

## • **Combine of zero forcing and mmse**

```
import numpy as np

import matplotlib.pyplot as plt

# Function to generate additive white Gaussian noise (AWGN)

def awgn_noise(signal, noise_power):

    noise = np.random.randn(*signal.shape) * np.sqrt(noise_power)

    return noise

# Function to simulate Massive MIMO system with Zero Forcing (ZF) detection

def simulate_mimo_system_zf(H, num_users, snr_values_db, num_trials=10000):

    # Generate random symbol vector x_true

    num_symbols = num_users

    x_true = np.random.randint(0, 2, num_symbols) * 2 - 1 # BPSK symbols {-1, 1}

    ber_values_zf = []

    for snr_db_val in snr_values_db:

        # Convert SNR from dB to linear scale

        snr_lin = 10**(snr_db_val / 10)

        noise_power = 1 / snr_lin

        num_errors = 0

        for _ in range(num_trials):

            # Generate received signal with AWGN

            y = np.dot(H, x_true) + awgn_noise(np.dot(H, x_true), noise_power)
```

```
# Zero Forcing (ZF) detection
```

```
H_pinv = np.linalg.pinv(H)
```

```
x_demod_zf = np.sign(np.dot(H_pinv, y.real)) # Demodulate symbols
```

```
# Calculate Bit Error Rate (BER) for ZF
```

```
num_errors += np.sum(x_demod_zf != x_true)
```

```
ber = num_errors / (num_trials * num_symbols)
```

```
ber_values_zf.append(ber)
```

```
return ber_values_zf
```

```
# Function to simulate Massive MIMO system with MMSE detection
```

```
def simulate_mimo_system_mmse(H, num_users, snr_values_db, num_trials=10000):
```

```
    # Generate random symbol vector x_true
```

```
    num_symbols = num_users
```

```
    x_true = np.random.randint(0, 2, num_symbols) * 2 - 1 # BPSK symbols {-1, 1}
```

```
    ber_values_mmse = []
```

```
    for snr_db_val in snr_values_db:
```

```
        # Convert SNR from dB to linear scale
```

```
        snr_lin = 10**(snr_db_val / 10)
```

```
        noise_power = 1 / snr_lin
```

```
        num_errors = 0
```

```
        for _ in range(num_trials):
```

```
            # Generate received signal with AWGN
```

```
            y = np.dot(H, x_true) + awgn_noise(np.dot(H, x_true), noise_power)
```

```

# MMSE detection

part1_w = np.conj(H.T) @ H

part2_W = np.linalg.inv(part1_w + noise_power * np.eye(num_users))

W_mmse = part2_W @ np.conj(H.T)

x_demod_mmse = np.sign(W_mmse @ y.real) # Demodulate symbols


# Calculate Bit Error Rate (BER) for MMSE

num_errors += np.sum(x_demod_mmse != x_true)


ber = num_errors / (num_trials * num_symbols)

ber_values_mmse.append(ber)


return ber_values_mmse


# Parameters

num_antennas = 8

num_users = 4 # Change this to the desired number of users

modulation_order = 2 # BPSK modulation

num_trials = 10000


# SNR in dB (from 2 dB to 20 dB)

snr_values_db = np.arange(2, 21, 2)


# Generate random channel matrix H

H = np.random.randn(num_antennas, num_users) + 1j * np.random.randn(num_antennas, num_users)

H = H / np.sqrt(2) # Scale every element by 1/sqrt(2)


# Simulate Massive MIMO system with Zero Forcing (ZF) detection for BPSK

ber_values_zf = simulate_mimo_system_zf(H, num_users, snr_values_db, num_trials)


# Simulate Massive MIMO system with MMSE detection for BPSK

```

```
ber_values_mmse = simulate_mimo_system_mmse(H, num_users, snr_values_db, num_trials)
```

```
# Plot SNR vs BER for both ZF and MMSE
```

```
plt.figure(figsize=(10, 6))
```

```
plt.semilogy(snr_values_db, ber_values_zf, marker='o', linestyle='-', label='ZF', color='blue')
```

```
plt.semilogy(snr_values_db, ber_values_mmse, marker='s', linestyle='--', label='MMSE', color='red')
```

```
plt.title('SNR vs Bit Error Rate (BER) for Massive MIMO with ZF and MMSE detection (BPSK)')
```

```
plt.xlabel('SNR (dB)')
```

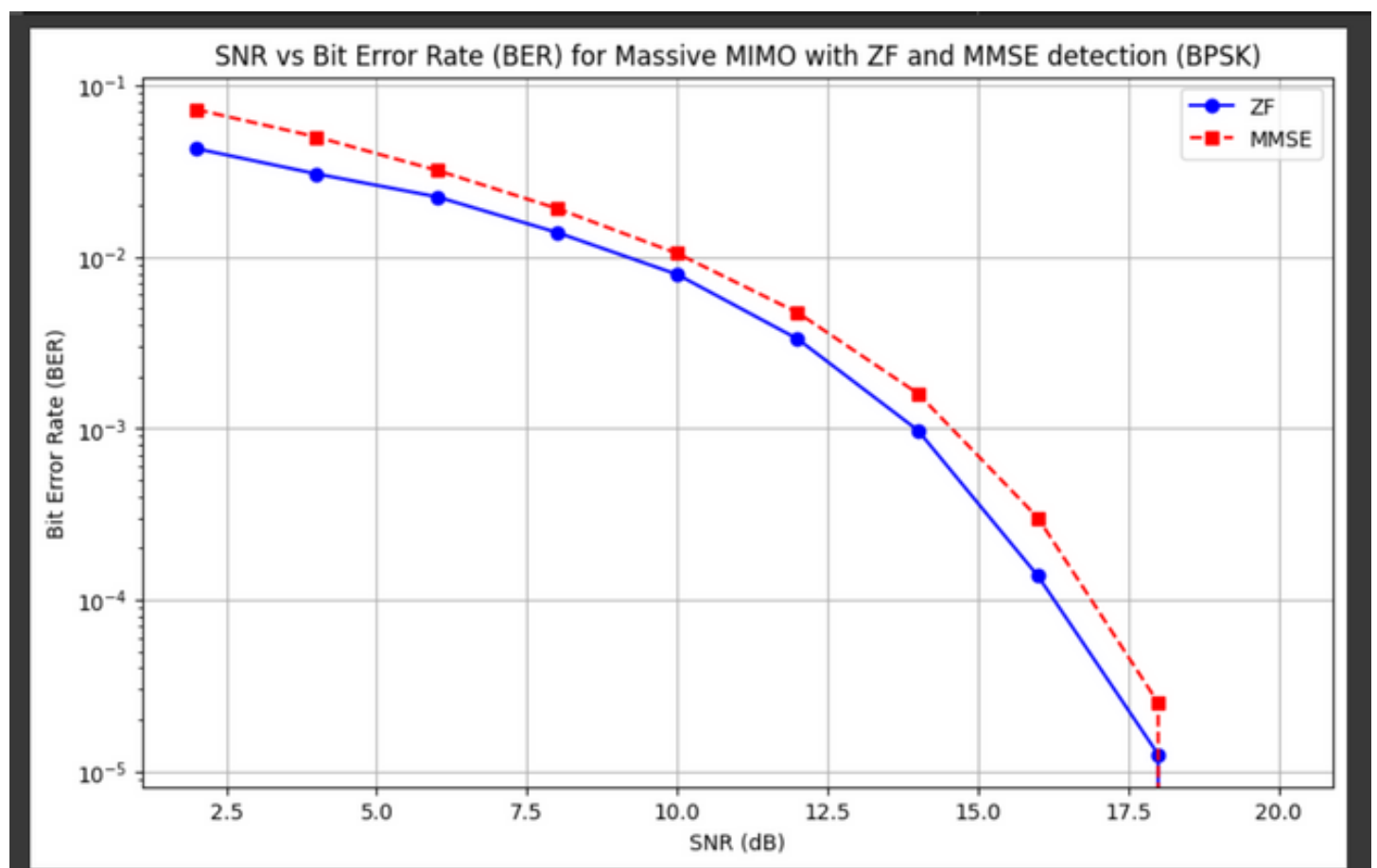
```
plt.ylabel('Bit Error Rate (BER)')
```

```
plt.legend()
```

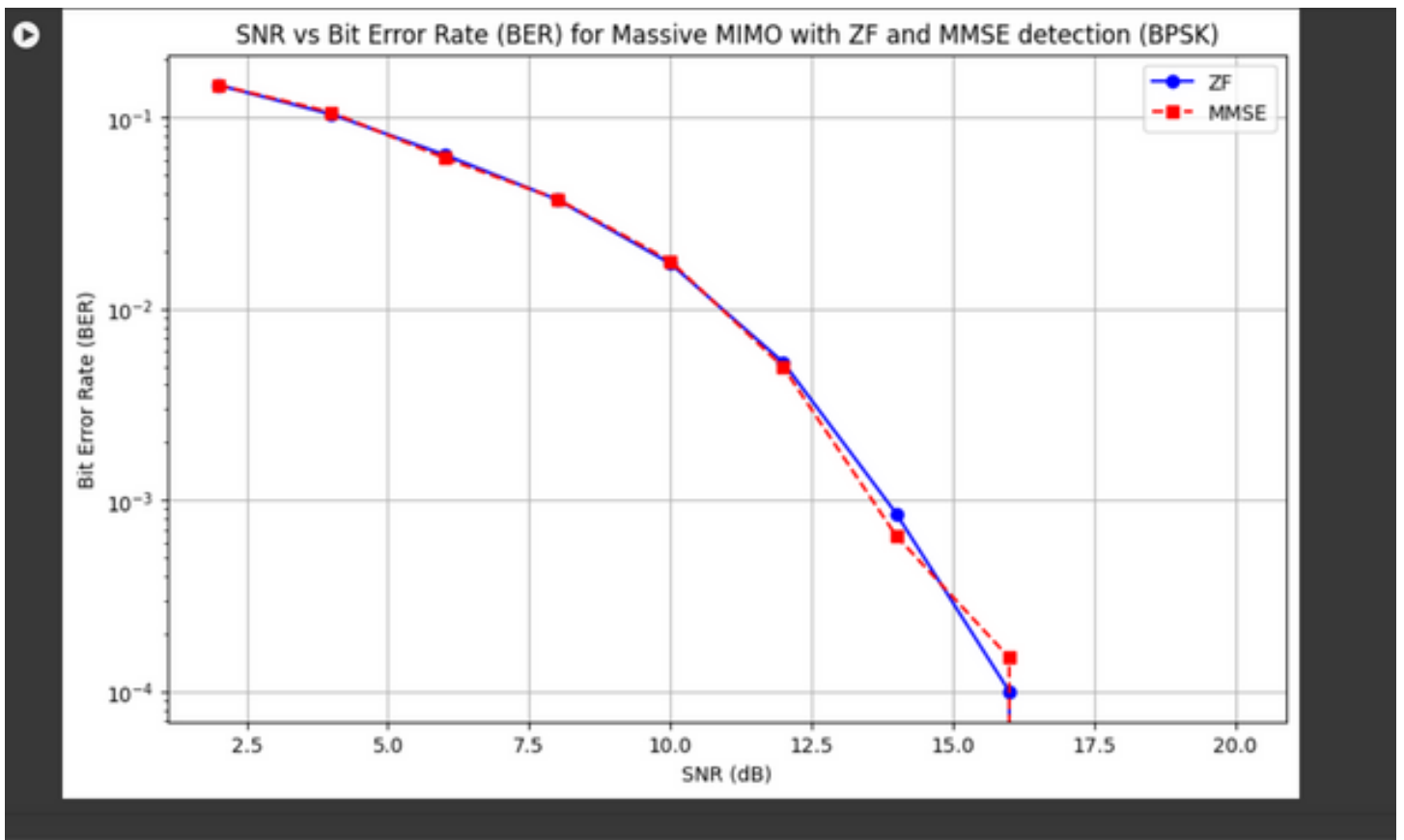
```
plt.grid(True)
```

```
plt.show()
```

**16X8**



2X4



## Zero Forcing Code :

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
# Function to generate additive white Gaussian noise (AWGN)
```

```
def awgn_noise(signal, noise_power):
```

```
noise = np.random.randn(*signal.shape) * np.sqrt(noise_power)
```

```
return noise
```

```
# Function to simulate Massive MIMO system with Zero Forcing (ZF) detection
```

```
def simulate_mimo_system(num_antennas, num_users, modulation_order, snr_db, num_trials=10000):
```

```
    # Generate random channel matrix H
```

```
    H = np.random.randn(num_antennas, num_users) + 1j * np.random.randn(num_antennas, num_users)
```

```
    H = H / np.sqrt(2) # Scale every element by 1/sqrt(2)
```

```
    # Generate random symbol vector x_true
```

```
    num_symbols = num_users
```

```
    x_true = np.random.randint(0, 2, num_symbols) * 2 - 1 # BPSK symbols {-1, 1}
```

```
    # Generate AWGN noise power from SNR
```

```
    snr_lin = 10**(snr_db / 10)
```

```
    noise_power = 1 / snr_lin
```

```
    # Initialize lists to store Bit Error Rate (BER) for each SNR value
```

```
    snr_values_db = np.arange(0, 16, 2) # SNR range from -10 dB to 15 dB
```

```
    ber_values = []
```

```
    for snr_db in snr_values_db:
```

```
        # Convert SNR from dB to linear scale
```

```
        snr_lin = 10**(snr_db / 10)
```

```
        noise_power = 1 / snr_lin
```

```
        num_errors = 0
```

```

for _ in range(num_trials):

    # Generate received signal with AWGN

    y = np.dot(H, x_true) + awgn_noise(np.dot(H, x_true), noise_power)

    # Zero Forcing (ZF) detection

    part1_w = np.conj(H.T) @ H

    part2_W = np.linalg.inv(part1_w)

    W_zf = part2_W @ np.conj(H.T)

    x_demod = np.sign(W_zf @ y.real) # Demodulate symbols

    # Calculate Bit Error Rate (BER)

    num_errors += np.sum(x_demod != x_true)

ber = num_errors / (num_trials * num_symbols)

ber_values.append(ber)

return snr_values_db, ber_values

# Parameters

num_antennas = 64

num_users = 32 # Change this to the desired number of users

modulation_order = 2 # BPSK modulation

num_trials = 10000

snr_db = 10 # Initial SNR value in dB

# Simulate Massive MIMO system with Zero Forcing (ZF) detection for BPSK

snr_values_db, ber_values = simulate_mimo_system(num_antennas, num_users, modulation_order, snr_db,
num_trials)

```

```
# Plot SNR vs BER
```

```
plt.figure(figsize=(10, 6))
```

```
plt.semilogy(snr_values_db, ber_values, marker='o', linestyle='-')
```

```
plt.title('SNR vs Bit Error Rate (BER) for Massive MIMO with Zero Forcing (ZF) detection (BPSK)')
```

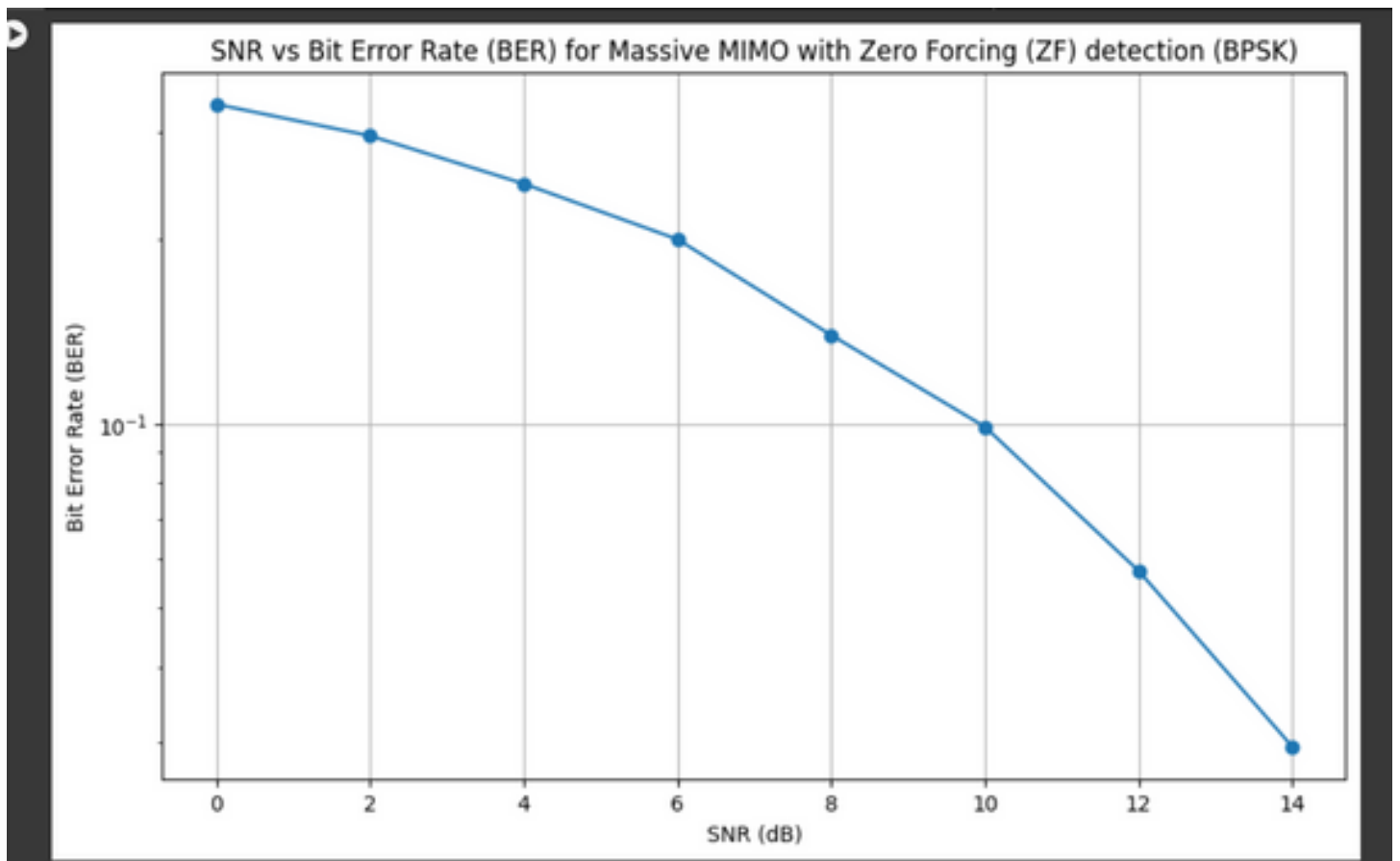
```
plt.xlabel('SNR (dB)')
```

```
plt.ylabel('Bit Error Rate (BER)')
```

```
plt.grid(True)
```

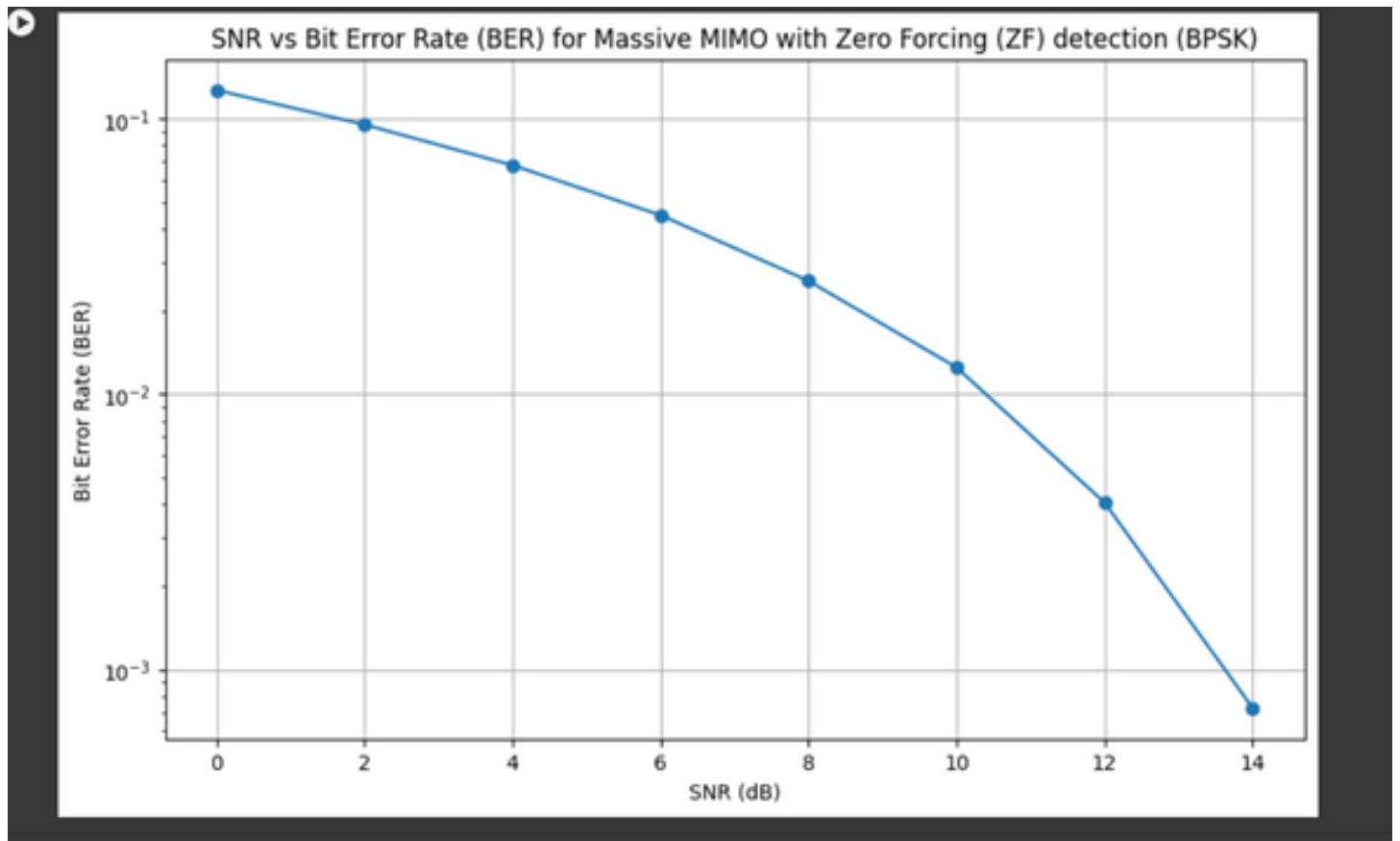
```
plt.show()
```

**2x4**

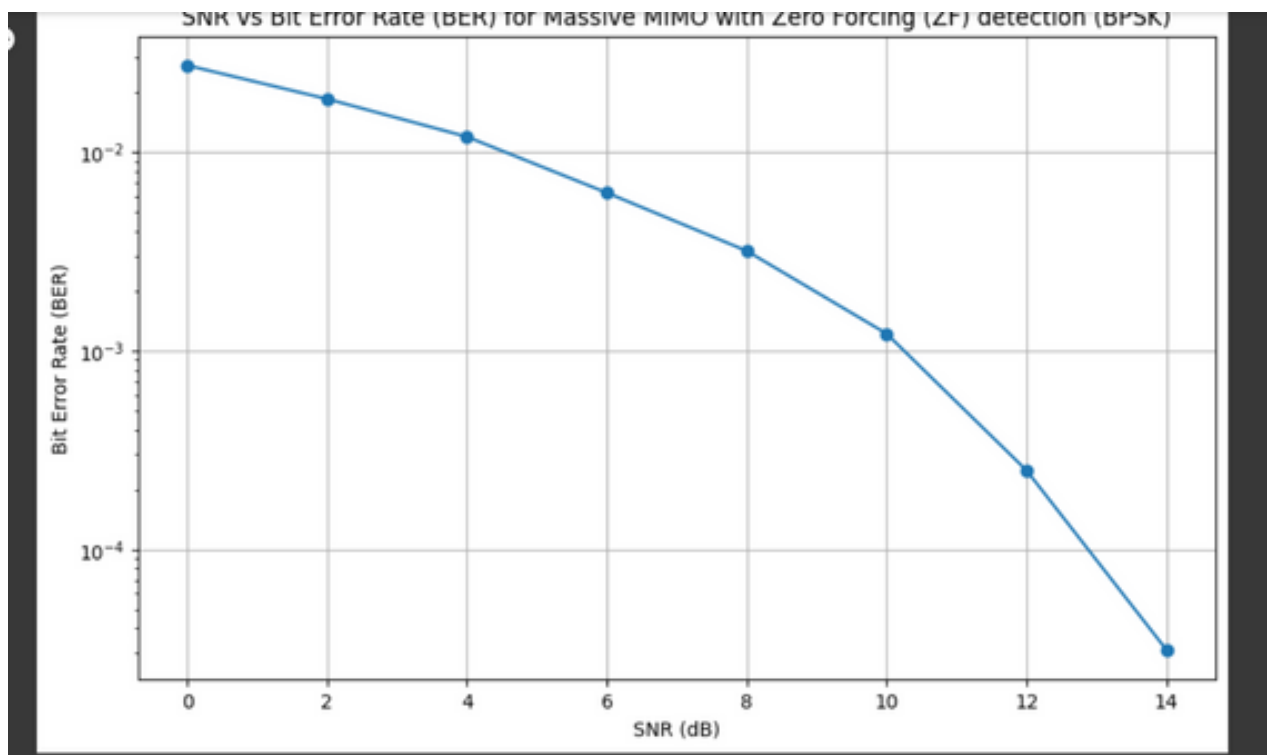




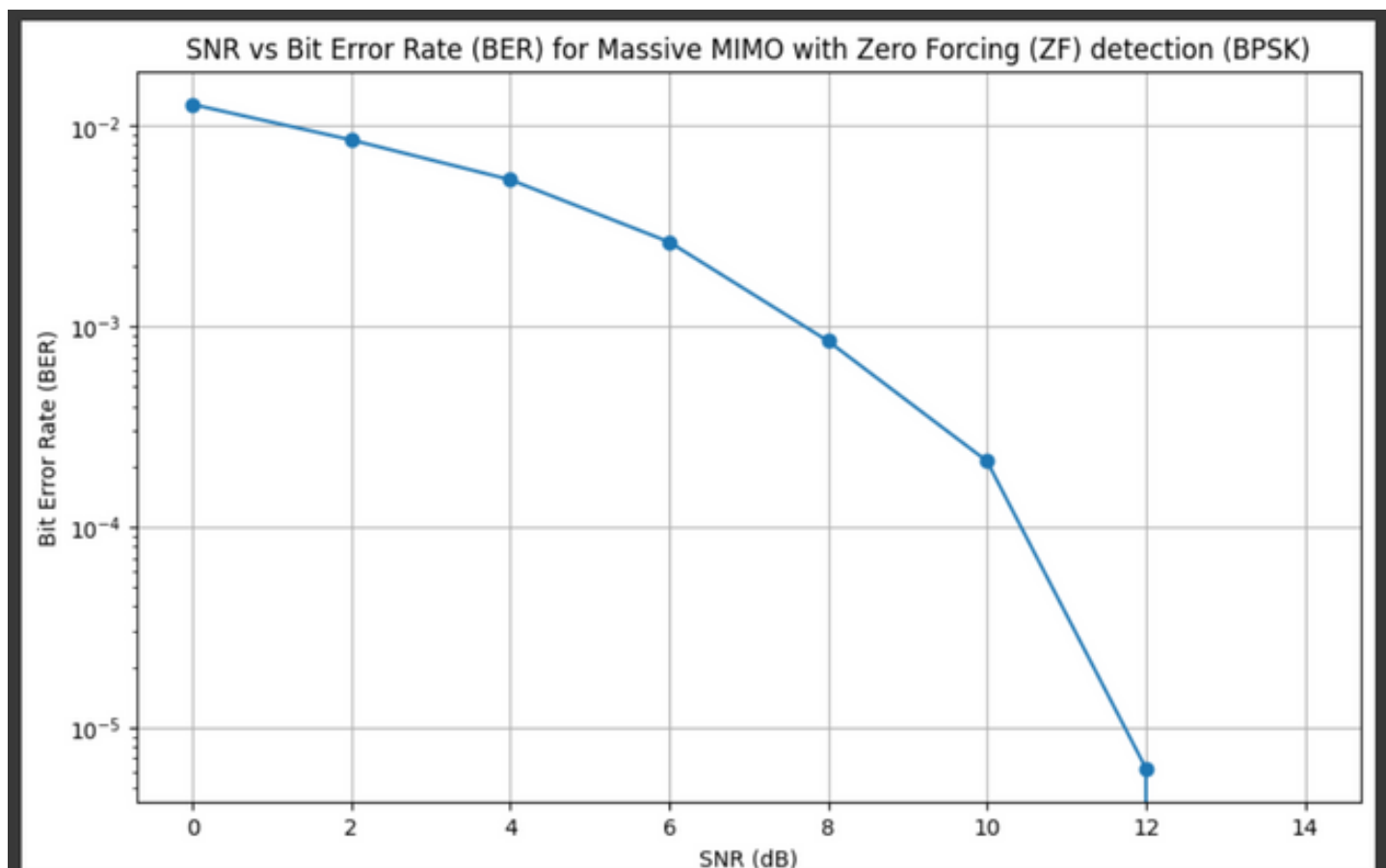
8X16



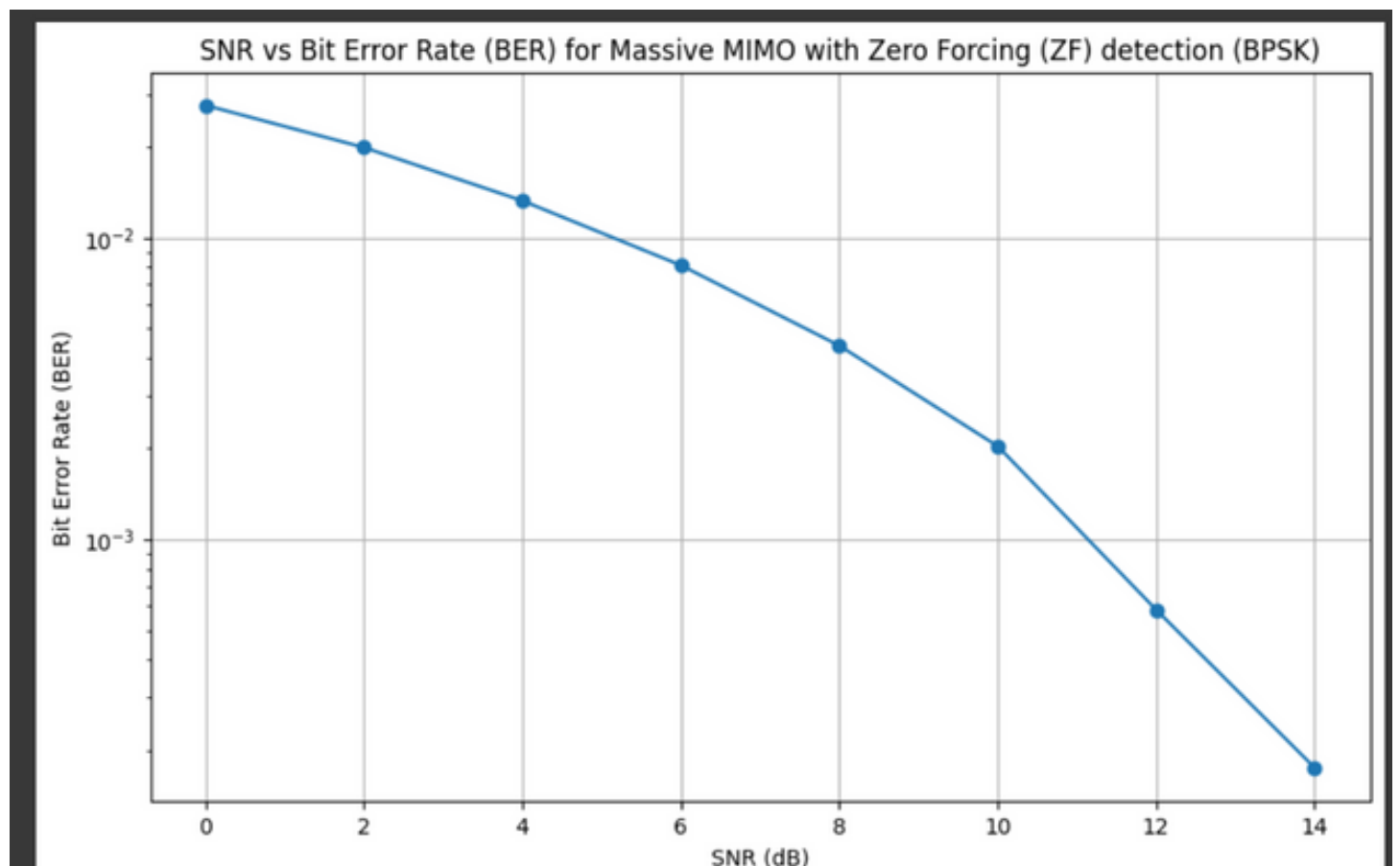
16X32



**16 x 64**



# 32X64



## MMSE

```
import numpy as np

import matplotlib.pyplot as plt

# Function to generate additive white Gaussian noise (AWGN)

def awgn_noise(signal, noise_power):

    noise = np.random.randn(*signal.shape) * np.sqrt(noise_power)

    return noise

# Function to simulate Massive MIMO system with MMSE detection

def simulate_mimo_system(num_antennas, num_users, modulation_order, snr_db, num_trials=10000):
```

```
# Generate random channel matrix H
```

```
H = np.random.randn(num_antennas, num_users) + 1j * np.random.randn(num_antennas, num_users)
```

```
H = H / np.sqrt(2) # Scale every element by 1/sqrt(2)
```

```
# Generate random symbol vector x_true
```

```
num_symbols = num_users
```

```
x_true = np.random.randint(0, 2, num_symbols) * 2 - 1 # BPSK symbols {-1, 1}
```

```
# Generate AWGN noise power from SNR
```

```
snr_lin = 10**(snr_db / 10)
```

```
noise_power = 1 / snr_lin
```

```
# Initialize lists to store Bit Error Rate (BER) for each SNR value
```

```
snr_values_db = np.arange(0, 16, 2) # SNR range from -10 dB to 15 dB
```

```
ber_values = []
```

```
for snr_db in snr_values_db:
```

```
    # Convert SNR from dB to linear scale
```

```
    snr_lin = 10**(snr_db / 10)
```

```
    noise_power = 1 / snr_lin
```

```
    num_errors = 0
```

```
    for _ in range(num_trials):
```

```
        # Generate received signal with AWGN
```

```
        y = np.dot(H, x_true) + awgn_noise(np.dot(H, x_true), noise_power)
```

```
        # MMSE detection
```

```
part1_w = np.conj(H.T) @ H

part2_W = np.linalg.inv(part1_w + noise_power * np.eye(num_users))

W_mmse = part2_W @ np.conj(H.T)

x_demod = np.sign(W_mmse @ y.real) # Demodulate symbols
```

```
# Calculate Bit Error Rate (BER)
```

```
num_errors += np.sum(x_demod != x_true)
```

```
ber = num_errors / (num_trials * num_symbols)
```

```
ber_values.append(ber)
```

```
return snr_values_db, ber_values
```

```
# Parameters
```

```
num_antennas = 4
```

```
num_users = 2 # Change this to the desired number of users
```

```
modulation_order = 2 # BPSK modulation
```

```
num_trials = 10000
```

```
snr_db = 10 # Initial SNR value in dB
```

```
# Simulate Massive MIMO system with MMSE detection for BPSK
```

```
snr_values_db, ber_values = simulate_mimo_system(num_antennas, num_users, modulation_order, snr_db,
num_trials)
```

```
# Plot SNR vs BER
```

```
plt.figure(figsize=(10, 6))
```

```
plt.semilogy(snr_values_db, ber_values, marker='o', linestyle='-')
```

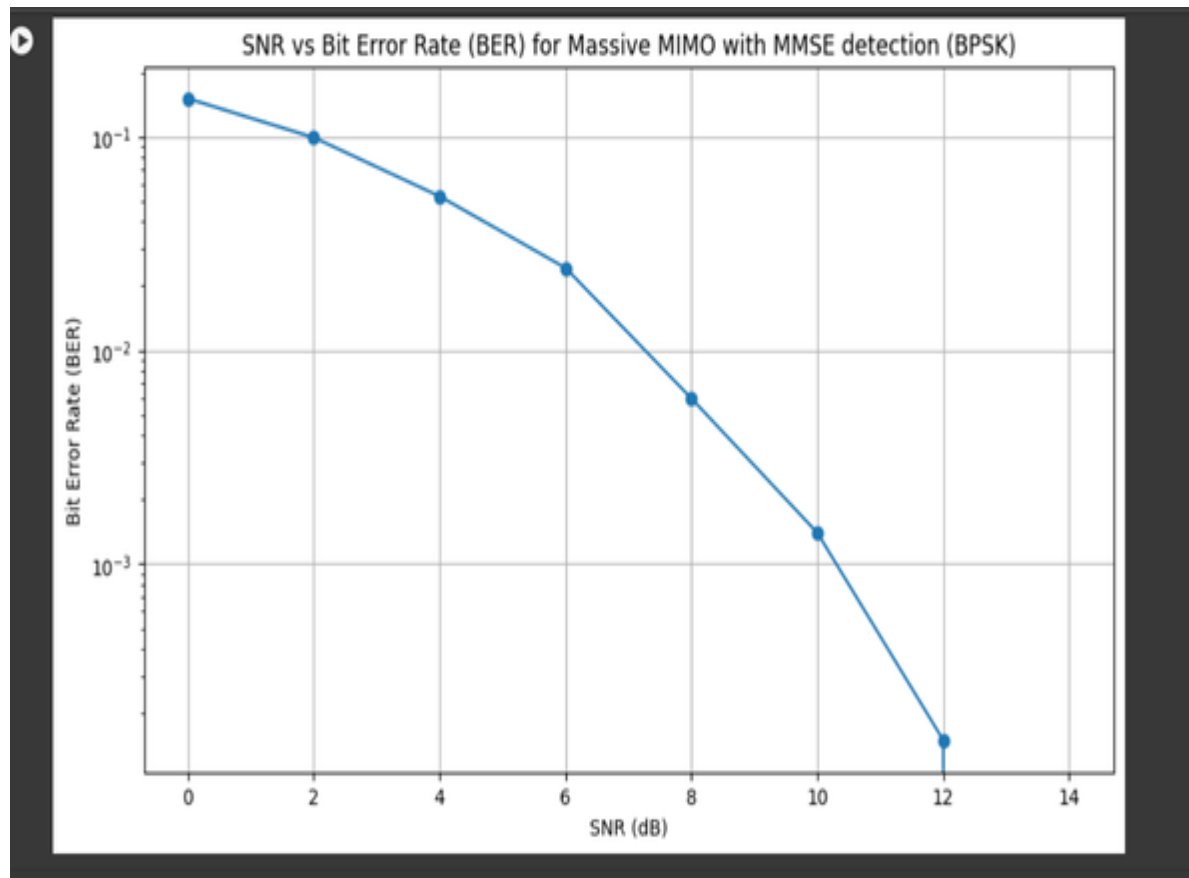
```
plt.title('SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK)')
```

```
plt.xlabel('SNR (dB)')
```

```
plt.ylabel('Bit Error Rate (BER)')
```

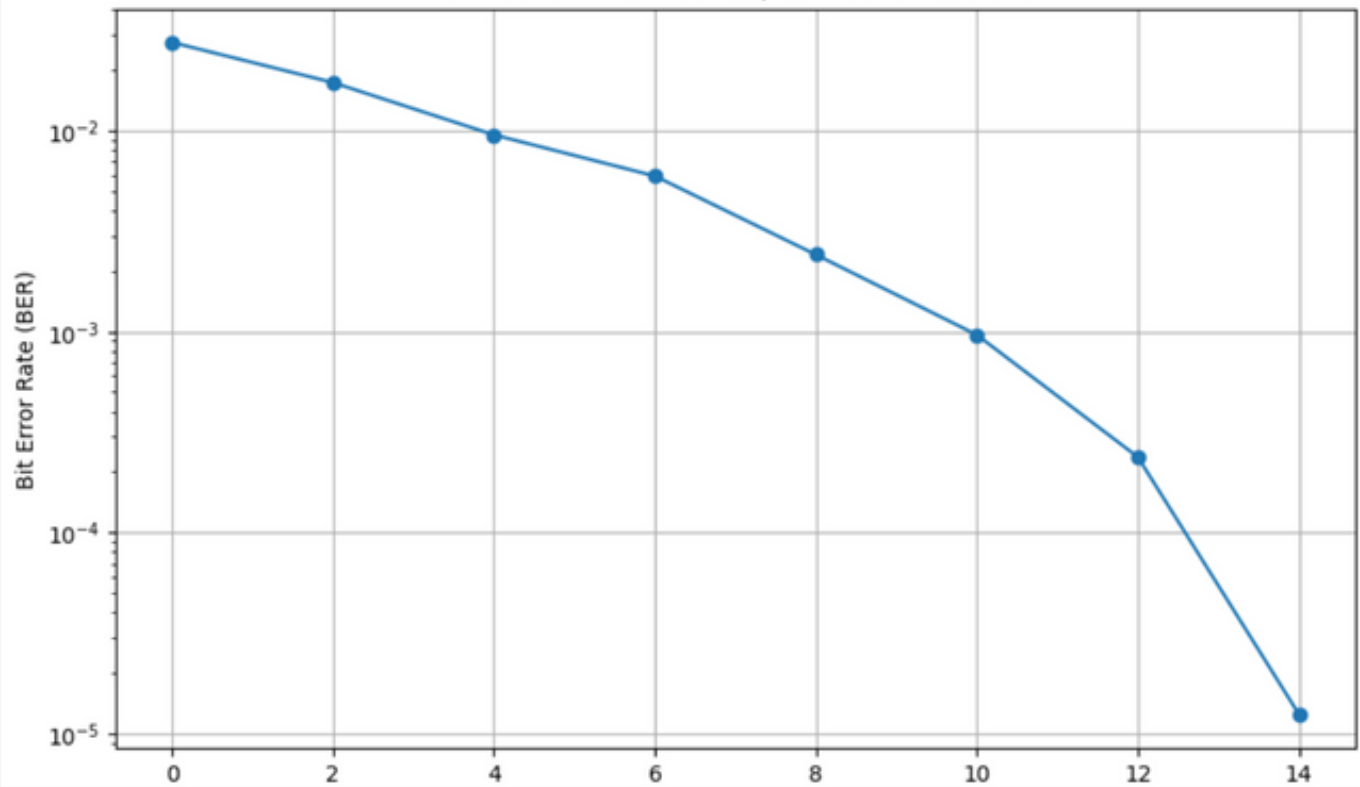
```
plt.grid(True)
```

```
plt.show()
```

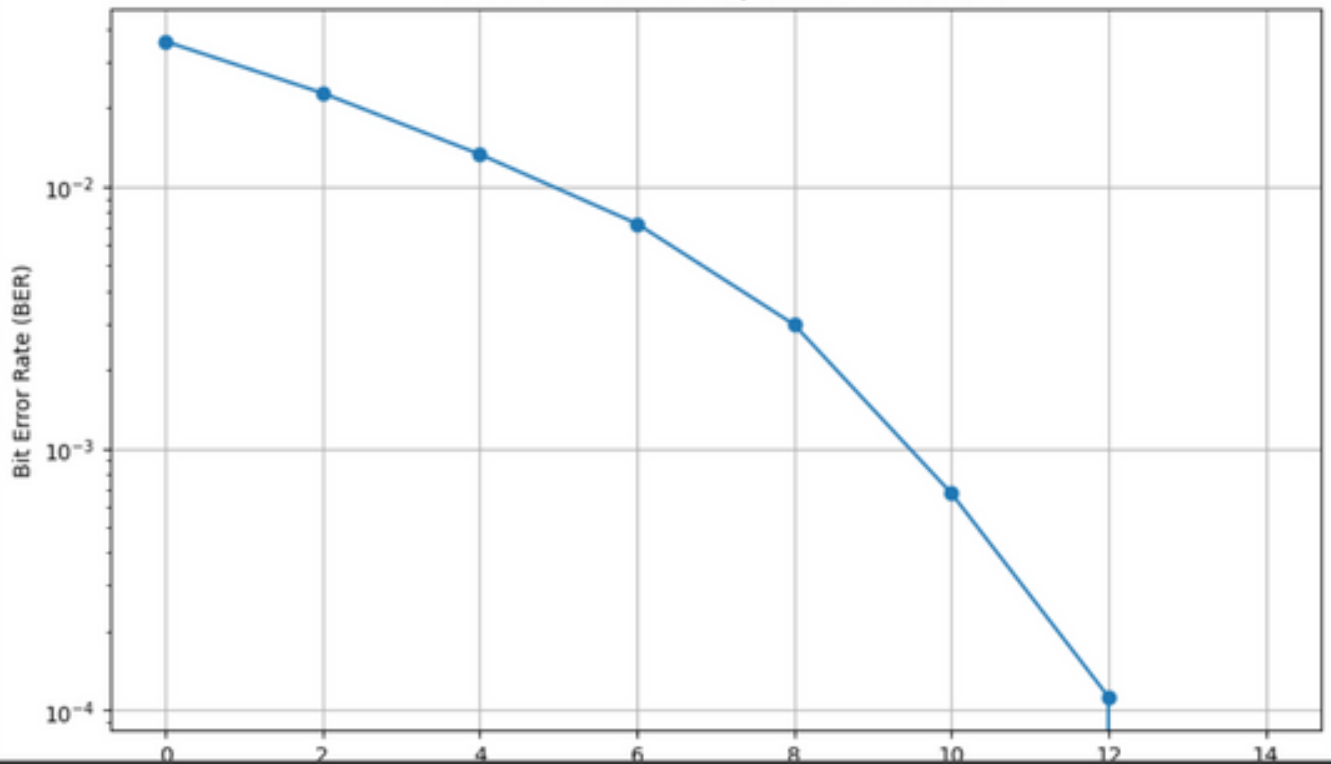


2X4

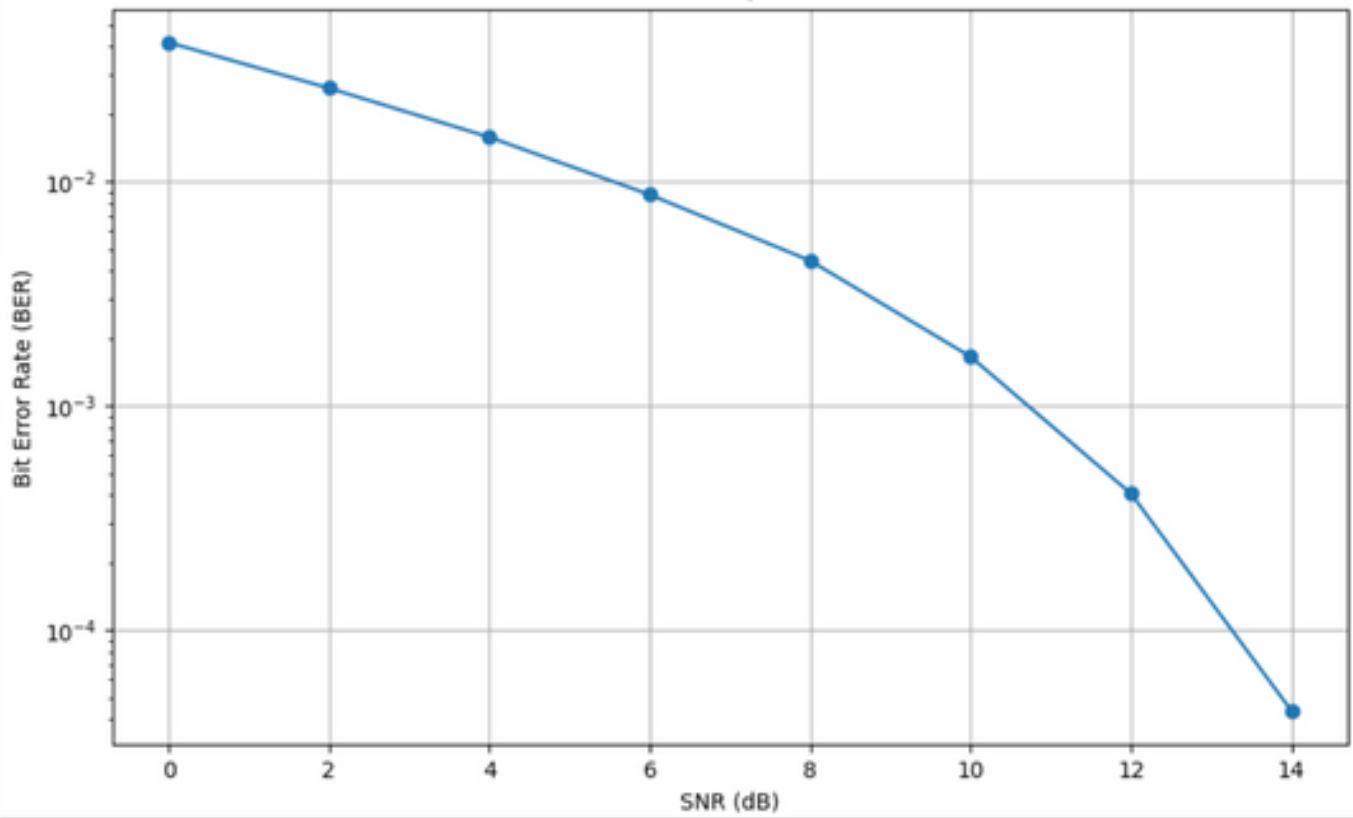
SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK)  
Number of Antennas: 16, Number of Users: 8



SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK)  
Number of Antennas: 32, Number of Users: 8



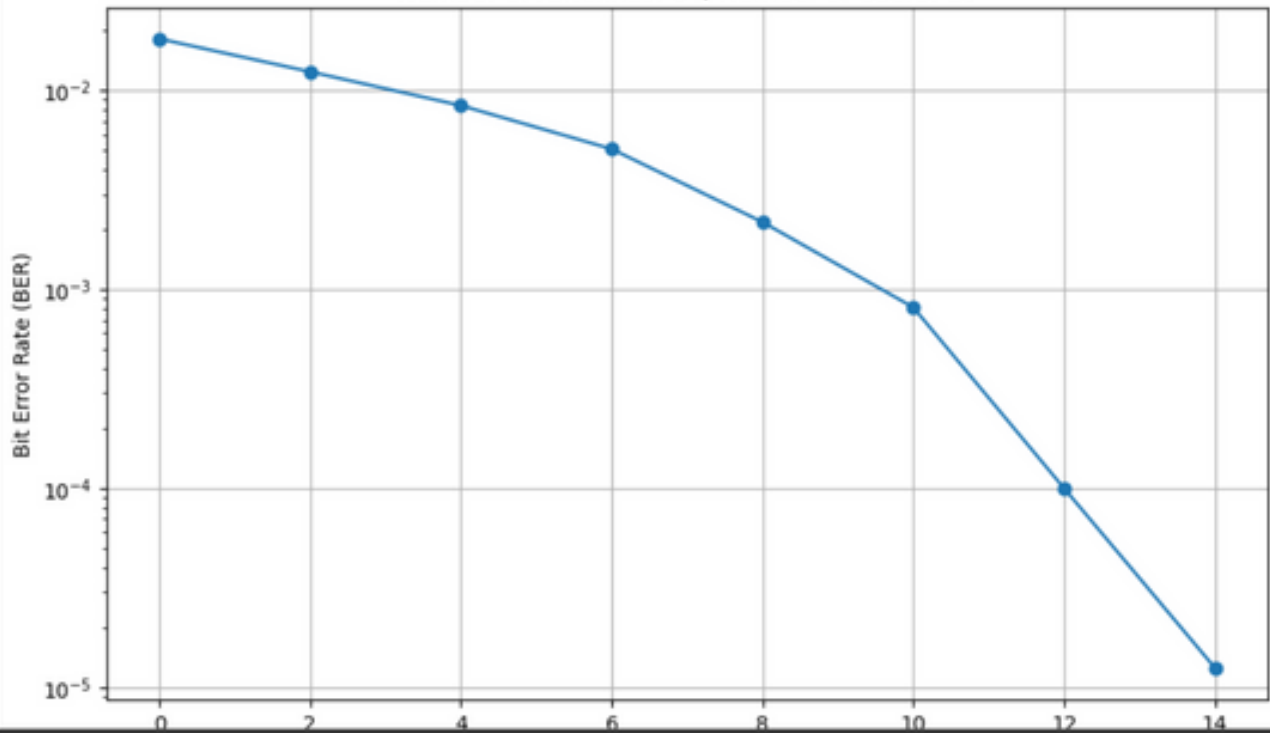
SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK)  
Number of Antennas: 32, Number of Users: 16







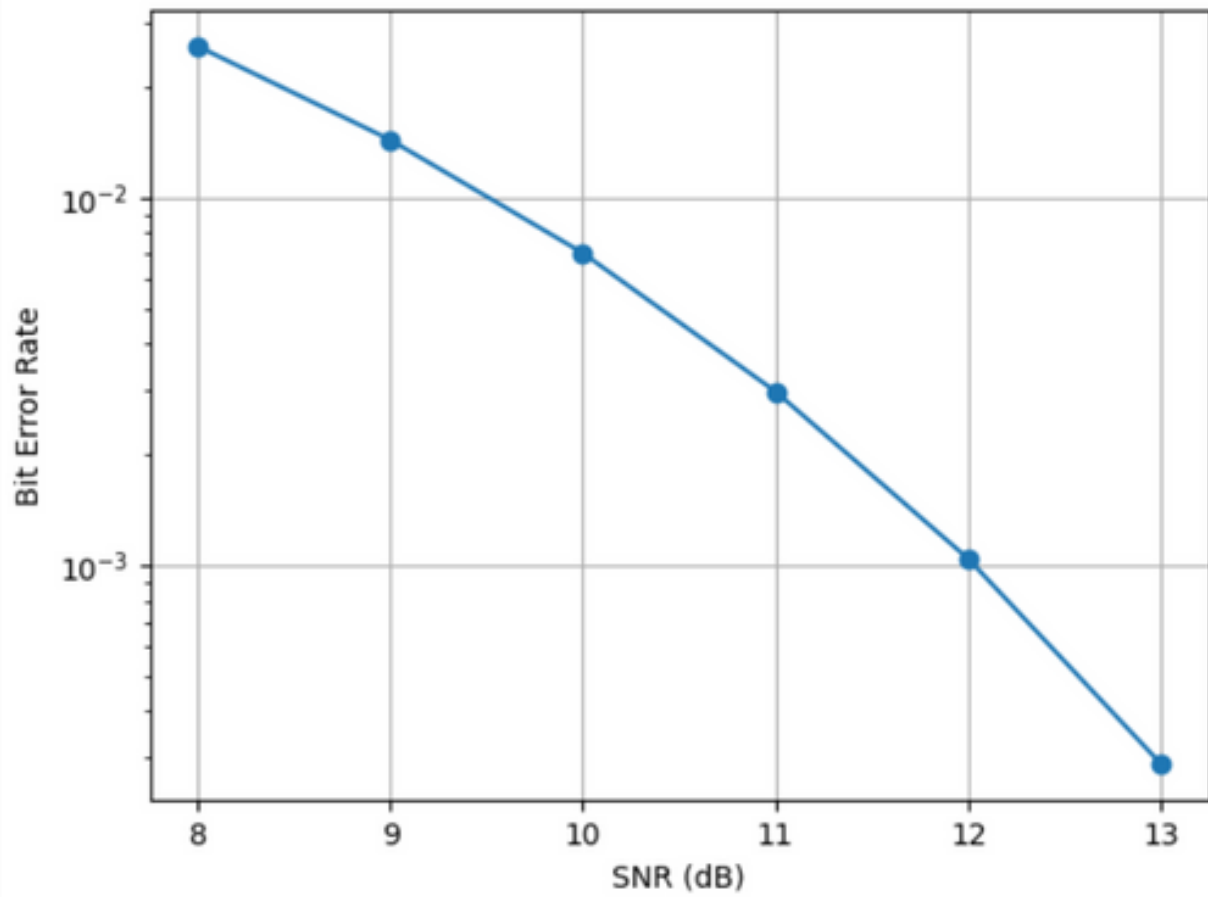
SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK)  
Number of Antennas: 64, Number of Users: 16



**Detnet**

[[3.67249794e-06]]

Bit Error Rate vs. SNR



- **COMBINED PLOT FOR ZERO FORCING WITH CONSTANT N (No. of antennas ) and varying K no of users**

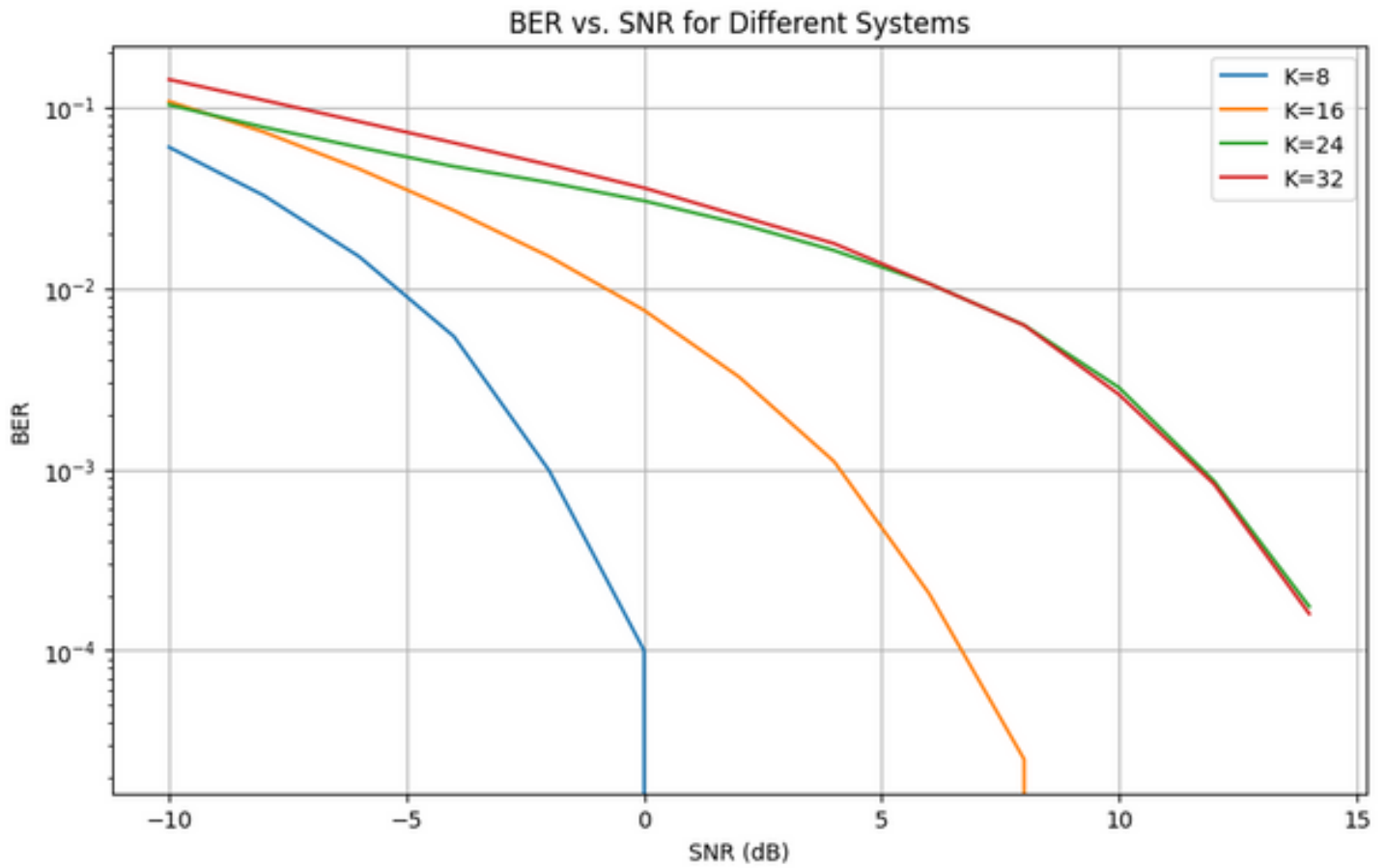


FIG 1) ZERO FOCRING for N=64 and varying K

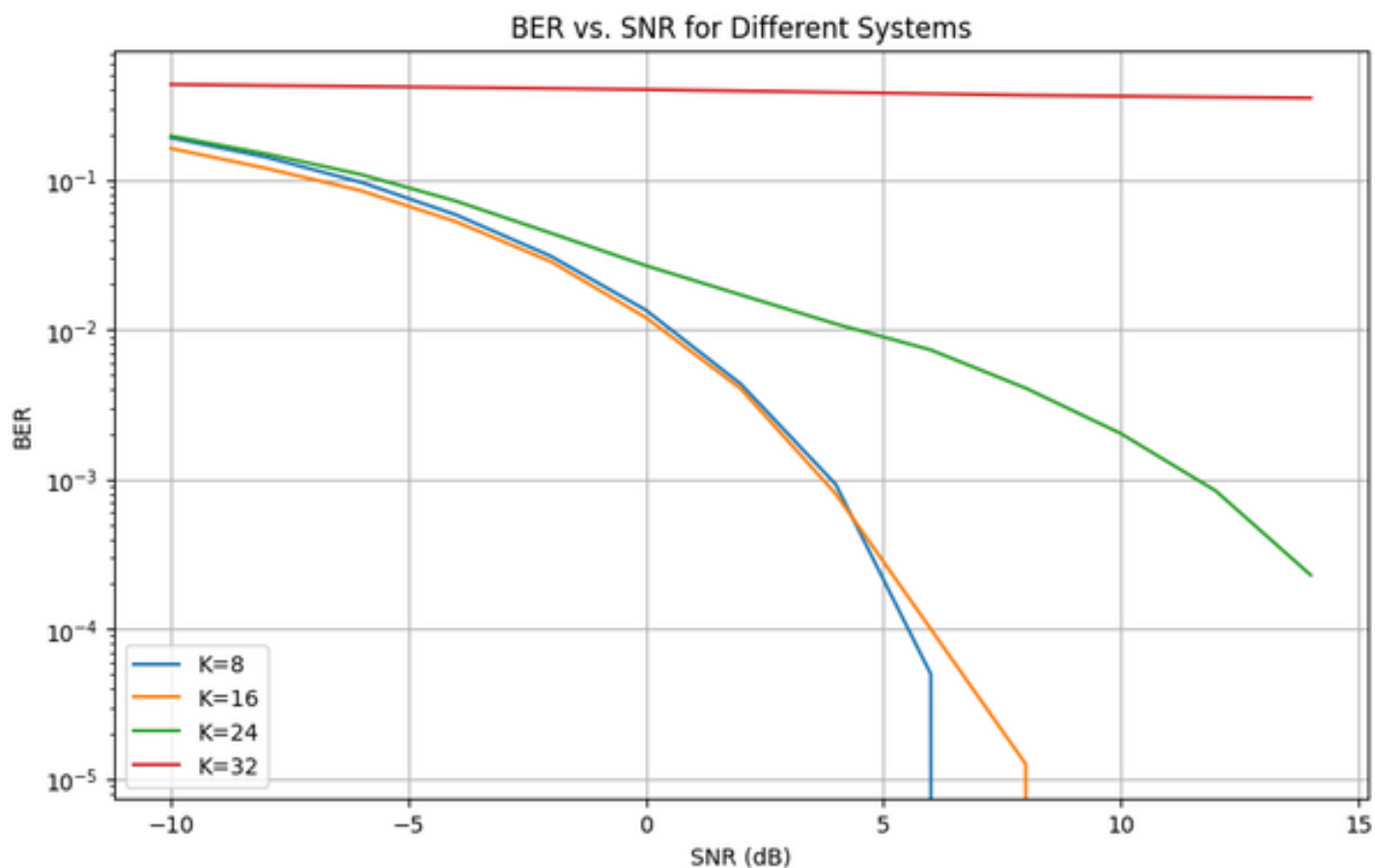
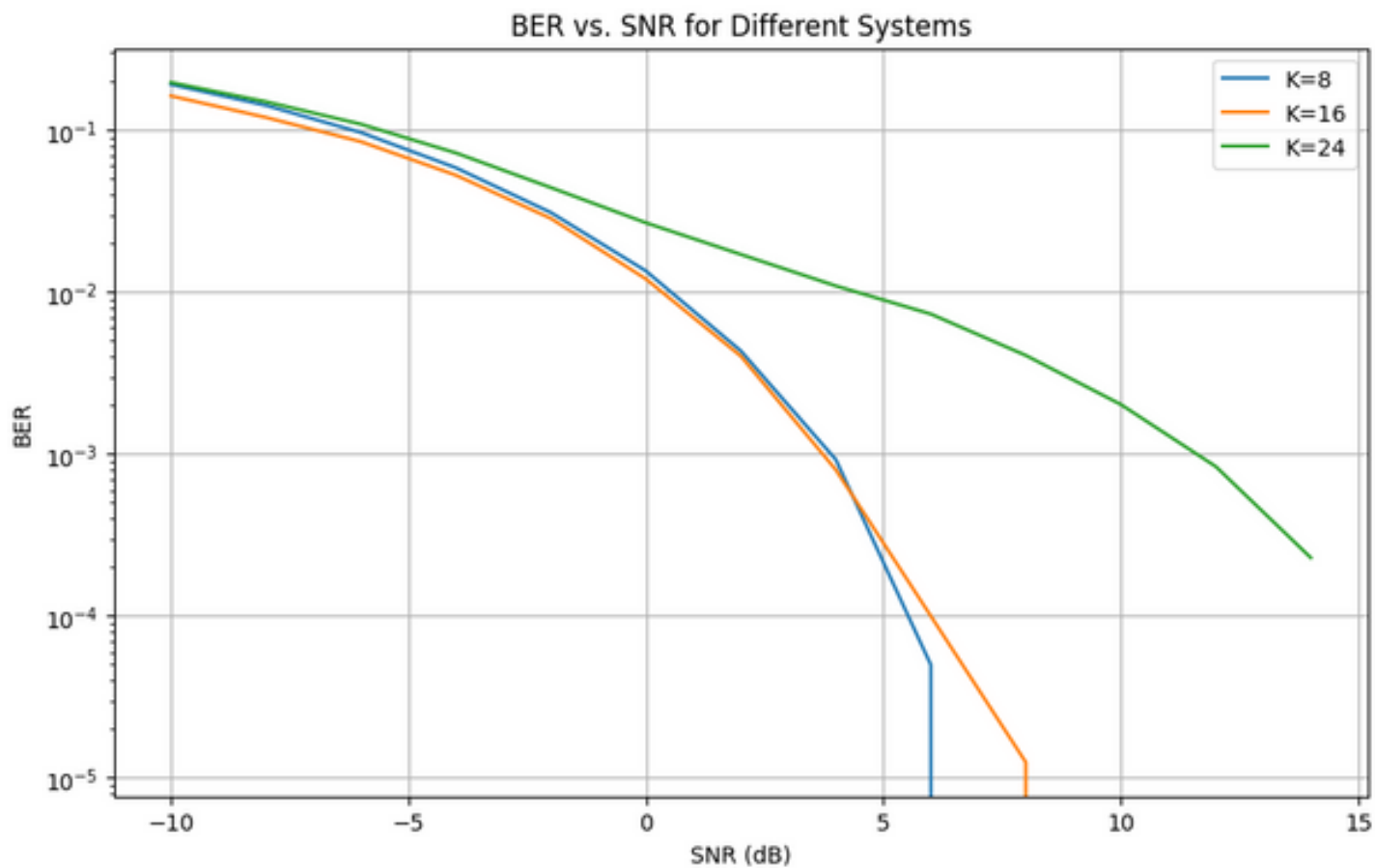
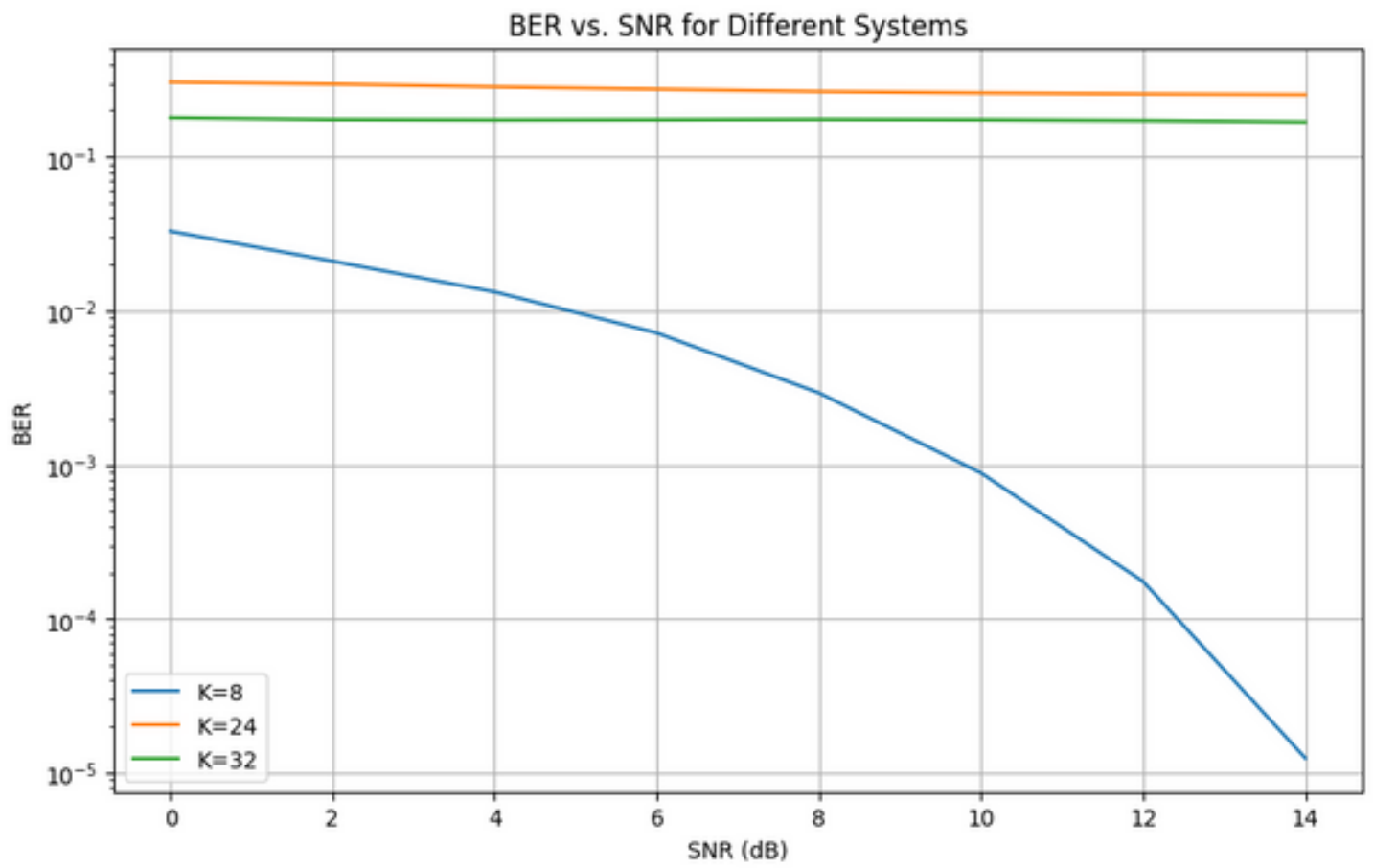


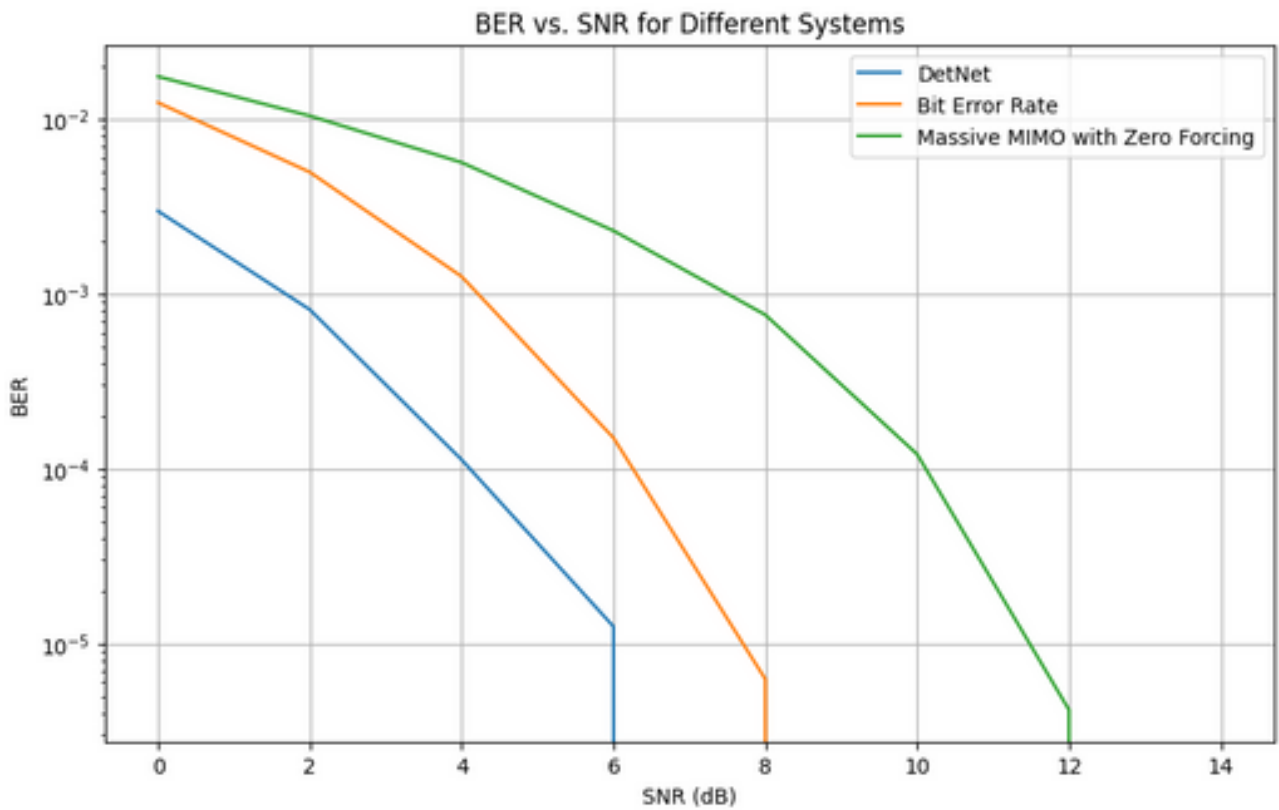
Fig2) ZF for N=32 and varying K(ALL)





[ZF] N=16 N K USERS

•



- **MMSE for fixed N and varying K**

FIG1) MMSE FOR N =64 and varying K

SNR vs Bit Error Rate (BER) for Massive MIMO with MMSE detection (BPSK) for N=16 and different values of K

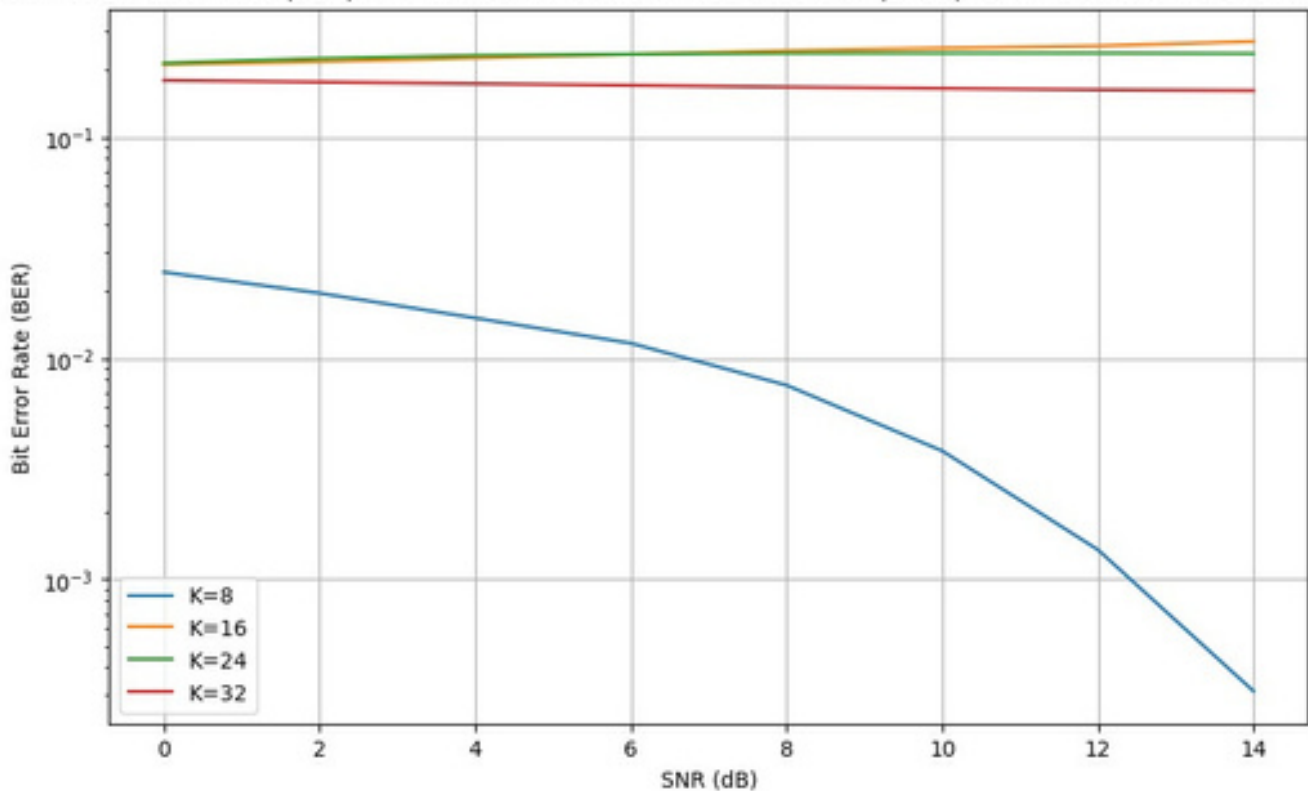


FIG 2) MMSE FOR N=16 AND DIFF K

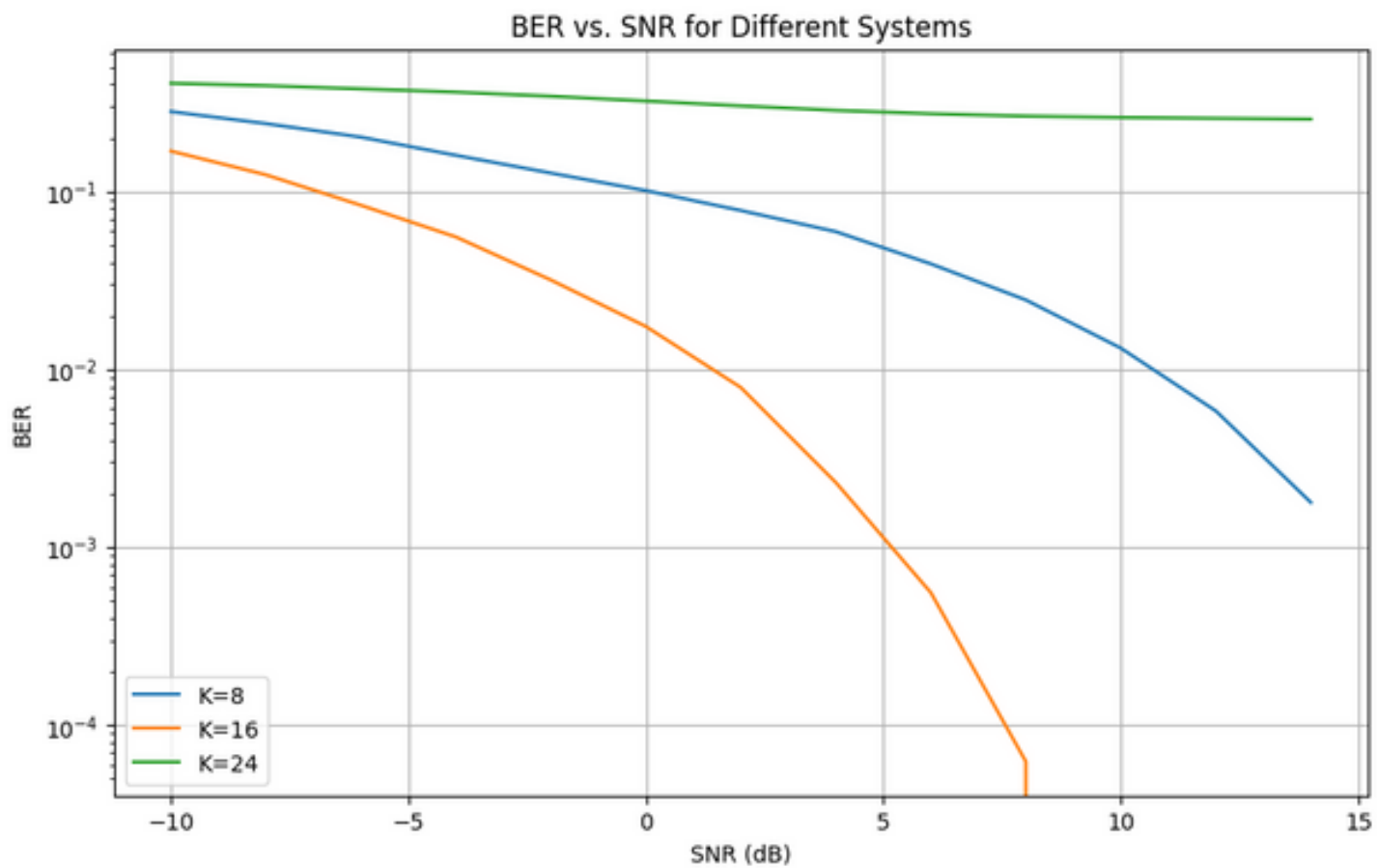
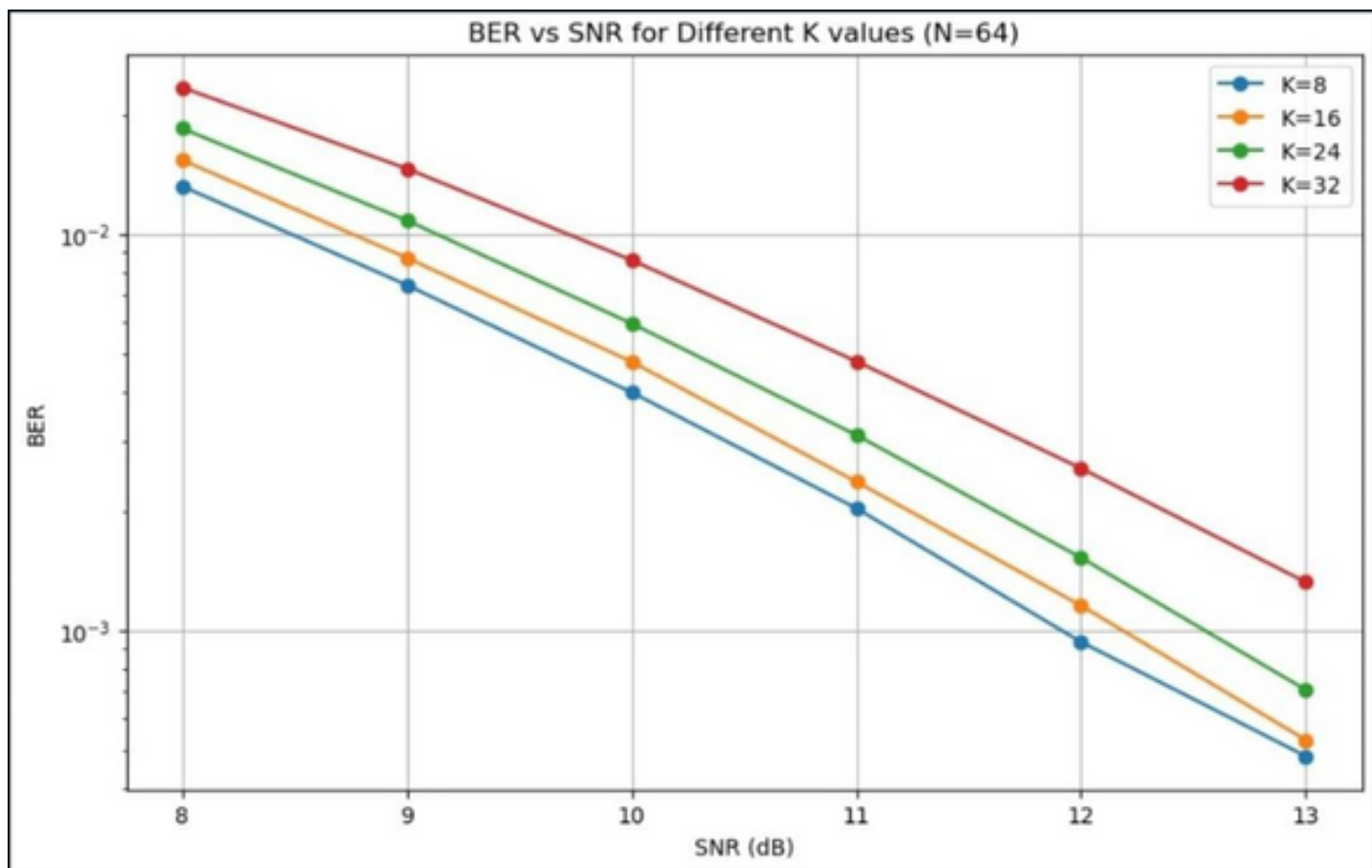


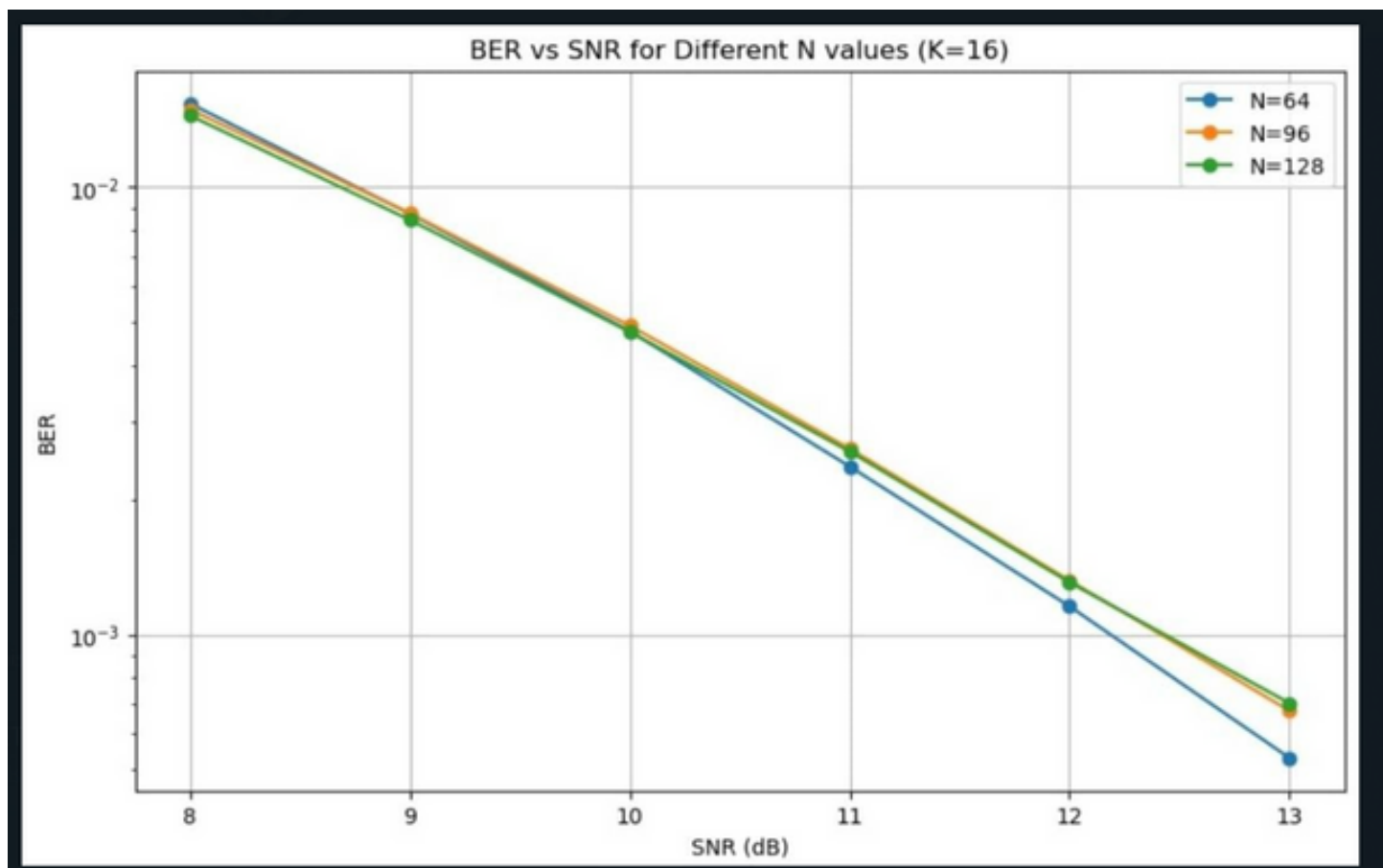
Fig 3) N=32 FOR MMSE



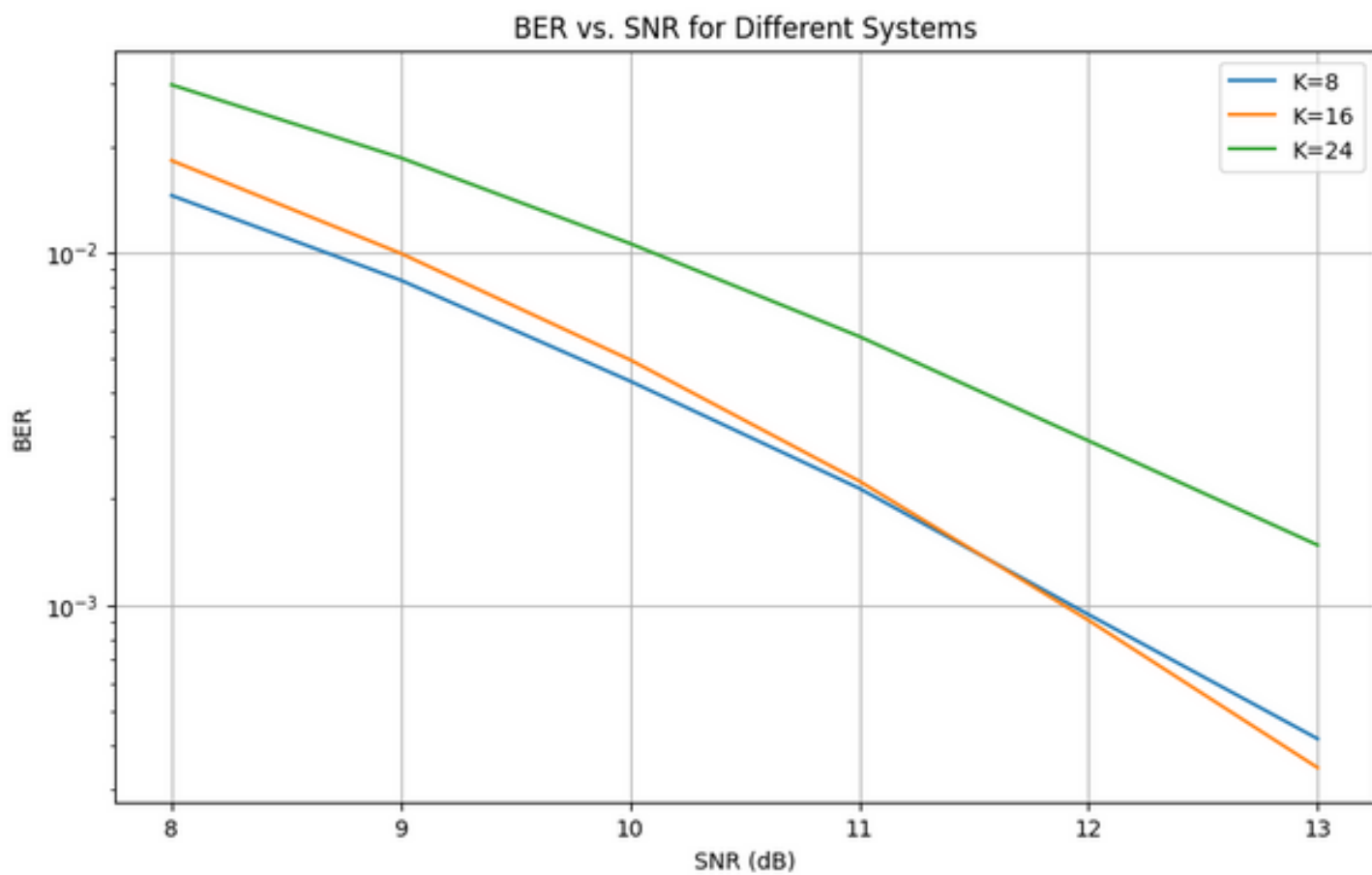
## DETNET

Fig 1) For N =64 and varying K

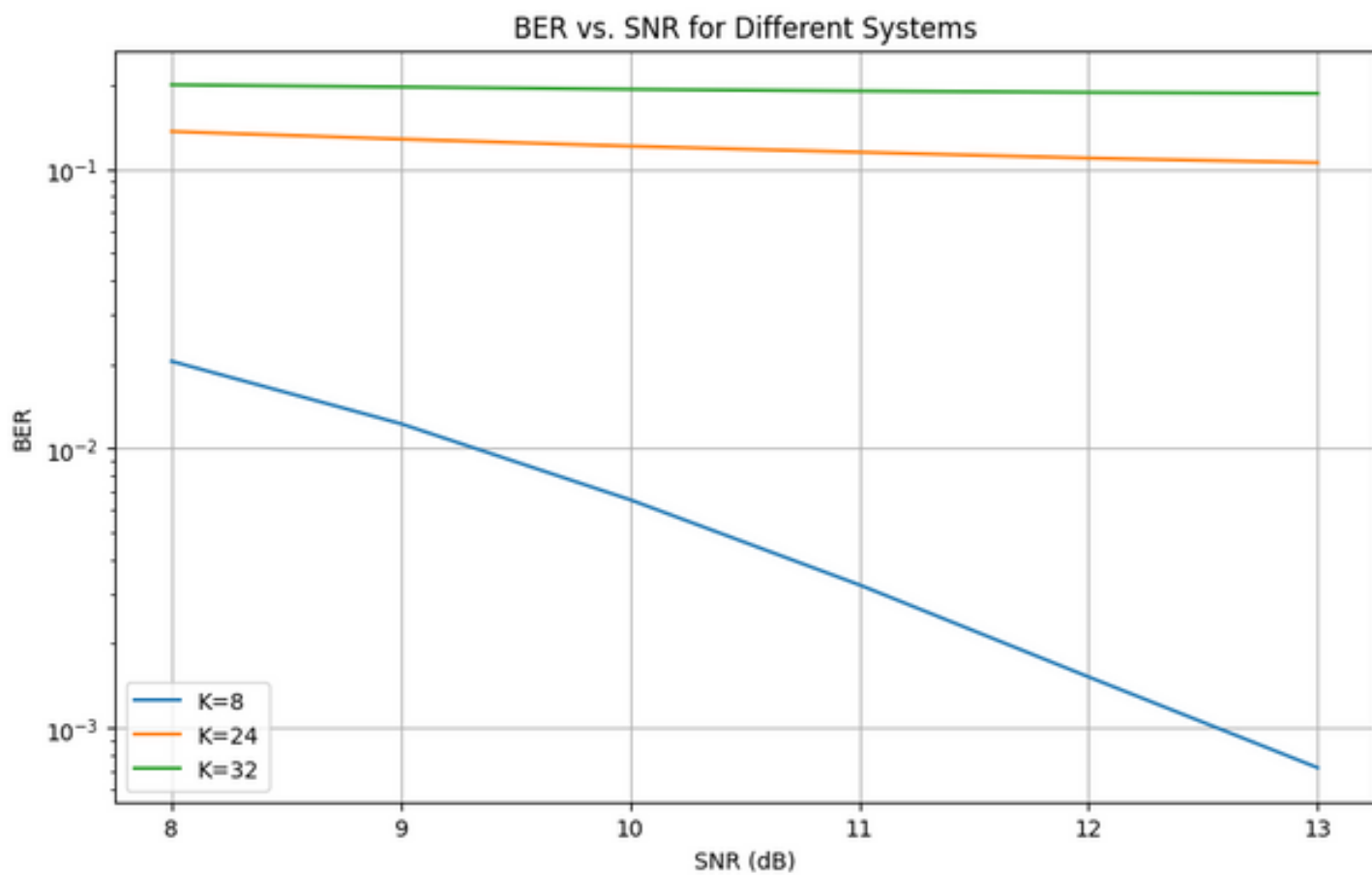




For K =16 and varying N



DETNET N=32 AND VARYING K



DETNET N=16 AND VARYING K

FIG 3) ZF for N=32 and K=8,16,24,32