

Agenda:

1. Find Maximum Subarray Sum
2. Find in row-wise and col-wise sorted matrix
3. Merge sorted Overlapping Intervals
4. Transpose of a square matrix
5. Rotate a matrix to 90 degree clockwise



Q → Given an integer array find max subarray sum.

continuous part
of array

0 1 2 3 4 5 6
 $A = [-20, 30, 5, 16, -2, 0, 8]$

Ans = 57

0 1 2 3 4
 $A = [4, 5, 2, 1, 6]$

Ans = 18

0 1 2 3 4
 $A = [-4, -3, -6, -9, -2]$

Ans = -2

Bruteforce → \forall subarrays calculate sum & take max.

TC = $O(N^3)$

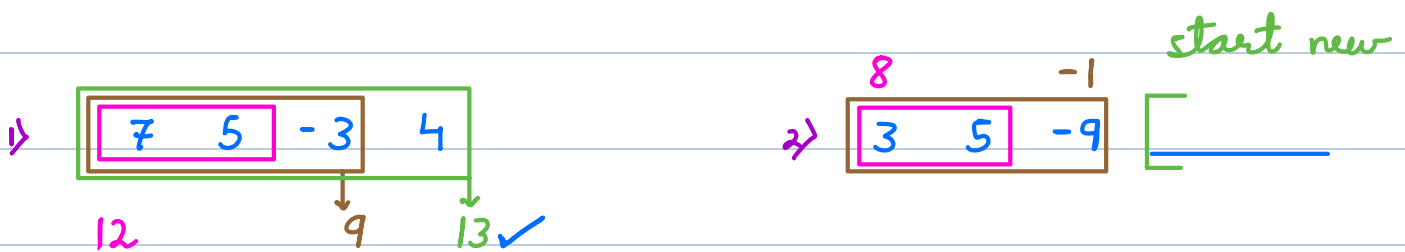
SC = $O(1)$

Carry Forward →

```
ans = A[0]
for i → 0 to (N-1) {
    sum = 0
    for j → i to (N-1) {
        sum += A[j]
        ans = max(ans, sum)
    }
}
```

TC = $O(N^2)$ SC = $O(1)$

Kadane's Algorithm



↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
0 1 2 3 4 5 6 7 8 9
A = [5 2 -3 -8 6 1 -5 11 0 -3]

sum = 5 7 4 ~~-4~~⁰ 6 7 2 13 13 10

ans = 5 7 13

$\begin{matrix} \checkmark & \checkmark & \checkmark & \checkmark & \checkmark & \checkmark & \checkmark \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{matrix}$
 $A = [-2 \quad 3 \quad 4 \quad -1 \quad 5 \quad -10 \quad 7]$

sum = ~~-2~~⁰ 3 7 6 11 + 8

ans = ~~-2~~ 3 7 11

ans = A[0]

sum = 0

for $i \rightarrow 0$ to $(N-1)$ {

sum += A[i] ✓

if (sum > ans) ans = sum

if (sum < 0) sum = 0

}

return ans

$\begin{matrix} \checkmark & \checkmark & \checkmark \\ 0 & 1 & 2 \end{matrix}$
 $A = [-5 \quad -3 \quad -8]$

sum = ~~-5~~⁰ ~~-3~~⁰ ~~-8~~⁰

ans = ~~-5~~
-3

TC = $O(N)$

SC = $O(1)$

ans = A[0] L = 0 R = 0 // L — R

sum = 0 st = 0

for $i \rightarrow 0$ to $(N-1)$ {

sum += A[i]

if (sum > ans) { ans = sum L = st R = i }

if (sum < 0) { sum = 0 st = i + 1 }

}

return ans

Q → Given a row-wise col-wise sorted matrix.
 Check if given element K is present. Ascending

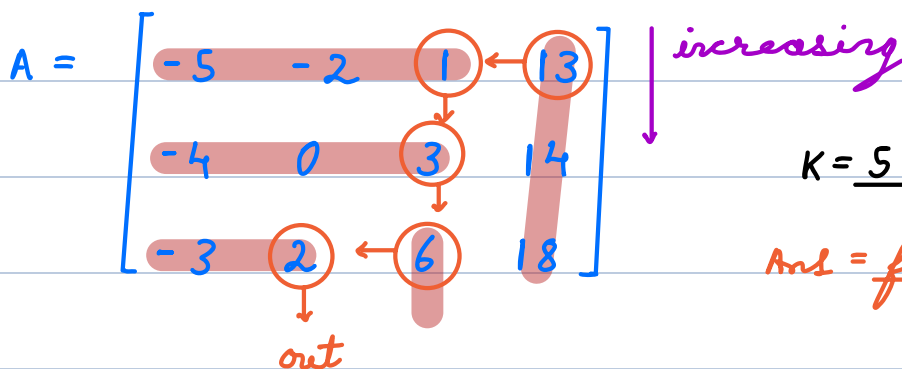
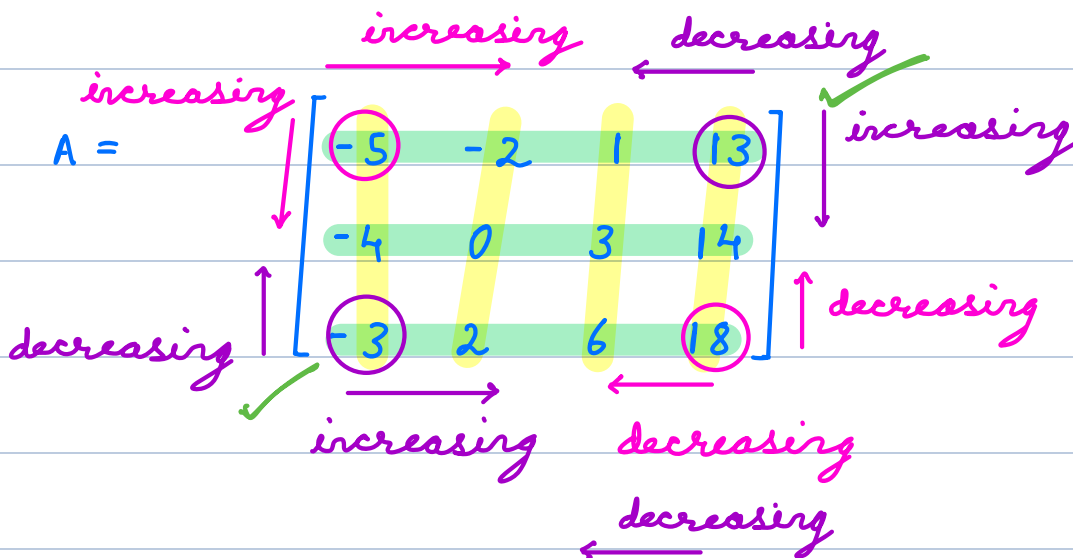
$$A = \begin{bmatrix} -5 & -2 & 1 & 13 \\ -4 & 0 & 3 & 14 \\ -3 & 2 & 6 & 18 \end{bmatrix}$$

$$K = 0 \quad \text{Ans} = \underline{\text{True}}$$

$$K = -1 \quad \text{Ans} = \underline{\text{false}}$$

Brute force → $\forall i, j$ check if $A[i][j] == K$.

$$TC = O(N * M) \quad SC = O(1)$$



$$\text{Ans} = \underline{\text{false}}$$

```

i = 0    j = M-1
while (i < N && j >= 0) {
    if (A[i][j] == K) return true
    if (A[i][j] < K) i++
    else j--
}

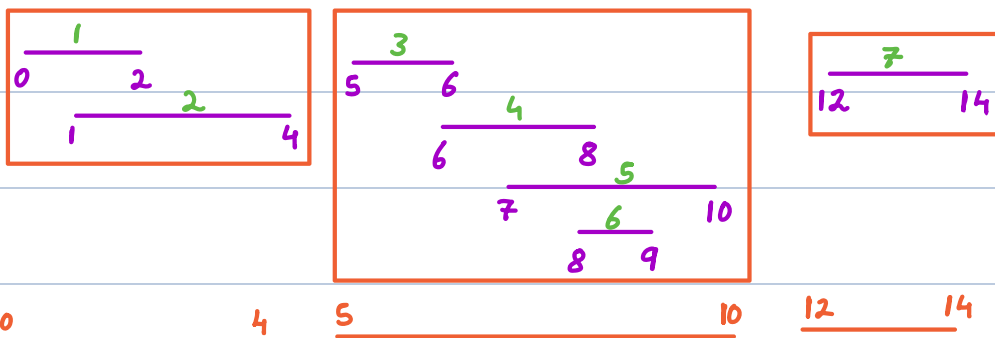
```

return false

TC = $O(N+M)$

SC = $O(1)$

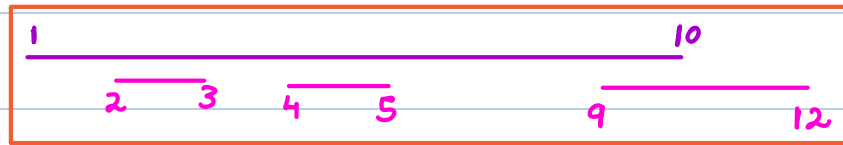
Q → Given a list of intervals, sorted wrt start time.
Merge all overlapping intervals & return the sorted list of non-overlapping intervals.



Ans →

Slot A & B are overlapping if $\text{start of B} \leq \text{end of A}$.

$A = [(1, 10) \quad (2, 3) \quad (4, 5) \quad (9, 12)]$



$S = A[0][0]$ $E = A[0][1]$ // $A[i][0] - A[i][1]$

for $i \rightarrow 1$ to $(N-1)$ {

```

    if (  $A[i][0] \leq E$  )     $E = \max(E, A[i][1])$ 
    else {    print (  $S, E$  )
            |
            |     $S = A[i][0]$      $E = A[i][1]$ 
            |
            }
}

```

print (S, E)

$TC = \underline{O(N)}$ $SC = \underline{O(1)}$

		i	i	i	i	i	i
	0	1	2	3	4	5	6
$A =$	[0	1	5	6	7	8	12]
	[2	4	6	8	10	9	14]

↙

$S = \cancel{0} \quad \cancel{5} \quad 12$

$E = \cancel{2} \quad \cancel{4} \quad \cancel{6} \quad \cancel{8} \quad \cancel{10} \quad 14$

o/p $\rightarrow 0, 4$

5, 10

12, 14

Q → Convert the given ^{square} matrix to its transpose.
 row ↔ column

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

Matrix Transpose → 7 min

$$i, j \leftrightarrow j, i$$

```

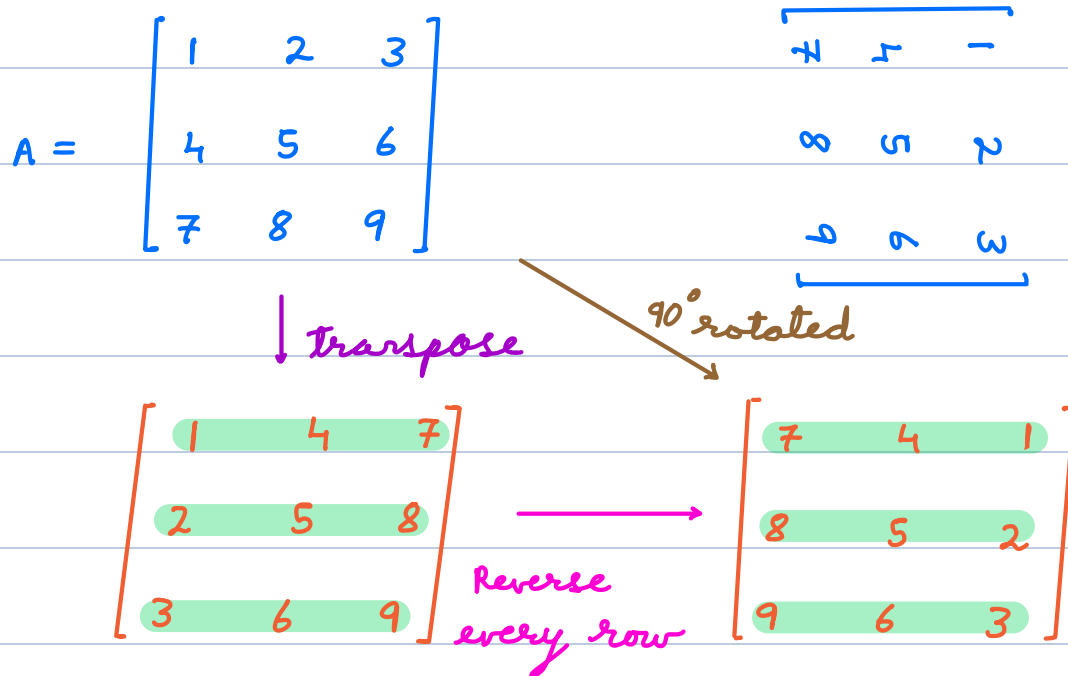
for i → 0 to (N-1) {
    for j → i+1 to (N-1) {
        t = A[i][j]           // swap i, j ↔ j, i
        A[i][j] = A[j][i]
        A[j][i] = t
    }
}
    
```

$TC = O(N^2)$ $SC = O(1)$

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

Diagram illustrating the swap operation for $i=0, j=1$ in the transpose algorithm. The elements 2 and 4 are circled and swapped. The indices $i=0$ and $j=1$ are indicated.

Q \rightarrow Rotate the given sq. matrix by 90° clockwise.



Sol \rightarrow 1) Transpose the given matrix
2) Reverse every row

$$TC = \underline{O(N^2)} \quad SC = \underline{O(1)}$$