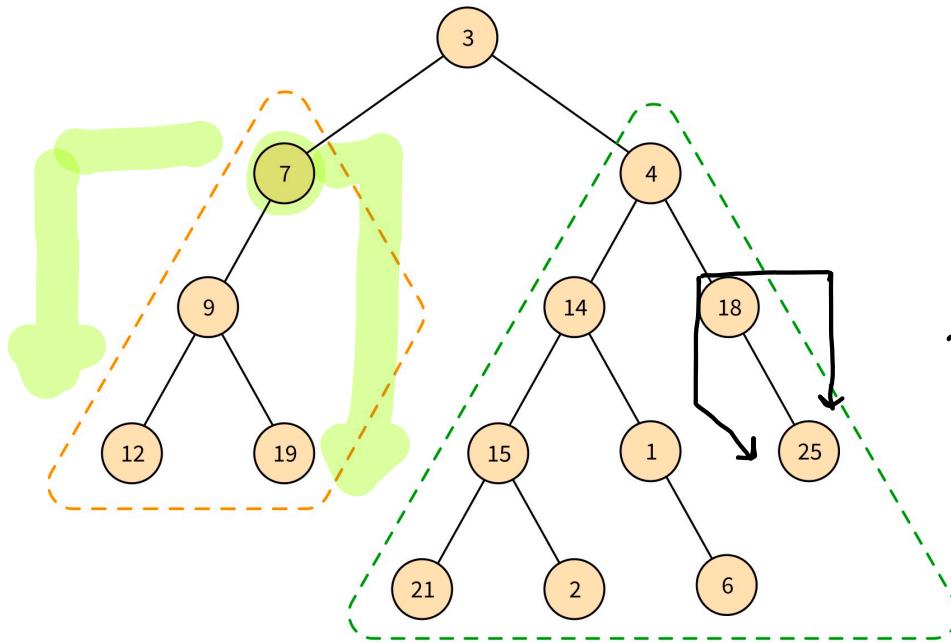
int val;

Node left;

Node right;



Sub-tree



```

class Node:
    def __init__(self, data):
        self.data = data
        self.left = None
        self.right = None

```

```
print("Hello, World!")
```

```

root = Node(10)
n1 = Node(20)
n2 = Node(30)
n3 = Node(30)
n4 = Node(30)

```

```

root.left = n1
root.right = n2
n1.left = n3
n1.right = n4

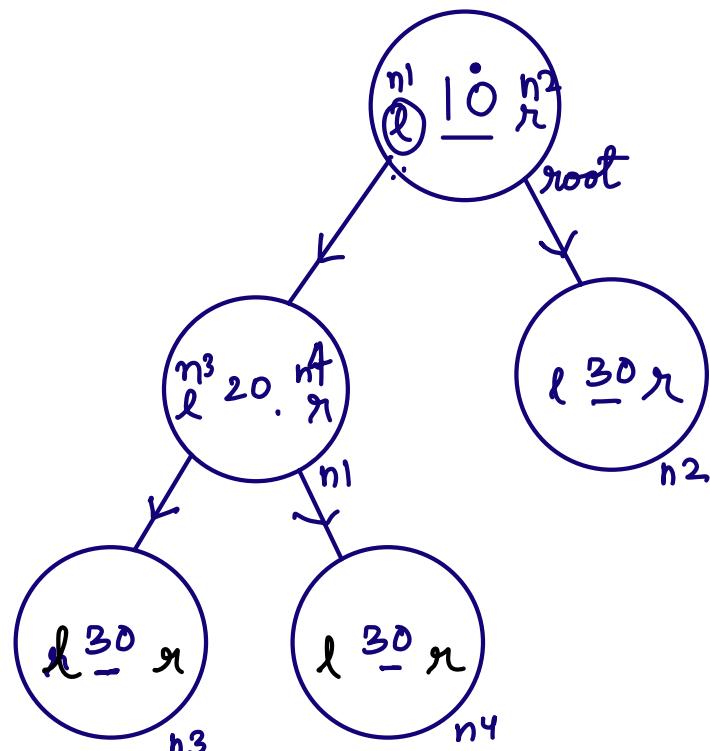
```

class Node {

```

def __init__(self, data):
    self.data = data
    self.left = None
    self.right = None

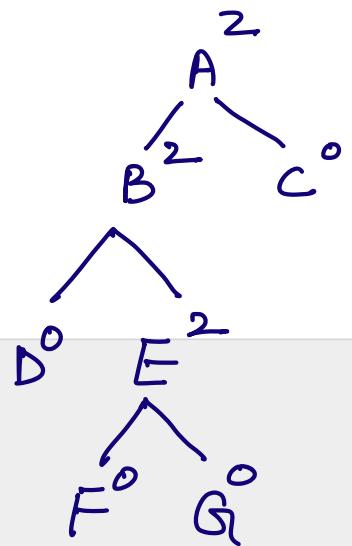
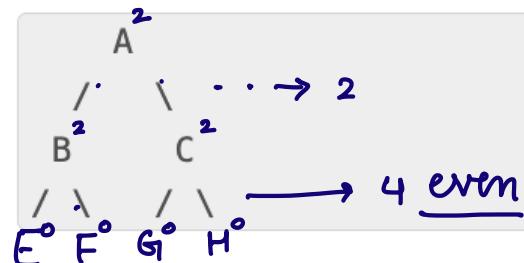
```



1. Proper Binary Tree (Strict Binary Tree):

Every node has either 0 or 2 children (never 1 child).

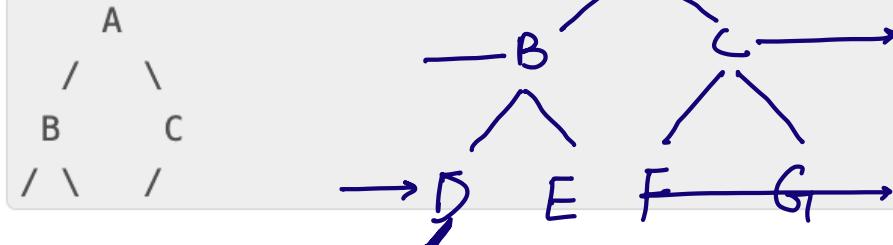
Diagram:



2. Complete Binary Tree:

All levels are filled except possibly the last level, which is filled left to right.

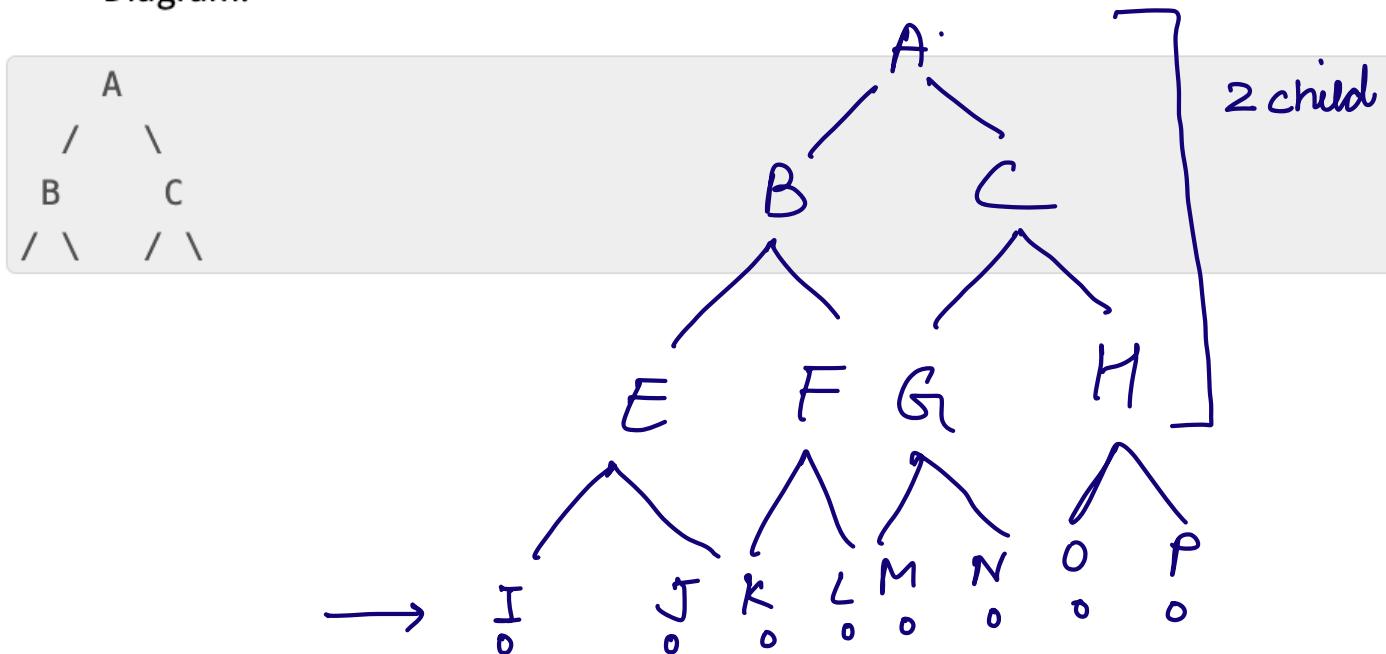
Diagram:



3. Perfect Binary Tree:

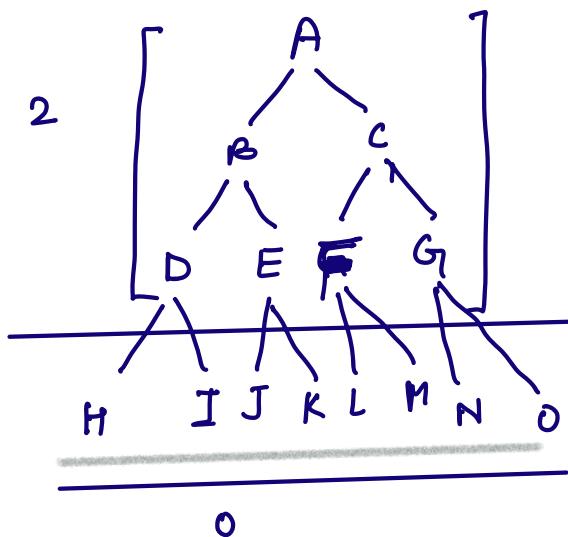
All internal nodes have exactly two children, and all leaf nodes are at the same level.

Diagram:



Quiz:

Perfect binary



✓ Proper → 2
0

✓ Complete Binary tree

Recursion - 1 level down

P void traverse_tree (Node root) {

 traverse_tree (root.left)

 traverse_tree (root.right)

 print (root)

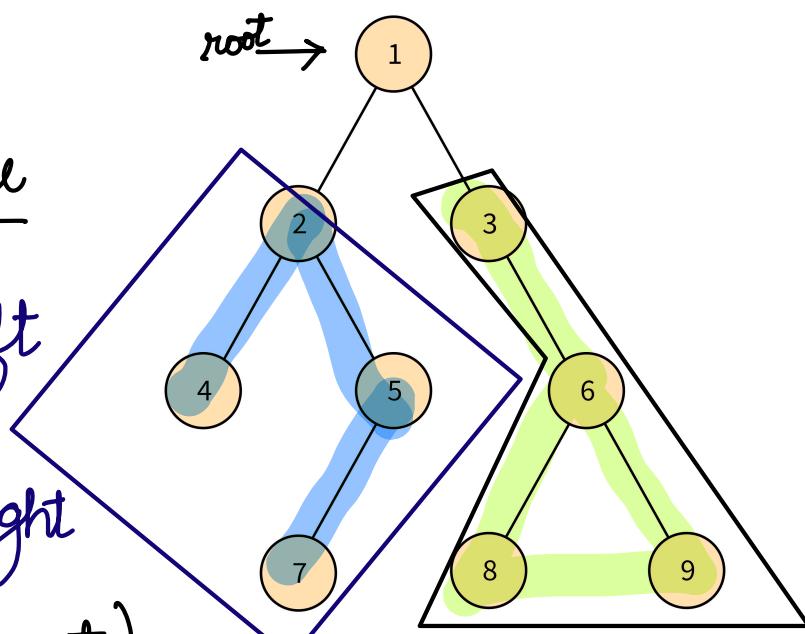
}

P - print tree

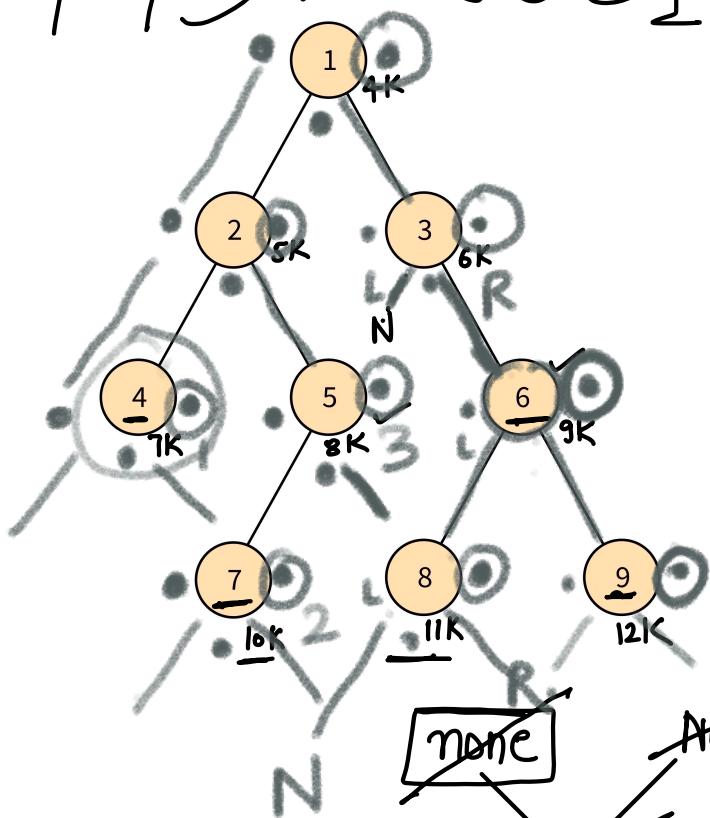
SP1 = root.left
2 4 5 7

SP2 = root.right
3 6 8 9

EW = print (root)



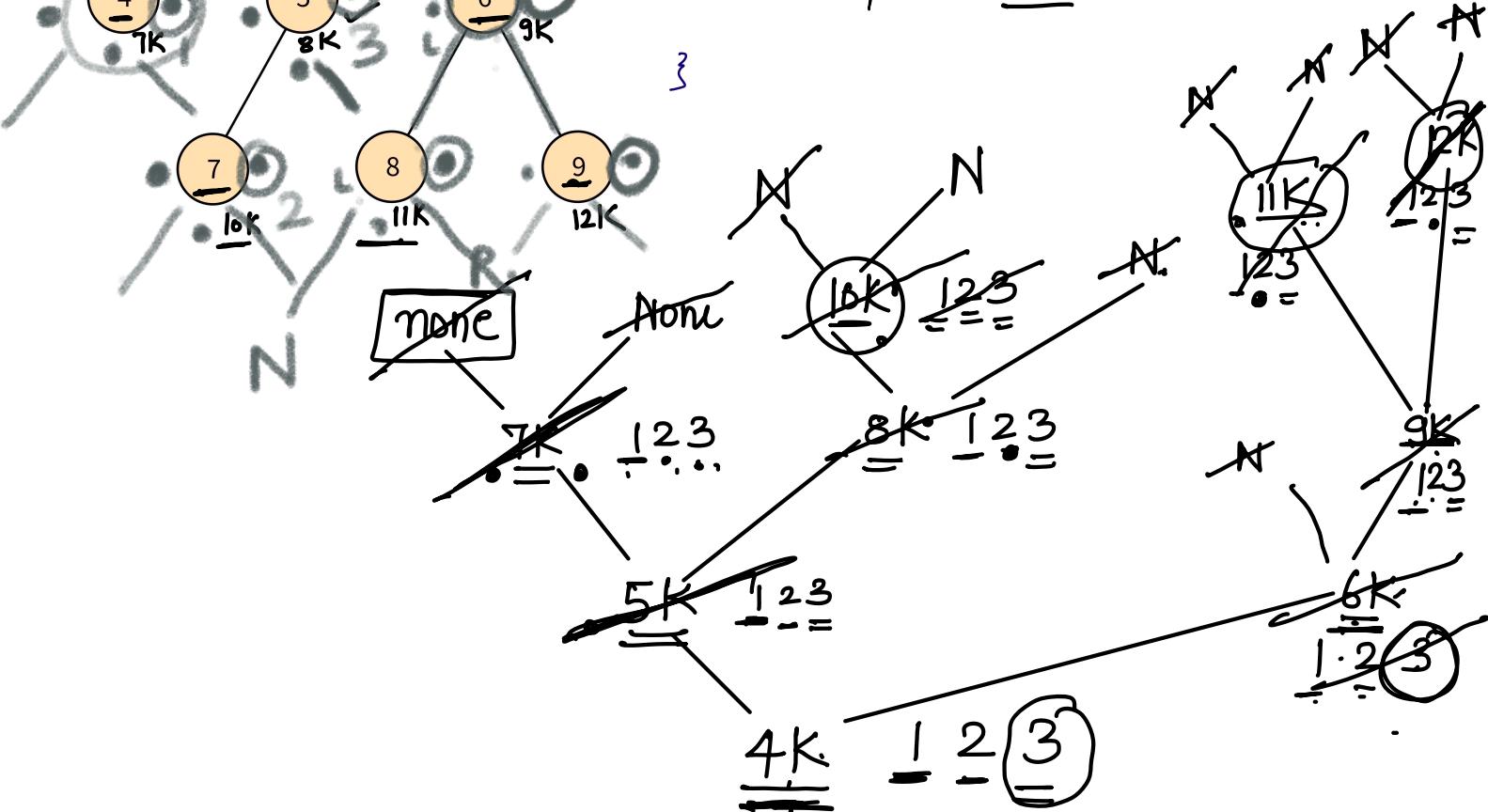
4 7 5 2 8 9 6 3 1

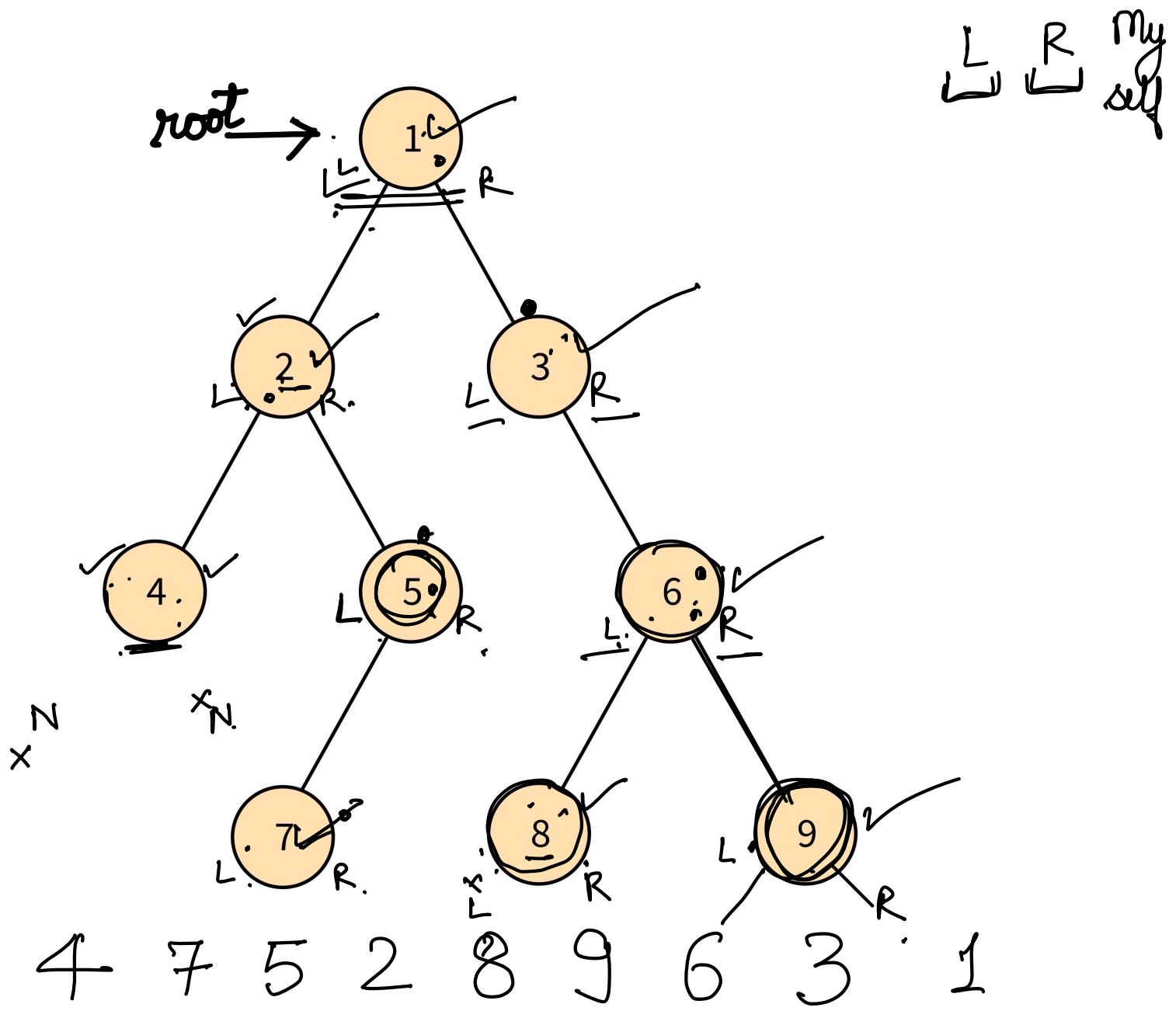


```

void traverse_tree (Node root) {
    if root == None: return
    traverse_tree (root.left) 1
    traverse_tree (root.right) 2
    print (root.data) 3
}

```





P

```
void printTree (Node root) {
```



SP1

```
    printTree (root.left)
```

SP2

```
    printTree (root.right)
```

→

```
    print (root.data)
```

}

```
void traverseTree (Node root) {
    if root == None: return
    traverseTree (root.left) 1
    traverseTree (root.right) 2
    print (root.data) 3
```

3

```
void traverseTree (Node root) {
    if root == None: return
    traverseTree (root.left) 1
    print (root.data) 2
    traverseTree (root.right) 3
```

3

Post
Order

InOrder

```
void traverse_tree (Node root) {  
    if root == None: return  
    print (root.data)  
    traverse—true (root.left)  
    traverse—true (root.right)
```

}

pre ✓

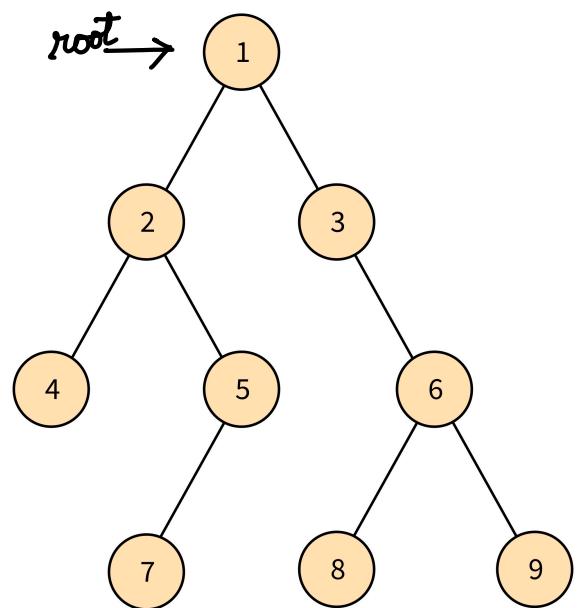
Binary Tree Traversal

Pre-order Traversal - Root Left Right

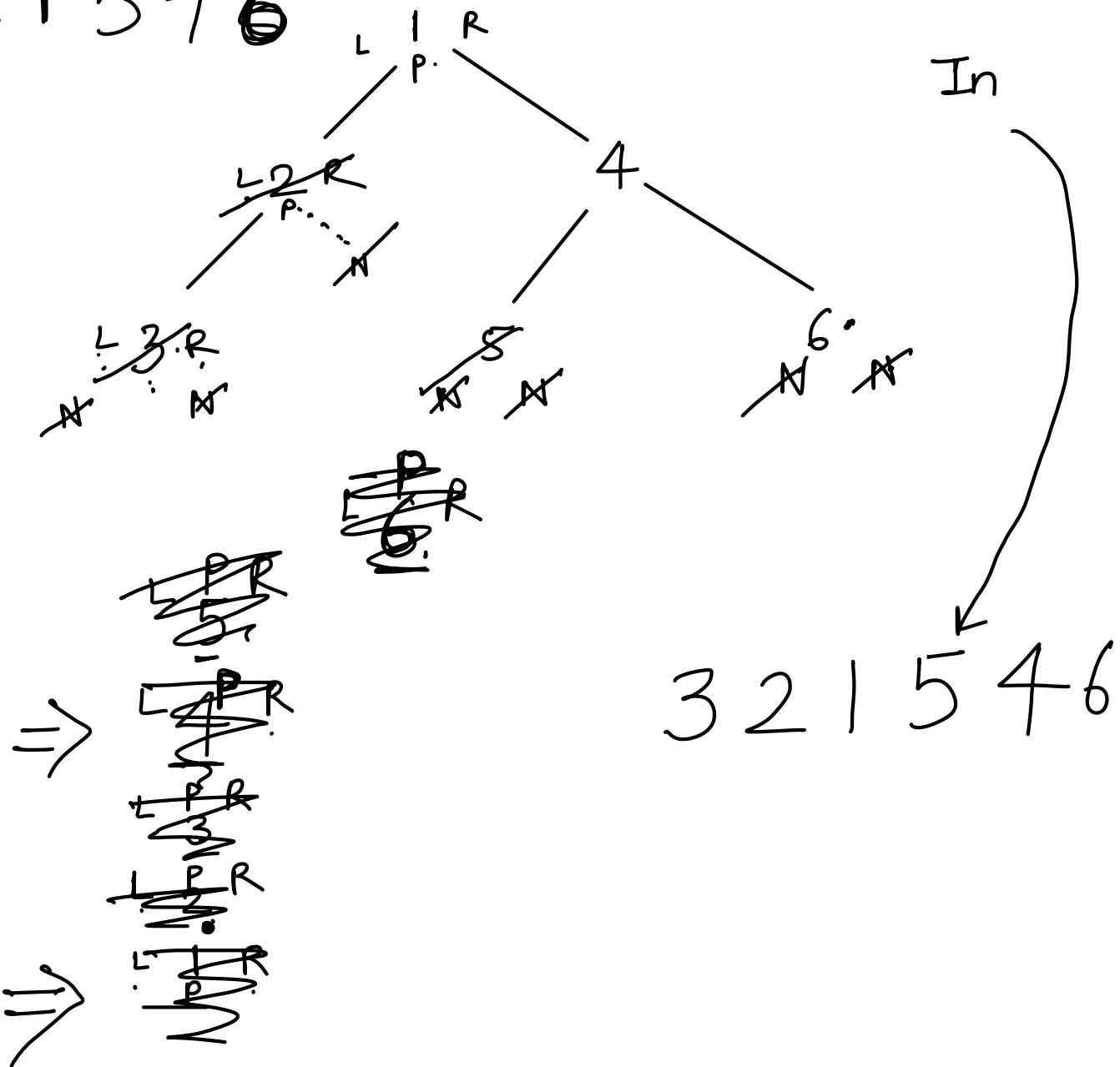
In-order Traversal - Left Root Right

Post-order Traversal - Left Right Root

} Recursive traversal



3 2 1 5 4 6



Iterative In-order Traversal

Recursion Stack
our own Stack

4 2 5 1 3

```
if (p == null)
    pop();
    print();
    pop().right
```

```
def inorder_iterative (root) :
    curr = root
    st = []
```

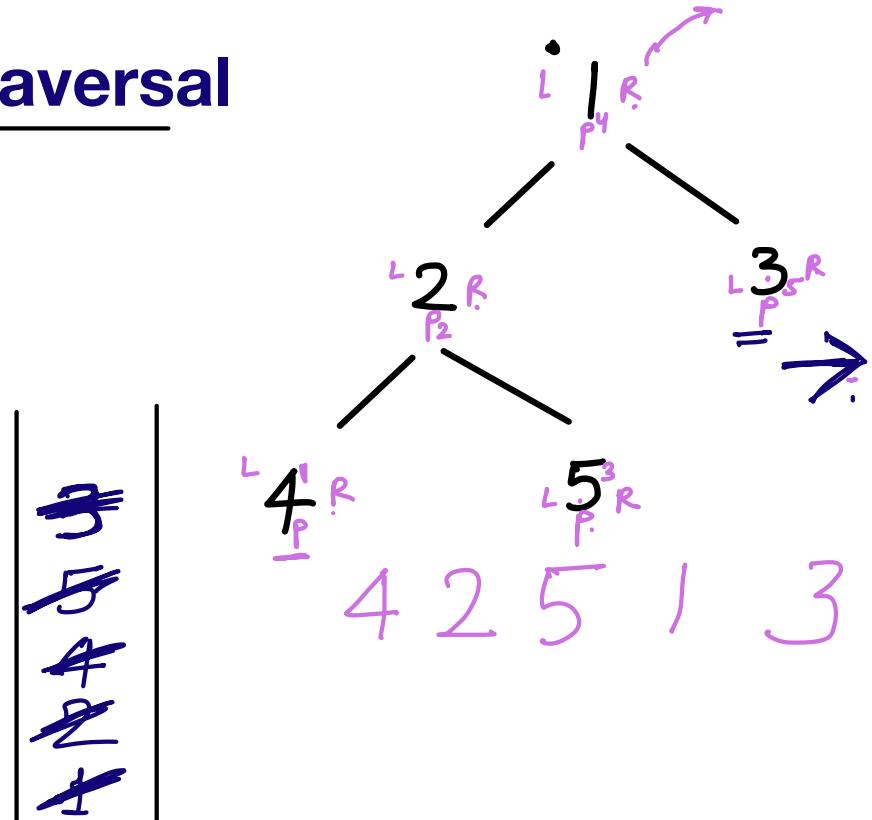
while curr != None or len(st) > 0 :

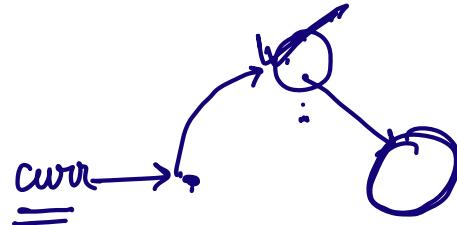
```
    if curr is not None :
        st.append(curr)
        curr = curr.left
```

```
    else :
        curr = st.pop()
        print (curr.data)
        curr = curr.right
```

TC: O(N)

SC: O(N)





 Pseudocode:

```

while ( st.isEmpty() == false || curr != null ) {
  if ( curr != null ) {
    st.push( curr )
    curr = curr.left
  } else {
    curr = st.pop()
    print( curr.data )
    curr = curr.right
  }
}
  
```

```
def inorder_iterative (root) :
```

 curr = root

 ✓ st = []

 while curr F != None or len(st) > 0:

 if curr is not None:

 st.append(curr)

 curr = curr.left

 else:

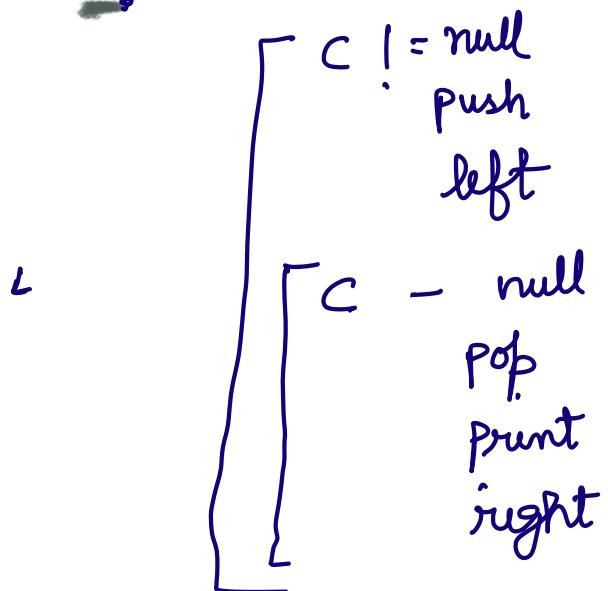
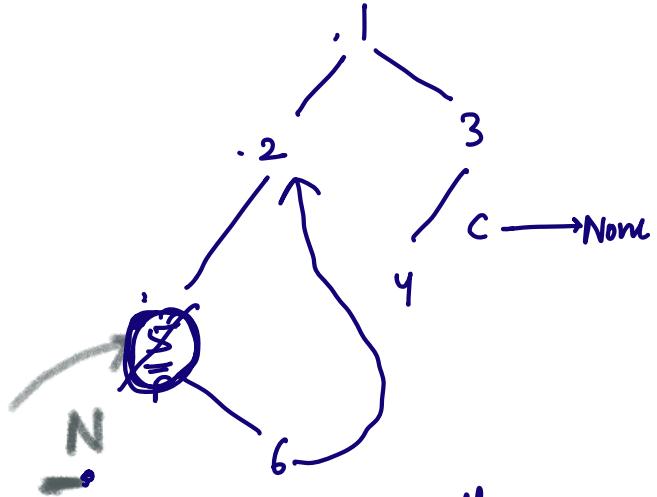
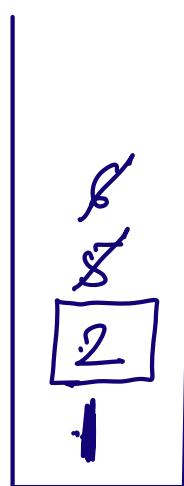
 curr = st.pop() ✓

 print (curr.data) ✓

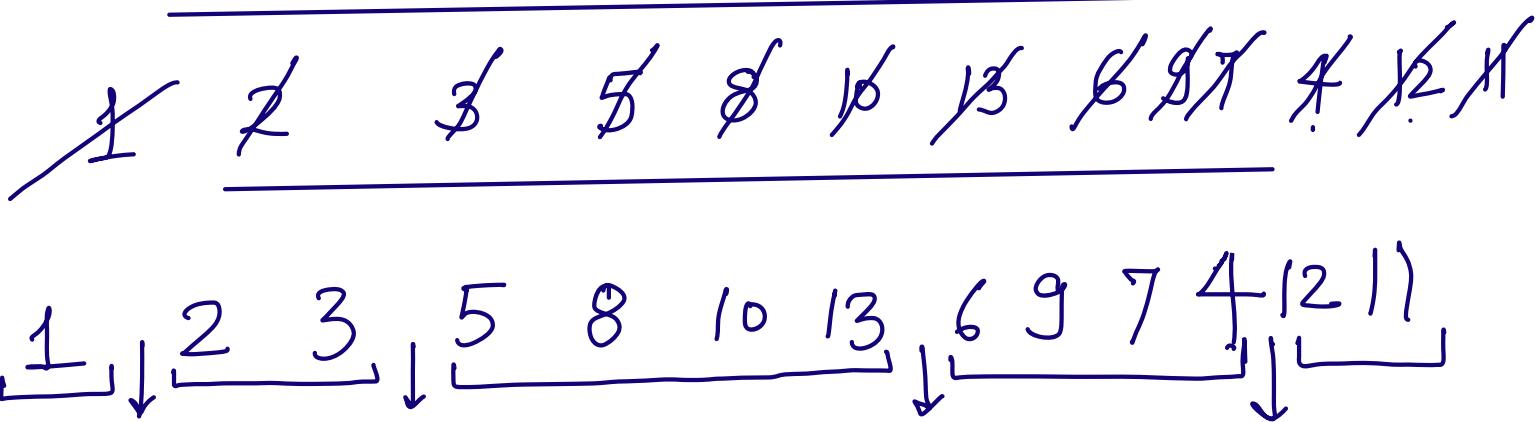
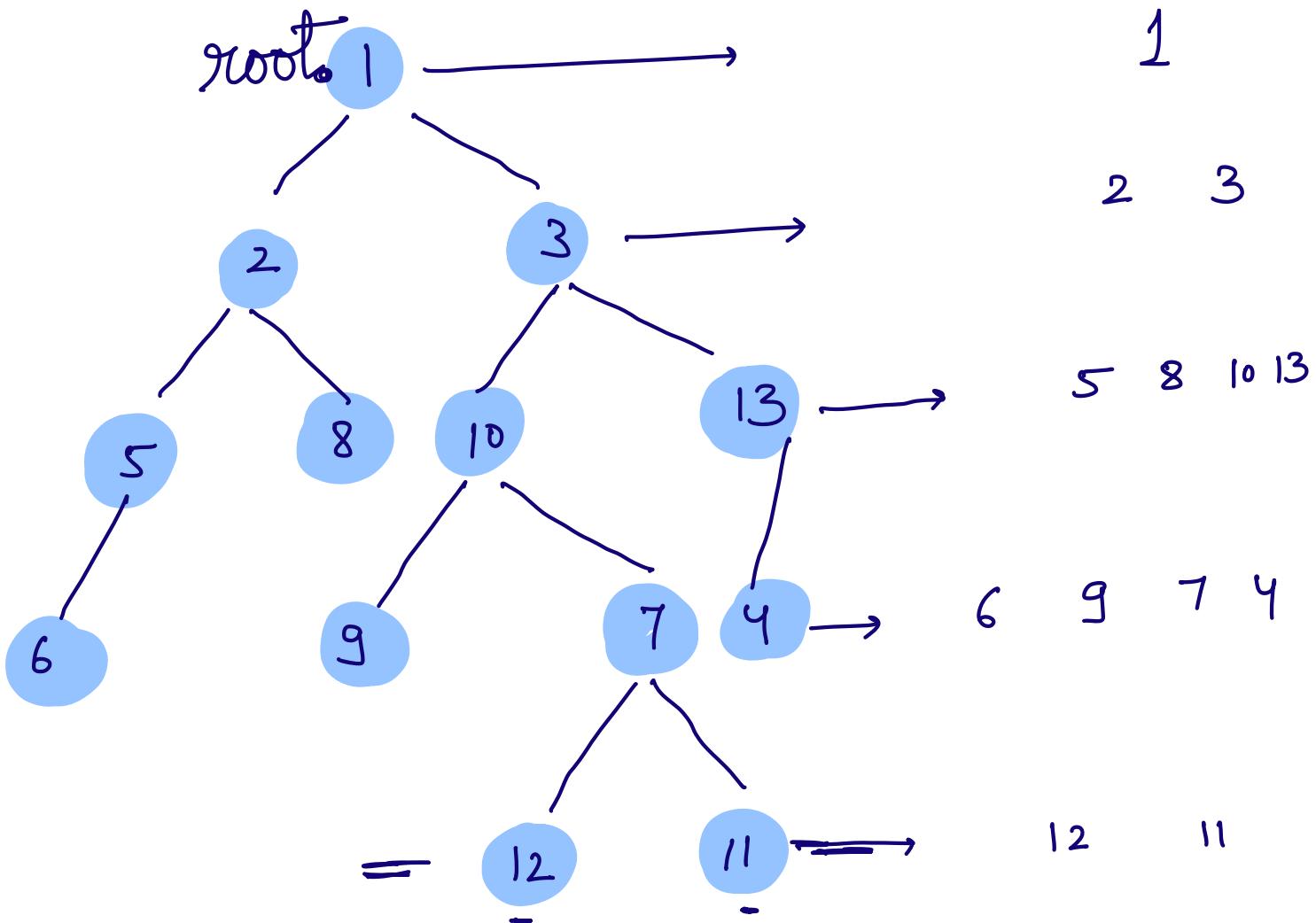
 curr = curr.right ✓

L p R
print

5 6 2 1 4 3



Level Order traversal



while

$q.\text{isEmpty}()$
== false

R
P
A L
A R

✓

$q.\text{enqueue}(root)$

while (not $q.\text{empty}()$)

$x = q.\text{dequeue}()$

print ($x.\text{data}$)

if $x.\text{left} \neq \text{none}$:

$q.\text{enqueue}(x.\text{left})$

if $x.\text{right} \neq \text{none}$:

$q.\text{enqueue}(x.\text{right})$

q. enqueue(root)

last

while (not q. empty())

x = q. dequeue()

print (x. data)

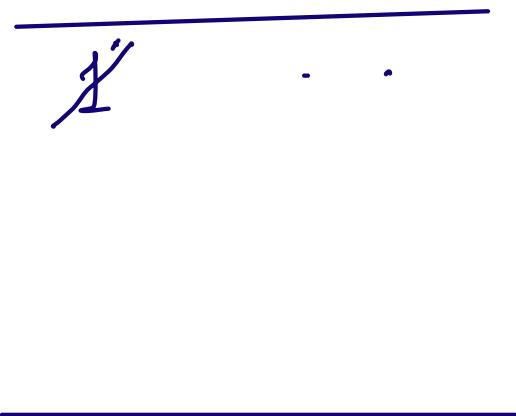
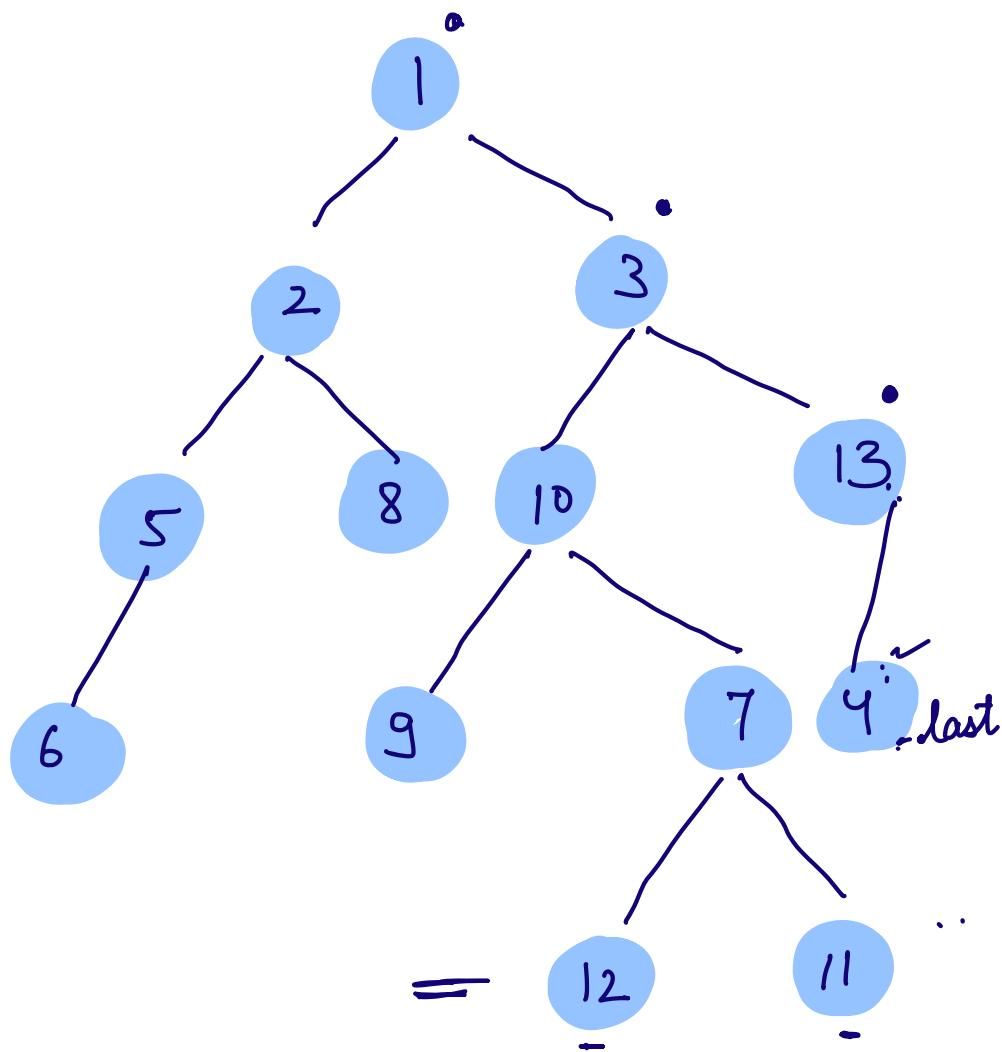
if x. left != none :

q. enqueue(x. left)

if x. right != none :

q. enqueue(x. right)

last = ①



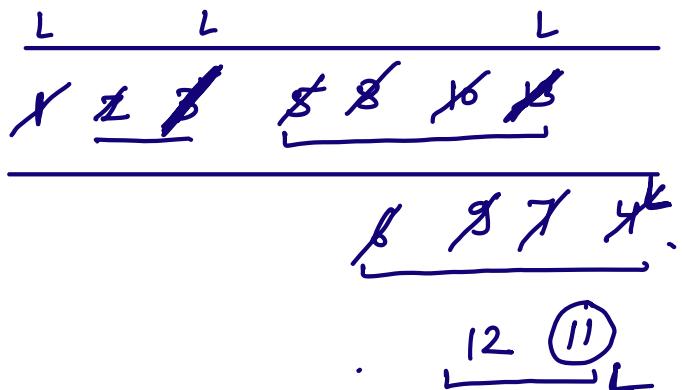
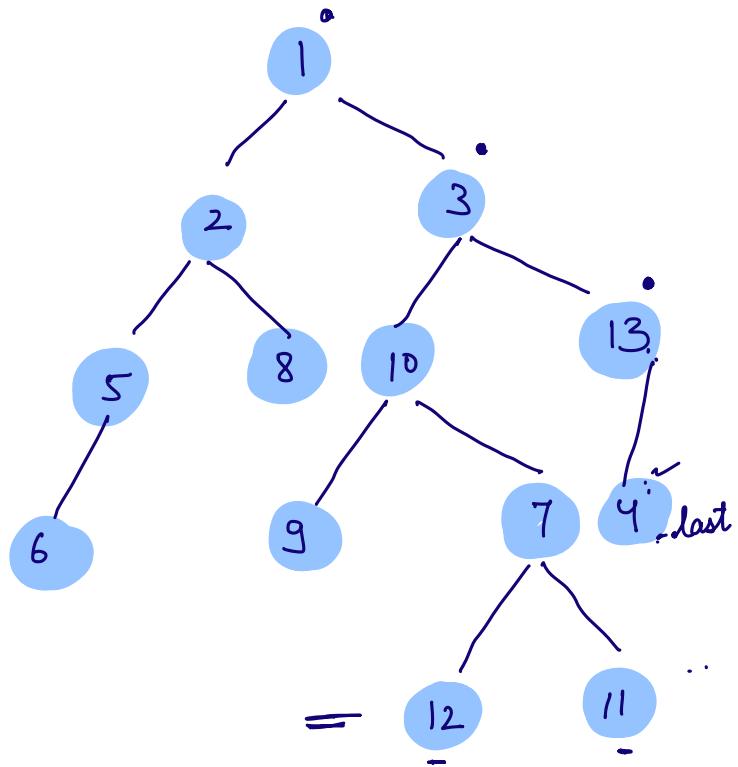
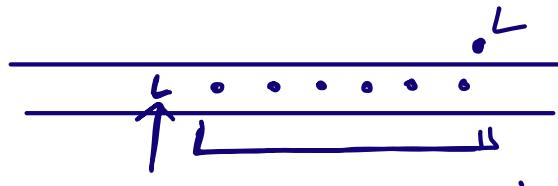
Case 1 → if last node → R & L

Last node = R
of next level

Case 2 → Last Node → L

Last of
next level = L

Case 3 → Last Node → None



when L is removed,
next level is
completely inside
queue

q. enqueue(root)

$$\text{last} = \sqrt{\text{root}}$$

```
last = root
while ( not q.empty() )
    |           x = q.dequeue()
```

brint (x. data)

if $x.\text{left} \neq \text{none}$: $q.\text{enqueue}(x.\text{left})$

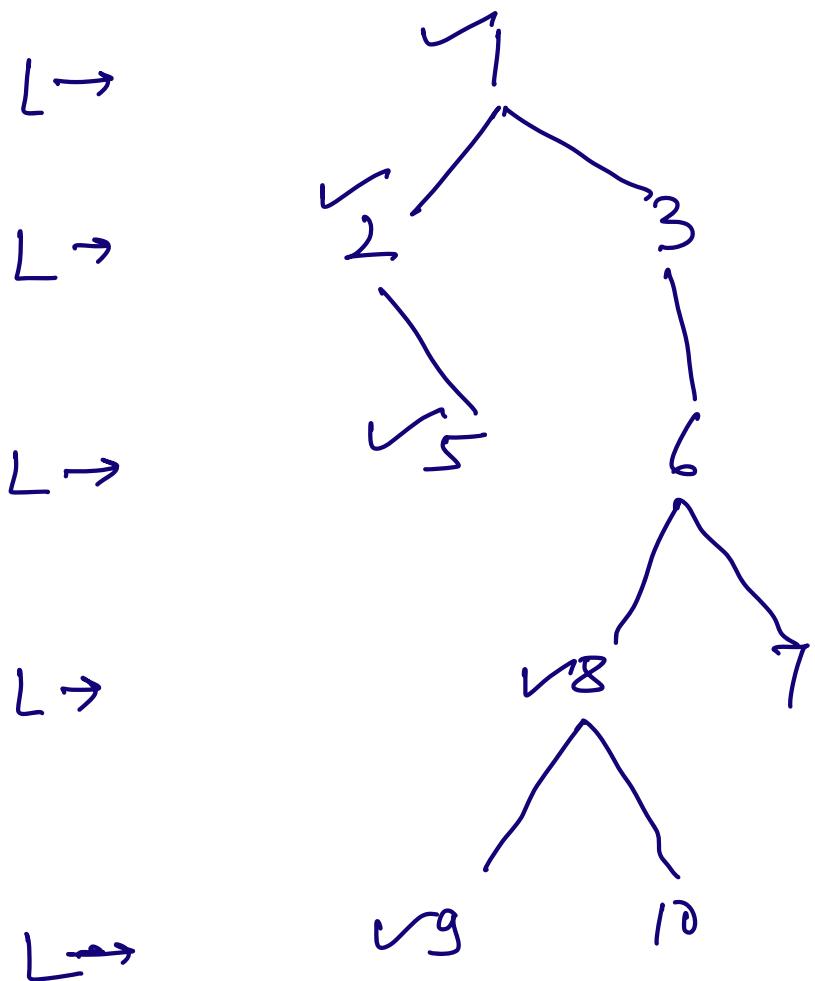
if $x.\text{right} \neq \text{none}$: $q.\text{enqueue}(x.\text{right})$

if ($x == \text{last}$) { print ("\\n") }

point ("\\n")
last = q.rear()

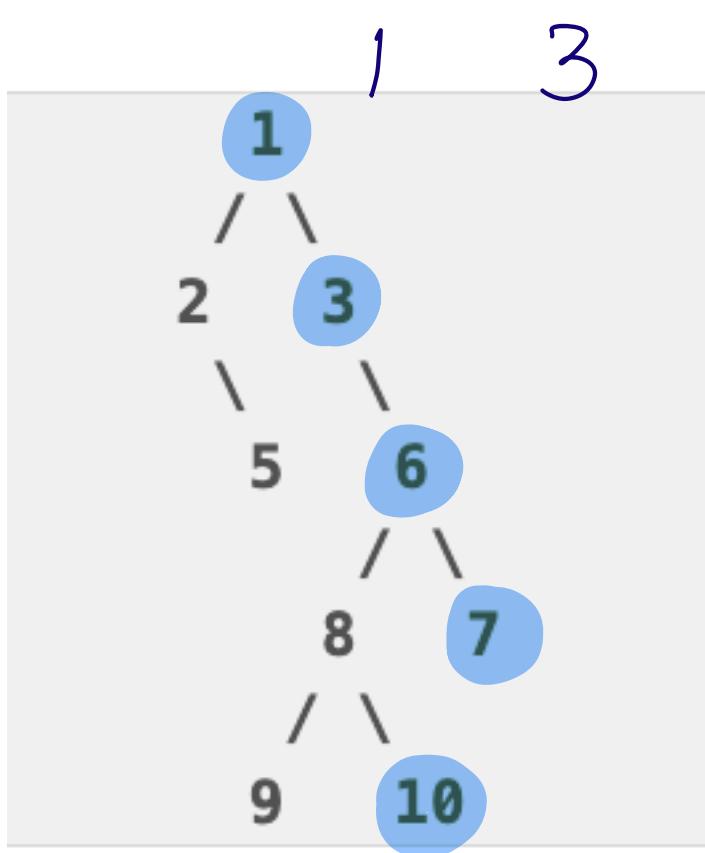
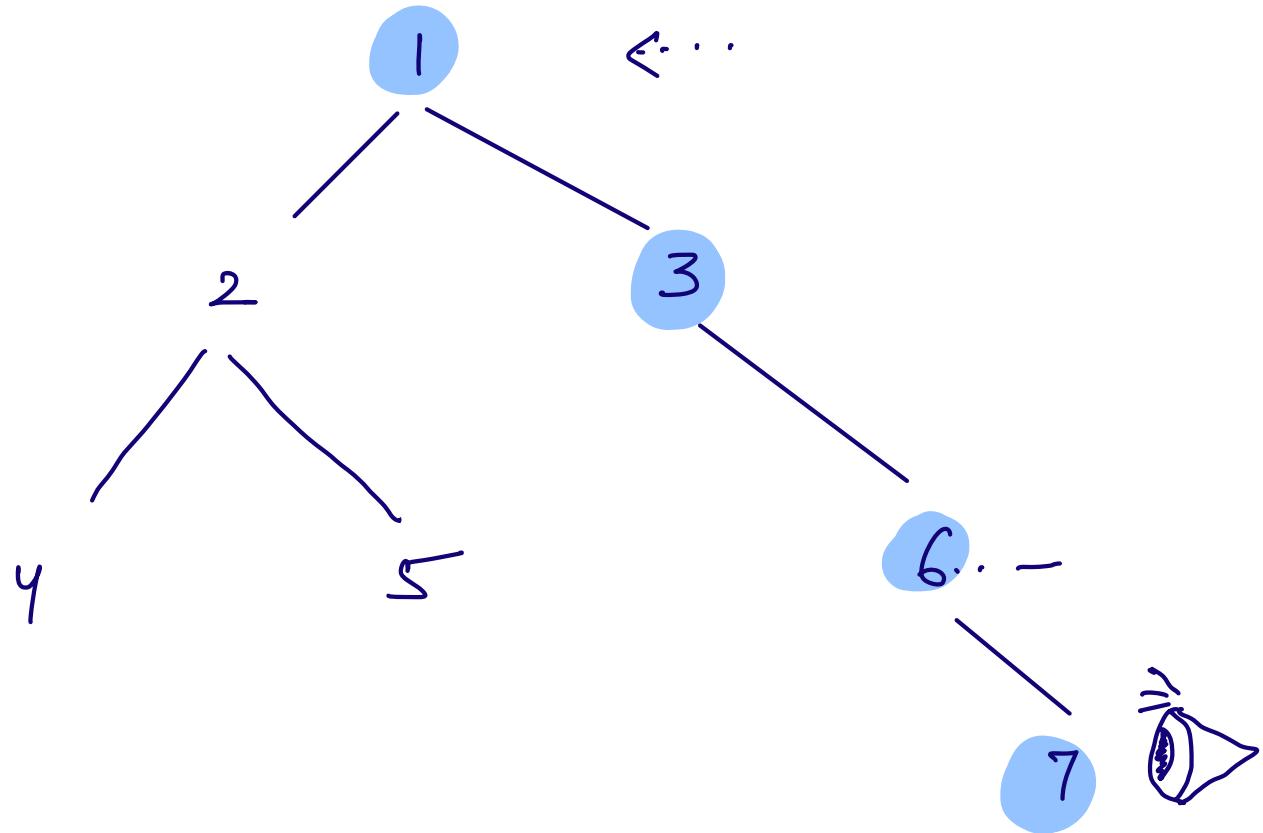
2 more questions →

Left view of tree



first
node
of every
level

Right view of tree

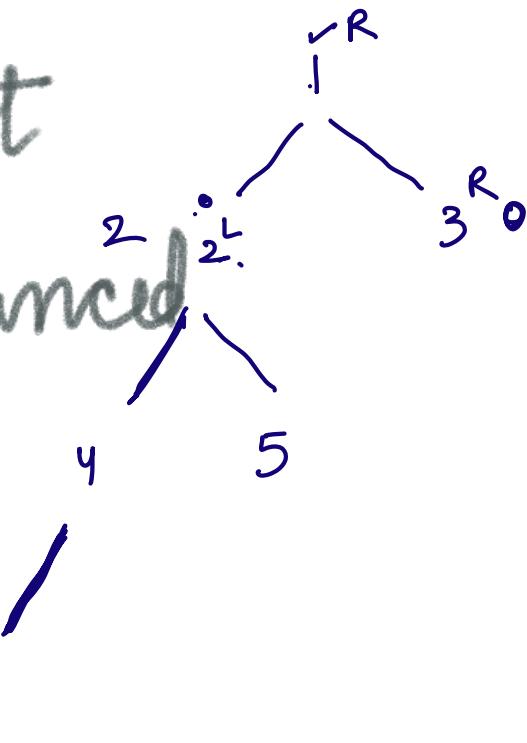


} Right view
= Last node
of every level

Q. Check if tree is height balanced

✓ not

balanced



balanced

$$|h_L - h_R| \leq 1$$

not balanced

✓ h_L

✓ h_R

work —