

Homework - 1

Sanket Patole

W1649988

1) $A + F$

$$\begin{bmatrix} 3 & 1 & 5 \\ 6 & 2 & 0 \end{bmatrix}_{2 \times 3} + \begin{bmatrix} 2 & 1 & 3 \\ 5 & 7 & -2 \end{bmatrix}_{2 \times 3}$$

$$\Rightarrow \begin{bmatrix} 5 & 2 & 8 \\ 11 & 9 & -2 \end{bmatrix}_{2 \times 3}$$

2) $E - D$

$$\begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix}_{2 \times 2} - \begin{bmatrix} 5 & 2 \\ 3 & 1 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} -2 & -4 \\ -2 & 3 \end{bmatrix}_{2 \times 2}$$

3) $C + B$

$$\begin{bmatrix} 2 & 4 \\ 3 & 6 \\ -1 & 2 \end{bmatrix}_{3 \times 2} + \begin{bmatrix} 6 \\ 4 \\ -1 \end{bmatrix}_{3 \times 1} \Rightarrow$$

We cannot perform the addition operation on these matrices as the dimensions do not match

4) $C(D)$

$$\begin{bmatrix} 2 & 4 \\ 3 & 6 \\ -1 & 2 \end{bmatrix}_{3 \times 2} \times \begin{bmatrix} 5 & 2 \\ 3 & 1 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} 2 \cdot 5 + 4 \cdot 3 & 2 \cdot 2 + 4 \cdot 1 \\ 3 \cdot 5 + 6 \cdot 3 & 3 \cdot 2 + 6 \cdot 1 \\ -1 \cdot 5 + 2 \cdot 3 & -1 \cdot 2 + 2 \cdot 1 \end{bmatrix}$$

$$\begin{bmatrix} 10+12 & 4+4 \\ 15+18 & 6+6 \\ -5+6 & -2+2 \end{bmatrix} \Rightarrow \begin{bmatrix} 22 & 8 \\ 33 & 12 \\ 1 & 0 \end{bmatrix}_{3 \times 2}$$

5) A(F)

$$\begin{bmatrix} 3 & 1 & 5 \\ 6 & 2 & 0 \end{bmatrix}_{2 \times 3} * \begin{bmatrix} 2 & 1 & 3 \\ 5 & 7 & -2 \end{bmatrix}_{2 \times 3}$$

NOT
EQUAL

⇒ we cannot perform matrix multiplication operation on these matrices. As the number of columns of matrix A does not match no. of rows of matrix F.

c) C^T

$$\begin{bmatrix} 2 & 4 \\ 3 & 6 \\ -1 & 2 \end{bmatrix}_{3 \times 2} \xrightarrow{\text{transform}} \begin{bmatrix} 2 & 3 & -1 \\ 4 & 6 & 2 \end{bmatrix}_{2 \times 3}$$

no. of rows become
no. of columns & vice versa

7) $F^T(E)$

value of F^T ; $F^T \Rightarrow \begin{bmatrix} 2 & 5 \\ 1 & 7 \\ 3 & -2 \end{bmatrix}$

Now, $F^T(E)$

$$\begin{bmatrix} 2 & 5 \\ 1 & 7 \\ 3 & -2 \end{bmatrix}_{3 \times 2} * \begin{bmatrix} 3 & -2 \\ 1 & 4 \end{bmatrix}_{2 \times 2}$$

$$\Rightarrow \begin{bmatrix} 2 \times 3 + 5 \times 1 & 2 \times -2 + 5 \times 4 \\ 1 \times 3 + 7 \times 1 & 1 \times -2 + 7 \times 4 \\ 3 \times 3 + -2 \times 1 & 3 \times -2 + -2 \times 4 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 6+5 & 4+20 \\ 3+7 & -2+28 \\ 9+(-2) & -6+(-8) \end{bmatrix} \Rightarrow \begin{bmatrix} 11 & 24 \\ 10 & 26 \\ 7 & -14 \end{bmatrix}_{3 \times 2}$$