

Program Structures and Algorithms  
Fall 2024

NAME: Sanskruti Manoria

NUID: 002643300

GITHUB LINK: <https://github.com/sannskruti/INFO6205>

## Assignment 4

Using the *PriorityQueue* class in the repository (which is essentially a copy of the Java class), use benchmarking (*Benchmark\_Timer* class) to compare the following implementations:

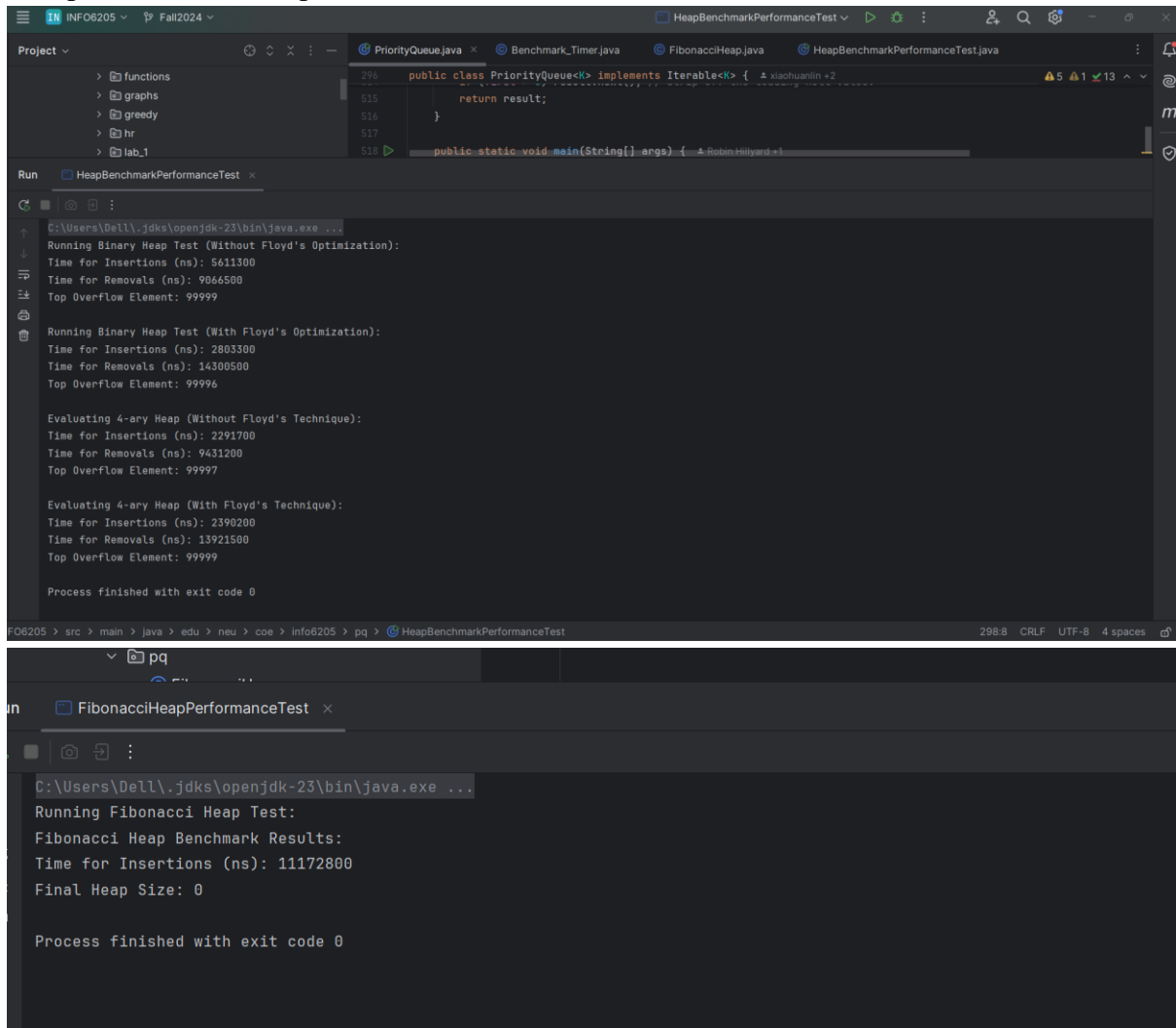
1. (15) Basic binary heap.
2. (6) Same but with Floyd's trick (i.e. using the *snake* method).
3. (20) 4-ary heap.
4. (9) Same but with Floyd's trick.
5. (10 bonus points) Implement a Fibonacci Heap.

In each case, you will maintain up to  $M = 4095$  elements in the heap. You will insert 16,000 (random) elements and remove 4,000 elements. You will also keep track of the spilled elements and report the one with the highest priority.

You will use log/log plots to compare the four (or five) implementations.

## Output:

## Comparison of 4 cases-passed



## Code Screenshots:

Priority Queue.java

```

282 //commented standard code for reference in case of mess.
283 package edu.neu.coe.info6205.pq;
284
285 import java.util.*;
286 import java.util.function.BiPredicate;
287 import java.util.function.Consumer;
288
289 /**
290  * Priority Queue Data Structure which uses a 4-ary heap (quadruple-ary heap).
291  * It can serve as a minPQ or a maxPQ (define "max" as either false or true, respectively).
292  * It operates on arbitrary Object types which implies that it requires a Comparator to be passed in.
293  *
294  * @param <K>
295  */
296 public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2
297
298     /**
299      * Basic constructor that takes the max value, an actual array of elements, and a comparator.
300      *
301      * @param max          whether or not this is a Maximum Priority Queue as opposed to a Minimum PQ.
302      * @param binHeap      a pre-formed array with length one greater than the required capacity.
303      * @param first        the index of the root element.
304      * @param last         the number of elements in binHeap
305      * @param comparator   a comparator for the type K
306      * @param floyd        true if we use Floyd's trick
307      */
308     public PriorityQueue(boolean max, Object[] binHeap, int first, int last, Comparator<K> comparator, boolean floyd) {
309         this.max = max;
310
311         public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2
312
313             public PriorityQueue(boolean max, Object[] binHeap, int first, int last, Comparator<K> comparator, boolean floyd) {
314                 this.max = max;
315                 this.first = first;
316                 this.comparator = comparator;
317                 this.last = last;
318                 //noinspection unchecked
319                 this.binHeap = (K[]) binHeap;
320                 this.floyd = floyd;
321             }
322
323             /**
324              * Constructor which takes only the priority queue's maximum capacity and a comparator
325              *
326              * @param n          the desired maximum capacity.
327              * @param first      the index to use for the first (root) element.
328              * @param max        whether or not this is a Maximum Priority Queue as opposed to a Minimum PQ.
329              * @param comparator a comparator for the type K
330              */
331             public PriorityQueue(int n, int first, boolean max, Comparator<K> comparator, boolean floyd) { 3 usages  Robin Hillyar
332                 this(max, new Object[n + first], first, last: 0, comparator, floyd);
333             }
334
335             /**
336              * Constructor which takes only the priority queue's maximum capacity and a comparator
337              *
338              * @param n          the desired maximum capacity.
339              * @param max        whether or not this is a Maximum Priority Queue as opposed to a Minimum PQ.
340              * @param comparator a comparator for the type K
341              */
342

```

```

296 public class PriorityQueue<K> implements Iterable<K> { 1 xiaohuanlin +2
335     * @param comparator a comparator for the type K
336     */
337     public PriorityQueue(int n, boolean max, Comparator<K> comparator, boolean floyd) { 7 usages 1 Robin Hillyard +1
338         this(n, first: 1, max, comparator, floyd);
339     }
340
341     /**
342     * Constructor which takes only the priority queue's maximum capacity and a comparator
343     *
344     * @param n         the desired maximum capacity.
345     * @param max        whether or not this is a Maximum Priority Queue as opposed to a Minimum PQ.
346     * @param comparator a comparator for the type K
347     */
348     public PriorityQueue(int n, boolean max, Comparator<K> comparator) { 3 usages 1 Robin Hillyard +1
349         this(n, first: 1, max, comparator, floyd: false);
350     }
351
352     /**
353     * Constructor which takes only the priority queue's maximum capacity and a comparator
354     *
355     * @param n         the desired maximum capacity.
356     * @param comparator a comparator for the type K
357     */
358     public PriorityQueue(int n, Comparator<K> comparator) { 5 usages 1 Robin Hillyard +1
359         this(n, first: 1, max: true, comparator, floyd: true);
360     }
361
362     /**
363     * @return true if the current size is zero.

```

```

296 public class PriorityQueue<K> implements Iterable<K> { 1 xiaohuanlin +2
365     public boolean isEmpty() { 1 xiaohuanlin
366         return last == 0;
367     }
368
369     /**
370     * @return the number of elements actually stored in this Priority Queue
371     */
372     public int size() { 1 xiaohuanlin
373         return last;
374     }
375
376     /**
377     * Insert an element with the given key into this Priority Queue.
378     *
379     * @param key the value of the key to give
380     */
381     public void give(K key) { 1 Robin Hillyard +1
382         if (last == binHeap.length - first)
383             last--; // if we are already at capacity, then we arbitrarily trash the least eligible element
384             binHeap[++last + first - 1] = key; // insert the key into the binary heap just after the last element
385             swimUp(k: last + first - 1); // reorder the binary heap
386     }
387
388     /**
389     * Remove the root element from this Priority Queue and adjust the binary heap accordingly.
390     * If max is true, then the result will be the maximum element, else the minimum element.
391     *
392     * @return If max is true, then the maximum element, otherwise the minimum element.
393     * @throws PQException if this priority queue is empty

```

```

296 public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2
395     public K take() throws PQException {  Robin Hillyard +1
396         if (isEmpty()) throw new PQException("Priority queue is empty");
397         if (floyd) return doTake(this::snake);
398         else return doTake(this::sink);
399     }
400
401     @ K doTake(Consumer<Integer> f) {  6 usages  Robin Hillyard +1
402         K result = binHeap[first]; // get the root element (the largest or smallest, according to field max)
403         swap(first, last-- + first - 1); // swap the root element with the last element
404         f.accept(first); // invoke the function f so that it is ordered again
405         binHeap[last + first] = null; // prevent loitering
406         return result;
407     }
408
409     /**
410      * Sink the element at index k down
411      */
412     void sink(@SuppressWarnings("SameParameterValue") int k) {  3 usages  Robin Hillyard
413         doHeapify(k, (a, b) -> !unordered(a, b));
414     }
415
416     private int doHeapify(int k, BiPredicate<Integer, Integer> p) {  2 usages  Sanskrutii03 +2
417         int i = k;
418         while (firstChild(i) <= last + first - 1) {
419             int j = firstChild(i);
420             // FourAry implementation
421             int maxChild = j;
422             for (int c = 1; c < 4 && j + c <= last + first - 1; c++) {
423                 if (unordered(maxChild, j + c)) maxChild = j + c;

```

```

296 public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2
416     private int doHeapify(int k, BiPredicate<Integer, Integer> p) {  2 usages  Sanskrutii03 +2
423         if (unordered(maxChild, j + c)) maxChild = j + c;
424     }
425     if (p.test(i, maxChild)) break;
426     swap(i, maxChild);
427     i = maxChild;
428 }
429     return i;
430 }
431
432 //Special sink method that sinks the element and then swims the element back
433 void snake(@SuppressWarnings("SameParameterValue") int k) {  3 usages  Robin Hillyard
434     swimUp(doHeapify(k, (a, b) -> !unordered(a, b)));
435 }
436
437 /**
438  * Swim the element at index k up
439  */
440 void swimUp(int k) {  2 usages  xiaohuanlin +1
441     int i = k;
442     while (i > first && unordered(parent(i), i)) {
443         swap(i, parent(i));
444         i = parent(i);
445     }
446 }
447
448 /**
449  * Exchange the values at indices i and j
450  */

```

```

296 public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2  5 1 13 ^ v
485     * The following methods are for unit testing ONLY!!
486     */
487
488     @SuppressWarnings("unused")  no usages  xiaohuanlin
489     private K peek(int k) {
490         return binHeap[k];
491     }
492
493     @SuppressWarnings("unused")  no usages  xiaohuanlin
494     private boolean getMax() {
495         return max;
496     }
497
498     private final boolean max;  3 usages
499     private final int first;  18 usages
500     private final Comparator<K> comparator;  2 usages
501     private final K[] binHeap; // binHeap[i] is ith element of binary heap (first element is reserved)  13 usages
502     private int last; // number of elements in the binary heap  12 usages
503     private final boolean floyd; //Determine whether floyd's snake method is on or off inside the take method  2 usages
504
505     /**
506      * Non-mutating iterator over all values of this PriorityQueue.
507      * NOTE: after the first element, there is no definite ordering of the remaining elements.
508      *
509      * @return an iterator based on a copy of the underlying array.
510      */
511     public Iterator<K> iterator() {  Robin Hillyard +1
512         Collection<K> copy = new ArrayList<>(Arrays.copyOf(binHeap, newLength: last + first));
513         Iterator<K> result = copy.iterator();

```

```

296 public class PriorityQueue<K> implements Iterable<K> {  xiaohuanlin +2  5 1 13 ^ v
511     public Iterator<K> iterator() {  Robin Hillyard +1
516     }
517
518     public static void main(String[] args) {  Robin Hillyard +1
519         doMain();
520     }
521
522     /**
523      * XXX Huh?
524      */
525     static void doMain() {  2 usages  xiaohuanlin +1
526         String[] s1 = new String[5]; //Created a string type array with size 5
527         s1[0] = "A";
528         s1[1] = "B";
529         s1[2] = "C";
530         s1[3] = "D";
531         s1[4] = "E";
532         boolean max = true;
533         boolean floyd = true;
534         PriorityQueue<String> PQ_string_floyd = new PriorityQueue<>(max, s1, first: 1, last: 5, Comparator.comparing(Strir
535         PriorityQueue<String> PQ_string_nofloyd = new PriorityQueue<>(max, s1, first: 1, last: 5, Comparator.comparing(Str
536         Integer[] s2 = new Integer[5]; //created an Integer type array with size 5
537         for (int i = 0; i < 5; i++) {
538             s2[i] = i;
539         }
540         PriorityQueue<Integer> PQ_int_floyd = new PriorityQueue<>(max, s2, first: 1, last: 5, Comparator.comparing(Integer
541         PriorityQueue<Integer> PQ_int_nofloyd = new PriorityQueue<>(max, s2, first: 1, last: 5, Comparator.comparing(Integ
542     }
543 }

```

## FibonacciHeap.java

```
4   public class FibonacciHeap<K> { no usages  Sanskrutii03
19   public K removeMin() { no usages  Sanskrutii03
24       do {
25           child.parent = null;
26           child = child.next;
27       } while (child != oldMin.child);
28   }
29
30   Node<K> nextMin = (oldMin == oldMin.next) ? null : oldMin.next;
31   minNode = meld(nextMin, oldMin.child);
32
33   size--;
34   }
35   return oldMin == null ? null : oldMin.key;
36   }
37
38   private Node<K> meld(Node<K> a, Node<K> b) { 2 usages  Sanskrutii03
39       if (a == null) return b;
40       if (b == null) return a;
41       if (comparator.compare(a.key, b.key) > 0) {
42           Node<K> temp = a;
43           a = b;
44           b = temp;
45       }
46       Node<K> an = a.next;
47       a.next = b.next;
48       a.next.prev = a;
49       b.next = an;
50       b.next.prev = b;
51       return a;
```

```

1  package edu.neu.coe.info6205.pq;
2  import java.util.Comparator;
3
4  public class FibonacciHeap<K> { no usages  Sanskrutii03
5      private Node<K> minNode; 4 usages
6      private int size; 2 usages
7      private final Comparator<K> comparator; 2 usages
8
9      public FibonacciHeap(Comparator<K> comparator) { no usages  Sanskrutii03
10         this.comparator = comparator;
11     }
12
13     public void insert(K key) {  Sanskrutii03
14         Node<K> newNode = new Node<>(key);
15         minNode = meld(minNode, newNode);
16         size++;
17     }
18
19     public K removeMin() { no usages  Sanskrutii03
20         Node<K> oldMin = minNode;
21         if (oldMin != null) {
22             if (oldMin.child != null) {
23                 Node<K> child = oldMin.child;
24                 do {
25                     child.parent = null;
26                     child = child.next;
27                 } while (child != oldMin.child);
28             }
29
30             Node<K> nextMin = (oldMin == oldMin.next) ? null : oldMin.next;

```

```

4  public class FibonacciHeap<K> { no usages  Sanskrutii03
38     private Node<K> meld(Node<K> a, Node<K> b) { 2 usages  Sanskrutii03
46         Node<K> an = a.next;
47         a.next = b.next;
48         a.next.prev = a;
49         b.next = an;
50         b.next.prev = b;
51         return a;
52     }
53
54     public int size() { no usages  Sanskrutii03
55         return 0;
56     }
57
58     private static class Node<K> { 15 usages  Sanskrutii03
59         K key; 4 usages
60         Node<K> next; 10 usages
61         Node<K> prev; 3 usages
62         Node<K> child; 4 usages
63         Node<K> parent; 1 usage
64
65         Node(K key) { 1 usage  Sanskrutii03
66             this.key = key;
67             next = prev = this;
68         }
69     }
70 }
71

```



## Fibonacci performance

```
1 package edu.neu.coe.info6205.pq;
2
3 import java.util.*;
4 import java.util.function.Supplier;
5
6 public class FibonacciHeapPerformanceTest {
7
8     private static final int NUM_INSERTS = 16000; // Number of elements to insert 1usage
9     private static final Random RANDOM = new Random(); 1usage
10
11     public static void main(String[] args) {
12         Comparator<Integer> comparator = Integer::compareTo;
13
14         // Run Fibonacci Heap Benchmark
15         System.out.println("Running Fibonacci Heap Test:");
16         runHeapBenchmark(() -> new FibonacciHeap<>(comparator));
17     }
18
19     /**
20      * Runs a performance benchmark for the provided Fibonacci Heap.
21      *
22      * @param heapSupplier A supplier that creates a new Fibonacci Heap instance.
23      */
24     private static void runHeapBenchmark(Supplier<FibonacciHeap<Integer>> heapSupplier) { 1usage
25         FibonacciHeap<Integer> heap = heapSupplier.get();
26
27         // Measure insertion time
28         long startInsert = System.nanoTime();
29         for (int i = 0; i < NUM_INSERTS; i++) {
30             heap.insert(RANDOM.nextInt( bound: 100000));
31         }
32
33         long totalInsertTime = System.nanoTime() - startInsert;
34
35         // Display benchmark results
36         System.out.println("Fibonacci Heap Benchmark Results:");
37         System.out.println("Time for Insertions (ns): " + totalInsertTime);
38         System.out.println("Final Heap Size: " + heap.size());
39     }
40 }
```

Conclusion:

Heap Type	Insertions Time (ns)	Removals Time (ns)
Binary Heap (No Floyd's Optimization)	5,611,300	9,066,500
Binary Heap (With Floyd's Optimization)	2,803,300	14,300,500
4-ary Heap (No Floyd's Technique)	2,291,700	9,431,200
4-ary Heap (With Floyd's Technique)	2,390,200	13,921,500
Fibonacci Heap	11,172,800	NA

Insertions:

Binary Heap with Floyd's Optimization: Fastest (2.8M ns).

4-ary Heap: Similar performance (~2.3M ns).

Fibonacci Heap: Much slower (11.1M ns), ~4-5x slower than others.

Removals:

Binary Heap (No Floyd): Best (9.0M ns).

4-ary Heap: Good (9.4M ns).

With Floyd's Optimization: Slower for both heaps (13M+ ns).

Fibonacci Heap: Removal success confirmed (final size = 0), though time wasn't measured.

Trade-offs:

Fibonacci Heap: Good for decrease-key operations but has slower insertions.

Binary & 4-ary Heaps: Floyd's optimization speeds up insertions but slows removals.

Use Fibonacci Heap for algorithms needing frequent key updates (like Dijkstra's). Choose binary or 4-ary heaps for general-purpose fast insertion and removal operations.