SMAI-2020-Homework

September 2020

1 Objective Question [1 mark]

What are the objectives of Principal Components Analysis (PCA)? Select all that are correct.

- 1. Maximize the variance along the new output dimensions
- 2. Minimize the variance along the new output dimensions
- 3. Maximizing the orthogonal distance between the data and the new output dimension $\frac{1}{2}$
- 4. Minimize the orthogonal distance between the data and the new output dimension

2 Subjective Question [2 markss]

Prove that there exist a relationship between PCA and SVD for a given data matrix X. Explain in one line how will you use the the SVD of the data matrix X to perform dimensionality reduction?

3 Programming Question [3 marks]

Consider the problem of Eigenfaces. Given a dataset of face images, your task is to find a lower dimensional representation by applying PCA. Write a program to output the following:

- 1. How many principal components are required such that 95% of the variance in the data is preserved?
- 2. Show the reconstruction of the first 10 face images using only 100 principal components.
- 3. Show the above two results for a noisy face dataset.