

30
25

③

MENSURATION

2D

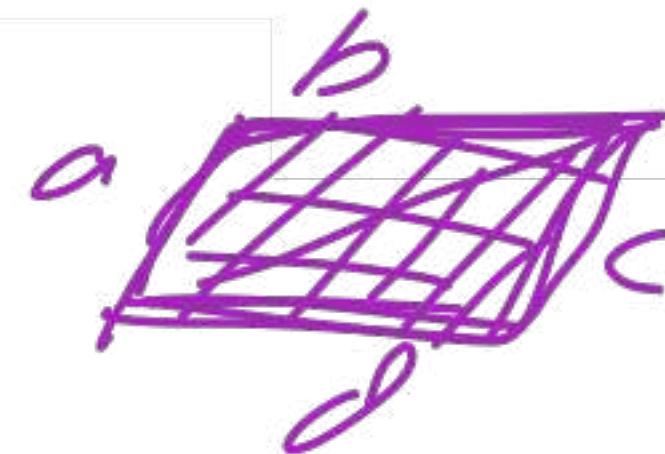
3DV

ग्रन्ति

- Perimeter (परिधि) :- Sum of length of all external boundary / सभी बाहरी सीमा की लंबाई का योग

उदाहरण

- Area (क्षेत्रफल) :- Region covered by external boundary / बाहरी सीमा द्वारा कवर किया गया क्षेत्र



□ Area of different triangles / विभिन्न त्रिभुजों का क्षेत्रफल

1. Area / क्षेत्रफल(Δ) = $\frac{1}{2} a \times h$

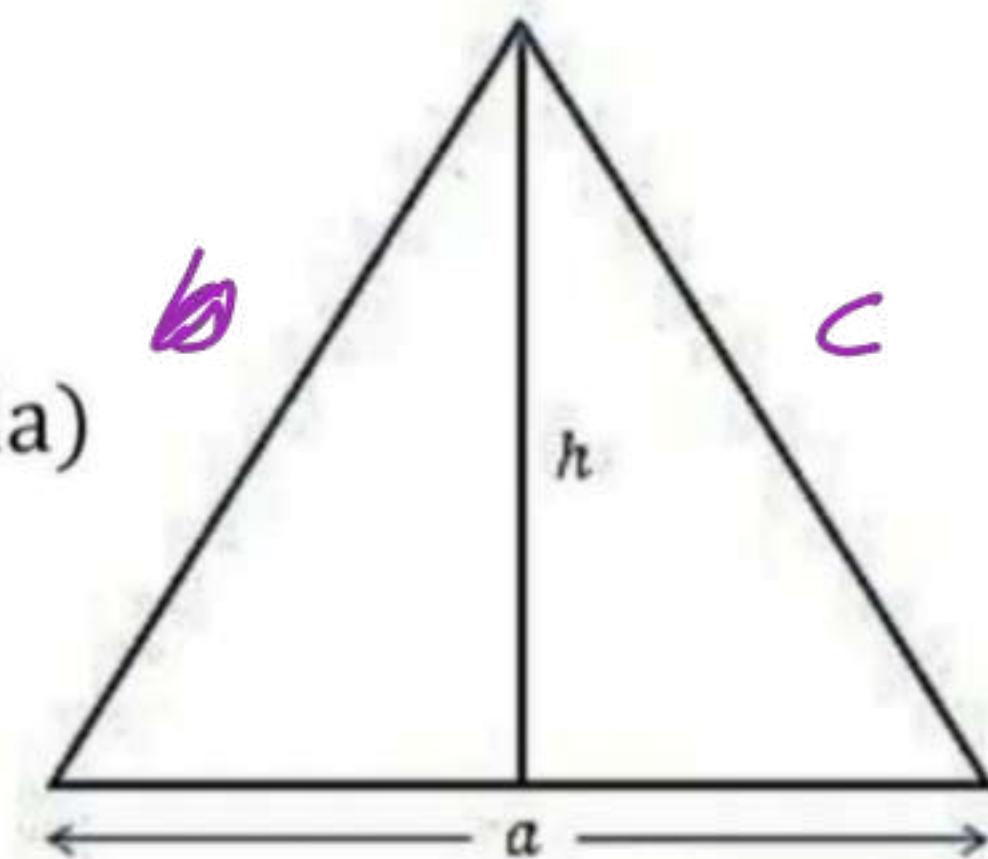
Area = $\sqrt{s(s - a)(s - b)(s - c)}$ (Hero's formula)

$$r = \frac{\Delta}{s}$$

r = inradius of incircle

(अन्तःवृत्त की अंतःत्रिज्या)

s = semiperimeter of triangle = $\frac{a+b+c}{2} : s$
 (त्रिभुज का अर्धपरिमाप)



3. Right angle triangle / समकोण त्रिभुज *(Right) Error △*

(a, b and c are sides of triangle / a, b और c त्रिभुज की भुजाएँ हैं)

- Perimeter(परिधि) = $a + b + c$

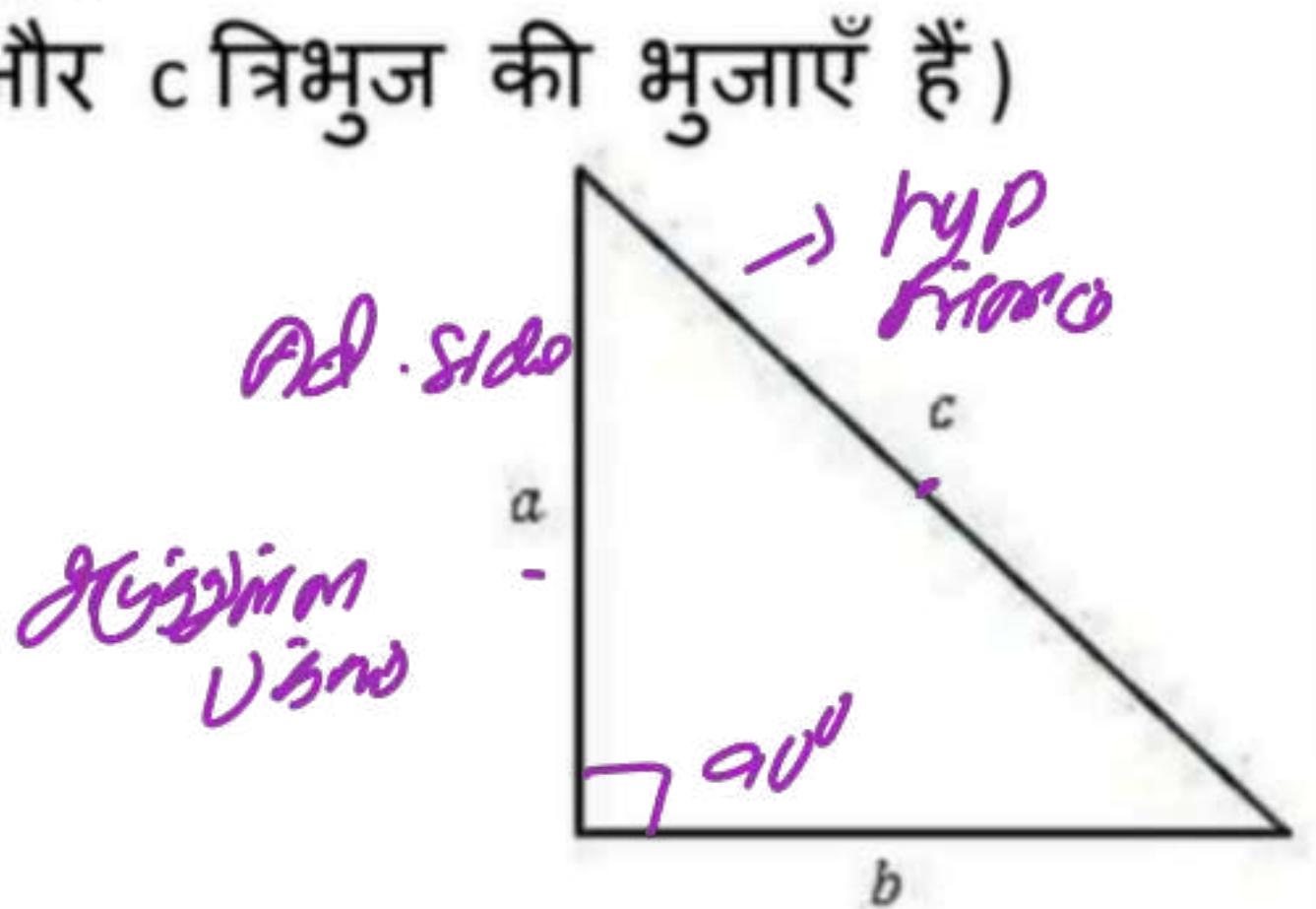
- $c^2 = a^2 + b^2$

$$c = \sqrt{a^2 + b^2}$$

- $\Delta = \frac{1}{2} a \times b$

*base
height*

- $R = \frac{c}{2}, r = \frac{a+b-c}{2}$

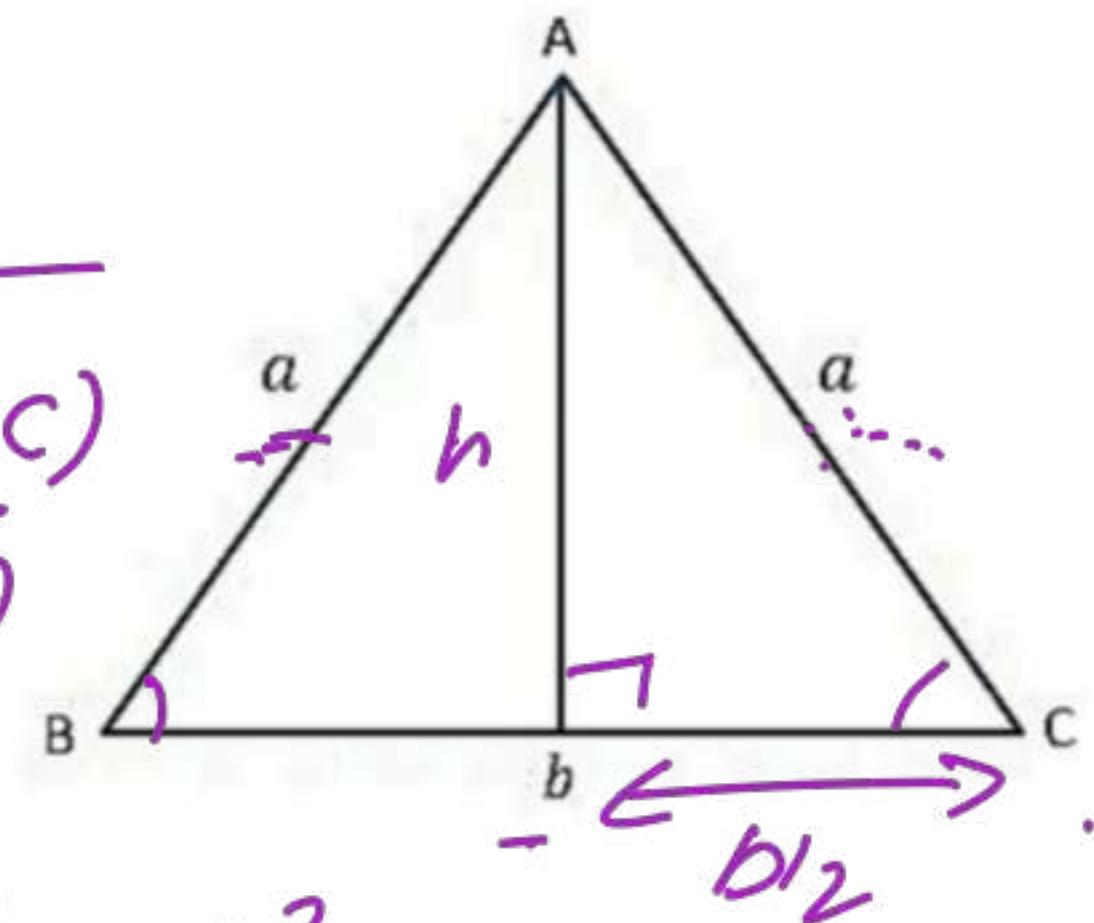


base - given

Isosceles Triangle

4. Isosceles Triangle / समद्विबाहु त्रिभुज

- $\angle B = \angle C$
- $\Delta = \frac{1}{4} b \sqrt{4a^2 - b^2}$ $= \sqrt{s(s-a)(s-b)(s-c)}$
 $= \sqrt{s(s-a)(s-a)(s-b)}$
- Perimeter = $2s = 2a + b$ ~~x~~
- Altitude(ऊंचाई) $= \frac{1}{2} \sqrt{4a^2 - b^2} \rightarrow h^2 + (p_h)^2 = a^2$
 $h^2 = \sqrt{a^2 - \frac{b^2}{4}} = \frac{1}{2} \sqrt{4a^2 - b^2}$ $h^2 = a^2 - \frac{b^2}{4}$



□ Circle (वृत्त) : -

गोणमान

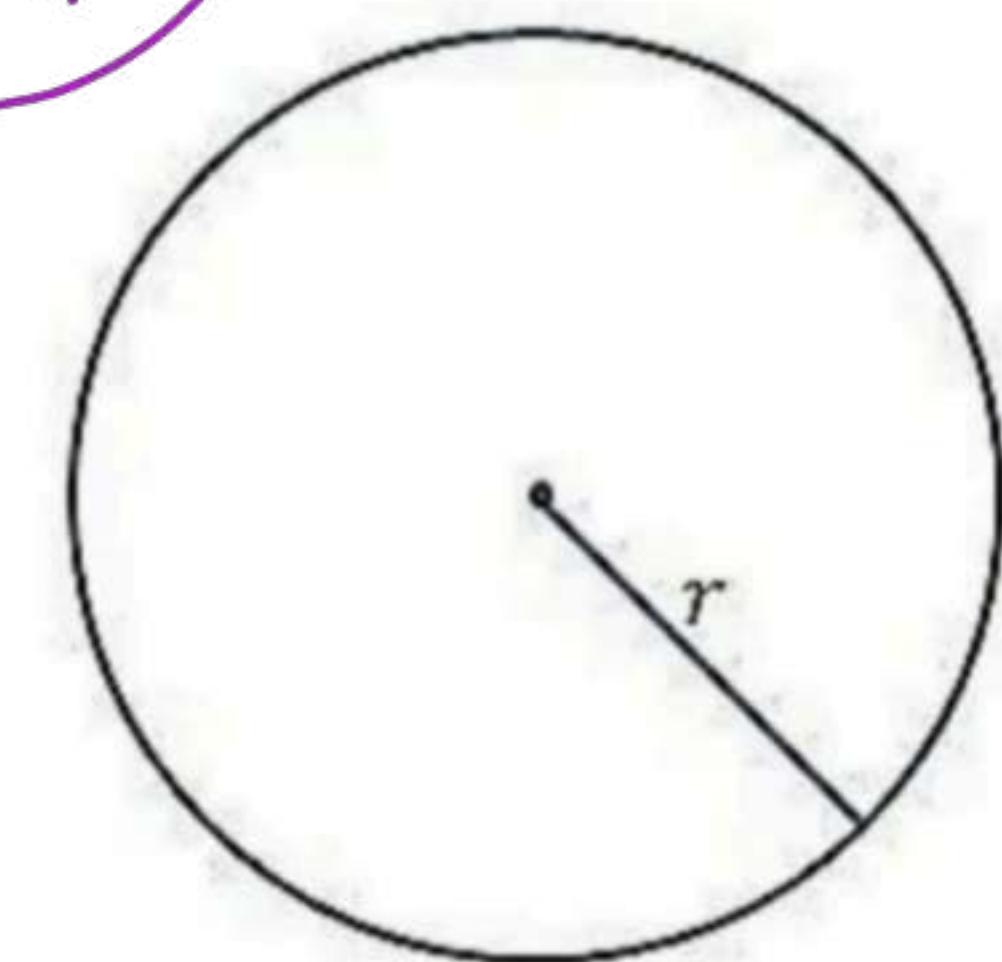
- Circumference(परिधि) = $2\pi r$
- Area(Δ) = πr^2

r - radius - वृत्तीय

D - Diameter - वृत्तीय

$$r = \frac{D}{2}$$

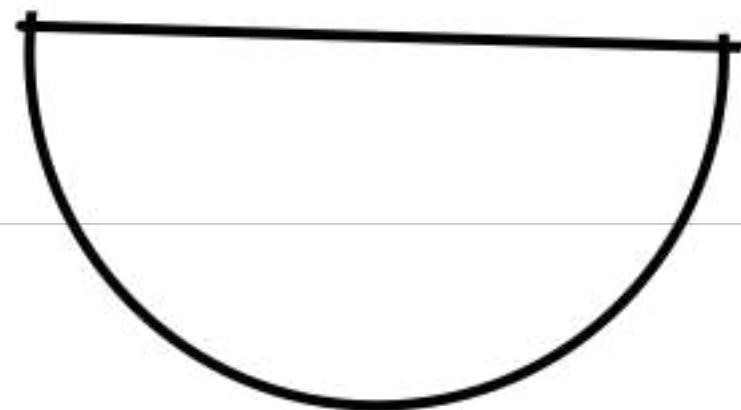
$$\pi = \frac{22}{7}$$



Semi Circle - gray solid

$$\text{Area} = \frac{1}{2} \pi r^2$$

$$\text{Perimeter} = \pi r + 2r$$

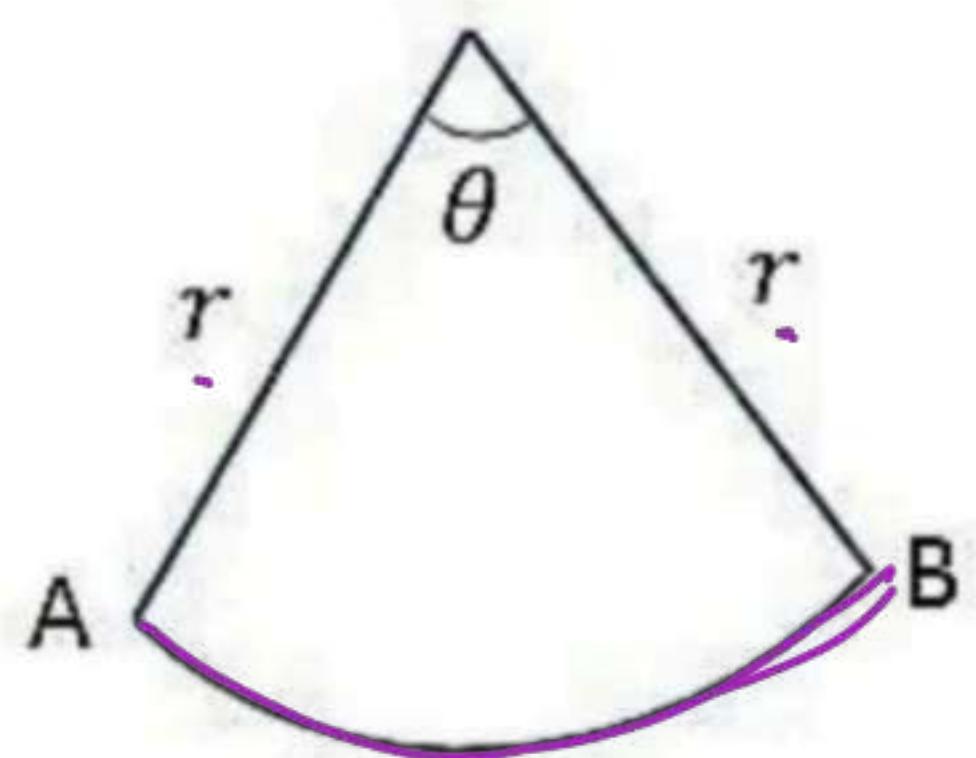


□ Arc (चाप) :

- $\text{Arc } AB = \frac{\theta}{360^\circ} \times 2\pi r$

- $\Delta = \frac{\theta}{360^\circ} \times \pi r^2$

$$360^\circ = 2\pi r$$
$$\theta = \frac{\theta}{360^\circ} \times 2\pi r$$



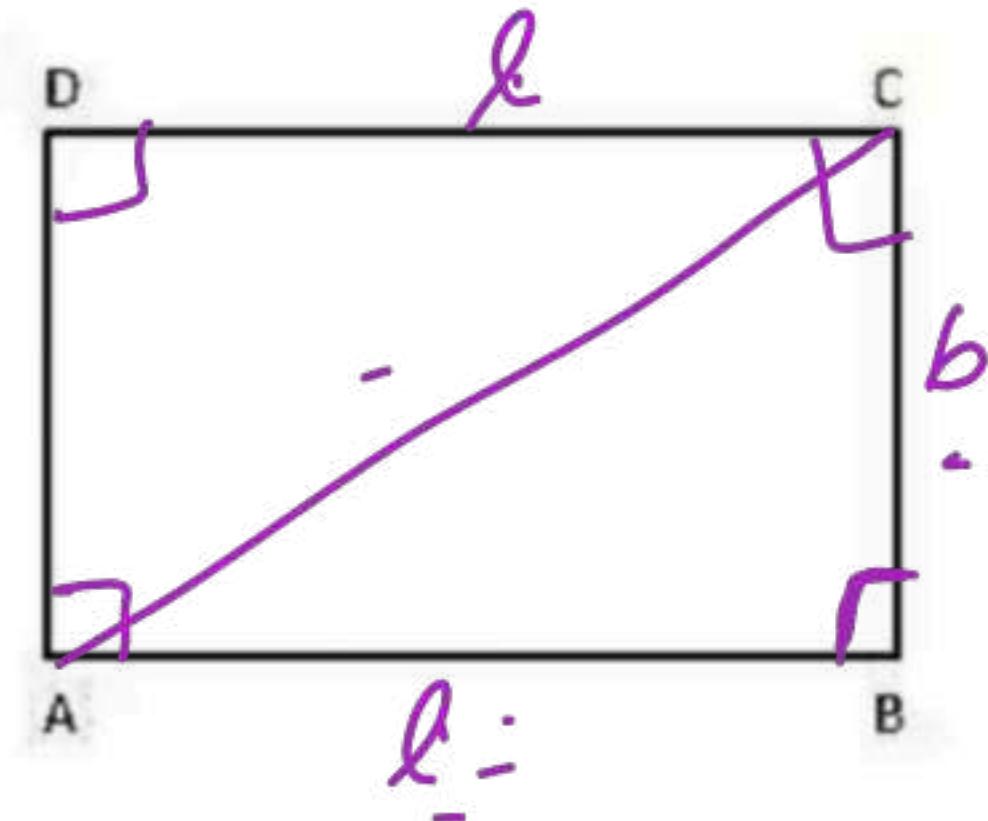
□ Rectangle (आयत) : Rectangle of length(लंबाई) 'l' and breadth(चौड़ाई) 'b']

४५२८

- Perimeter (परिमाप) = $2(l + b)$ = $2l + 2b$
 $= 2(l + b)$
- Area (क्षेत्रफल) = $l \times b$
- Diagonal (विकर्ण) = $\sqrt{l^2 + b^2}$

$$D^2 = l^2 + b^2$$

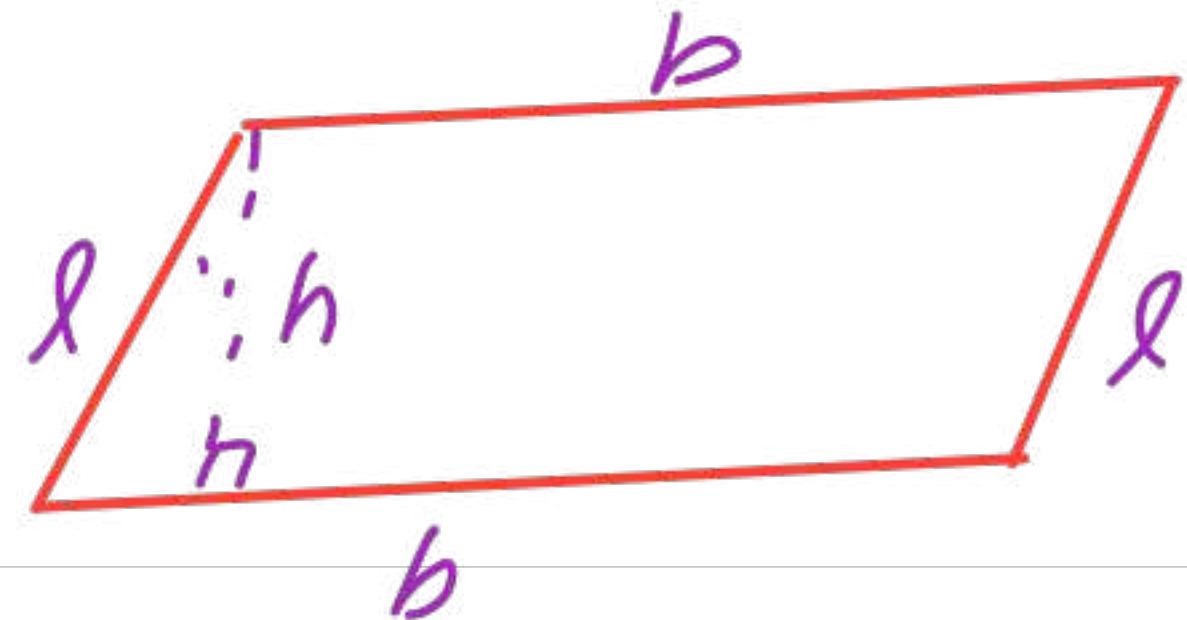
$$D = \sqrt{l^2 + b^2}$$



Parallelogram - Gorassu

$$\text{Area} = b \times h$$

$$\text{Perimeter} = a + b + c + d$$



Square (वर्ग) : Square of side a सूझो

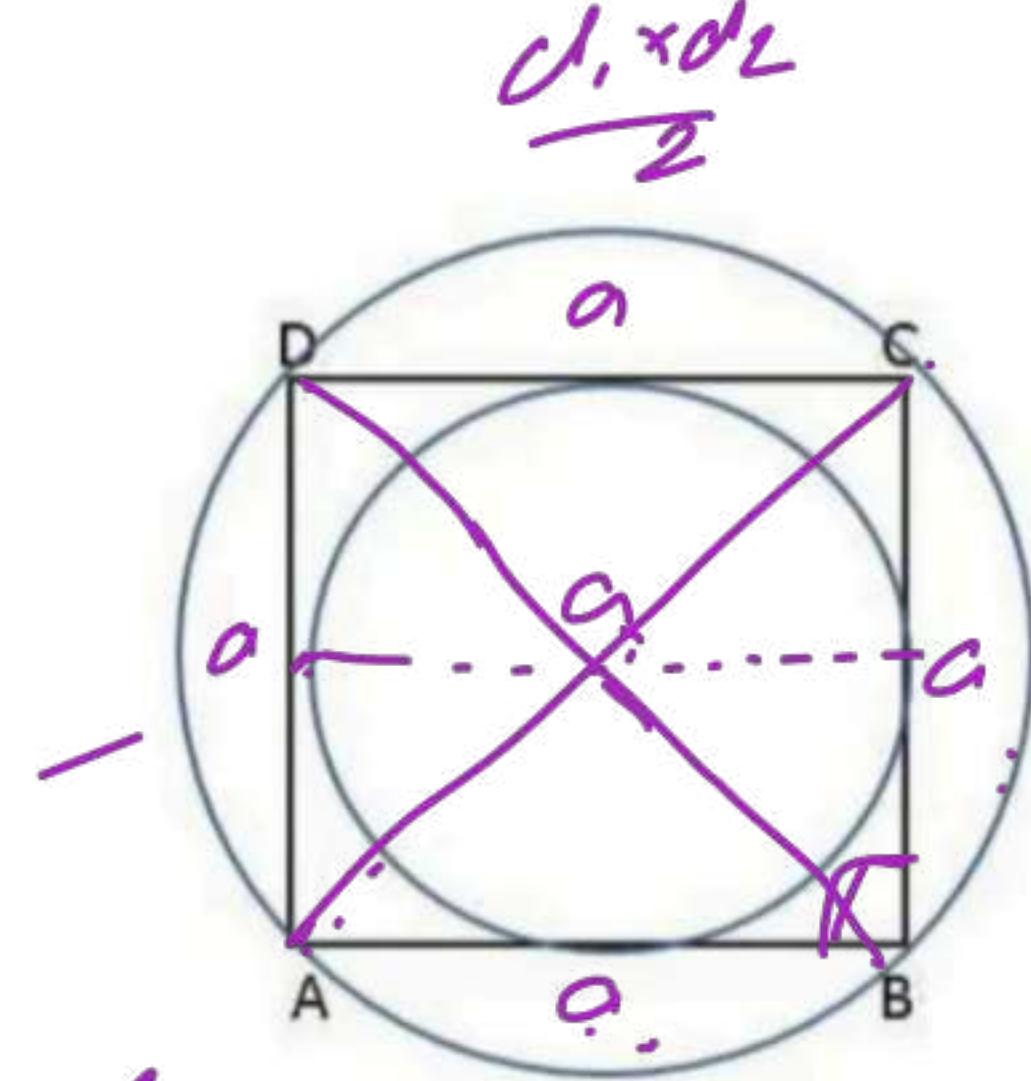
- Perimeter (परिमाप) = $4a$

- Area (क्षेत्रफल) = a^2 = \frac{d^2}{2}

- Diagonal (विकर्ण) = $\sqrt{2} a$

- $R = \frac{a\sqrt{2}}{2}$ d = \sqrt{a^2 + a^2} = \sqrt{2}a D = d R = \frac{\sqrt{2}a}{2}

- $r = \frac{a}{2}$



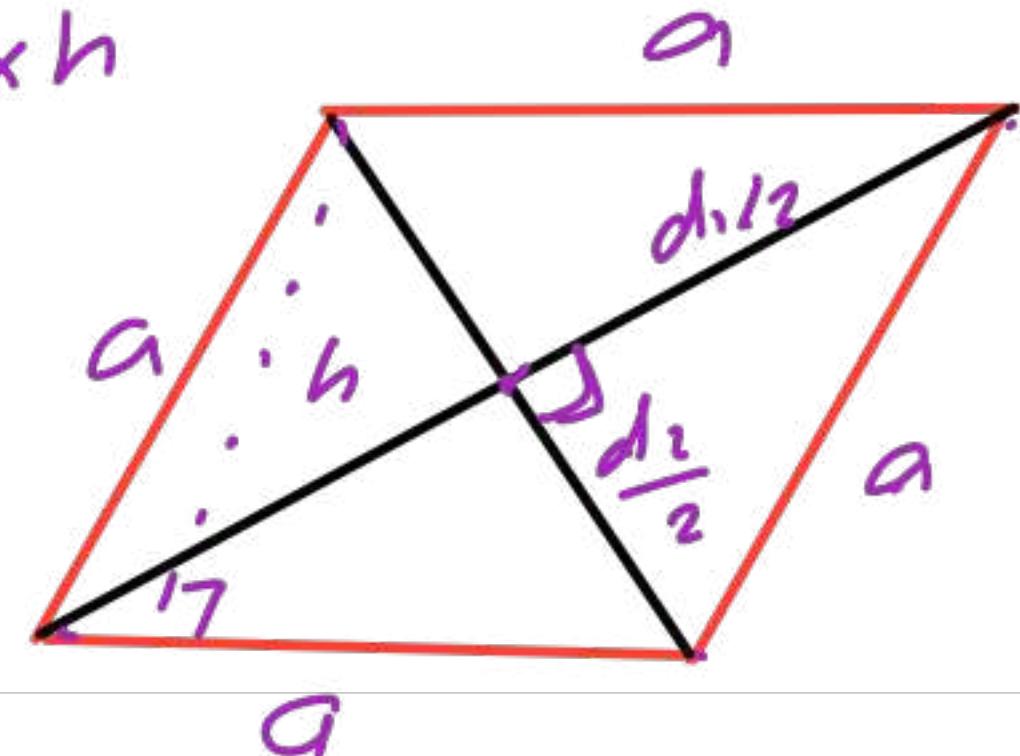
$$d_1 = d_2$$

Rhombus - Formel

$$\text{Area} = \frac{d_1 \cdot d_2}{2} = a \cdot h$$

$$d_1^2 + d_2^2 = 4a^2$$

$$h = \frac{d_1 \cdot d_2}{2a}$$



$$a^2 = \left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2$$

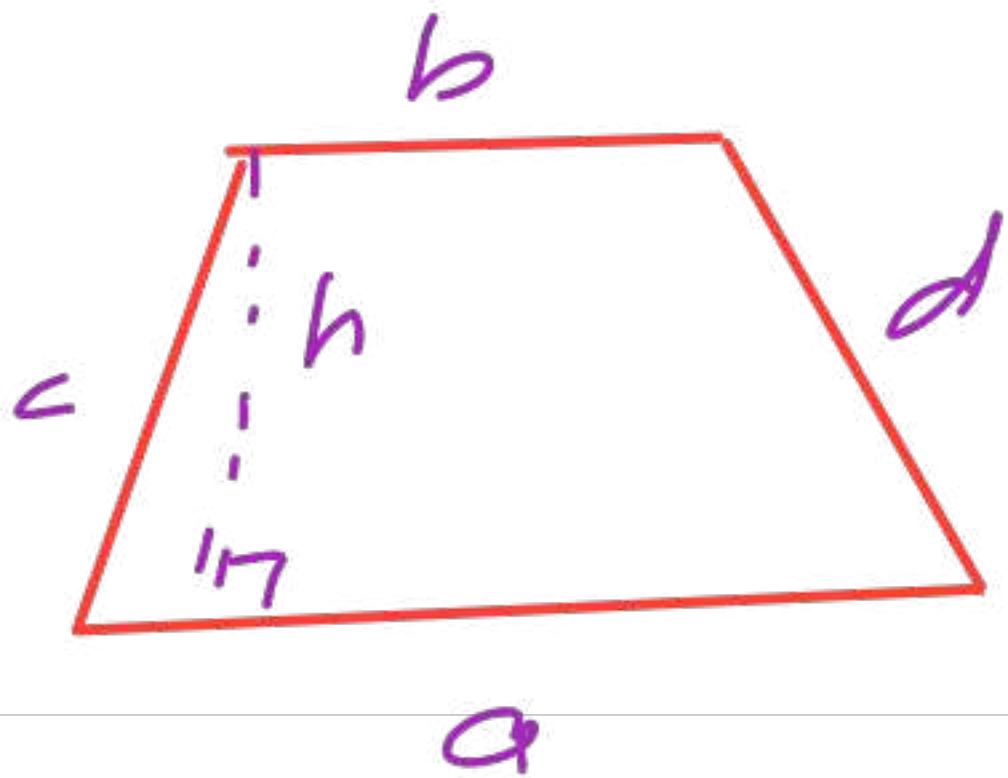
$$a^2 = \frac{d_1^2}{4} + \frac{d_2^2}{4} \Rightarrow d_1^2 + d_2^2 = 4a^2$$

$$d_1 \neq d_2$$

Trapezium - Fläche

$$\text{Area} = \frac{1}{2} (a+b) \times h \quad \checkmark$$

$$\text{Perimeter: } a+b+c+d$$



③

$$\begin{array}{ll} \text{Area} & m^2 \\ \underline{l \times b} & m^2 \text{ unit} \\ \underline{\frac{m}{cm} \frac{m}{cm} \frac{m}{cm}} & \end{array} \quad \begin{array}{ll} \text{Volume} & m^3 \\ \underline{\frac{l \times b \times h}{m}} & m^3 \text{ cm}^3 \\ \underline{m} & m^2 \text{ m}^3 \end{array}$$

MENSURATION 3D

SURFACE AREA & VOLUME

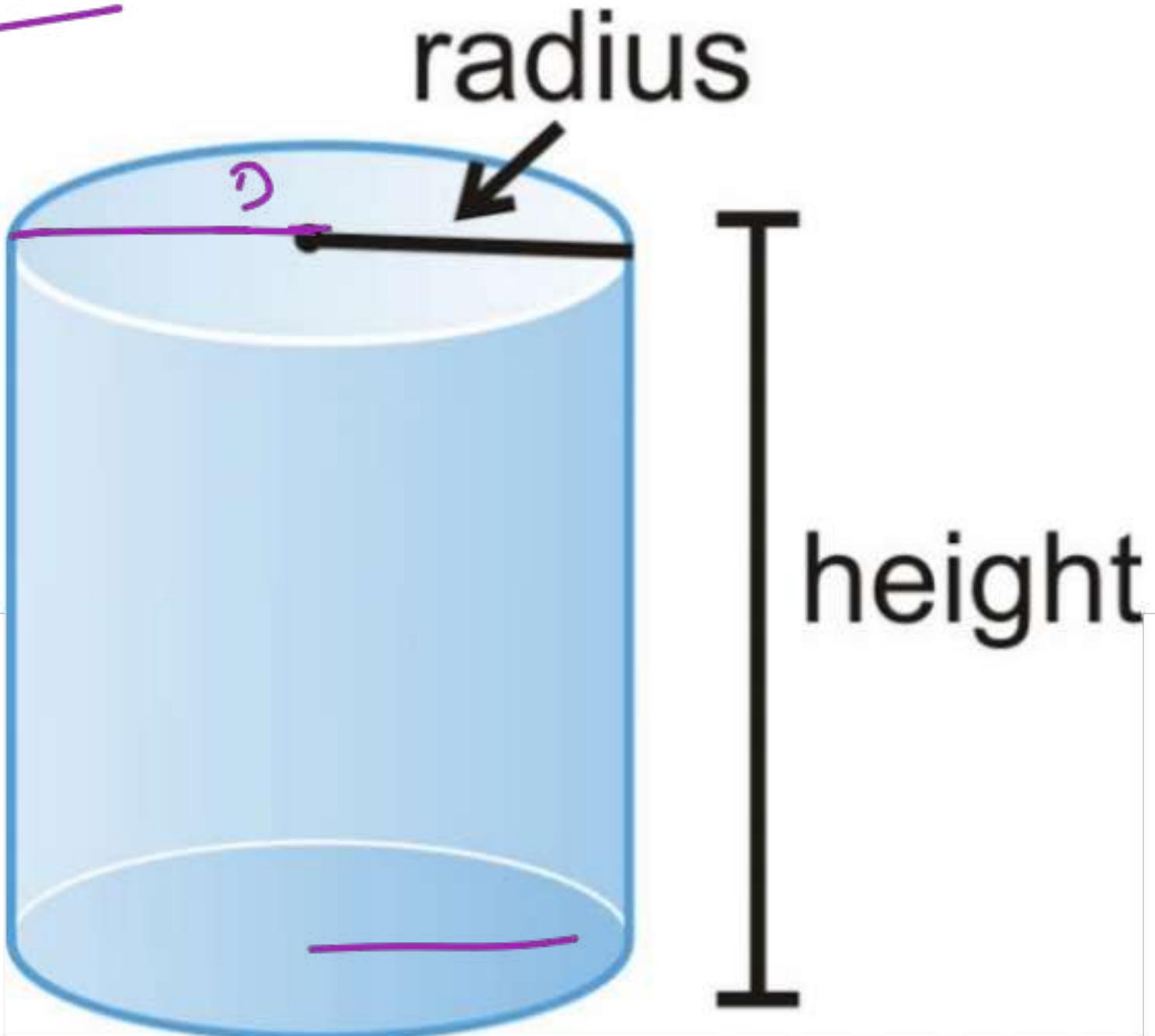
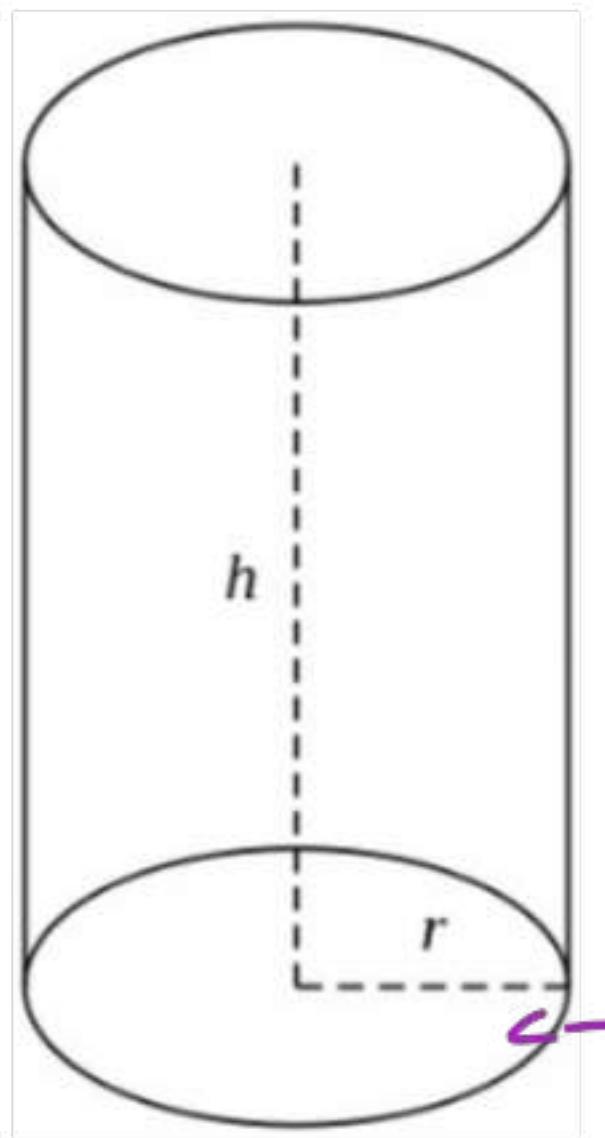
- 1) Cube
- 2) Cuboid
- 3) Cylinder
- 4) Cone
- 5) Sphere
- 6) Hemisphere
- 7) Prism
- 8) Pyramid

$$\begin{array}{r} 18 \\ \times 2 \\ \hline 20 \end{array}$$

③

- CUBOID
- CUBE
- CYLINDER
- PRISM
- VOLUME=
Area of base x height
- LSA =
Perimeter of base x height
- TSA =
LSA +2 X Area of base
- CONE
- PYRAMID
- TETRAHEDRON
- SPHERE
- HEMISPHERE
- VOLUME=
 $\frac{1}{3} \times \text{Area of base} \times \text{height}$
- LSA =
 $\frac{1}{2} \times \text{Perimeter of base} \times \text{height}$
- TSA =
LSA + Area of base

Cylinder



Cylinder - 20 min

volume: $\pi r^2 h$ = Area of base \times height

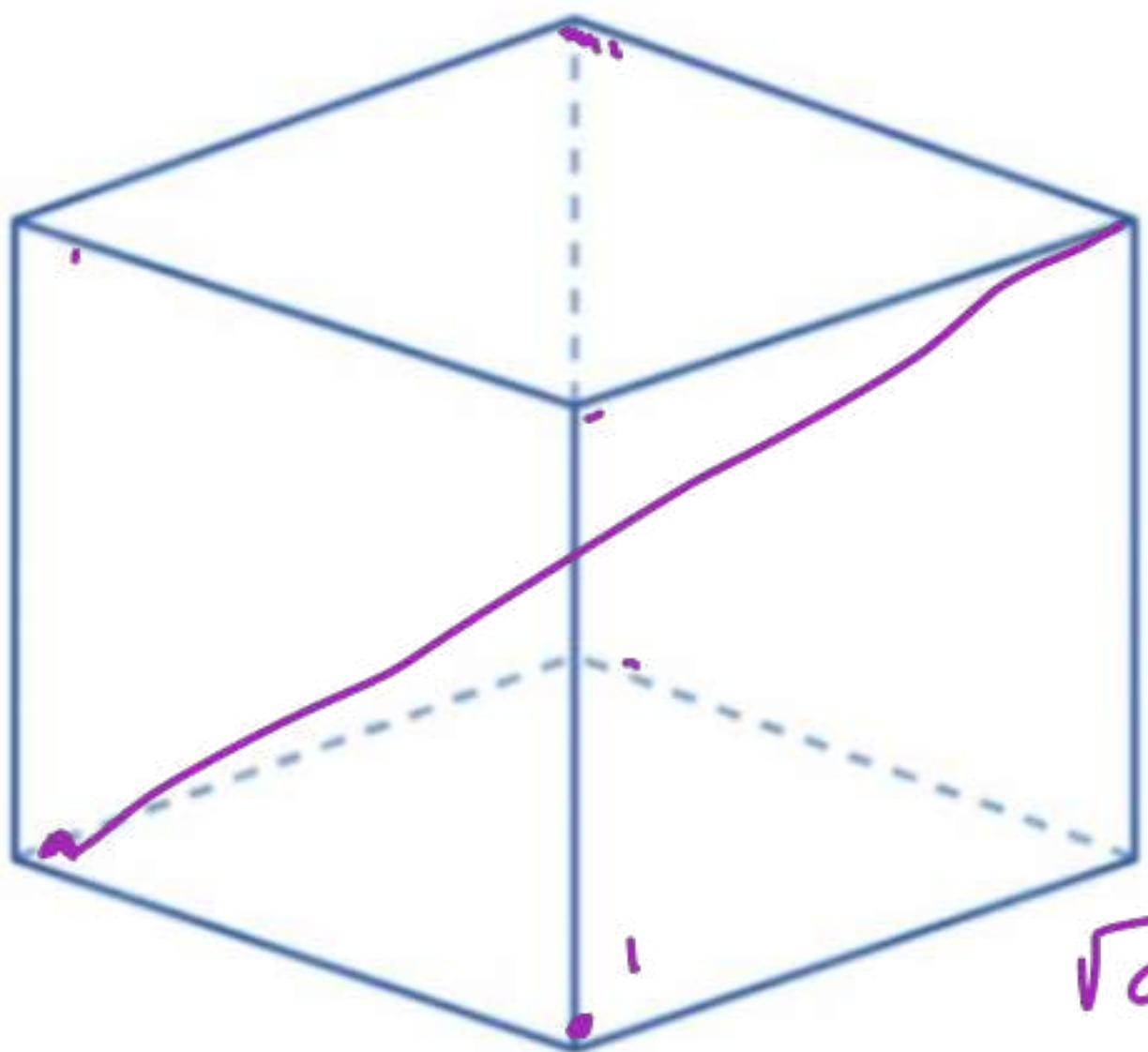
L.S.A = $2\pi r h$ = Perimeter of base \times h

T.S.A = $2\pi r h + 2\pi r^2$ = $2\pi r (r+h)$ = L.S.A + area of top & bottom

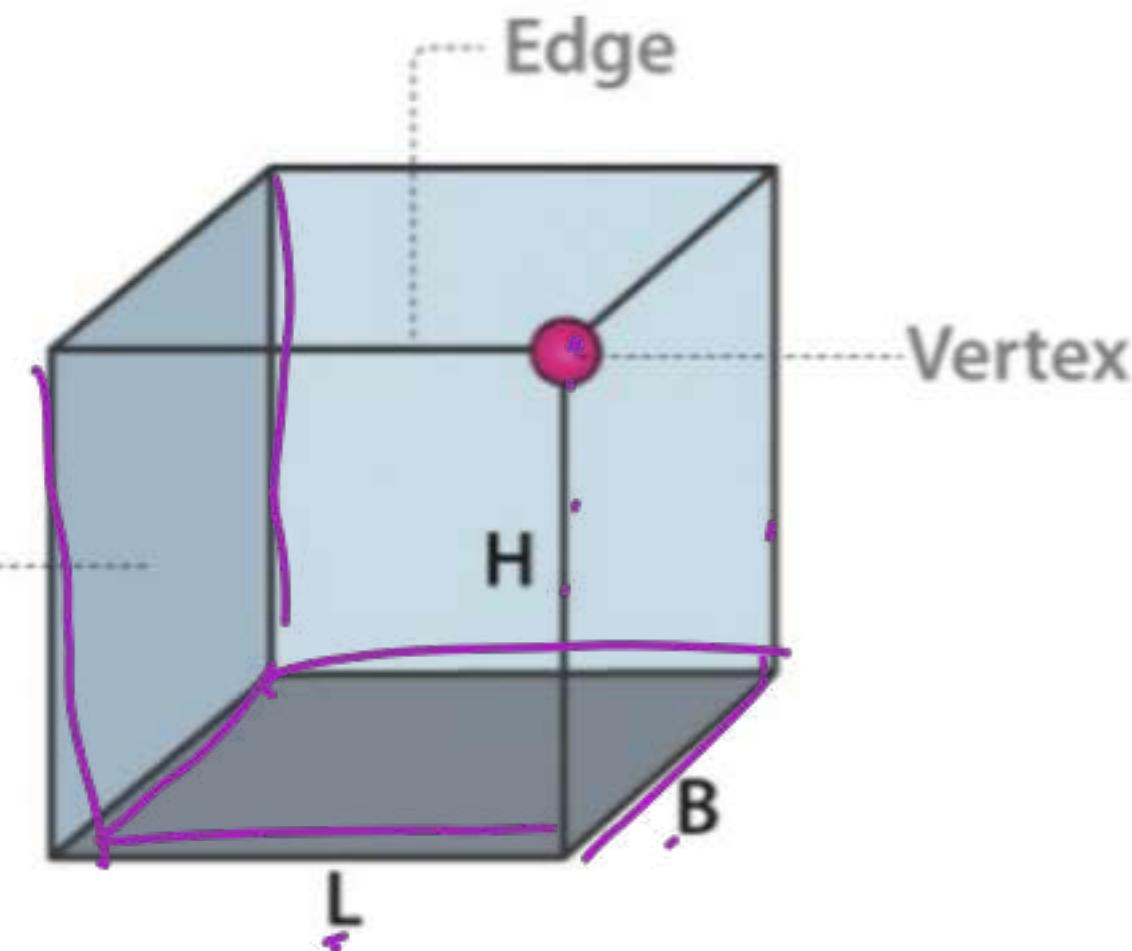
L.S.A - lateral surface area r - radius
T.S.A - total " "

h - height
 $r = \frac{D}{2}$

Cube - घन शृंखला



Face



$$\begin{aligned}\sqrt{a^2+a^2} &= \sqrt{2}a^2 \\ &= a\sqrt{2} \\ &= \text{diagonal edge}\end{aligned}$$

$L = B = H = a$: side

$a^2 \times a = a^3$ Edge

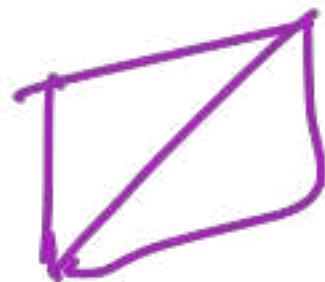
$$\text{volume} = a^3$$

$$\text{LSA} = 4a^2$$

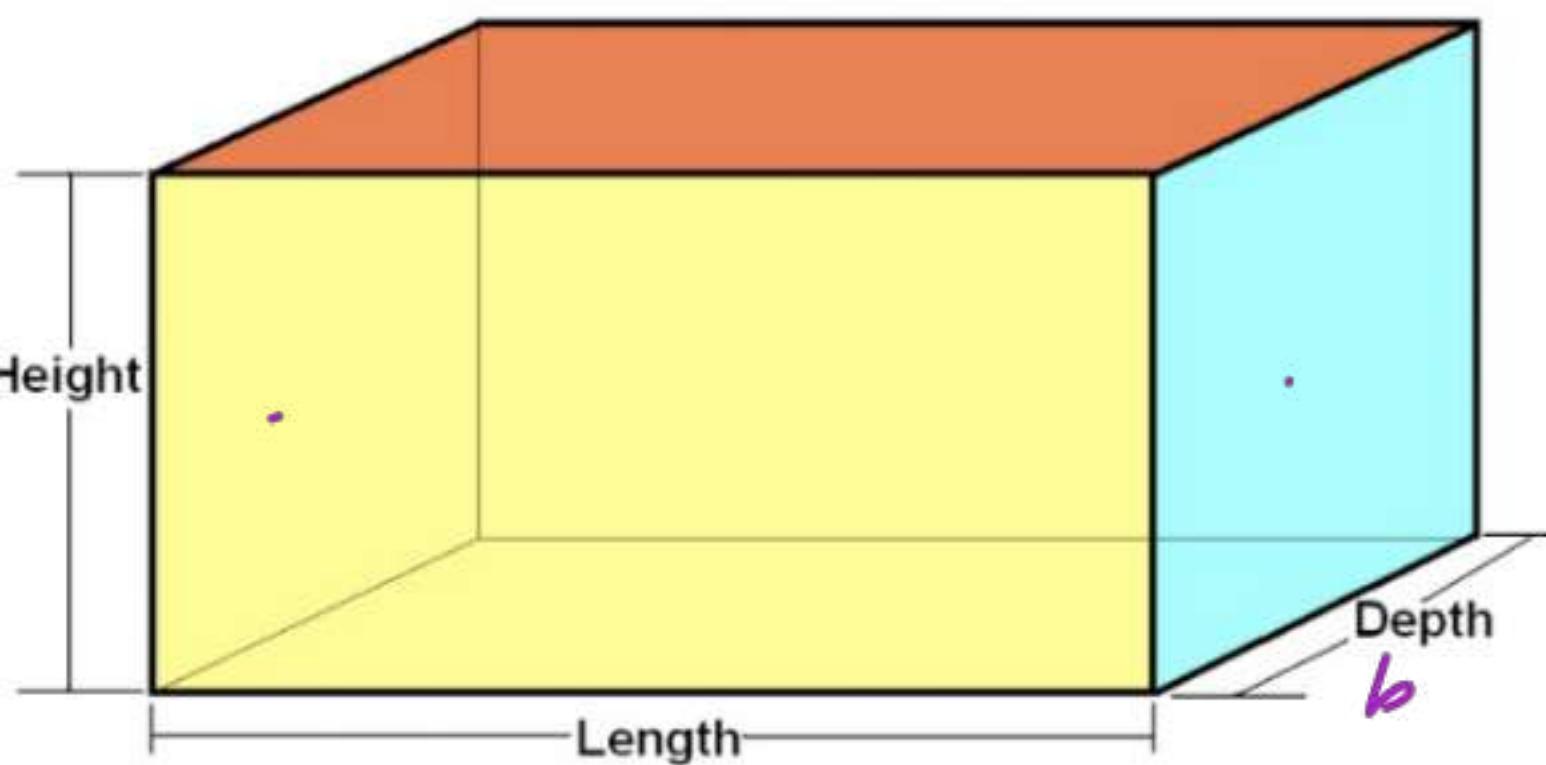
$$\text{TSA} = 6a^2$$

$$\text{Diagonal} = \sqrt{3} \times a = a\sqrt{3}$$

Cube



Cuboid - बॉर्ड नियम



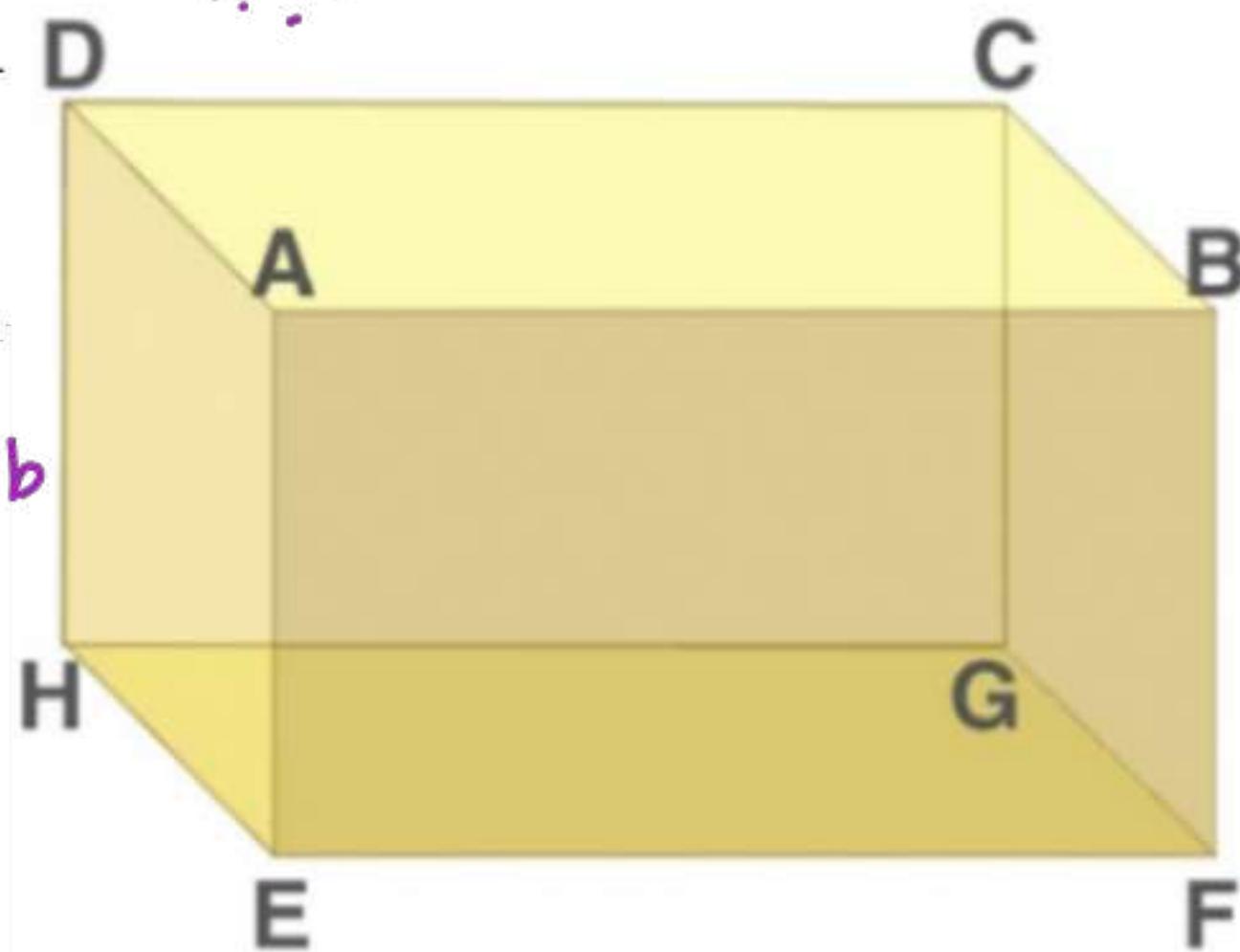
$$L + H + D$$

$$b$$

$$(l \times b \times h)$$

$$29ht + 2bht + 2lb$$

$$2(lht + bht + 8h)$$



Cuboid

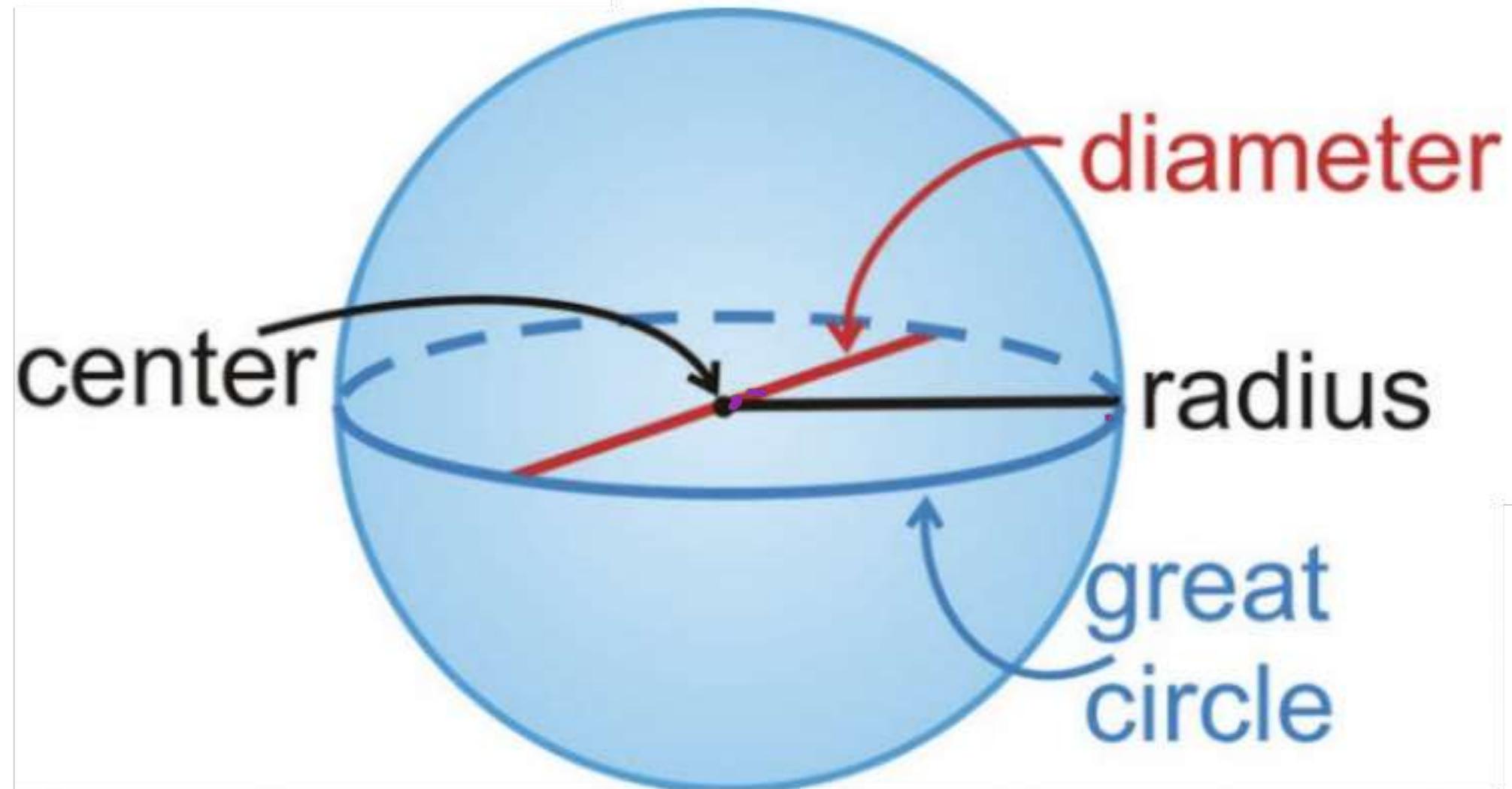
$$\text{Volume} = l b h$$

$$\text{LSA} = 2h(l+b)$$

$$\text{TSA} = 2(lht + bht + lb) = 2(lbh + bh + lh)$$

$$\text{Diagonal} = \sqrt{l^2 + b^2 + h^2}$$

sphere - Ebenü



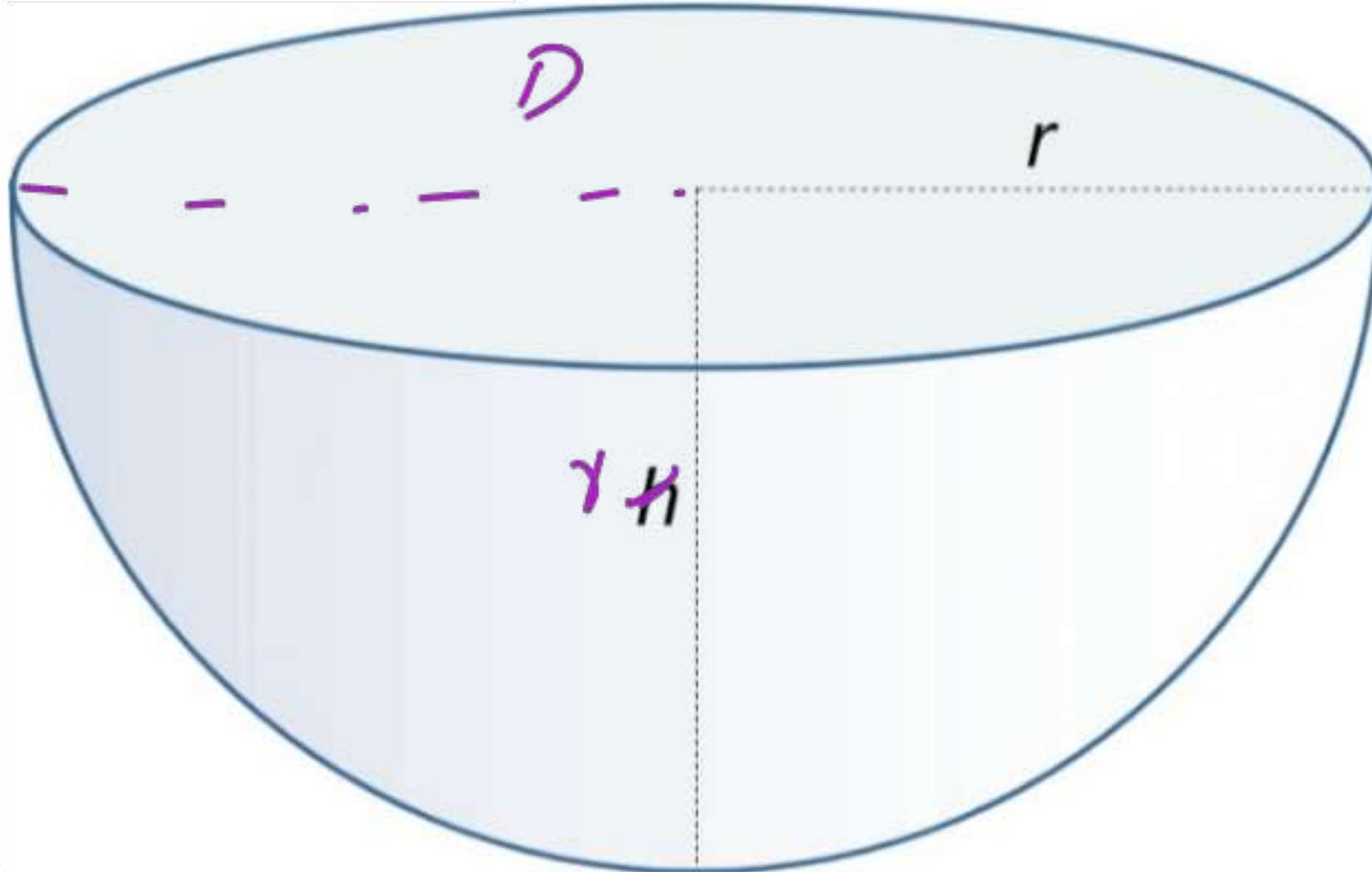
Sphere

$$\text{volume} = \frac{4}{3} \pi r^3$$

$$\text{LSA} = 4 \pi r^2$$

$$\text{TSA} = 4 \pi r^2$$

Hemisphere - Hohlhemisphäre



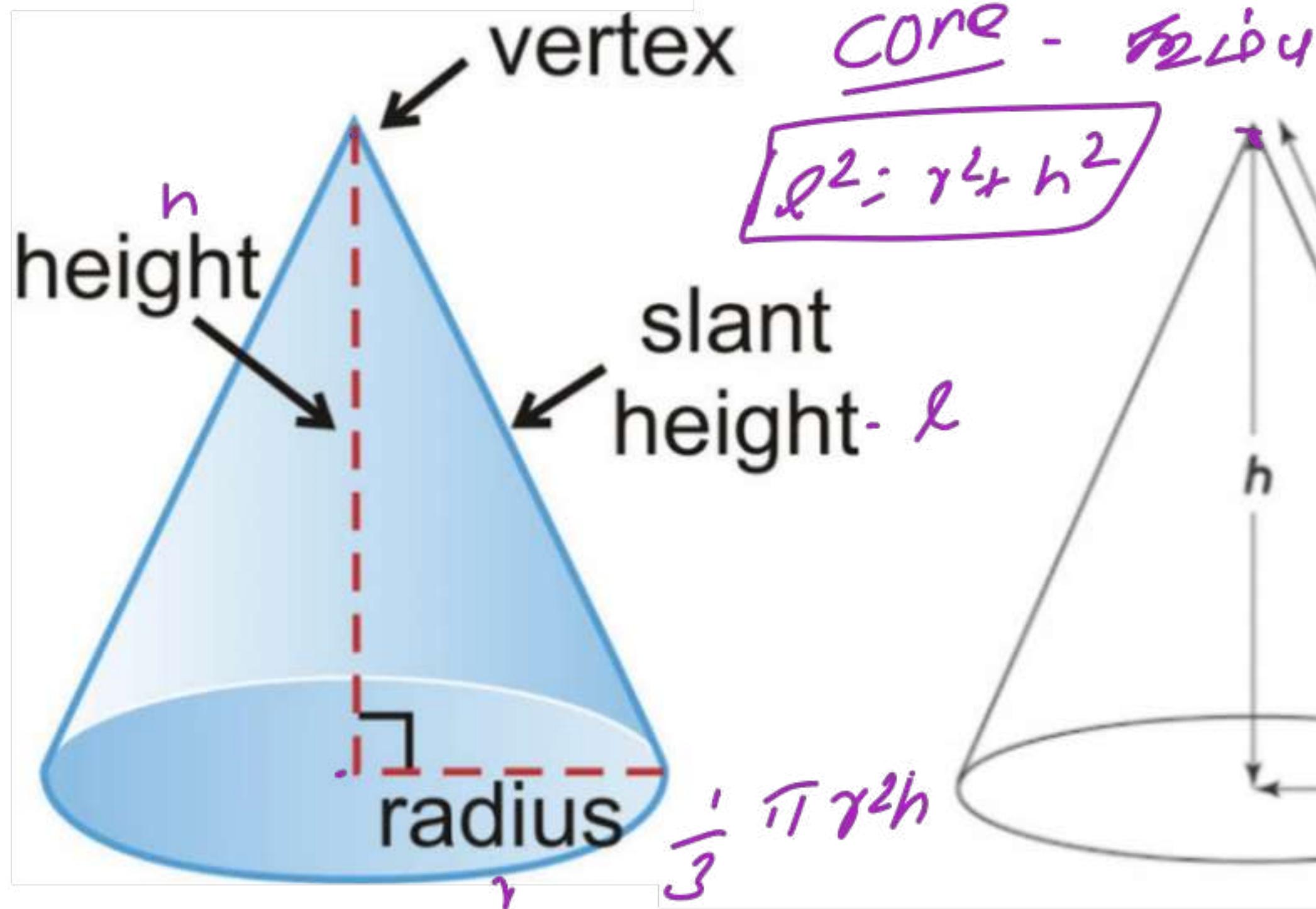
Hemisphere

$$\text{Volume} = \frac{2}{3} \pi r^3$$

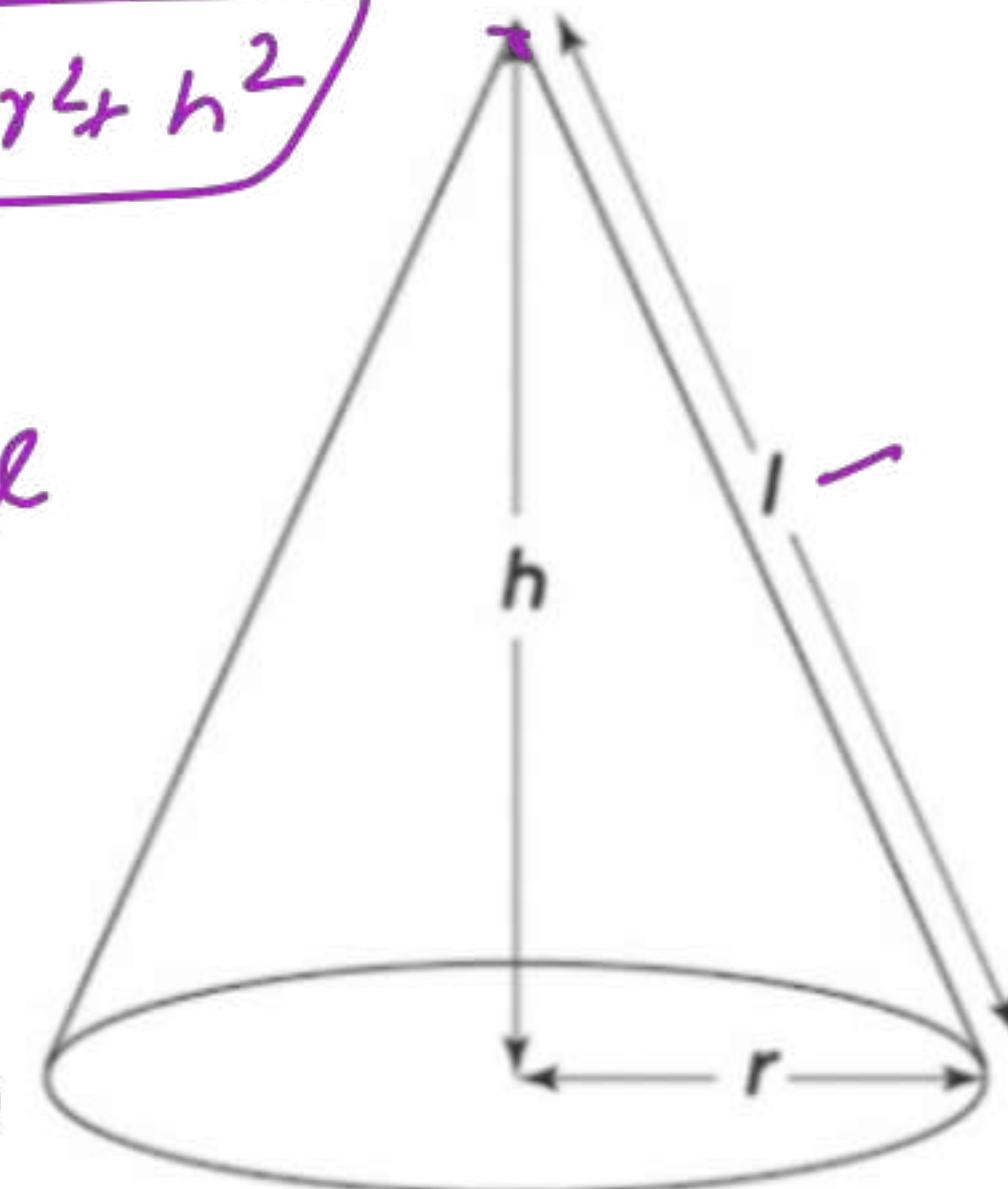
$$\frac{r^2}{3} \frac{\pi r^3}{2}$$

$$\text{LSA} = 2\pi r^2$$

$$\text{TSA} = 2\pi r^2 + \pi r^2 = 3\pi r^2$$



$$\frac{1}{3} \pi r^2 h$$



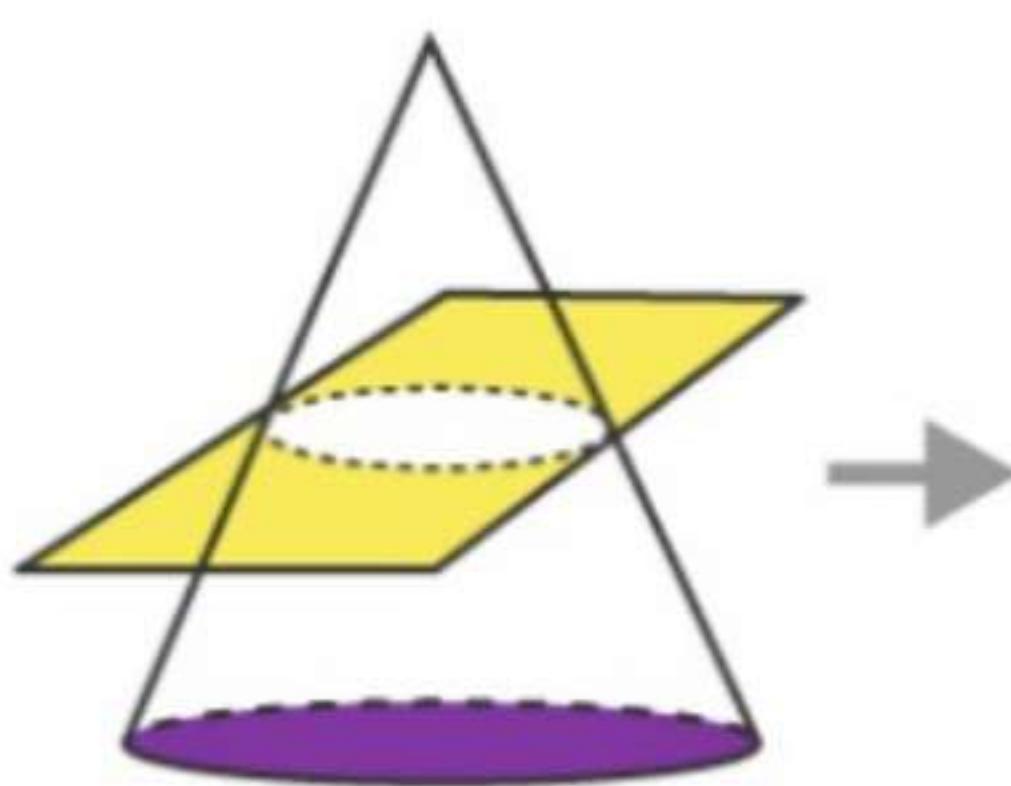
Cone

$$\text{Volume} = \frac{1}{3} \pi r^2 h$$

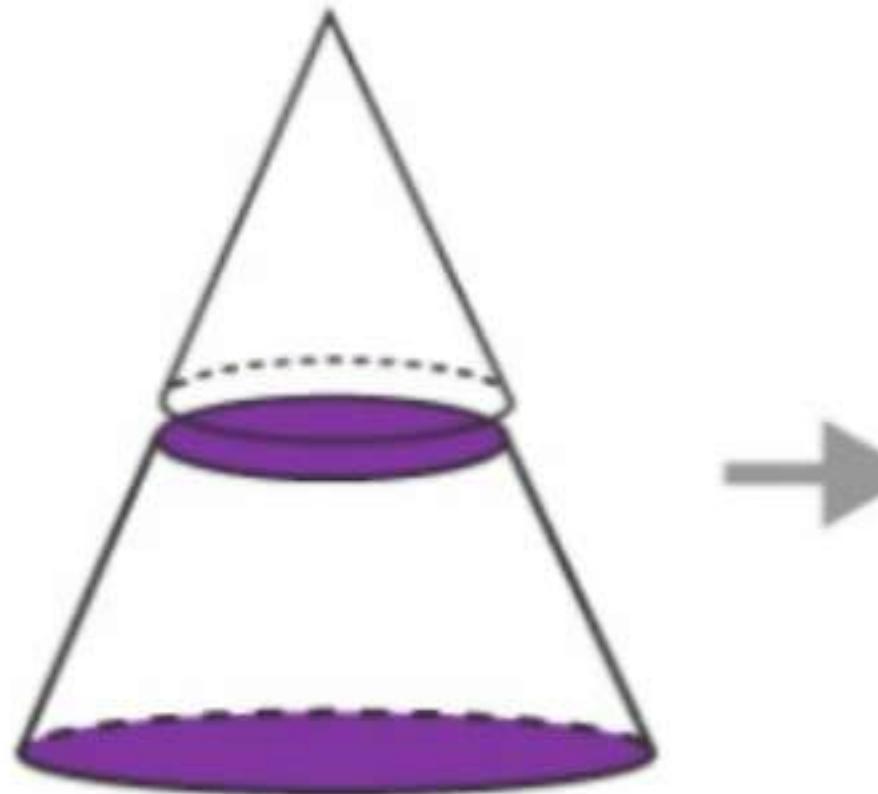
$$\text{LSA} = \pi r l$$

$$\text{TSA} = \pi r l + \pi r^2 = \pi r (l+r)$$

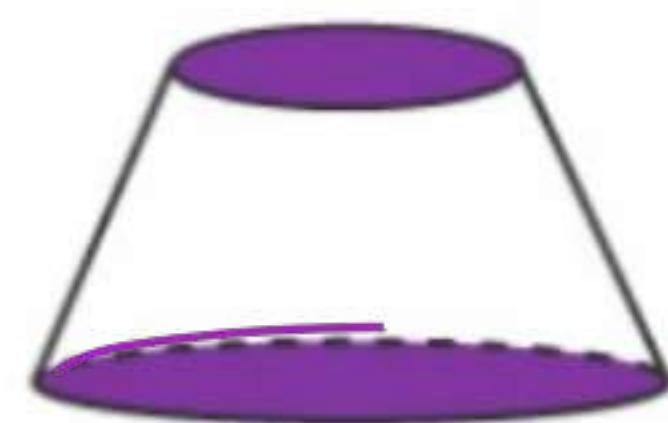
$$l^2 = h^2 + r^2 \rightarrow l = \sqrt{h^2 + r^2}$$



Plane parallel
to base cuts
the cone



Cone as two
separate parts



Frustum of
a cone

Frustum of cone

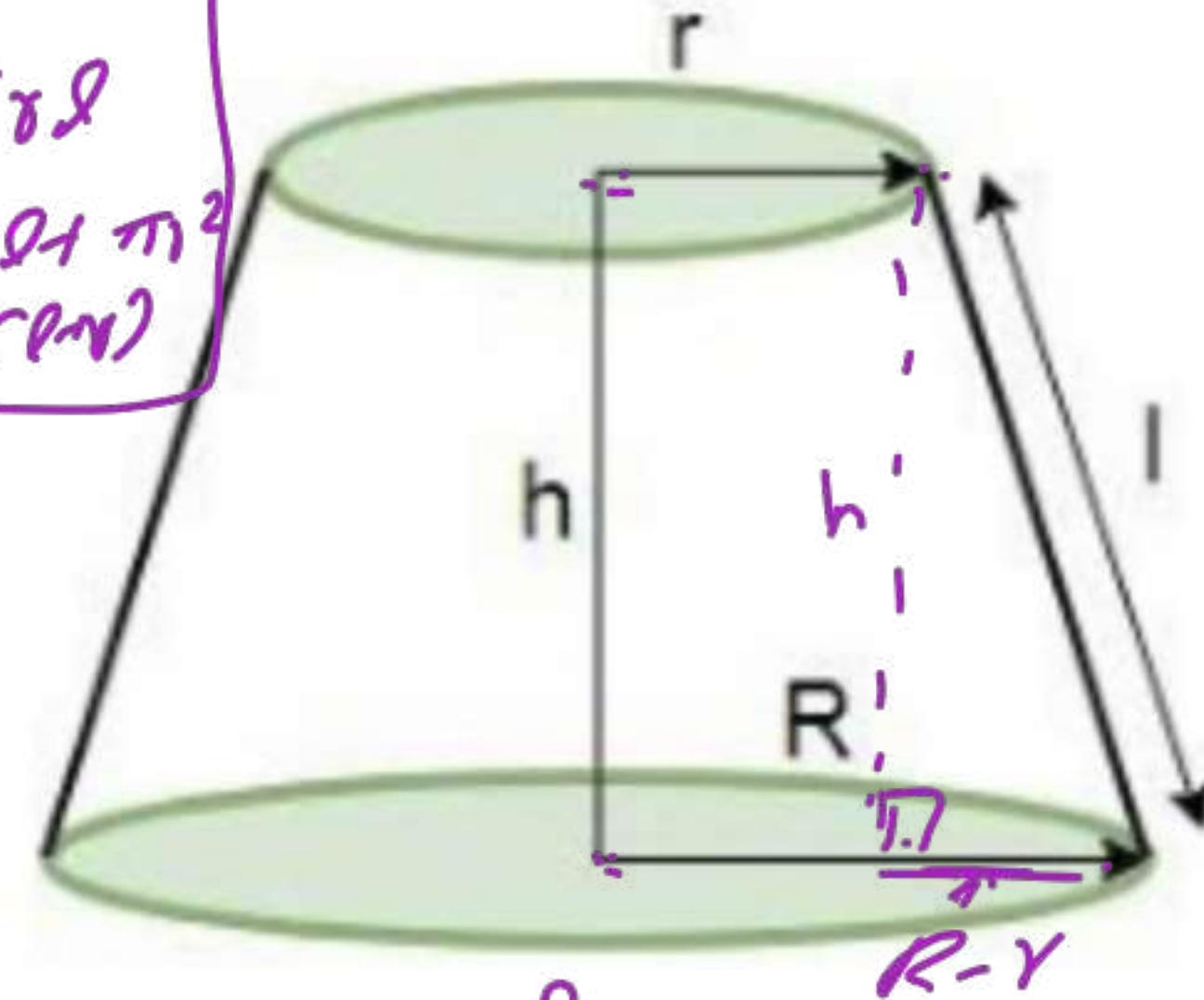
$$\text{Volume} = \frac{1}{3} \pi (R^2 + Rr + r^2) h$$

$$\text{CSA} = \pi(R+r) l$$

$$\begin{aligned}\text{TSA} &= \pi(R+r) l + \pi R^2 + \pi r^2 \\ &= \pi l (R+r) + \pi (R^2 + r^2)\end{aligned}$$

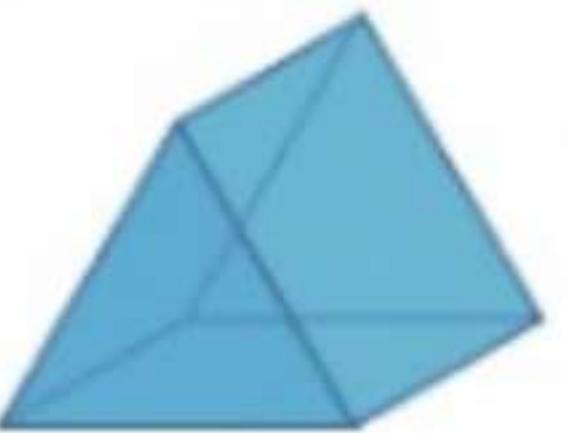
$$l^2 = h^2 + (R-r)^2$$

$$\begin{aligned}&\frac{1}{3} \pi r^2 h \\ &\cdot \pi r l \\ &\pi l (R+r) \\ &\pi (R^2 + r^2)\end{aligned}$$

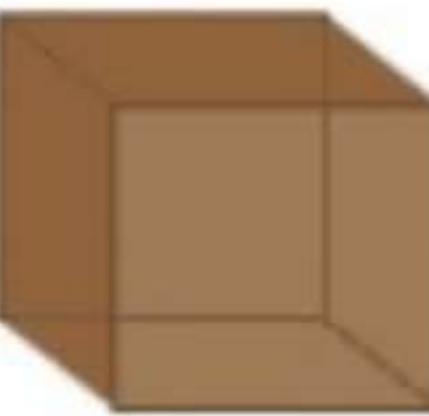


Curved = Lateral

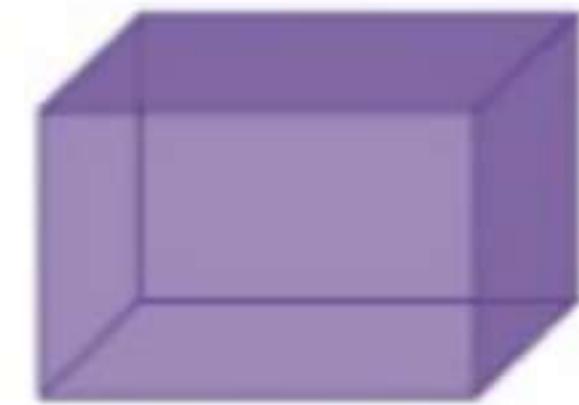
PRISMS



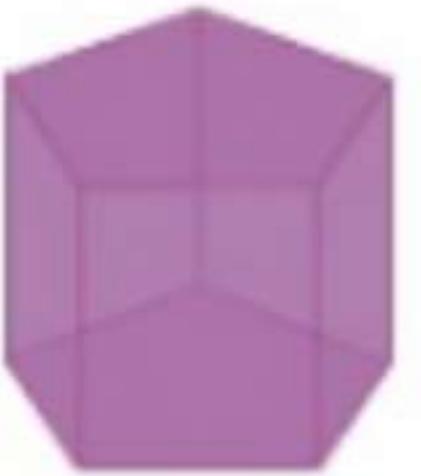
Triangular prism



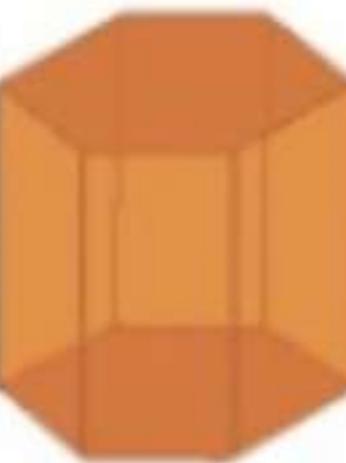
Square prism



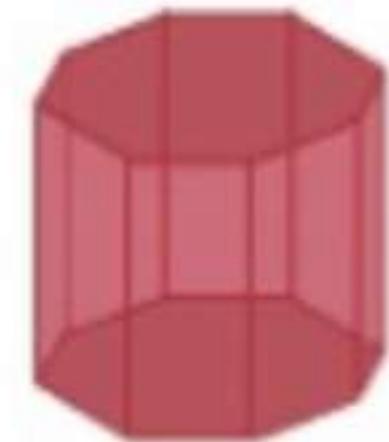
Rectangular prism



Pentagonal prism



Hexagonal prism



Octagonal prism

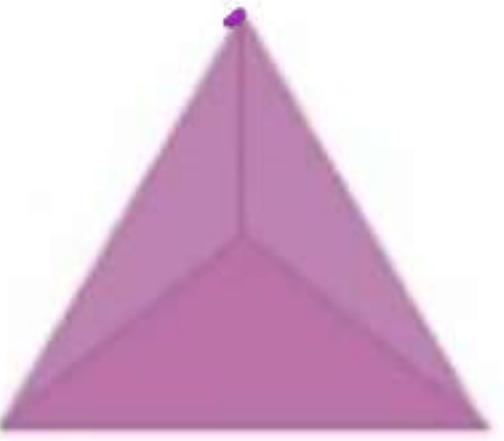
Prism

VOLUME = Area of base \times height

LSA = Perimeter of base \times height

TSA = LSA + 2 \times area of base

PYRAMIDS



Triangular pyramid



Square pyramid



Rectangular pyramid



Pentagonal pyramid



Hexagonal pyramid



Octagonal pyramid

Pyramid

VOLUME: $\frac{1}{3}$ Area of base \times height

LSA = $\frac{1}{2}$ Perimeter of base \times height

TSA = LSA + Area of base

What is the area of a triangle whose sides are 7 cm, 24 cm and 25 cm?

X 1. 72 cm^2

X 2. 108 cm^2

✓ 3. 84 cm^2

X 4. 42 cm^2

$$= 4 \times 7 \times 3$$

$$= 84 \text{ cm}^2$$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{28 \times 21 \times 13 \times 3}$$

$$= \sqrt{1 \times 7 \times 13 \times 6 \times 3}$$

$$= 4 \times 7 \times 3$$

$$= 84 \text{ cm}^2$$

$$a = 7, b = 24, c = 25$$

$$7^2 + 24^2 = 25^2$$

$$49 + 576 = 625$$

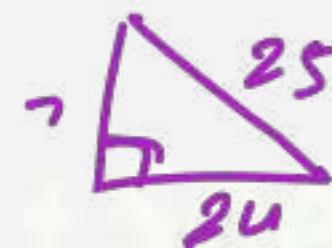
$$625 = 625$$

$$A = \frac{1}{2}ab \times h$$

$$= \frac{1}{2} \times 24 \times 7 = 84 \text{ cm}^2$$

$$s = \frac{a+b+c}{2} = \frac{7+24+25}{2}$$

$$s = \frac{56}{2} = 28$$



The area of a rhombus is 300 cm^2 . If the length of one of the diagonals of the rhombus is 30 cm , then what is the length (in cm) of the second diagonal?

- 1. 25
- 2. 10
- 3. 20 ✓
- 4. 30

$$A = \frac{d_1 \times d_2}{2}$$

$$300 = \frac{d_1 \times 30}{2}$$

$$d_1 = 20 \text{ cm}$$

If the lengths of the diagonals of a rhombus are 24 cm and 18 cm, then what is the area of the rhombus?

- 1. 196 cm²
- 2. 188 cm²
- 3. 204 cm²
- 4. 216 cm²

$$A = \frac{d_1 \times d_2}{2}$$
$$A = \frac{20 \times 18}{2}$$

180 24
 9

The sides of an isosceles triangles are 10 cm, 10 cm and 12 cm. What is the area of the triangle?

1. 60 cm^2

2. 48 cm^2

3. 40 cm^2

a b c

$$s = \frac{32}{2} = 16$$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{16 \times 6 \times 6 \times 4}$$

$$= \sqrt{16^2 \times 6^2 \times 2^2} = 4 \times 6 \times 2 = 48 \text{ cm}^2$$

The base and hypotenuse of a right angled triangle are 9 cm and 41 cm respectively. What is the area of the triangle?

✓ 1. 180 cm^2 ✓

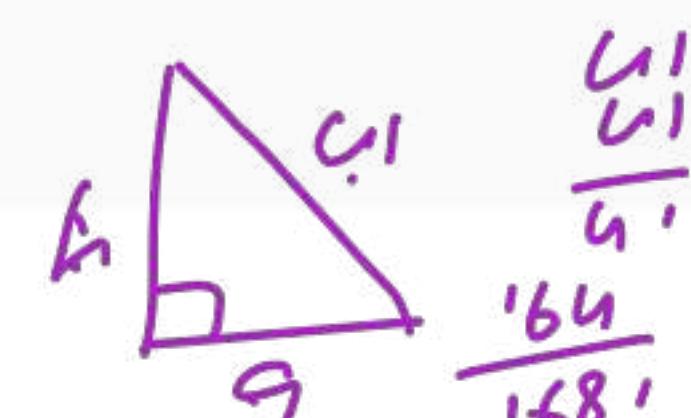
✗ 2. 170 cm^2

$$A = \frac{1}{2} \times b \times h$$

✗ 3. 190 cm^2

$$\begin{aligned} A &= \frac{1}{2} \times 9 \times 40 \\ &= 180 \text{ cm}^2 \end{aligned}$$

✗ 4. 160 cm^2



$$h^2 + 9^2 = 41^2$$

$$h^2 = 1681 - 81$$

$$h = \sqrt{1600} = 40$$

The area of a square is 144 cm^2 . What is the perimeter of the square formed with the diagonal of the original square as its side?

✓ 1. $48\sqrt{2} \text{ cm}$ ✓

✗ 2. 48 cm

✗ 3. $24\sqrt{2} \text{ cm}$

✗ 4. 24 cm

$$\text{Area} = a^2 = 144 \rightarrow \cancel{d} \quad d \sqrt{2} \cdot d = 144$$

$$a^2 = 144$$

$$a = 12$$

$$d = a\sqrt{2} = 12\sqrt{2}$$

$$P = 4a = 4 \times 12\sqrt{2} = 48\sqrt{2} \text{ cm}$$

The length of one of the diagonals of a rhombus is 48 cm. If the side of the rhombus is 26 cm, then what is the area of the rhombus?

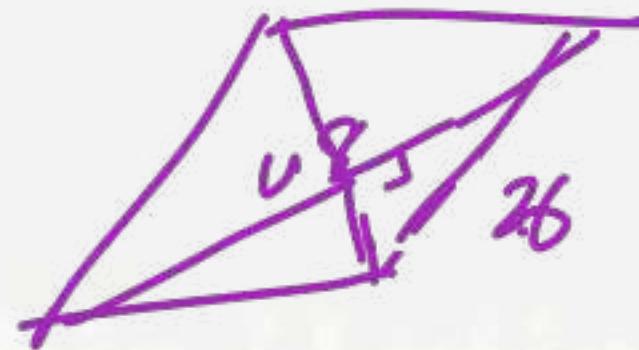
1. 540 cm^2

2. 420 cm^2

3. 360 cm^2

4. 480 cm^2

$$\begin{aligned} \text{Area} &= \frac{d_1 \times d_2}{2} \\ &= \frac{48 \times 28}{2} \\ &= 672 \text{ cm}^2 \end{aligned}$$



$$d_1^2 + d_2^2 = 4a^2$$

$$48^2 + d_2^2 = 4 \times 26^2$$

$$d_2^2 = 2704 - 2304$$

$$d_2^2 = 400$$

$$d_2 = 20$$

$$\begin{array}{r} 48 \\ \times 48 \\ \hline 384 \\ 192 \\ \hline 2304 \end{array}$$

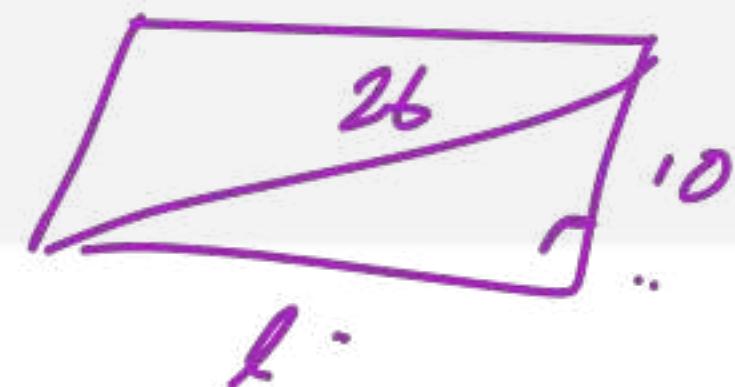
$$\begin{array}{r} 676 \\ \times 2704 \\ \hline 2704 \\ 1352 \\ \hline 1808 \\ 1352 \\ \hline 1808 \\ 1352 \\ \hline 2304 \end{array}$$

The length of the diagonal of a rectangle is 26 cm and one side is 10 cm. The area of the rectangle is:

✓ 1. 240 cm^2

✗ 2. 260 cm^2

$$\begin{aligned}A &= l \times b \\&= 20 \times 10 = 200\end{aligned}$$



$$d = \sqrt{l^2 + b^2}$$

$$d^2 = l^2 + b^2$$

$$676 = l^2 + 100 \quad l = 20$$

$$l^2 = 576 = 20^2$$

The diagonal of a square measures $6\sqrt{2}$ cm. The measure of the diagonal of a square whose area is twice that of the first square is:

- ✓ 1. 12 cm ✓

$$d = 6\sqrt{2} \text{ cm}$$



$$A_1 = \frac{d^2}{2} = \frac{6^2 \times 2}{2} = 36$$

$$A_2 = 2 \times 36 = 72 = \frac{D^2}{2}$$

$$D^2 = 144$$

$$D^2 = 12^2$$

$$D = 12$$

The area of a rectangle is 180 cm². If the ratio of length and breadth of the rectangle is 5 : 4, then what is the length (in cm) of diagonal of the rectangle?

1. $\sqrt{423}$

$$l \times b = 180 \text{ cm}^2 \quad l:b = 5:4$$

2. $\sqrt{317}$

$$5x \times 4x = 180 \quad d = \sqrt{l^2 + b^2}$$

3. $\sqrt{369}$ ✓

$$x^2 = 9 \quad l:b = 5:4$$

4. $\sqrt{371}$

$$x = 3 \quad l = 5x, b = 4x$$

$$l = 15 \quad b = 12$$

$$d = \sqrt{225 + 144} \\ = \sqrt{369}$$

What is the area of the largest square which can be inscribed in a circle of radius 14 cm?

(Take $\pi = \frac{22}{7}$)

✓ 1. 392 cm^2 ✓

✗ 2. 484 cm^2

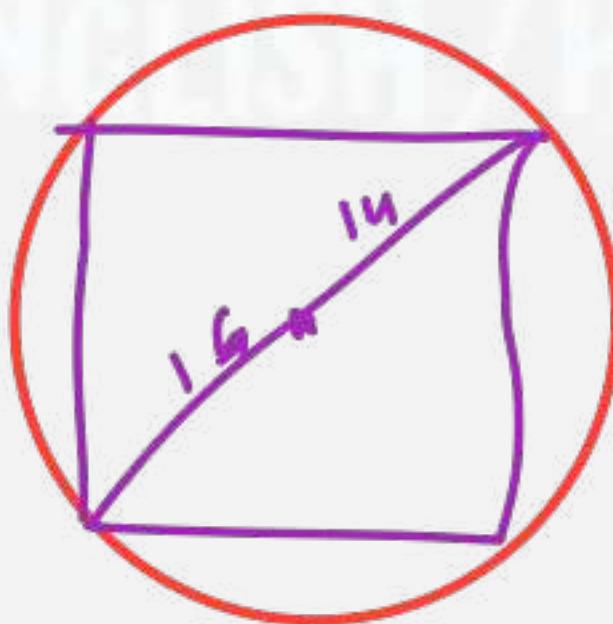
✗ 3. 196 cm^2

✗ 4. 784 cm^2

Dia: 28 = d

$A = \frac{d^2}{2}$

$A = \frac{14^2}{2}$
 $A = \frac{28 \times 28}{2}$



What is the circumference of the largest circle which can be inscribed in a square of side 14 cm?

(Take $\pi = \frac{22}{7}$)

1. 66 cm

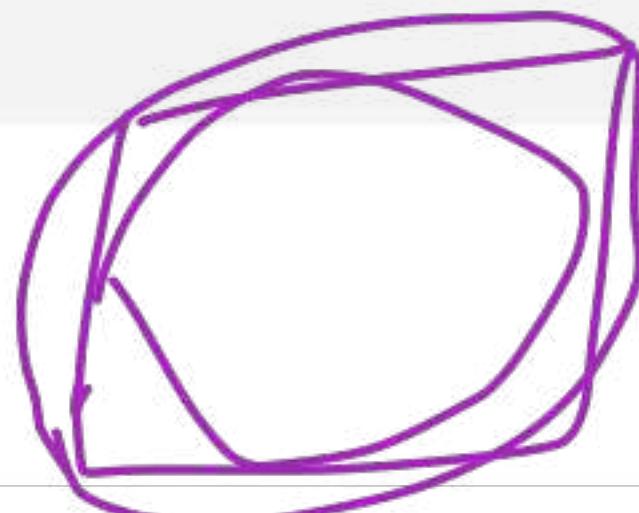
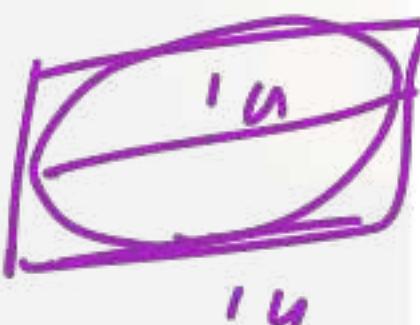
2. 88 cm

3. 22 cm

4. 44 cm ✓

$$\begin{aligned} &= 2\pi r \\ &= 2 \times \frac{22}{7} \times 7 \\ &= 44 \end{aligned}$$

$$\begin{aligned} D &= 14 \\ r &= 7 \end{aligned}$$



$$r = \frac{d}{2}$$

$$r = \frac{14}{2} : 7$$

$$r = \frac{d}{2}$$

$$R = \frac{d}{2}$$

What is the area of the largest circle which can be inscribed in a square of side 28 cm?

(Take $\pi = \frac{22}{7}$)

\times 1. 308 cm²

\checkmark 2. 616 cm²

\times 3. 476 cm²

\times 4. 512 cm²

diameter = Side of square

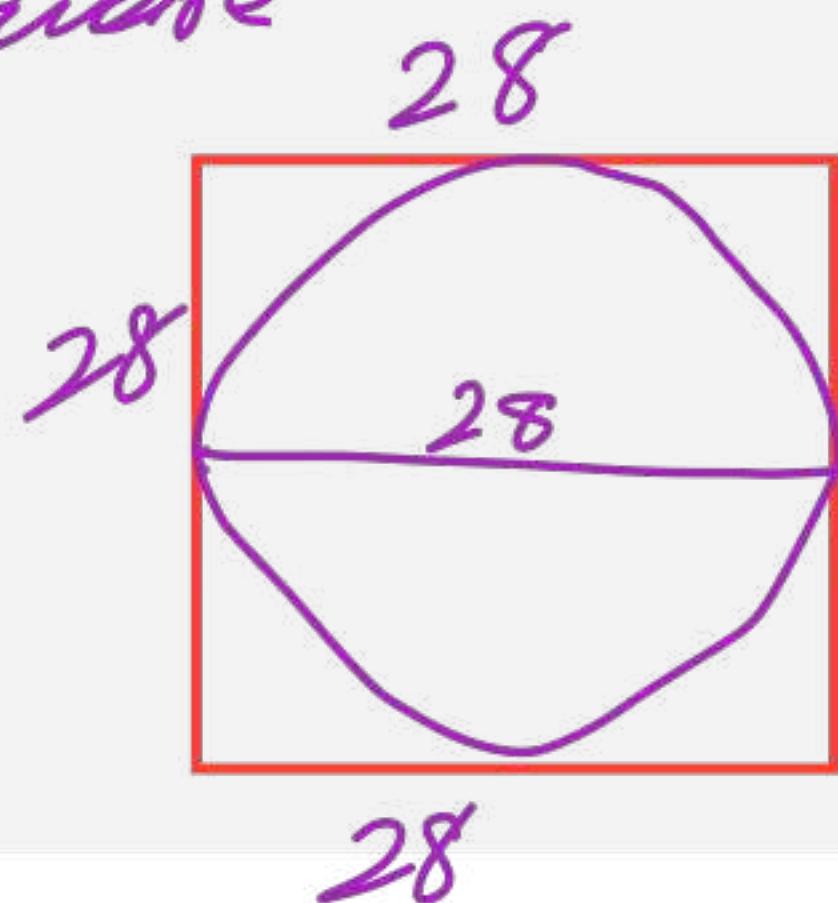
$$D = 28$$

$$r = 14$$

$$A = \pi r^2$$

$$= \frac{22}{7} \times 14 \times 14$$

$$= 616 \text{ cm}^2$$

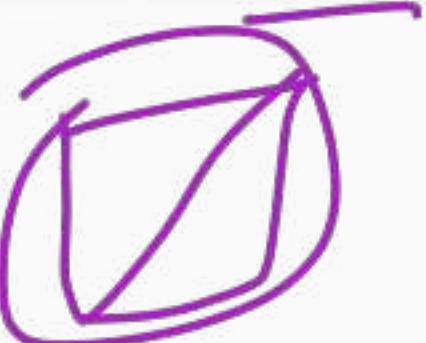


$$\begin{array}{r} 28 \\ \times 22 \\ \hline 56 \\ \hline 616 \end{array}$$

What is the area of the largest square which can be inscribed in a circle of radius 28 cm?

1. 3136 cm^2

$r = 28$



2. 1568 cm^2

$D = 56 = d$

3. 784 cm^2

$A = \frac{d^2}{2} = \frac{56 \times 56}{2}$

4(8)

4. 196 cm^2

$R = \frac{ar^2}{2}$

$r_2 \times r_2 \times 2 \times 28 = a$

$a = 28r_2$

$A = a^2 = 28^2 \times 2$

Radius of base of a right circular cone and a sphere is each equal to r . If the sphere and the cone have the same volume, then what is the height of the cone?

1. $7r$

2. $4r$

3. $2r$

4. $3r$

$$V_{\text{sphere}} = V_{\text{cone}}$$

$$\frac{4}{3}\pi r^3 = \frac{1}{3}\pi r^2 h$$

$$h = 4r$$



$$7H = \pi r$$

The side of a cube is 15 cm. What is the base area of a cuboid whose volume is 175 cm^3 less than that of the cube and whose height is 32 cm?

1. 200 cm^2

2. 100 cm^2

3. 160 cm^2

4. 325 cm^2

$$\frac{225}{5}$$

$a = 15 \text{ cm}$ $\sim h = 32 \text{ cm}$ -

$$V_{\text{cuboid}} = V_{\text{cube}} - 175$$

$$V_{\text{cuboid}} = a^3 - 175$$

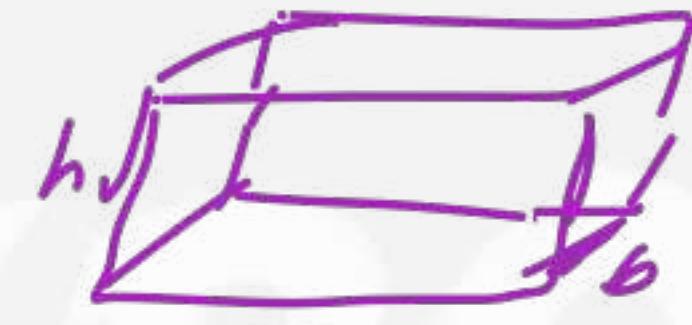
$$= 15^3 - 175$$

$$= 3375 - 175$$

$$V_{\text{cuboid}} = 3200$$

$$l b h = 3200$$

$$l b = \frac{3200}{32} = 100$$



$$l \times b$$

$$l b h =$$

$$\frac{3375 - 175}{32} \cdot 100$$

The total surface area of a hollow cuboid is 340 cm^2 . If the length and the breadth of the cuboid are 10 cm and 8 cm respectively, then what is the length of the longest stick that can be fitted inside the cuboid?

~~X~~ 1. 10 cm

$$TSA = 340 \text{ cm}^2$$

~~X~~ 2. $4\sqrt{41} \text{ cm}$

$$2(lb + bh + hl) = 340$$

~~✓~~ 3. $3\sqrt{21} \text{ cm}$

$$10 \times 8 + 8h + 10h = 170$$

~~X~~ 4. 21 cm

$$\begin{aligned} 18h &= 170 - 80 = 90 \\ h &= 90 / 18 = 5 \end{aligned}$$



$$l = 10, b = 8$$

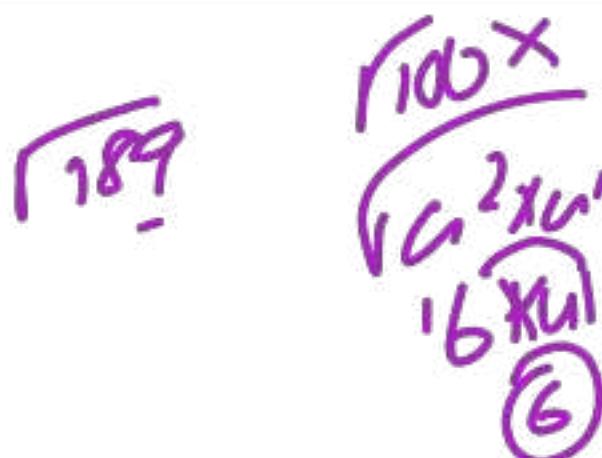
$$\text{Diagonal} = \sqrt{l^2 + b^2 + h^2}$$

$$= \sqrt{100 + 64 + 25}$$

$$= \sqrt{189}$$

$$= \sqrt{9 \times 21}$$

$$= 3\sqrt{21}$$



The height of a right circular cone is 5 cm and its base radius is 12 cm. What is the curved surface area of the cone?

- 1. $132\pi \text{ cm}^2$
- 2. $143\pi \text{ cm}^2$
- 3. $156\pi \text{ cm}^2$
- 4. $168\pi \text{ cm}^2$

$$\begin{aligned}CSA &= \pi r l \\&= \pi \times 12 \times 13 \\&= 156\pi \text{ cm}^2\end{aligned}$$



$$\begin{aligned}h &= 5 \text{ cm} \\r &= 12 \text{ cm}\end{aligned}$$

$$\begin{aligned}l^2 &= h^2 + r^2 \\l &= \sqrt{25 + 144} \\l &= \sqrt{169} \\l &= 13\end{aligned}$$

The length, breadth and height of a cuboid are 5 cm, 2 cm and 4 cm respectively. What is the total surface area of the cuboid?

- 1. 84 cm^2
- 2. 152 cm^2
- 3. 38 cm^2
- 4. 76 cm^2

$$\begin{aligned}l & b & h \\TSA &= 2(lb + bh + lh) \\&= 2 \times (10 + 8 + 20) \\&= 2 \times 38 = 76 \text{ cm}^2\end{aligned}$$

The volume of a cube is 216 cm^3 . What is the area of one face of the cube?

✓ 1. 36 cm^2

✗ 2. 12 cm^2

✗ 3. 24 cm^2

✗ 4. 30 cm^2

$$\text{volume} = a^3 = 216$$

$$a^3 = 6^3$$

$$a = 6$$

$$a^2 = 6 \times 6 = 36$$



The edge of a cube is 8 cm. What is the total surface area of the cube?

1. 128 cm^2

$a = 8 \text{ cm}$

2. 256 cm^2

$TSA = 6a^2$

3. 384 cm^2 ✓

$= 6 \times 64$

4. 484 cm^2

$= 384 \text{ cm}^2$

$\frac{6}{384} 4^2$

A room is in the shape of cube and the length of the longest rod placed in it is $21\sqrt{3}$ cm. The area of the floor is:

✓ 1. 441 cm^2 ✓

Diagonal = $21\sqrt{3}$

✗ 2. 144 cm^2

$a\sqrt{3} = 21\sqrt{3}$

✗ 3. 169 cm^2

$a = 21$

✗ 4. 961 cm^2

$a^2 = 21^2 = 441$



The area of the sheet metal needed to make a box of size $7 \text{ cm} \times 8 \text{ cm} \times 9 \text{ cm}$ is:

✓ 1. 382 cm^2

✗ 2. 156 cm^2

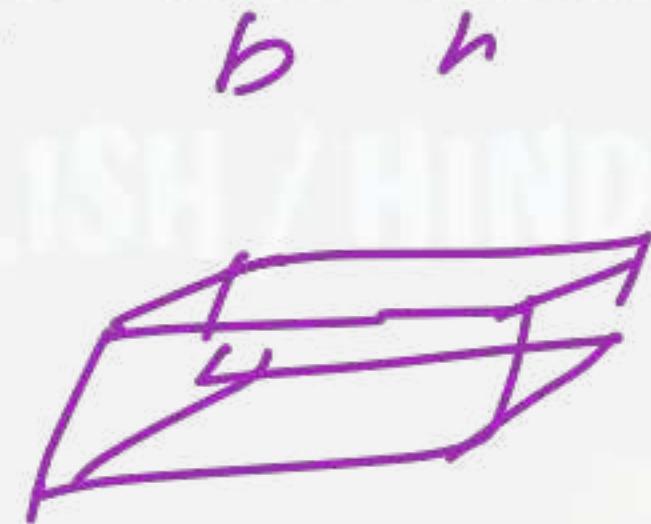
✗ 3. 412 cm^2

✗ 4. 139 cm^2

$$\text{TSA: } 2(lb + bh + hl)$$

$$= 2(56 + 72 + 63)$$

$$= 2 \times 191 = 382$$



The volume of prism is 308 cm^3 and height is 11 cm . The base area of prism is:

1. 21 cm^2

$$V = \text{Base Area} \times h$$

2. 14 cm^2

$$\frac{28}{308} = \text{BA} \times 11$$

3. 28 cm^2 ✓

$$= 28 \text{ cm}^2$$

4. 22 cm^2

The total surface area of a hemisphere is 462 cm^2 . What is its diameter?

(Take $\pi = \frac{22}{7}$)

✓ 1. 14 cm ✓

✗ 2. 7 cm

✗ 3. 17.5 cm

✗ 4. 10.5 cm

$$TSA = 3\pi r^2 = 462$$

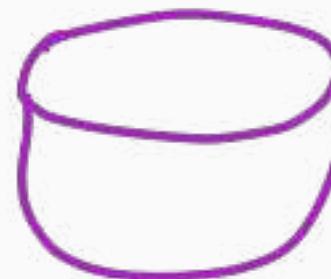
$$3 \times \frac{22}{7} \times r^2 = 462$$

$$r^2 = \frac{462 \times 7}{3 \times 22}$$

$$r^2 = 7^2$$

$$r = 7$$

$$D = 2r = 14 \text{ cm}$$



What is the total surface area of a cone which has a radius of 21 cm and a height of 28 cm?

(Take $\pi = \frac{22}{7}$)

✓ 1. 3696 cm²

✗ 2. 1848 cm²

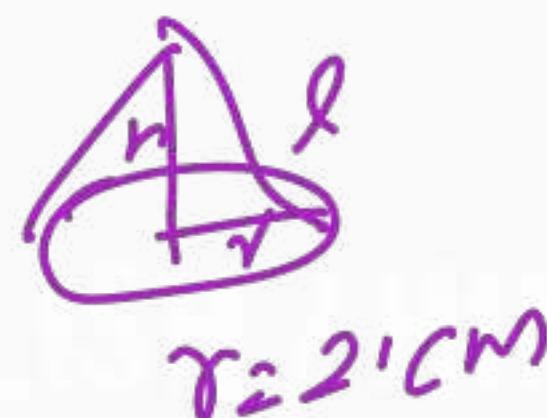
✗ 3. 5544 cm²

✗ 4. 7392 cm²

$$\begin{aligned} \text{TSA} &= \pi r l + \pi r^2 \\ &= \pi r(r+l) \\ &= \frac{22}{7} \times 21(35+21) \\ &= 22 \times 3 \times 56 \\ &= 3696 \end{aligned}$$

36

$$\begin{array}{c} 1225 \\ \hline 245 \\ \hline 49 \\ \hline 7 \end{array} \quad \sqrt{r^2 + h^2} = \sqrt{21^2 + 28^2} = \sqrt{35^2} = 35$$



$$r = 21 \text{ cm}$$

$$h = 28$$

$$l^2 = h^2 + r^2$$

$$l = \sqrt{28^2 + 21^2}$$

$$= \sqrt{784 + 441}$$

$$= \sqrt{1225}$$

$$l = \sqrt{35^2} = 35$$

A hemisphere of radius 30 cm is moulded to form a cylinder of height 180 cm. The diameter of the cylinder is:

- 1. 15 cm
- 2. 10 cm
- 3. 5 cm
- 4. 20 cm

$$V_{\text{hemisphere}} = V_{\text{cylinder}}$$

$$\frac{2}{3}\pi r^3 = \pi R^2 h$$



$$V = V$$

$$\frac{2}{3} \times \frac{30 \times 30 \times 30}{10} = R^2$$

$$R^2 = \sqrt{2 \times 10 \times 10}$$
$$= \sqrt{2 \times 1 \times 5 \times 5}$$

$$R = 2 \times 5 = 10$$

$$D = 2R = 2 \times 10 = 20$$

If the volumes of two cubes are in the ratio of 64 : 125, then what is the ratio of their total surface areas?

~~X~~ 1. 9 : 16

~~X~~ 2. 4 : 5

✓ 3. 16 : 25 ✓

~~X~~ 4. 64 : 125

$$\frac{a_1^3}{a_2^3} = \frac{64}{125}$$

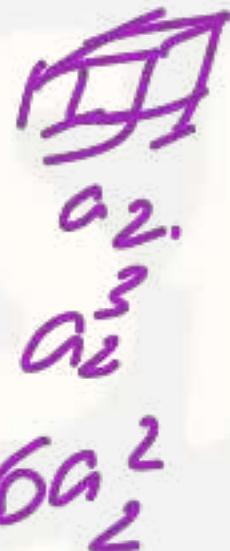
$$\frac{a_1^3}{a_2^3} = \frac{4^3}{5^3}$$

$$\frac{a_1}{a_2} = \frac{4}{5}$$

$$\frac{a_1^3}{a_2^3} = \frac{4^3}{5^3}$$

$$\frac{a_1}{a_2} = \frac{4}{5}$$
$$= \frac{64}{125}$$

6/5



$$6a_1^2$$

$$6a_2^2$$

$$\frac{6a_1^2}{6a_2^2} = \left(\frac{a_1}{a_2}\right)^2$$

$$= \left(\frac{4}{5}\right)^2 = \frac{16}{25}$$

The radii of a right circular cone and a right circular cylinder are in the ratio 2 : 3. If the ratio of the heights of the cone and the cylinder is 3 : 4, then what is the ratio of the volumes of the cone and the cylinder?

1. 1 : 6

2. 1 : 3

3. 1 : 9 ✓

4. 2 : 3

$$\frac{r}{R} = \frac{2}{3}$$

$$\frac{h}{H} = \frac{3}{4}$$

cone
sum

cylinder
cups.

$$\frac{\text{Volume of cone}}{\text{Volume of cylinder}} = \frac{\frac{1}{3}\pi r^2 h}{\pi R^2 H} = \frac{1}{3} \times \frac{r}{R} \times \frac{r}{R} \times \frac{h}{H}$$
$$= \frac{1}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{3}{4}$$
$$= \frac{1}{9} \quad 1:9$$

If height of a circular cone is decreased by 10% and its radius is increased by 10%, then what will be the change in its volume?

1. Decreases by 8.9%.

2. Decreases by 3.2%.

3. Increases by 8.9%.

4. Increases by 3.2%.

$$h = \frac{100}{90} \quad r = \frac{100}{110}$$

$$V = \frac{1}{3} \pi r^2 h$$

$$\frac{V_1}{V_2} = \frac{100}{110} \times \frac{100}{110} \times \frac{100}{90}$$

$$= \frac{1000}{1089}$$

$$\frac{V_1}{V_2} = \frac{100}{108.9} \Rightarrow 8.9$$

8.9 : ↑

$$\frac{121}{9},$$

The radii of two cylinders A and B are in the ratio of 5 : 6 and the heights are in the ratio of 7 : 4 respectively. The ratio of curved surface area of cylinder B to that of A is:

~~X~~ 1. $35 : 24$

~~✓~~ 2. $24 : 35$

~~X~~ 3. $49 : 35$

~~X~~ 4. $35 : 49$

$$\frac{r_A}{r_B} = \frac{5}{6} \quad \frac{h_A}{h_B} = \frac{7}{4}$$

$$\frac{CSA_B}{CSA_A} = \frac{2\pi r_B h_B}{2\pi r_A h_A}$$

$$= \frac{6}{5} \times \frac{4}{7} = \frac{24}{35}$$

$24 : 35$



$$CSA = 2\pi rh$$

The volume of a right circular cylinder is 3 times the volume of a right circular cone. The radius of the cone and the cylinder are 3 cm and 6 cm respectively. If the height of the cylinder is 1 cm, then what is the slant height of the cone?

1. $\sqrt{13}$ cm

2. 4 cm

3. 5 cm ✓

VOLUME

Cylinder

Cone

$$3$$

$$R = 6$$

$$H = 1$$

$$r = 3$$

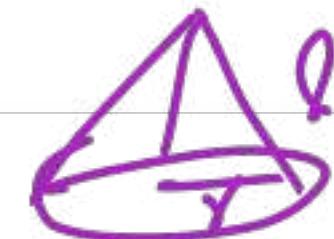
$$h =$$

$$\frac{V_{cy}}{V_{cn}} = \frac{3}{1}$$

$$\frac{\pi R^2 H}{\frac{1}{3} \pi r^2 h} = 3 \times \frac{1}{3}$$

$$R^2 H : r^2 h$$

$$h = \frac{R^2 H}{r^2} = \frac{36 \times 1}{9} = 4$$



$$\begin{aligned} l &= \sqrt{h^2 + r^2} \\ &= \sqrt{16 + 9} = \sqrt{25} \\ l &= 5 \end{aligned}$$

The diameter of a right circular cylinder is decreased to one third of its initial value. If the volume of the cylinder remains the same, then the height becomes how many times of the initial height?

1. 1

2. 9

3. 6

4. 3

$$\frac{V}{V_1} = \frac{3}{1} \times \frac{3}{1} \times \frac{h}{h_1}$$

$$V = \pi r^2 h$$

$$\cdot \underline{\underline{1/3}} \quad D \quad \frac{3}{1}$$

$$r = \frac{D}{2} \cdot \frac{3}{1}$$

$$\frac{3}{1} \times \frac{1}{2}$$

$$1 \times 9 = 9$$

$$\textcircled{1} \textcircled{9} = 9$$

A rectangular paper of width 7 cm is rolled along its width and a cylinder of radius 9 cm is formed. The volume of the cylinder is:

(Take $\pi = 22/7$)

~~1.~~ 1525 cm^3

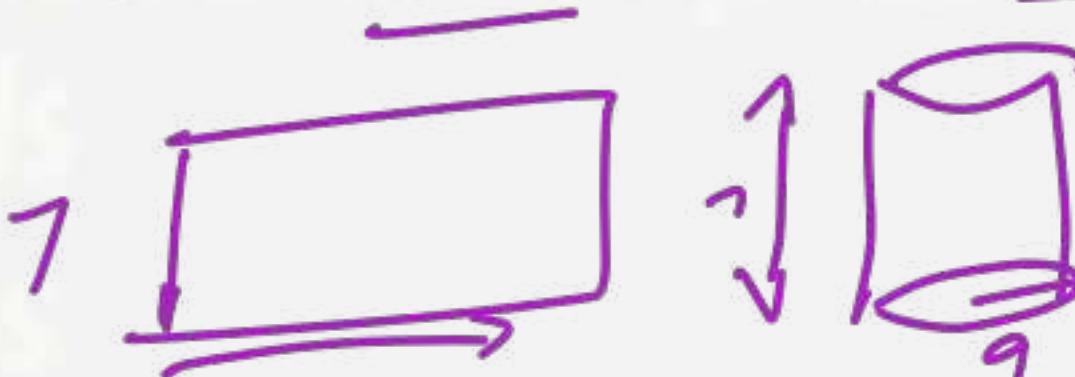
~~2.~~ 900 cm^3

~~3.~~ 1750 cm^3

~~4.~~ 891 cm^3

5. 1782 cm^3

$$\begin{aligned}V &= \pi r^2 h \\V &= \frac{22}{7} \times 8^2 \times 7 \\&= 1782 \text{ cm}^3\end{aligned}$$



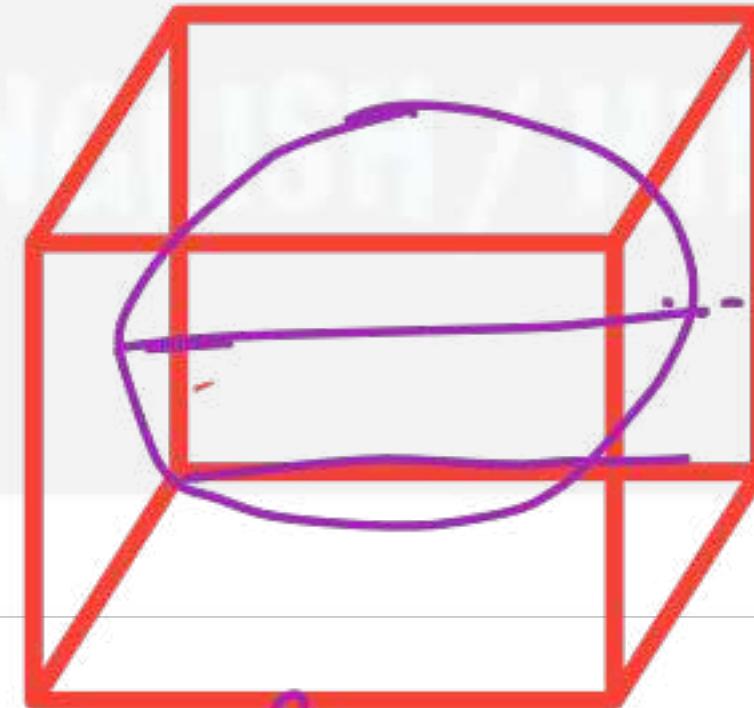
②

$$\begin{array}{r} 81 \\ 22 \\ \hline 162 \\ 162 \\ \hline 1782 \end{array}$$

A sphere is inscribed in a cube. What is the ratio of the volume of the cube to the volume of the sphere?

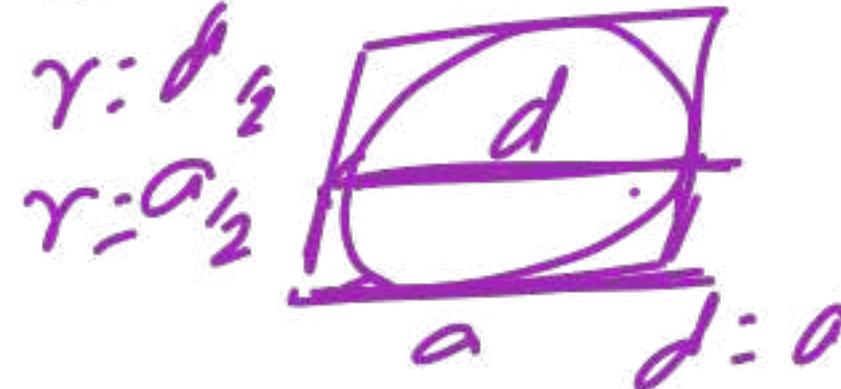
- 1. $6 : \pi$
- 2. $8 : \pi$
- 3. $11 : 2\pi$
- 4. $9 : 2\pi$

$$\frac{V_{\text{cube}}}{V_{\text{sphere}}} = \frac{a^3}{\frac{4}{3}\pi r^3}$$
$$= \frac{3a^3}{4 \times \pi \times \frac{a^2}{2^3}}$$
$$= \frac{3 \times 8}{4 \pi}$$
$$\frac{V_{\text{cube}}}{V_{\text{sp}}} = 6/\pi \quad 6:\pi$$



$$a = d$$

$$r = \frac{d}{2}$$



The height of a right circular cone is 24 cm and the radius of its base is 7 cm. What is the cost of painting the curved surface area of the cone at the rate of ₹6 per cm^2 ?

(Take $\pi = \frac{22}{7}$)

1. ₹3600

2. ₹3300 ✓

3. ₹880

4. ₹4200

$$\text{CSA} = \pi r l \quad : \text{cm}^2 \quad 6$$

$$\text{CSA} = \pi r l$$

$$= \frac{22}{7} \times 7 \times 25$$

$$\text{CSA} = 22 \times 25 \times \frac{6}{150}$$

$$\begin{array}{r} 22 \\ \times 15 \\ \hline 110 \\ 22 \\ \hline 3300 \end{array}$$

$$= 22 \times 150$$

$$= 3300$$



$$h = 24 \text{ cm}$$

$$r = 7 \text{ cm}$$

$$l = \sqrt{h^2 + r^2}$$

$$= \sqrt{576 + 49}$$

$$l = \sqrt{625} = 25$$

A room is in the shape of a cuboid, with dimensions $12\text{m} \times 10\text{m} \times 3\text{m}$. What is the cost of painting the four walls of the room at the rate of ₹50 per m^2 ?

- 1. ₹15000
- 2. ₹15600
- 3. ₹6600
- 4. ₹7500

l b h

$$2lh + 2bh$$

$$\text{LSA} = 2h(l+b)$$

$$= 2 \times 3 \times 22$$

$$\begin{aligned}\text{LSA} &= 132 \text{ m}^2 \times \underline{\underline{50}} \\ &= 6600\end{aligned}$$

$$\frac{132}{50} \underline{\underline{6600}}$$

The radius of a hemisphere is 14 cm. What is the cost of painting the outer curved surface of the hemisphere at the rate of ₹45 per cm^2 ?

(Take $\pi = \frac{22}{7}$)

- 1. ₹53160
- 2. ₹55440
- 3. ₹56820
- 4. ₹58280

$$\begin{aligned}CSA &= 2\pi r^2 \\CSA &= 2 \times \frac{22}{7} \times \overbrace{14 \times 14}^{\text{radius}} \times 45 \\&= 44 \times 90 \times 10 \\&= 44 \times 9 \times 100 \\&= 6 \text{ } \textcircled{0}\end{aligned}$$



0.1 percent of 1.728×10^6 spherical droplets of water, each of diameter 2 mm, coalesce to form a spherical bubble. What is the diameter (in cm) of the bubble?

X 1. 1.2

X 2. 1.6

X 3. 1.8

✓ 4. 2.4

$$1.728 \times 10^6 \times \frac{0.1}{1000} \cdot 10^3$$

$$1.728 \times \frac{1000000}{1000}$$

$$= 1728$$

$$\text{Count} \rightarrow 1.728 \times 10^6$$

$$2 \text{ mm} \rightarrow 000000$$

$$\gamma = 1 \text{ mm}$$



$$1 - 15^3$$

$$1 \text{ mm} = \frac{1}{10} \text{ cm}$$

$$1728 \times \frac{4\pi r^3}{3} = \frac{4}{3}\pi R^3$$

$$R = 12$$

$$R^3 = \frac{1728}{12^3}$$

$$D = 20 \text{ mm} = 2.0 \text{ cm}$$

$$10 \text{ mm} = 1 \text{ cm}$$

A rectangular park was redesigned and as a result of which its length increased by 50%. If the area of the park remained unchanged, then by how much percentage had the breadth been reduced?

1. 25

2. 50

3. 33.33

4. 40.33

$$A = l \times b$$

$$\therefore \frac{A}{A} = \frac{100}{150} \times \frac{x}{y}$$

$$x/y = \frac{150}{100} \downarrow -50$$

$$\% \text{ change} = \frac{50}{150} \times 100 \quad 33.33 \% \quad \checkmark$$



km	Hecto.m	Deko.m	m	decim	cm	mm
1 km	10 hm	100	1000	10000	100000	1000000
1	10 ⁻¹	10 ⁻²	100	1000	-	-

10 theta m: 1km

'O deo m = 'vedam

km m decm m decim cm mm

1 10 100

1m; 100cm

The sides of a triangular park are 200 m, 210 m and 290 m. The area of the park (in hectares) is:

~~X~~ 1. 2.4

~~X~~ 2. 1.8

✓ 3. 2.1 ✓

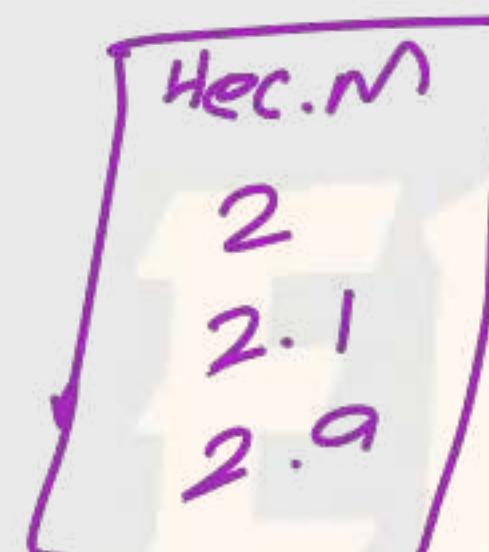
~~X~~ 4. 2.9

m

200

210

290



6m

Hec.m

Deco.m

m

!

'0

'00

$$2^2 + 2.1^2 = 2.9^2$$

$$4 + 4.41 = 8.01$$

$$8.01 = 8.01$$

$$A = \frac{1}{2} \times b \times h = \frac{1}{2} \times 2.1 \times 2.1$$

$$A = 2.1 \text{ ha}$$

$$S = \frac{7}{2} : 3.5$$

$$A = \sqrt{3.5 \times 1.5 \times 1.0 \times 0.6}$$

$$= \sqrt{\frac{35}{10} \times \frac{15}{10} \times \frac{10}{10} \times \frac{6}{10}}$$

$$A = \frac{1}{100} \sqrt{7 \times 5 \times 3 \times 5 \times 7 \times 2 \times 3 \times 2}$$

$$= \frac{7 \times 5 \times 2 \times 3}{100} = \frac{210}{100} : 2.1$$

What is the area (in m^2) of a triangular field whose sides measure 25 m, 39 m and 56 m?

- 1. 210
- 2. 240
- 3. 420
- 4. 480

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

$$s = \frac{a+b+c}{2} = 60$$

$$= \sqrt{60 \times 35 \times 21 \times 14}$$

$$= \sqrt{\frac{10 \times 6}{5 \times 2} \times \frac{3 \times 2}{3 \times 2} \times \frac{7 \times 5}{5 \times 2} \times \frac{7 \times 3 \times 4}{3 \times 2}}$$

$$= 5 \times 2 \times 3 \times 7 \times 2$$

$$= 420 \text{ m}^2$$

The diagonal of a square is equal to the side of an equilateral triangle. If the area of the square is $18\sqrt{3}$ sq. cm. What is the area (in cm^2) of the equilateral triangle?

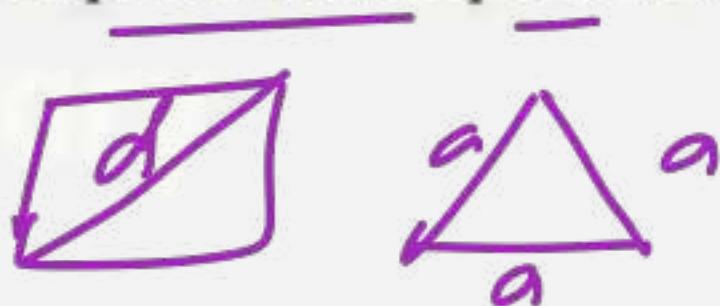
1. $54\sqrt{2}$

2. $27\sqrt{2}$

3. 54

4. $27\checkmark$

Area of square = $\frac{d^2}{2}$



$$d = a$$

$$\frac{d^2}{2} = 18\sqrt{3}$$

$$d^2 = 18\sqrt{3} \times 2$$

$$a^2 = 18\sqrt{3} \times 2$$

Area $\Delta = \frac{\sqrt{3}}{4} a^2$

$$= \frac{\sqrt{3}}{4} \times 18\sqrt{3} \times 2$$

$$= 3 \times 9$$

$$= 27 \text{ cm}^2$$

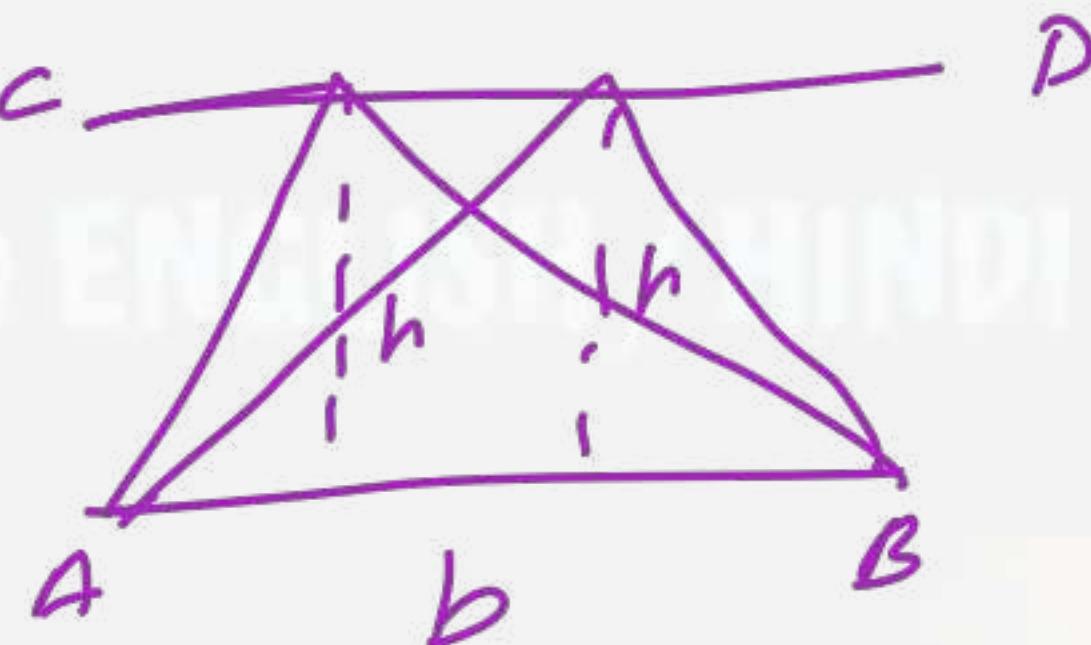
Let $\triangle ABC$ and $\triangle ABD$ be on the same base AB and between the same parallels AB and CD. Then the relation between areas of $\triangle ABC$ and $\triangle ABD$ will be:

~~X~~ 1. $\text{Area}(\triangle ABC) = \frac{1}{2} \text{Area}(\triangle ABD)$

~~✓~~ 2. $\text{Area}(\triangle ABC) = \text{Area}(\triangle ABD)$

~~X~~ 3. $\text{Area}(\triangle ABD) = \frac{1}{3} \text{Area}(\triangle ABC)$

~~X~~ 4. $\text{Area}(\triangle ABD) = \frac{1}{2} \text{Area}(\triangle ABC)$



$$\text{Area}_1 = \frac{1}{2} b \times h$$

$$\text{Area}_2 = \frac{1}{2} b \times h$$

The diameter of a wheel is 70 cm. It completes 600 revolutions in 1 minute. The speed, in km/h, of the vehicle is:
 (Take $\pi = \frac{22}{7}$)

1. 78.4

2. 79.2 ✓

3. 77.8

4. 78.2

	km	m	Decom	m	Decim	cm	mm
	1	10	100	1000	10,000	100,000	1,000,000

$$\text{Perimeter} = 2\pi r$$

$$r = \frac{70}{2}$$

$$= 2 \times \frac{22}{7} \times \frac{70}{2}$$

$$= \frac{22 \times 600 \times 60}{100000} \text{ km/hr}$$

$$1 \text{ min} = 600 \text{ rev}$$

$$60 \text{ min} = 600 \times 60 \text{ rev}$$

$$\text{Distance} = P \times N \text{ of Rev}$$

$$= \frac{22 \times 36}{10}$$

$$= \frac{792}{10} \text{ km/hr}$$

$$\frac{36}{72}$$

$$\frac{12}{792}$$

$$\text{km/hr}$$

A wire, in the form of a circle, encloses an area 3118.5 cm^2 . It is now bent to form a rectangle whose length and breadth are very nearly in the ratio $7 : 4$. The length of the rectangle, in cm, is:

(Take $\pi = \frac{22}{7}$)

1. 56

2. 49

3. 70

4. 63 ✓

$$\pi r^2 = 3118.5$$

$$r^2 = \frac{3118.5}{\frac{22}{7}} \times \frac{7}{22}$$

$$r = \sqrt{\frac{567 \times 7}{2 \times 2}} = \sqrt{\frac{81 \times 7 \times 7}{2 \times 2}}$$

$$r = \frac{9 \times 7}{2}$$



$$2\pi r = 2(l+b)$$

$$2 \times 22 \times x = 567$$

$$44x = 567$$

$$x = 13$$

$$22 \times \frac{9 \times 7}{2} = 7x + 4x$$

$$14 \times 9 = 11x$$

$$x = 9$$

$$7x = 7 \times 9 = 63$$

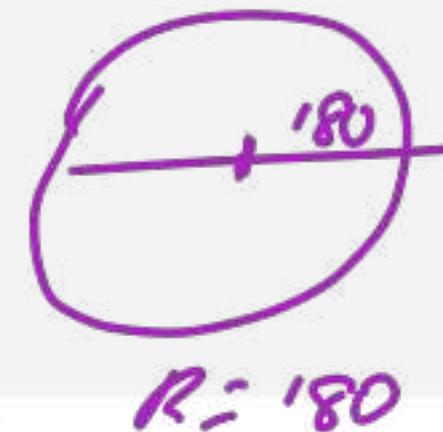
How many balls of radius 45 cm can be made by melting a bigger ball of diameter 360 cm?

✓ 1. 64

✗ 2. 128

✗ 3. 32

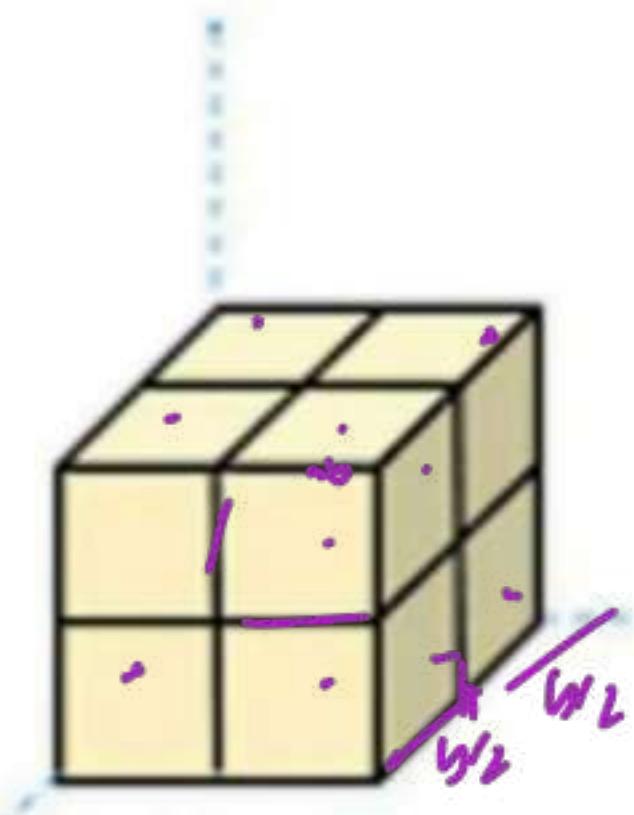
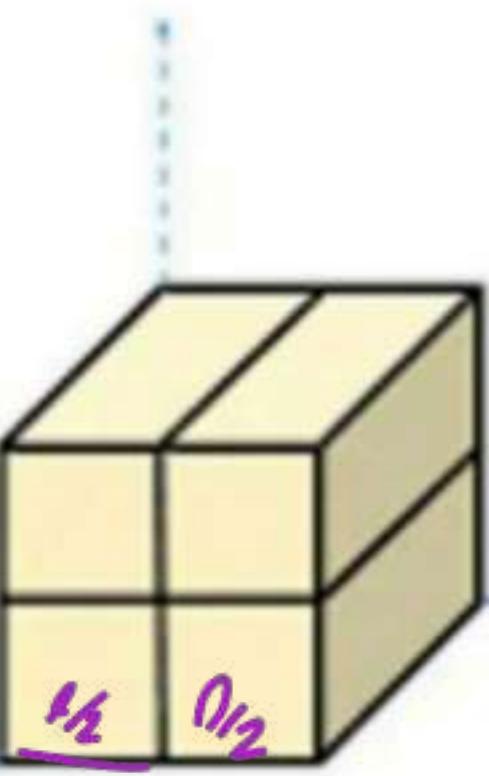
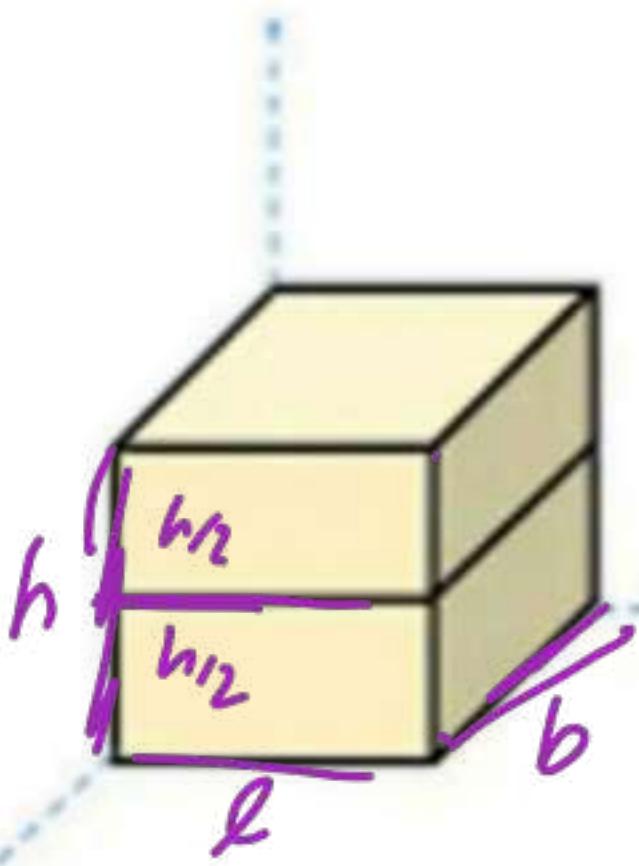
$$\pi \cdot \frac{4}{3} \pi r^3 = \cancel{\pi} \cdot \frac{4}{3} \pi R^3$$
$$\cancel{\pi} \cdot \frac{R^3}{r^3} = \frac{180 \times 180 \times 180}{45 \times 45 \times 45}$$



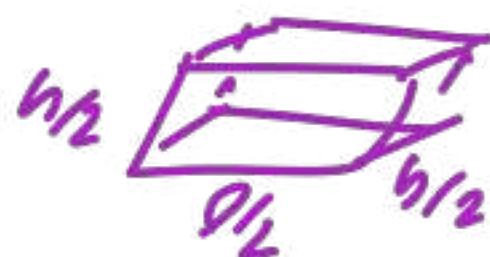
$$R = 180$$
$$r = 45$$

0 0 0 0
0 0 0 0

$$\boxed{k = 64}$$



$8 \times \text{TSA}$



A cuboid of size 100 cm \times 80 cm \times 60 cm cut into eight identical parts by three cuts. What is the total surface area (in square cm.) of all the eight parts?

- 1. 22500
- 2. 84100
- 3. 50750
- 4. 75200

$$l = 50 \text{ cm}, b = 40 \text{ cm}, h = 30 \text{ cm}$$

$$\begin{aligned} \text{TSA} &= 8 \times 2(lb + bh + hl) \\ &= 8 \times 2(2000 + 1200 + 1500) \\ &= 16 \times 47 \times 100 \end{aligned}$$

Q2

U6

How many cubes with a side 10 cm can be cut out of a cube having a side of 10 metre?

1. 10,000

2. 1,00,00,000

3. 1,00,000

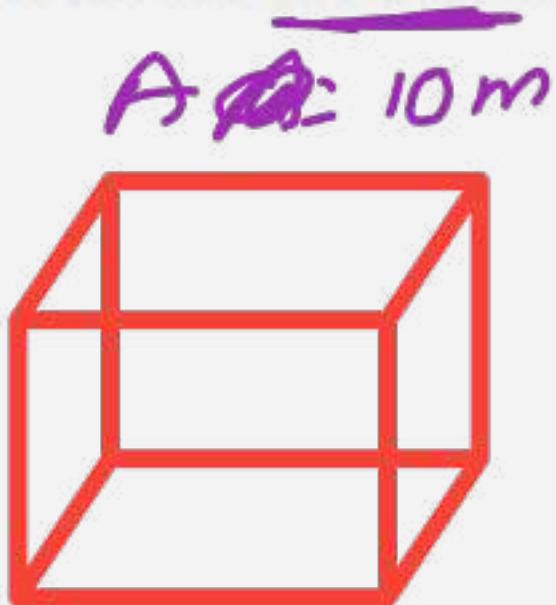
4. 10,00,000

$$A^3 = x \times a^3$$

$$x = \frac{A^3}{a^3}$$

$$x = \frac{1000 \times 1000 \times 1000}{10 \times 10 \times 10}$$

$$x = 10,00,000$$



$$a = 10 \text{ cm}$$

$$100 \text{ cm} = 1 \text{ m}$$

$$A = 10 \times 10 \text{ m}$$

$$A = 1000 \text{ m}$$

What is the volume of the sphere whose diameter is 42 cm?

(Take $\pi = \frac{22}{7}$)

$$V = \frac{4}{3}\pi r^3$$

$$\begin{aligned}D &= 42 \text{ cm} \\r &= 21 \text{ cm}\end{aligned}$$

X 1. 9702 cm^3

$$V = \frac{4}{3} \times \frac{22}{7} \times 21^2 \times 21$$

✓ 2. 38808 cm^3

$$\textcircled{B} \quad 8 \quad 8$$

X 3. 19404 cm^3

The length and the breadth of a rectangle are 15 cm and 12 cm respectively. If the rectangle is given one full rotation about its breadth as the axis, what is the volume (in cm^3) through which the rectangle moves?

1. 2160π

2. 1440π

3. 1800π

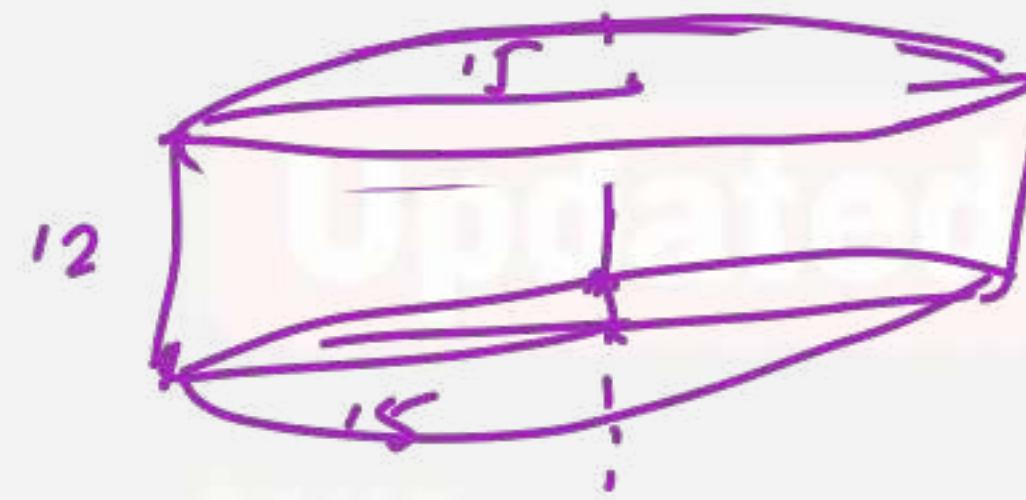
4. 2700π

$$V = \pi r^2 h$$

$$V = \pi \times 15^2 \times 12$$

$$= \pi \times 225 \times 12$$

$$= 2700 \pi$$



$$\begin{array}{r} 225 \\ \times 2 \\ \hline 450 \\ +225 \\ \hline 4500 \end{array}$$

A spherical ball of diameter 35 cm rolls 20 times. How much is the distance (in m) covered by it?

(Take $\pi = \frac{22}{7}$)

35 cm - 20 times

✓ 1. 22 ✓

✗ 2. 20

✗ 3. 35

✗ 4. 44

Perimeter: $2\pi r$

Distance = $\pi D \times 20$

$$= \frac{22}{7} \times 35 \times 20$$

$$= 110 \times 20$$

$$= 22 \times 100 \text{ cm}$$

$$= 22 \text{ m}$$



cm \tilde{m}
100 cm 1m

100 cm 1m

The length and the breadth of a cuboid are increased by 10% each, whereas the height is reduced by 10%. By how much did the volume change?

1. 10% decrease

2. 8.9% increase

3. 8.9% decrease

4. 10% increase

$$l \overset{100}{\cancel{l}} \quad b \overset{100}{\cancel{b}} \quad h \overset{100}{\cancel{h}}$$

$$v = l b h$$

$$\frac{v_1}{v_2} = \frac{100}{110} \times \frac{100}{110} \times \frac{100}{90} \cdot \frac{9}{089}$$

$$= \frac{1000}{1089}$$

$$= \frac{100}{1089} \cdot 8.9\%$$

$$\frac{8.9}{1000} \cdot 100$$

The volume of a sphere is $36\pi \text{ cm}^3$. What is the radius of the sphere?

- 1. 4 cm
- 2. 2 cm
- 3. 5 cm
- 4. 3 cm ✓

$$\begin{aligned}V &= \frac{4}{3}\pi r^3 = 36\pi \\r^3 &= \frac{36 \times 3}{4\pi} \\r^3 &= 27 = 3^3 \\r &= 3 \text{ cm}\end{aligned}$$

What are respectively the curved surface area and volume of a hemisphere of radius 21 cm?
(Take $\pi = \frac{22}{7}$)

✓ 1. 2772 cm^2 , 19404 cm^3

✗ 2. 4158 cm^2 , 19404 cm^3

✗ 3. 2772 cm^2 , 4158 cm^3

✗ 4. 2772 cm^2 , 9702 cm^3

$$CSA = 2\pi r^2$$

$$= 2 \times \frac{22}{7} \times \frac{3}{2} \times 21 \times 21$$

∴ ②

$$V = \frac{2}{3} \pi r^3$$

$$= \frac{2}{3} \times \frac{22}{7} \times \frac{3}{2} \times 21 \times 21 \times 21$$

③

④



The radius of a solid right circular cylinder is $66\frac{2}{3}\%$ of its height. If height is h centimetres then its total surface area (in cm^2) is:

✓ 1. $\frac{20}{9}\pi h^2$

✗ 2. $\frac{40}{9}\pi h^2$

✗ 3. $\frac{44}{9}\pi h^2$

✗ 4. $4\pi h^2$

$$\begin{aligned} \text{TSA} &= 2\pi r(h+r) & r &= 66\frac{2}{3}\% h \\ &= 2\pi \times \frac{2}{3}h \left(h + \frac{2}{3}h \right) & r &= \frac{200}{3 \times 100} h \\ &= \frac{4\pi h}{3} \left(\frac{3h+2h}{3} \right) & r &= \frac{2}{3}h \\ &= \frac{4\pi h}{3} \times \frac{5h}{3} = \frac{20\pi h^2}{9} \end{aligned}$$

1000 solid spherical balls each of radius 0.6 cm are melted and recast into a single spherical ball. What is the surface area (in cm^2) of ball so formed?

1. 144π

2. 128π

3. 124π

4. 108π

$$V = \frac{4}{3}\pi r^3$$

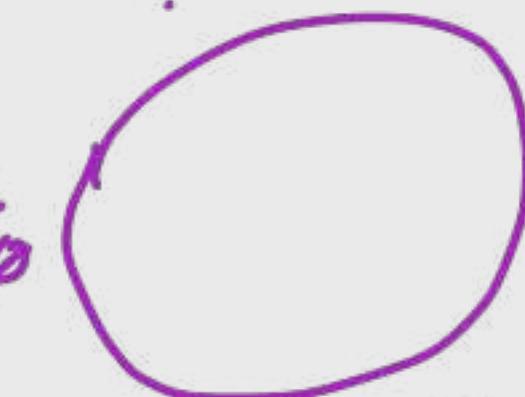
$$1000 \times \frac{4}{3}\pi r^3 = \frac{4}{3}\pi R^3$$

$$R^3 = 1000 \times \frac{6}{10} \times \frac{6}{10} \times \frac{6}{10}$$

$$R^3 = 6^3$$

$$R = 6 \text{ cm}$$

$$r = 0.6 \text{ cm} = \frac{6}{10}$$



$$\text{TSA} = 4\pi R^2$$

$$= 4\pi \times 6 \times 6$$

$$= 144\pi$$

$$\underline{\underline{144}}$$

The height of a cone is equal to its base radius and its volume is $72\pi \text{ cm}^3$. What is its curved surface area in cm^2 ?

~~X~~ 1. $72\sqrt{2}\pi$

✓ 2. $36\sqrt{2}\pi$ ✓

~~X~~ 3. $48\sqrt{2}\pi$

~~X~~ 4. $54\sqrt{2}\pi$

$$V = \frac{1}{3}\pi r^2 h = 72\pi$$

$$\frac{1}{3}\pi r^2 \times r^2 = 72\pi$$

$$r^3 = 72 \times 3$$

$$r = \sqrt[3]{2^3 \times 3^3}$$

$$r = 2 \times 3 = 6$$

$$h = 6$$

$$\therefore l = \sqrt{h^2 + r^2} = \sqrt{36^2 + 6^2} = \sqrt{361 \times 36} = \sqrt{72}$$

$$\begin{array}{c} 2 \\ | \\ 2 \\ | \\ 3 \end{array} \quad \begin{array}{c} 72 \\ | \\ 36 \\ | \\ 18 \\ | \\ 9 \\ | \\ 3 \end{array}$$

$$\pi r^2 = 72 \quad \pi : \cancel{72} \text{ } \cancel{(36)}$$



$$h = r$$

$$\text{CSA} : \pi r l$$

$$= \pi \times 6 \times \sqrt{72}$$

$$= \pi \times 6 \times \sqrt{36 \times 2}$$

$$= \pi \times 6 \times 6 \sqrt{2}$$

$$= 36 r_2 \pi$$

A copper wire of radius 0.5 mm and length $42\frac{2}{3}$ m is melted and converted into a sphere of radius R cm. What is the value of R?

~~X~~ 1. 3 $0.5 \text{ mm} = \frac{0.5}{10} \text{ cm}$ $L = 42\frac{2}{3} = \frac{128}{3} \text{ m}$ $\frac{\text{m}}{10} \text{ decim cm mm}$

✓ 2 ✓ $r = 0.05 \text{ cm}$ $R - \text{cm}$

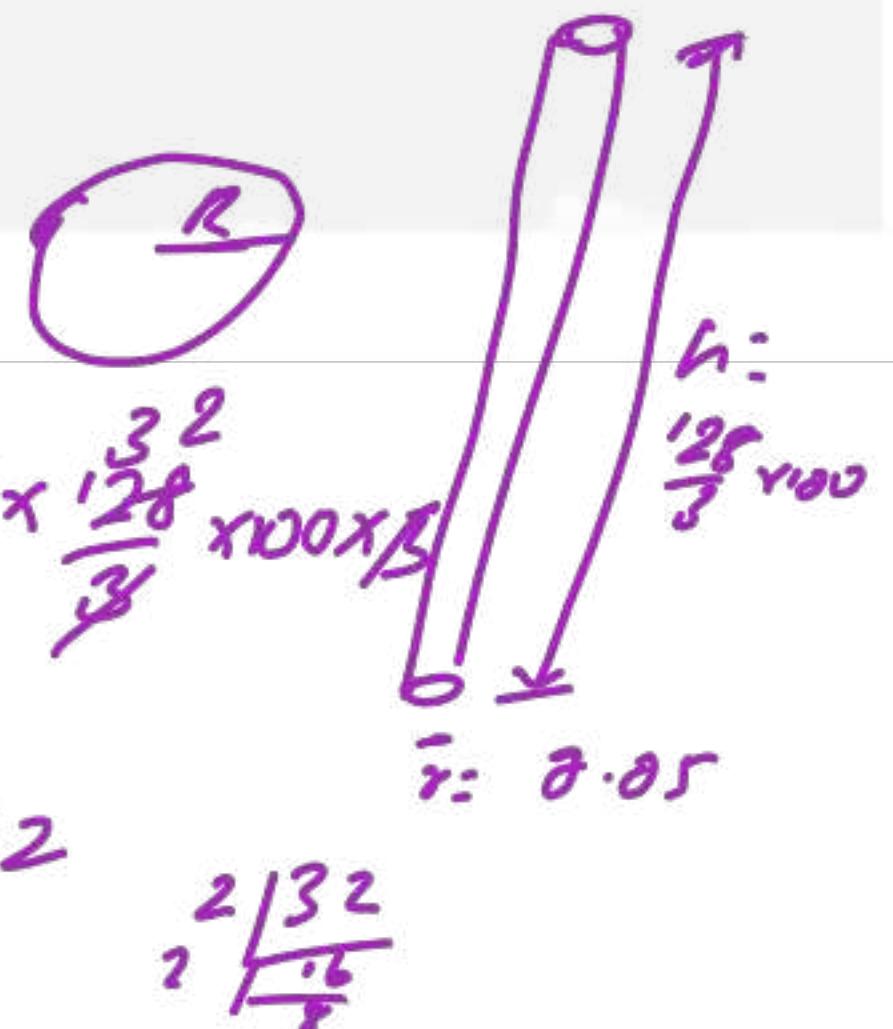
~~X~~ 3. 1.5 $= \frac{128}{3} \times 100 \text{ cm}$

~~X~~ 4. 1.8 $V_{\text{cyl}} = V_{\text{sph}}$

$$R^3 = \frac{\pi r^2 h}{100} \cancel{\pi r^2 h} = \frac{4}{3} \pi R^3$$

$$R^3 = \frac{\pi r^2 h}{100} \times 3 = \frac{0.05 \times 0.05 \times \frac{128}{3} \times 100 \times 3}{\cancel{\pi}}$$

$$R^3 = 0.05 \times 5 \times 32$$



The diameter of the base of a right circular cone is 10 cm and its height is 12 cm. What is the total surface area (in cm^2) of the cone?

- 1. 90π ✓
- 2. 70π
- 3. 84π
- 4. 65π

$$r: 5 \quad h: 12$$

$$\text{TSA} = \pi r r + \pi r^2$$

$$= \pi r (r + l)$$

$$= \pi \times 5(13+5)$$

$$= \pi \times 5 \times 18$$

$$= 90\pi$$

$$l = \sqrt{r^2 + h^2}$$

$$l = \sqrt{25 + 144}$$

$$l = \sqrt{169} = 13$$

The area of the base of a right circular cone is $\frac{1408}{7} \text{ cm}^2$ and its height is 6 cm. Taking $\pi = \frac{22}{7}$, the curved surface area of the cone is _____.

1. $\frac{7160}{7} \text{ cm}^2$

$$\pi r^2 = \frac{1408}{7}$$

2. $\frac{1670}{7} \text{ cm}^2$

$$2\pi r l = \frac{1670}{7}$$

3. $\frac{1760}{7} \text{ cm}^2$

$$r^2 - 64 = 8^2$$

4. $\frac{1067}{7} \text{ cm}^2$

$$l = \sqrt{64+36} = 10$$

$$h=6$$

$$CSA = \pi rl$$



$$CSA = \frac{22}{7} \times 8 \times 10$$

$$= \frac{760}{7} \text{ cm}^2$$

If the surface area of two spheres is in the ratio 49 : 25, then the ratio of their volumes will be:

✓ 1. $343 : 125$

✗ 2. $64 : 27$

✗ 3. $25 : 49$

✗ 4. $343 : 64$

$$\frac{4\pi r_1^2}{4\pi r_2^2} = \frac{49}{25}$$

$$\left(\frac{r_1}{r_2}\right)^2 = \left(\frac{7}{5}\right)^2$$

$$\frac{r_1}{r_2} = \frac{7}{5}$$

$$\frac{r_1^3}{r_2^3} = \frac{343}{125}$$

$$4\pi r_1^2$$

$$\frac{V_1}{V_2} = \frac{\frac{4}{3}\pi r_1^3}{\frac{4}{3}\pi r_2^3}$$

If the area of the base of a cone is increased then it becomes 1.96 times of original area. If the volume is increased by:

1. 40%

2. 96% 

3. 141%

4. 100%

$$\frac{V_1}{V_2} = \frac{1}{1.96}$$

$$= \frac{100}{196} > 96\%$$

$$\frac{1}{r_1^2} : \frac{1.96}{r_2^2}$$


$$V = \frac{1}{3} \pi r_2^2 h$$

The base area of a cuboid is 34 sq cm. and height is 3.5 cm. What is the volume of cuboid?

- 1. 125 cm^3
- 2. 97 cm^3
- 3. 119 cm^3
- 4. 108 cm^3

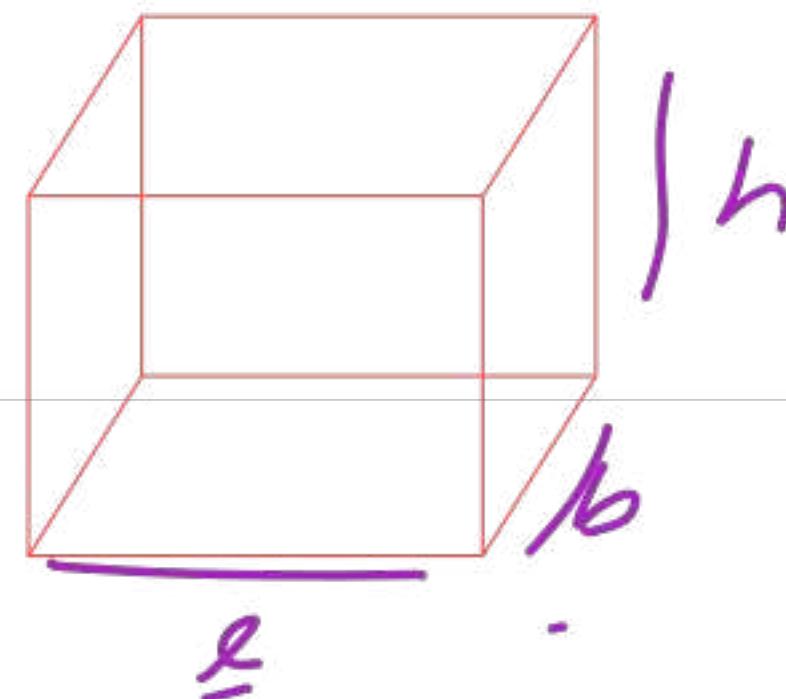
$l \times b$

$$V = l b h$$

$$\begin{aligned} V &= 34 \times 3.5 \\ &= 119 \text{ cm}^3 \end{aligned}$$

\overline{h}
 l, b, h

$$\begin{array}{r} 34 \\ 35 \\ \hline 170 \\ 102 \\ \hline 119.0 \end{array}$$



Find the total surface area of a cube whose volume is 64 cm^3 .

1. 84 cm^2

Side - a

2. 64 cm^2

TSA = $6a^2$

3. 16 cm^2

$V = a^3 = 6u$
 $a^3 = u^3$

4. 96 cm^2 ✓

$a = u$

TSA = 6×16
= 96

Height of a right circular cone is 28 cm. If diameter of its base is 42 cm, then what will be the curved surface area of the cone?

- 1. 4620 cm^2
- 2. 170 cm^2
- 3. 2310 cm^2
- 4. 1540 cm^2

$$D = 42 \text{ cm}$$

$$r = 21 \text{ cm}$$

$$h = 28 \text{ cm}$$

$$l = \sqrt{r^2 + h^2}$$

$$l = \sqrt{441 + 784}$$

$$= \sqrt{1225} = \sqrt{35^2}$$

$$\begin{aligned}CSA &= \pi r l \\&= \frac{22}{7} \times 21 \times 35\end{aligned}$$

$$\begin{aligned}&= 66 \times 35 \\&= 2310 \text{ cm}^2\end{aligned}$$

$$l = 35$$

$$\begin{array}{r} 66 \\ \times 35 \\ \hline 330 \\ 198 \\ \hline 2310 \end{array}$$

The volume of a right circular cone is equal to the volume of that right circular cylinder whose height is 48 cm and diameter of its base is 20 cm. If the height of the cone is 16 cm, then what will be the diameter of its base?

1. 45 cm

2. 130 cm

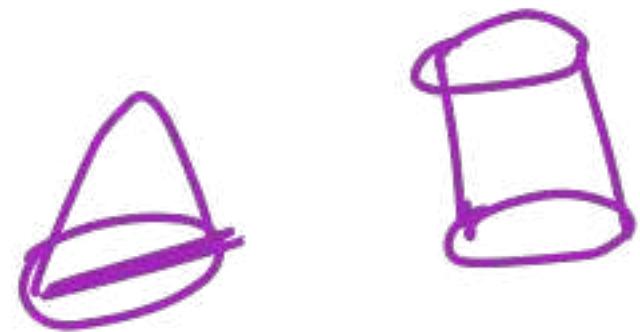
3. 25 cm

4. 60 cm ✓

$$H = 48 \text{ cm}$$

$$D = 20, R = 10 \text{ cm}$$

$$h = 16 \text{ cm} \quad r = ? \quad d = ?$$



$$V_{co} = V_{cy} \text{ (cans)}$$

$$\frac{1}{3}\pi r^2 h = \pi R^2 H$$

$$r^2 = \frac{10 \times 10 \times 48 \times 3}{16}$$

$$r = 10 \times 3 = 30$$

$$d = 30 \times 2 = 60 \text{ cm}$$

The volume of a frustum of a cone with radii 8 cm and 10 cm and height is 21 cm is: (Take: $\pi = \frac{22}{7}$)

✓ 1. 5368 cm³

✗ 2. 4328 cm³

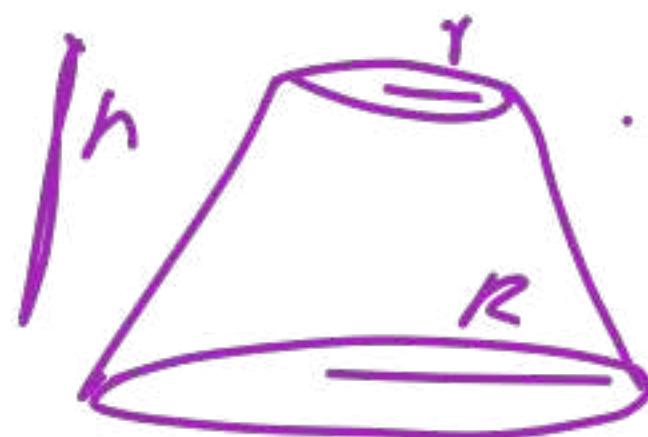
✗ 3. 6112 cm³

✗ 4. 4816 cm³

$R = 10 \text{ cm}$ $r = 8 \text{ cm}$

$h = 21 \text{ cm}$

$V = \frac{1}{3} \pi (R^2 r + Rr^2) \cdot h$



$$V = \frac{1}{3} \pi \frac{22}{7} \times (10^2 + 8^2 + 10 \times 8) \times 21$$

$$= 22 \times (100 + 64 + 80)$$

$$= 22 \times 244 \quad (B)$$

$$= 5368 \text{ cm}^3$$

$$\begin{array}{r} 244 \\ \times 22 \\ \hline 488 \\ 488 \\ \hline 5368 \end{array}$$

A reservoir is in the shape of a frustum of a right circular cone. The radii of its circular ends are 4 m and 8 m and its depth is 7 m. How many kilolitre of water (correct up to one decimal place) can it hold? $\bar{r} \quad R$

(Take $\pi = \frac{22}{7}$)

$$V = \frac{1}{3} \pi (R^2 + r^2 + Rr) h \text{ m}^3$$

✓ 1. 821.3

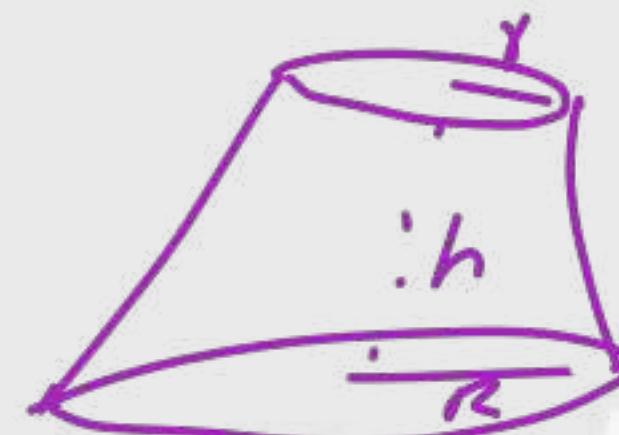
✗ 2. 815.7

✗ 3. 792.3

✗ 4. 775.7

$$= \frac{1}{3} \times \frac{22}{7} \times (64 + 16 + 32) \times 7$$

$$= \frac{1}{3} \times 22 \times 112 \quad 37.33$$



$$1L = 1000 \text{ cm}^3$$

$$1000 \text{ cm}^3 = 1000 \times \frac{1}{1000000} \times \frac{1}{100} \times \frac{1}{100} \text{ m}^3$$

$$100 \text{ cm} = 1 \text{ m}$$

$$1 \text{ cm} = \frac{1}{100} \text{ m}$$

$$1 \text{ cm}^3 = \frac{1}{100} \times \frac{1}{100} \times \frac{1}{100} \text{ m}^3$$

$$1L = \frac{1}{1000} \text{ m}^3$$

$$1kL = \frac{1}{1000} \times 1000 \text{ m}^3$$

3

The capacity of a cylindrical tank is 246.4 litres. If the height is 4 metres, what is the diameter of the base? (Use $\pi \frac{22}{7}$)

- 1. 0.14 metres
- 2. 2.8 metres
- 3. 0.28 metres
- 4. 1.4 metres

$$\frac{\pi r^2 h}{7} = \frac{246.4}{1000}$$
$$\frac{22}{7} \times 4 \times r^2 = 0.2464$$
$$r^2 = \frac{0.2464 \times 7}{22 \times 4}$$
$$r^2 = 0.0343$$
$$r = \sqrt{0.0343}$$
$$r = 0.185$$

$$\therefore r^2 = \frac{246.4}{1000} \times 4$$
$$r^2 = 0.2464$$
$$r = \sqrt{0.2464}$$
$$r = 0.185$$

$$\therefore r^2 = \frac{16600}{10000}$$
$$r^2 = 1.66$$
$$r = \sqrt{1.66}$$
$$r = 1.29$$

A wire encloses an area of 616 cm^2 when it is bent in the form of a circle. If the wire is bent in the form of a square,

then its area (in cm^2) is very nearly equal to: (Take $\pi = \frac{22}{7}$)

1. 400

2. 576

3. 441

4. 484 ✓

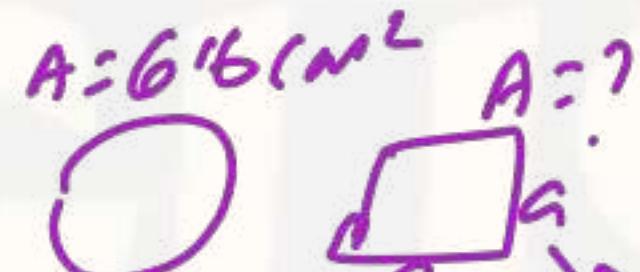
$$\text{Area}_C = \pi r^2 = 616$$

$$r^2 = \frac{616 \times 7}{22} = 14$$

$$r = \sqrt{14 \times 7} = \sqrt{4 \times 7 \times 7} = 2 \times 7 = 14$$

$$a = \frac{22}{7} \times \frac{14}{2} = 22$$

$$A_s = a^2 = 22^2 = 484$$



$$A = \pi r^2$$
$$2\pi r = 60$$
$$a = \frac{2\pi r}{4} = \frac{\pi r}{2}$$

The areas of two squares are 16:9. The ratio of their perimeter is:

- 1. 9:16
- 2. 12:16
- 3. 9:12
- 4. 16:12 ✓

$$\frac{A_1}{A_2} = \frac{16}{9} = \frac{a_1^2}{a_2^2}$$

$A = a^2$
 $P = 4a$

$$\frac{a_1}{a_2} = \sqrt{\frac{16}{9}} = \frac{4}{3}$$

$$\frac{P_1}{P_2} = \frac{4a_1}{4a_2} = \frac{4 \times 4}{4 \times 3} = \frac{16}{12}$$

$\textcircled{4/3}$

The Area of a rectangle is 27 m^2 and its length is 3 times of its breadth. The perimeter of the rectangle is:

- 1. 28cm
- 2. 12cm
- 3. 24cm
- 4. 42cm

$$\begin{array}{cc} l & b \\ 3x & x \end{array}$$

$$l \times b = 27$$

$$3x \times x = 27^9$$

$$x^2 = 9$$

$$x = 3$$

$$P = 2(l+b)$$

$$= 2(3x+x)$$

$$= 2 \times 4x$$

$$= 2 \times 4 \times 3 = 24 \text{ m}$$

A wheel makes 4000 revolution in covering a distance of 60km. The radius of the wheel is:

- 1. 4.68m
- 2. 2.39 m ✓
- 3. 8m
- 4. 8.25m

$$\begin{array}{ccc} \text{Rev} & & \text{Dist} \\ 4000 & & 60 \times 1000 \text{ m} \\ u \Rightarrow 60 \text{ m} & & \\ l \Rightarrow 15 \text{ m} & & \end{array}$$

$$2\pi r = 15$$
$$r = \frac{15}{2\pi} = \frac{15}{2} \times \frac{7}{22} = \frac{105}{44} \stackrel{110}{=} 2.39$$

A circle with radius 8 cm which has the area equal to the area of triangle with base 8 cm. Then the length of the corresponding altitude of triangle is _____.

- 1. 38π cm
- 2. 18π cm
- 3. 8π cm
- 4. 16π cm ✓



$$\pi r^2 = \frac{1}{2} \times b \times h$$

$$\pi \times 8 \times 8 = \frac{1}{2} \times 8 \times h$$

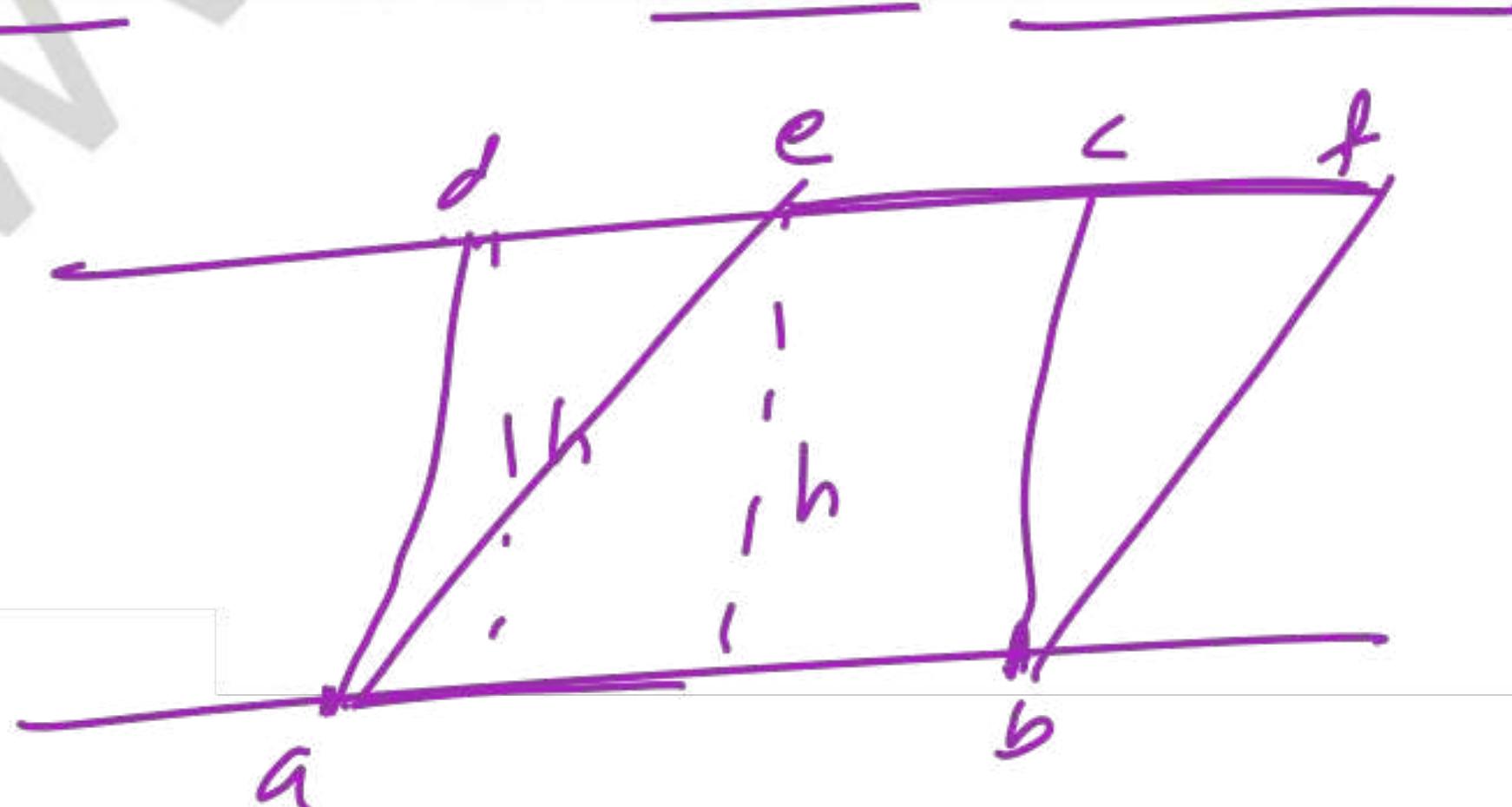
$$h = 16\pi$$

Two parallelogram stand on equal bases and between the same parallel. The ratio of their areas is:

- 1. 1 : 3
- 2. 2 : 1
- 3. 1 : 1
- 4. 1 : 2

$$A : b \times h : b \times h \\ 1 : 1$$

abcd abef



The diagonal of a square A is $(a + b)$. The diagonal of a square whose area is twice the area of square A is

$\times 1.$ $2(a + b)$

$\times 2.$ $\sqrt{2}(a - b)$

$\checkmark 3.$ $\sqrt{2}(a + b)$

$\times 4.$ $2(a + b)^2$

$$A_1 = \frac{d^2}{2}$$

$$A = \frac{(a+b)^2}{2}$$

$$A_2 = 2 \times \frac{(a+b)^2}{2}$$

$$\frac{d_2^2}{2} = (a+b)^2 \Rightarrow d_2^2 = \sqrt{2(a+b)^2} \\ = \sqrt{2(a+b)} r_2$$



$$A$$
$$d = a+b$$



$$2A$$
$$d_2$$

$$A_2 = \frac{d_2^2}{2}$$

The circumference of a given circle is 176 cm. What is the approximate diagonal of a square whose side is half of the radius of a given circle?

1. 15 cm

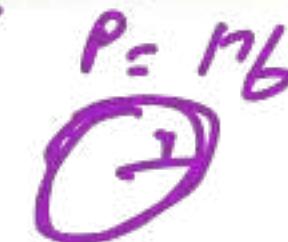
2. 24 cm

3. 12 cm

4. 20 cm

$$2\pi r = 176$$
$$\pi \approx \frac{22}{7}$$
$$r = \frac{176}{2} \times \frac{7}{22} = 28$$

$$a = \frac{28}{2} = 14$$



$$a = 14$$

$$d = a\sqrt{2}$$

$$\sqrt{2} = 1.414$$

$$d = 1.414 \times 14$$

$$\frac{14}{14}$$

$$\frac{14}{14} \times 1.414 \approx 20$$

If the length of a rectangle is increased in the ratio $4 : 5$ and its breadth is decreased in the ratio $3 : 2$, then its area will be decreased in the ratio _____

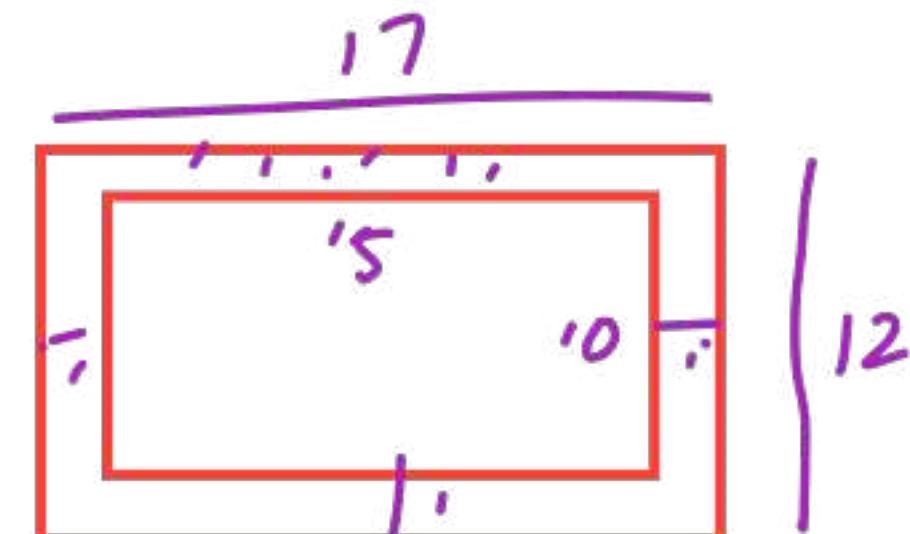
- 1. $2 : 1$
- 2. $4 : 3$
- 3. $10 : 3$
- 4. $6 : 5$

$$A = l b$$
$$\frac{x}{y} = \frac{4}{5} \times \frac{3}{2} = \frac{6}{5} \quad 6 : 5$$

The length and breadth of a painting is 15 cm and 10 cm respectively. A 1 cm wide boarder is made around the painting. What is the area of boarder?

- 1. 45 sq cm.
- 2. 60 sq cm.
- 3. 54 sq cm.
- 4. 16 sq cm.

$$\begin{aligned}l \times b &= 17 \times 12 - 15 \times 10 \\&= 204 - 150 \\&= 54 \text{ cm}^2\end{aligned}$$



What is the perpendicular distance (in cm) between the parallel sides of a trapezium whose area is 108 sq cm. and the lengths of the parallel sides are 9 cm and 36 cm?

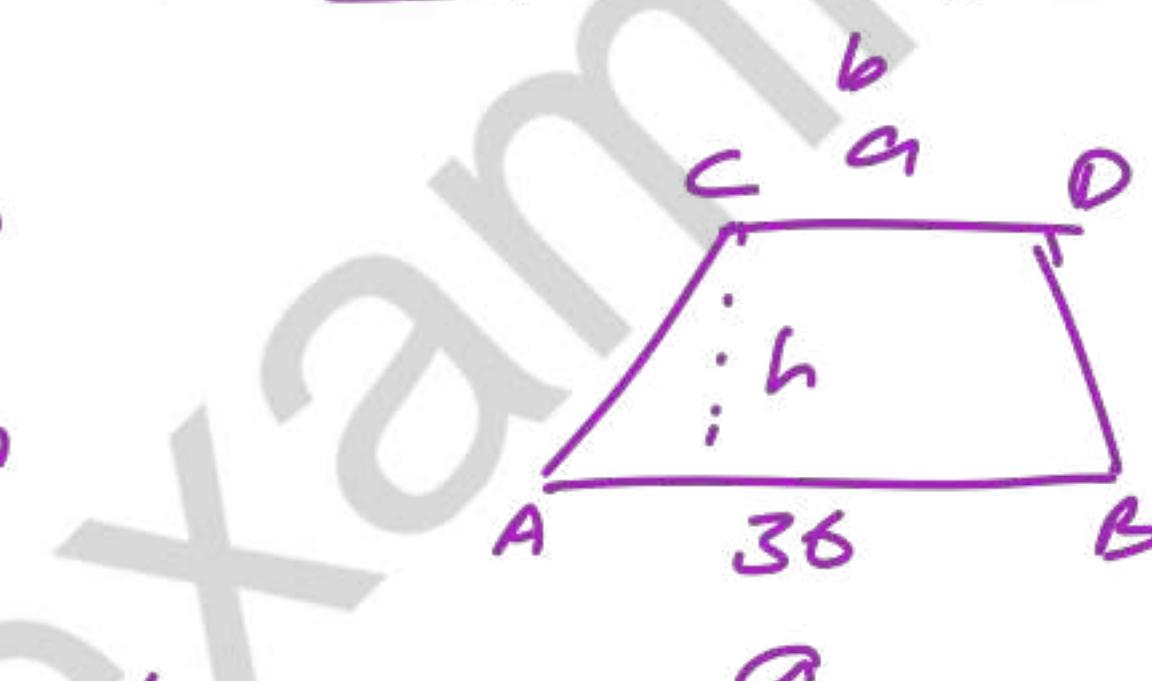
- 1. 7 cm
- 2. 3.6 cm
- 3. 6 cm
- 4. 4.8 cm

$$A = \frac{1}{2} (a+b) \times h$$

$$108 = \frac{1}{2} (36+9) \times h$$

$$h = \frac{108 \times 2}{45} = \frac{216}{45}$$

$$\begin{array}{r} 216 \\ \times 45 \\ \hline 180 \\ 840 \\ \hline 972 \end{array}$$



Area of a rhombus is 175 cm². Length of one diagonal is 25 cm. What is the length of other diagonal?

- 1. 12 cm
- 2. 14 cm
- 3. 10 cm
- 4. 15 cm

$$A = \frac{d_1 \times d_2}{2}$$

$$175 = \frac{25 \times d_2}{2}$$

$$d_2 = 10 \text{ cm}$$

A rectangular field has length of 1200 m and breadth of 500 m. A road has to be made along its diagonal at the rate of ₹ 25 per m. What is the cost of making road?

~~X~~ 1. ₹ 25600

~~✓~~ 2. ₹ 32500 ✓

~~X~~ 3. ₹ 35000

~~X~~ 4. ₹ 28400

$$d = \sqrt{l^2 + b^2}$$

$$= \sqrt{1200^2 + 500^2}$$

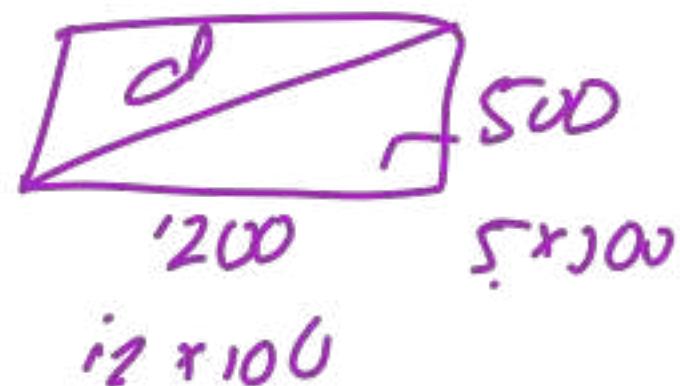
$$= \sqrt{(100)^2 (12^2 + 5^2)}$$

$$= 100 \sqrt{144 + 25} = 100 \sqrt{169} = 100 \times 13 = 1300 \text{ m}$$

$$1 \text{ m} \Rightarrow 25$$

$$1300 \text{ m} \Rightarrow 25 \times 1300$$

$$= 32500$$



$$\begin{array}{r} 250 \\ \times 1300 \\ \hline 32500 \end{array}$$

If the diameter of a circle increases by 15%, then what will be the percentage increase in its area?

X 1. 35.75%

X 2. 30.3%

X 3. 25%

✓ 4. 32.25%

$$A = \pi r^2$$

$$\frac{A}{y} = \frac{\pi}{\pi} \times \frac{20}{23} \times \frac{20}{23}$$

$$\frac{D}{2} \uparrow$$

$$r \uparrow$$

$$\gamma = 15\% \uparrow$$

$$15\% \uparrow$$

$$r = \frac{100}{115} = \frac{20}{23}$$

$$32.25$$

$$A \Rightarrow \frac{A}{y} = \frac{400}{529} \downarrow 129 \uparrow$$

$$\gamma \uparrow = \frac{129}{400} \times 100$$

$$32.25\%$$

The perimeter of a square and a circle are same. If the area of the circle is 1386 cm^2 , then what will be the area of the square?

✓ 1. 1089 cm^2

✗ 2. 841 cm^2

✗ 3. 1024 cm^2

✗ 4. 1225 cm^2

$$a^2 = ?$$

$$\pi r^2 = 1386$$

$$r^2 = \frac{1386}{\pi} \times \frac{7}{22}$$

$$r^2 = \sqrt{63 \times 7}$$

$$r = \sqrt{9 \times 7 \times 7} = 3 \times 7 = 21 \quad a = 33 \text{ cm}$$



$$4a = 2\pi r$$

$$a = \frac{2\pi r}{4} = \frac{\pi r}{2}$$

$$A = a^2$$

$$= 33 \times 33 \quad 9$$

If the side of a square increases by 20%, then what will be percent increase in its perimeter?

- 1. 44%
- 2. 20% ✓
- 3. 80%
- 4. 40%

$$P = 4a$$
$$\frac{\Delta P}{P} = \frac{1}{4} \times \frac{100}{120} \rightarrow 20\%$$

$$\frac{20}{100} \times 100$$

The sides of a triangle are in the ratio $5 : 2 : 1$. If the perimeter of the triangle is 88 cm, then what will be the length of the largest side?

- 1. 38 cm
- 2. 40 cm
- 3. 55 cm ✓
- 4. 44 cm

$a : b : c$

$$a = 5x, \quad b = 2x, \quad c = x$$



$$P = a + b + c$$

$$8x = 88$$

$$x = 11$$

$$5x = 55$$