

You are given an  $m \times n$  pixelated image, where each pixel is  $1\text{mm} \times 1\text{mm}$ . Some pixels are black and others are white. White pixels should be considered as empty. If two black pixels are adjacent (where each pixel  $p$  has four adjacent pixels, i.e. above, below, to the right, and to the left, then we say those two pixels are part of the same **object**. Being part of the same object is transitive: if black pixels  $a$  and  $b$  are part of the same object and  $b$  and  $c$  are, then  $a$  and  $c$  are as well.

Describe an algorithm which, given the description of a pixelated image stating which pixels are black and white (you could imagine the input is an array  $A[1..m][1..n]$  where  $A[i][j]$  is the color of pixel  $(i, j)$ ), outputs the number of objects, *and* for each object the area of the smallest axis-aligned rectangle that encloses it.

pixelated image containing four objects, whose bounding boxes (drawn in red) have areas 6, 4, 15, and 1.

