# Linear Regression Analysis: Regression Case Study

Neerja Doshi, Sri Santhosh Hari, Ker-Yu Ong, Nicha Ruchirawat

## Part I: Explanatory Modelling

## Task 0: Exploratory Data Analysis and Data Cleaning

```
##
## $ MSZoning : Factor w/ 5 levels "C (all)", "FV",...: 4 4 4 4 4 4 4 5 4 ...
## $ LotFrontage : int
## $ LotArea
## $ Street
## $ Alley
                   : Factor w/ 2 levels "Grv1", "Pave": NA ...
                   : Factor w/ 4 levels "IR1", "IR2", "IR3", ...: 4 4 1 1 1 1 4 1 4 4 ...
## $ LotShape
## $ LandContour : Factor w/ 4 levels "Bnk", "HLS", "Low", ...: 4 4 4 4 4 4 4 4 4 ...
## $ Utilities : Factor w/ 2 levels "AllPub", "NoSeWa": 1 1 1 1 1 1 1 1 1 1 ...
## $ LotConfig
                   : Factor w/ 5 levels "Corner", "CulDSac", ...: 5 3 5 1 3 5 5 1 5 1 ...
                 : Factor w/ 3 levels "Gtl", "Mod", "Sev": 1 1 1 1 1 1 1 1 1 1 ...
## $ LandSlope
## $ Neighborhood : Factor w/ 25 levels "Blmngtn", "Blueste",..: 6 25 6 7 14 12 21 17 18 4 ...
## $ Condition1 : Factor w/ 9 levels "Artery", "Feedr", ...: 3 2 3 3 3 3 3 5 1 1 ...
## $ Condition2
                   : Factor w/ 8 levels "Artery", "Feedr", ...: 3 3 3 3 3 3 3 3 1 ...
                   : Factor w/ 5 levels "1Fam", "2fmCon", ...: 1 1 1 1 1 1 1 1 2 ...
## $ BldgType
                   : Factor w/ 8 levels "1.5Fin", "1.5Unf", ...: 6 3 6 6 6 1 3 6 1 2 ...
## $ HouseStyle
## $ OverallQual : int 7 6 7 7 8 5 8 7 7 5 ...
## $ OverallCond : int 5 8 5 5 5 5 6 5 6 ...
                 : int
                         2003 1976 2001 1915 2000 1993 2004 1973 1931 1939 ...
## $ YearBuilt
##
   $ YearRemodAdd : int
                         2003 1976 2002 1970 2000 1995 2005 1973 1950 1950 ...
                  : Factor w/ 6 levels "Flat", "Gable", ...: 2 2 2 2 2 2 2 2 2 2 ...
## $ RoofStyle
## $ RoofMatl
                   : Factor w/ 8 levels "ClyTile", "CompShg", ...: 2 2 2 2 2 2 2 2 2 2 ...
## $ Exterior1st : Factor w/ 15 levels "AsbShng", "AsphShn",..: 13 9 13 14 13 13 13 7 4 9 ...
## $ Exterior2nd : Factor w/ 16 levels "AsbShng", "AsphShn",..: 14 9 14 16 14 14 7 16 9 ...
## $ MasVnrType : Factor w/ 4 levels "BrkCmn", "BrkFace",..: 2 3 2 3 2 3 4 4 3 3 ...
## $ MasVnrArea : int 196 0 162 0 350 0 186 240 0 0 ...
## $ ExterQual
                  : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 4 3 4 3 4 3 4 4 4 ....
## $ ExterCond
                  : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 5 5 ...
                   : Factor w/ 6 levels "BrkTil", "CBlock", ...: 3 2 3 1 3 6 3 2 1 1 ...
## $ Foundation
                   : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 3 3 4 3 3 1 3 4 4 ...
## $ BsmtQual
## $ BsmtCond
                   : Factor w/ 4 levels "Fa", "Gd", "Po", ...: 4 4 4 2 4 4 4 4 4 4 ....
## $ BsmtExposure : Factor w/ 4 levels "Av", "Gd", "Mn", ...: 4 2 3 4 1 4 1 3 4 4 ...
```

```
$ BsmtFinType1 : Factor w/ 6 levels "ALQ", "BLQ", "GLQ", ...: 3 1 3 1 3 3 3 1 6 3 ...
                  : int 706 978 486 216 655 732 1369 859 0 851 ...
##
   $ BsmtFinSF1
   $ BsmtFinType2 : Factor w/ 6 levels "ALQ", "BLQ", "GLQ", ...: 6 6 6 6 6 6 6 6 2 6 6 ...
##
                  : int 0000003200...
##
   $ BsmtFinSF2
##
   $ BsmtUnfSF
                   : int
                          150 284 434 540 490 64 317 216 952 140 ...
##
   $ TotalBsmtSF : int 856 1262 920 756 1145 796 1686 1107 952 991 ...
   $ Heating
                   : Factor w/ 6 levels "Floor", "GasA", ...: 2 2 2 2 2 2 2 2 2 2 ...
##
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 1 1 1 3 1 1 1 1 3 1 ...
##
   $ HeatingQC
##
   $ CentralAir
                   : Factor w/ 2 levels "N", "Y": 2 2 2 2 2 2 2 2 2 2 ...
                   : Factor w/ 5 levels "FuseA", "FuseF",...: 5 5 5 5 5 5 5 5 5 2 5 ...
##
   $ Electrical
   $ X1stFlrSF
                          856 1262 920 961 1145 796 1694 1107 1022 1077 ...
                          854 0 866 756 1053 566 0 983 752 0 ...
   $ X2ndFlrSF
##
                   : int
                         0 0 0 0 0 0 0 0 0 0 ...
##
   $ LowQualFinSF : int
                   : int 1710 1262 1786 1717 2198 1362 1694 2090 1774 1077 ...
##
   $ GrLivArea
##
   $ BsmtFullBath : int 1 0 1 1 1 1 1 1 0 1 ...
##
   $ BsmtHalfBath : int
                         0 1 0 0 0 0 0 0 0 0 ...
##
   $ FullBath
                  : int 2 2 2 1 2 1 2 2 2 1 ...
##
   $ HalfBath
                   : int 1010110100...
   $ BedroomAbvGr : int 3 3 3 3 4 1 3 3 2 2 ...
##
##
   $ KitchenAbvGr : int 1 1 1 1 1 1 1 2 2 ...
##
   $ KitchenQual : Factor w/ 4 levels "Ex", "Fa", "Gd", ...: 3 4 3 3 3 4 3 4 4 4 ...
  $ TotRmsAbvGrd : int 8 6 6 7 9 5 7 7 8 5 ...
                   : Factor w/ 7 levels "Maj1", "Maj2",...: 7 7 7 7 7 7 7 7 3 7 ...
##
   $ Functional
   $ Fireplaces
                   : int 0 1 1 1 1 0 1 2 2 2 ...
##
##
   $ FireplaceQu : Factor w/ 5 levels "Ex", "Fa", "Gd",..: NA 5 5 3 5 NA 3 5 5 5 ...
   $ GarageType
                   : Factor w/ 6 levels "2Types", "Attchd", ...: 2 2 2 6 2 2 2 6 2 ...
##
   $ GarageYrBlt : int
                          2003 1976 2001 1998 2000 1993 2004 1973 1931 1939 ...
   $ GarageFinish : Factor w/ 3 levels "Fin", "RFn", "Unf": 2 2 2 3 2 3 2 2 3 2 ...
##
##
   $ GarageCars
                  : int 2 2 2 3 3 2 2 2 2 1 ...
##
   $ GarageArea
                   : int 548 460 608 642 836 480 636 484 468 205 ...
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 2 3 ...
##
   $ GarageQual
##
   $ GarageCond
                   : Factor w/ 5 levels "Ex", "Fa", "Gd", ...: 5 5 5 5 5 5 5 5 5 5 5 ...
                   : Factor w/ 3 levels "N", "P", "Y": 3 3 3 3 3 3 3 3 3 3 ...
##
   $ PavedDrive
   $ WoodDeckSF
                          0 298 0 0 192 40 255 235 90 0 ...
##
                   : int
##
   $ OpenPorchSF
                  : int
                          61 0 42 35 84 30 57 204 0 4 ...
##
   $ EnclosedPorch: int 0 0 0 272 0 0 0 228 205 0 ...
##
  $ X3SsnPorch
                  : int 0 0 0 0 0 320 0 0 0 0 ...
##
   $ ScreenPorch : int
                          0 0 0 0 0 0 0 0 0 0 ...
##
   $ PoolArea
                   : int
                          0 0 0 0 0 0 0 0 0 0 ...
                   : Factor w/ 3 levels "Ex", "Fa", "Gd": NA ...
##
   $ PoolQC
  $ Fence
                   : Factor w/ 4 levels "GdPrv", "GdWo", ...: NA ...
##
  $ MiscFeature : Factor w/ 4 levels "Gar2", "Othr", ...: NA NA NA NA NA 3 NA 3 NA NA ...
##
                   : int 0 0 0 0 0 700 0 350 0 0 ...
   $ MiscVal
##
  $ MoSold
                   : int 2 5 9 2 12 10 8 11 4 1 ...
   $ YrSold
                   : int 2008 2007 2008 2006 2008 2009 2007 2009 2008 2008 ...
                   : Factor w/ 9 levels "COD", "Con", "ConLD", ...: 9 9 9 9 9 9 9 9 9 9 ...
   $ SaleType
   $ SaleCondition: Factor w/ 6 levels "Abnorm1", "AdjLand",..: 5 5 5 1 5 5 5 5 1 5 ...
                   : int 208500 181500 223500 140000 250000 143000 307000 200000 129900 118000 ...
```

At first glance, we see that most of the variables are categorical - both numeric and character types - and only a handful are continuous. The response variable for our analysis is SalePrice, and the remaining 79 variables (excluding the record ID column) are considered potential predictor variables. Checking the data dictionary, we found the following distribution for the predictor variables:

• 49 categorical

- 19 are continuous, e.g. area, price
- 11 are discrete, e.g. count, year

There are 0 duplicate rows in the dataset.

#### Handling NA Values

Below, we compute that number and percentage of NAs per variable in the dataset having at least 1 NA.

Table 1: Variable NA Count and Percentage

Variable	Number of NA	Percentage of NA
PoolQC	1,453	99.52 %
MiscFeature	1,406	96.3~%
Alley	1,369	93.77 %
Fence	1,179	80.75 %
FireplaceQu	690	47.26 %
LotFrontage	259	17.74~%
GarageType	81	5.55~%
GarageYrBlt	81	5.55~%
GarageFinish	81	5.55~%
GarageQual	81	5.55~%
GarageCond	81	5.55~%
BsmtExposure	38	2.6~%
BsmtFinType2	38	2.6~%
BsmtQual	37	2.53 %
BsmtCond	37	2.53 %
BsmtFinType1	37	2.53 %
MasVnrType	8	0.55~%
MasVnrArea	8	0.55~%
Electrical	1	0.07 %

The data dictionary tells us that for most of the fields in Table 1, NA is actually meaningful, indicating non-applicability or a lack of the feature rather than missing data. After checking the data dictionary for the meaning of each field, we imputed - for every categorical variable for which NA was meaningful - NAs with 0s.

```
# Create a copy of rawDF to be our working data frame
housingDF <- rawDF

# Update NAs with Os for applicable fields
levels(housingDF$PoolQC) <- c("0", levels(housingDF$PoolQC))</pre>
```

```
housingDF$PoolQC[is.na(housingDF$PoolQC)] <- "0"</pre>
levels(housingDF$MiscFeature) <- c("0", levels(housingDF$MiscFeature))</pre>
housingDF$MiscFeature[is.na(housingDF$MiscFeature)] <- "0"
levels(housingDF$Alley) <- c("0", levels(housingDF$Alley))</pre>
housingDF$Alley[is.na(housingDF$Alley)] <- "0"</pre>
levels(housingDF$Fence) <- c("0", levels(housingDF$Fence))</pre>
housingDF$Fence[is.na(housingDF$Fence)] <- "0"</pre>
levels(housingDF$FireplaceQu) <- c("0", levels(housingDF$FireplaceQu))</pre>
housingDF$FireplaceQu[is.na(housingDF$FireplaceQu)] <- "0"
levels(housingDF$GarageType) <- c("0", levels(housingDF$GarageType))</pre>
housingDF$GarageType[is.na(housingDF$GarageType)] <- "0"</pre>
levels(housingDF$GarageFinish) <- c("0", levels(housingDF$GarageFinish))</pre>
housingDF$GarageFinish[is.na(housingDF$GarageFinish)] <- "0"</pre>
levels(housingDF$GarageQual) <- c("0", levels(housingDF$GarageQual))</pre>
housingDF$GarageQual[is.na(housingDF$GarageQual)] <- "0"
levels(housingDF$GarageCond) <- c("0", levels(housingDF$GarageCond))</pre>
housingDF$GarageCond[is.na(housingDF$GarageCond)] <- "0"</pre>
levels(housingDF$BsmtExposure) <- c("0", levels(housingDF$BsmtExposure))</pre>
housingDF$BsmtExposure[is.na(housingDF$BsmtExposure)] <- "0"</pre>
levels(housingDF$BsmtFinType2) <- c("0", levels(housingDF$BsmtFinType2))</pre>
housingDF$BsmtFinType2[is.na(housingDF$BsmtFinType2)] <- "0"
levels(housingDF$BsmtQual) <- c("0", levels(housingDF$BsmtQual))</pre>
housingDF$BsmtQual[is.na(housingDF$BsmtQual)] <- "0"
levels(housingDF$BsmtCond) <- c("0", levels(housingDF$BsmtCond))</pre>
housingDF$BsmtCond[is.na(housingDF$BsmtCond)] <- "0"
levels(housingDF$BsmtFinType1) <- c("0", levels(housingDF$BsmtFinType1))</pre>
housingDF$BsmtFinType1[is.na(housingDF$BsmtFinType1)] <- "0"
```

We then re-check the count and percentage of NAs per variable left in the dataset.

Table 2: Variable NA Count and Percentage(after replacing NAs with 0s, where appropriate)

Variable	Number of NA	Percentage of NA
LotFrontage	259	17.74 %
GarageYrBlt	81	5.55~%
MasVnrType	8	0.55~%
MasVnrArea	8	0.55~%
Electrical	1	0.07 %

#### colnames(housingDF)

```
[1] "Id"
                         "MSSubClass"
##
                                          "MSZoning"
                                                           "LotFrontage"
##
    [5] "LotArea"
                         "Street"
                                          "Alley"
                                                           "LotShape"
  [9] "LandContour"
                         "Utilities"
                                          "LotConfig"
                                                           "LandSlope"
                                                           "BldgType"
## [13] "Neighborhood"
                         "Condition1"
                                          "Condition2"
## [17] "HouseStyle"
                         "OverallQual"
                                          "OverallCond"
                                                           "YearBuilt"
## [21] "YearRemodAdd"
                         "RoofStyle"
                                          "RoofMatl"
                                                           "Exterior1st"
## [25] "Exterior2nd"
                         "MasVnrType"
                                          "MasVnrArea"
                                                           "ExterQual"
## [29] "ExterCond"
                         "Foundation"
                                          "BsmtQual"
                                                           "BsmtCond"
## [33] "BsmtExposure"
                         "BsmtFinType1"
                                          "BsmtFinSF1"
                                                           "BsmtFinType2"
## [37] "BsmtFinSF2"
                         "BsmtUnfSF"
                                          "TotalBsmtSF"
                                                           "Heating"
                                                           "X1stFlrSF"
## [41] "HeatingQC"
                         "CentralAir"
                                          "Electrical"
## [45] "X2ndFlrSF"
                         "LowQualFinSF"
                                          "GrLivArea"
                                                           "BsmtFullBath"
## [49] "BsmtHalfBath"
                         "FullBath"
                                          "HalfBath"
                                                           "BedroomAbvGr"
## [53] "KitchenAbvGr"
                         "KitchenQual"
                                          "TotRmsAbvGrd"
                                                           "Functional"
## [57] "Fireplaces"
                         "FireplaceQu"
                                          "GarageType"
                                                           "GarageYrBlt"
## [61] "GarageFinish"
                         "GarageCars"
                                          "GarageArea"
                                                           "GarageQual"
## [65] "GarageCond"
                         "PavedDrive"
                                          "WoodDeckSF"
                                                           "OpenPorchSF"
                         "X3SsnPorch"
                                          "ScreenPorch"
                                                           "PoolArea"
## [69] "EnclosedPorch"
## [73] "PoolQC"
                                                           "MiscVal"
                         "Fence"
                                          "MiscFeature"
## [77] "MoSold"
                         "YrSold"
                                          "SaleType"
                                                           "SaleCondition"
## [81] "SalePrice"
```

Table 2 shows the list of remaining variables where NA indicates missing data. We impute NAs in these variables with

- mean of the data, for continuous variables (LotFrontage)
- median of the data, for discrete variables (GarageYrBlt)
- mode of the data, for categorical variables (MasVnrType, Electrical)

```
# Function to get mode of data
getmode <- function(v) {</pre>
    uniqv <- unique(v)</pre>
    uniqv[which.max(tabulate(match(v, uniqv)))]
}
# Impute NAs
housingDF$LotFrontage[is.na(housingDF$LotFrontage)] <- mean(housingDF$LotFrontage,
    na.rm = T)
housingDF$GarageYrBlt[is.na(housingDF$GarageYrBlt)] <- median(housingDF$GarageYrBlt,
    na.rm = T)
housingDF$MasVnrType[is.na(housingDF$MasVnrType)] <- getmode(housingDF$MasVnrType)
housingDF$MasVnrArea[is.na(housingDF$MasVnrArea)] <- 0
housingDF$Electrical[is.na(housingDF$Electrical)] <- getmode(housingDF$Electrical)
# Convert MSSubClass to factor
housingDF$MSSubClass <- factor(housingDF$MSSubClass)</pre>
housingDF$MoSold <- factor(housingDF$MoSold)</pre>
```

Since Masonry veneer area (MasVnrArea) is directly related to MasVnrType, we impute for area based on the mode of MasVnrType, which is None. Our cleaned dataset is named housingDF.

#### **Exploratory Data Visualization**

With our clean dataset, we perform exploratory data visualization of the distribution of key measures such as volume and sale price of houses by what we hypothesize to be key predictor variables.

To begin with, we check the distribution of sale prices using a histogram and box-plot.

```
# hist(housingDF$SalePrice, main = 'Histogram of Sale Price')
# boxplot(housingDF$SalePricem, main = 'Boxplot of Sale Price')
summary(housingDF$SalePrice)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 34900 129975 163000 180921 214000 755000
```

Intuition suggests the neighborhood is a key determining factor in a house's sale price, hence below, we plot the distribution of sale price by neighborhood.

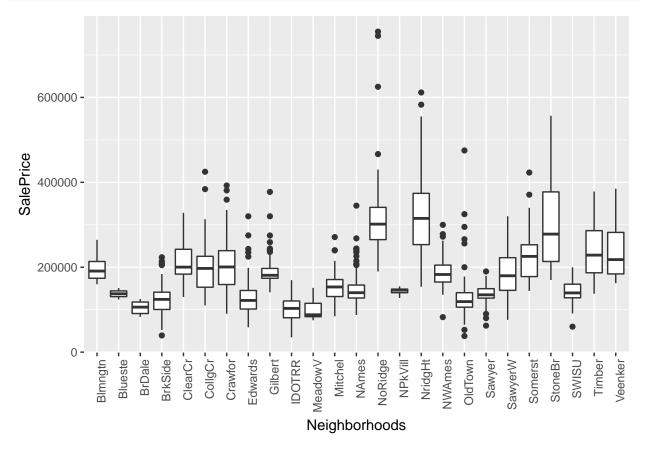


Figure 1: SalePrice distribution per neighborhood

From Figure 1, we can observe that Brookside and Meadow Vista have the lowest median house price while Northridge and Northridge Height have the heighest median house price as well as several outliers.

We then distribution of houses by a number of key features we hypothesize to be important in determining housing price: the property's zoning class (MSZoning), type of road access to the property (Street), type of alley access to the property (Alley), and type of utilies available (Utilities)

```
plotHist <- function(data_in, i) {
   data <- data.frame(x = data_in[[i]])</pre>
```

```
p <- ggplot(data = data, aes(x = factor(x))) + stat_count() +</pre>
        xlab(colnames(data_in)[i]) + theme_light() + theme(axis.text.x = element_text(angle = 90,
        hjust = 1)
    return(p)
}
doPlots <- function(data_in, fun, ii, ncol = 3) {</pre>
    pp <- list()</pre>
    for (i in ii) {
        p <- fun(data_in = data_in, i = i)</pre>
        pp \leftarrow c(pp, list(p))
    do.call("grid.arrange", c(pp, ncol = ncol))
}
plotDen <- function(data_in, i) {</pre>
    data <- data.frame(x = data_in[[i]], SalePrice = data_in$SalePrice)</pre>
    p <- ggplot(data = data) + geom_line(aes(x = x), stat = "density",</pre>
        size = 1, alpha = 1) + xlab(paste0((colnames(data_in)[i]),
        "\n", "Skewness: ", round(skewness(data_in[[i]], na.rm = TRUE),
            2))) + theme_light()
    return(p)
}
plotCorr <- function(data in, i) {</pre>
    data <- data_frame(x = data_in[[i]], SalePrice = data_in$SalePrice)</pre>
    p <- ggplot(data, aes(x = x, y = SalePrice)) + geom_point(na.rm = TRUE) +</pre>
        geom_smooth(method = lm) + xlab(paste0(colnames(data_in)[i],
        "\n", "R-Squared: ", round(cor(data_in[[i]], data$SalePrice,
            use = "complete.obs"), 2))) + theme_light()
    return(suppressWarnings(p))
}
doPlots(housingDF, fun = plotHist, ii = c(3, 6, 7, 10), ncol = 2)
```

We also plot the distribution of houses against a number of features related to the physical geography of the property:

```
doPlots(housingDF, fun = plotHist, ii = c(8, 9, 11, 12), ncol = 2)
```

Figure 2 suggests that most of the houses are located in Medium/Low Density residential areas. We can also observe that most of the houses have paved road access, do not have alleys and have all public utilities(E,G,W,&S). From Figure ??{fig:hist2}, we can notice that most of the properties are regular or slightly irregular in share, built on level surfaces with gentle slope.

```
housingDF %>% dplyr::select(LandSlope, Neighborhood) %>% arrange(Neighborhood) %>%
    group_by(Neighborhood, LandSlope) %>% summarize(Count = n()) %>%
    ggplot(aes(Neighborhood, Count)) + geom_bar(aes(fill = LandSlope),
    position = "dodge", stat = "identity") + theme(axis.text.x = element_text(angle = 90,
    hjust = 1))
```

From Figure ??{fig:hist3}, we can see that houses with severe slope are located only in Clear Creek and Timberland while more than 10 neighborhoods have properties with moderate slope.

```
num_var <- names(housingDF)[which(sapply(housingDF, is.numeric))]
housing_numeric <- housingDF[num_var]</pre>
```

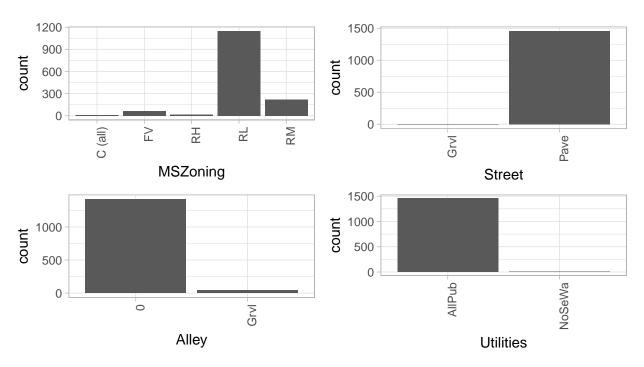


Figure 2: Locality, access, utility features distribution

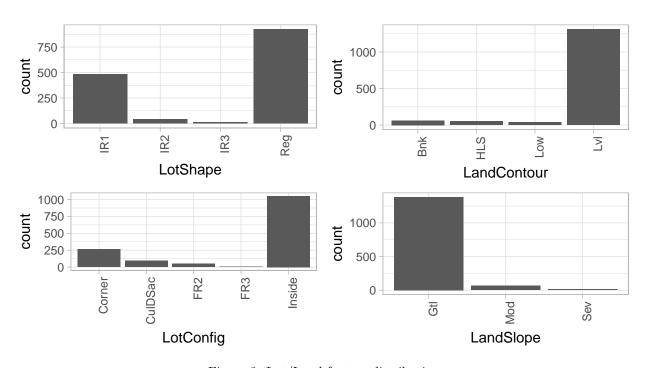


Figure 3: Lot/Land feature distribution

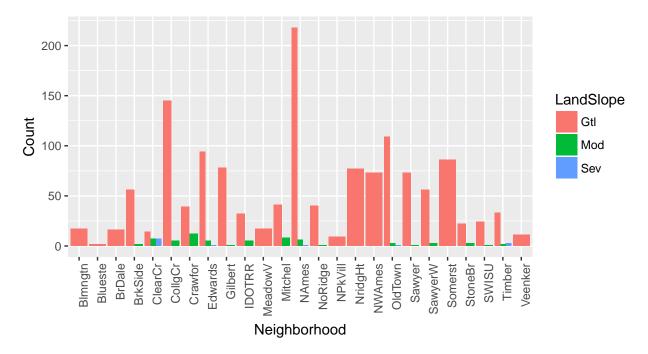


Figure 4: Neighborhood level slope distribution

## Task 1. Building the Explanatory Model

#### Testing for Influential Points

Having dealt with the NAs in our dataset, we use the model.matrix() function from the glmnet package to convert each categorical variable into an appropriate set of binary indicators: for a categorical variable that takes k levels, model.matrix() produces k-1 binary indicators. We then reappend our response vector SalePrice to the resulting wide design matrix designDF to create workingDF, which includes both the converted predictors and response variables.

```
designDF <- model.matrix(SalePrice ~ ., data = housingDF)[, -1]
designDF <- as.data.frame(designDF)
workingDF <- cbind(designDF, SalePrice = housingDF$SalePrice)</pre>
```

In looking for influential points, we leverage the OLSRR package to test observations for influence according to the DFFITS diagnostic. We do this by first fitting a saturated model on workingDF and then calling ols\_dffits\_plot() on it.

```
ols_model <- lm(SalePrice ~ ., data = workingDF)
ols_dffits_plot(ols_model)</pre>
```

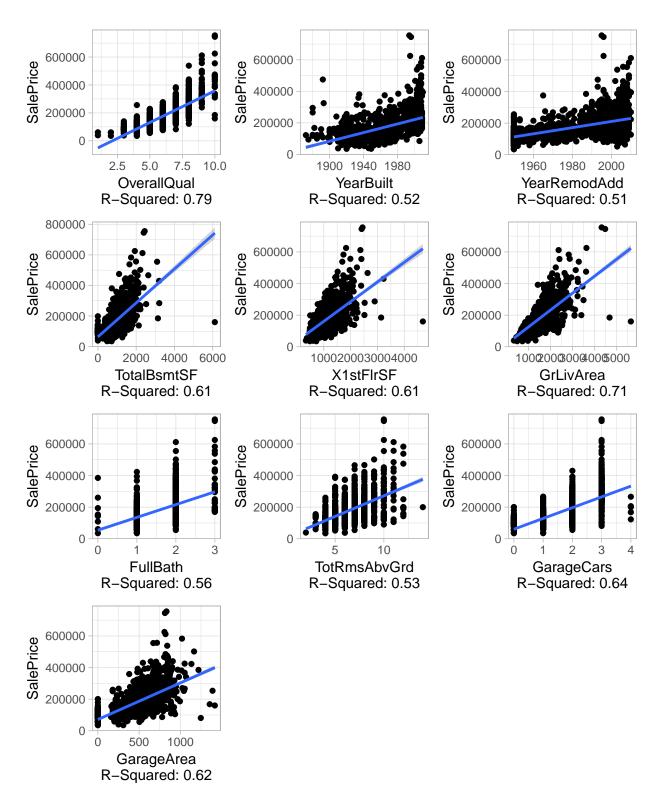
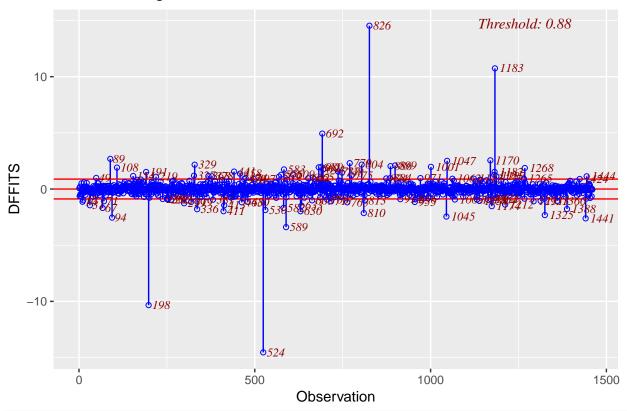


Figure 5: Scatter plot of variables showing linear relationship with SalePrice

## Influence Diagnostics for SalePrice

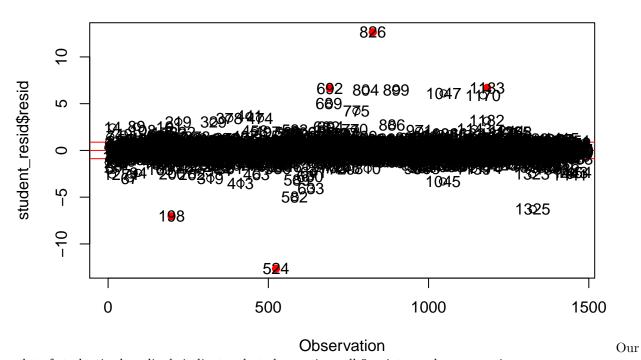


```
# identify threshold t for points of influence
n = nrow(workingDF)
p = ncol(workingDF - 1) # remove response var
t = 2 * sqrt(p/n)
```

Note that according to the criterion of threshold t = 2\*sqrt(n/p) = 0.85, the DFFITS plot shows a large number of influential observations. We look specifically at 6 points greater than threshold = abs(5): 198, 524, 692, 826 and 1183. Below we plot the standardized and studentized residuals to check these observations for being outliers and/or points of leverage respectively.

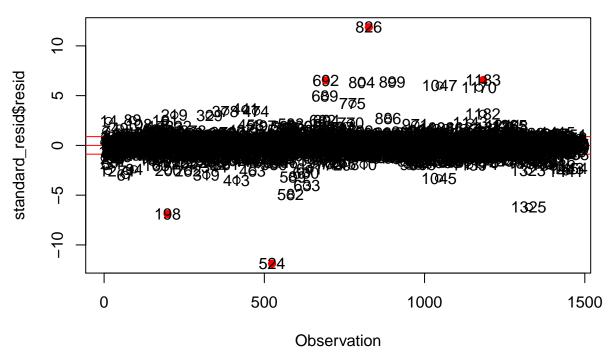
```
# Creating from scratch because OLSRR ols_srsd_plot() function is
# not working.
# Create df of studentized residuals
student_resid <- as.data.frame(rstudent(ols_model))</pre>
student_resid <- setDT(student_resid, keep.rownames = TRUE)[]</pre>
colnames(student_resid) <- c("ix", "resid")</pre>
# Plot
plot(student_resid$ix, student_resid$resid, col = ifelse(workingDF$Id ==
    198 | workingDF$Id == 524 | workingDF$Id == 692 | workingDF$Id ==
    826 | workingDF$Id == 1183, "red", "black"), pch = ifelse(workingDF$Id ==
    198 | workingDF$Id == 524 | workingDF$Id == 692 | workingDF$Id ==
    826 | workingDF$Id == 1183, 19, 1), main = "Plot of Studentized Residuals",
    xlab = "Observation")
abline(h = t, col = "red")
abline(h = 0, col = "red")
abline(h = -t, col = "red")
```

## **Plot of Studentized Residuals**



plot of studentized resdiuals indicates that observations all 5 points are leverage points.

## Plot of Standardized Residuals



Our plots of studentized and standardized resdiulds indicate that all 5 observations are both points of leverage and outliers. We remove them from our dataset and recreate the saturated OLS model below:

```
# remove influential points
workingDF <- filter(workingDF, !Id %in% c(198, 524, 692, 826, 1183))
# nrow(workingDF) #1455

# recreate model
ols_model <- lm(SalePrice ~ ., data = workingDF)</pre>
```

For the purposes of variable selection, we refer to the saturated OLS model created above and perform stepwise model selection according to both AIC and BIC criterions.

Per the AIC criterion, the following are the predictor variables signficant at the alpha = 0.05 level.

```
# load('/Users/booranium/usf/601_regression/project/IowaHousing/AIC_model.rda')
# # model loaded as 'model_aic'
load("/Users/santhoshhari/Documents/Coursework/LinearRegression/IowaHousing/AIC_model.rda") # model lo
# Find coefficients significant at the alpha = 0.01 level
bool_aic <- summary(model_aic)$coeff[-1, 4] < 0.01
sig_var_aic <- names(bool_aic)[bool_aic == TRUE]
length(sig_var_aic)</pre>
```

```
## [1] 75
```

Per the BIC criterion, the following are the predictor variables signficant at the alpha = 0.05 level.

```
# load('/Users/booranium/usf/601_regression/project/IowaHousing/BIC_model.rda')
# # model loaded as 'model_bic'
load("/Users/santhoshhari/Documents/Coursework/LinearRegression/IowaHousing/BIC_model.rda")
# find coefficients significant at the alpha = 0.01 level
bool_bic <- summary(model_aic)$coeff[-1, 4] < 0.01
sig_var_bic <- names(bool_bic)[bool_bic == TRUE]</pre>
```

# model lo

Note that both criterions select the same set of variables.

```
setdiff(sig_var_aic, sig_var_bic)
```

#### ## character(0)

We can now perform OLS regression with our subset of 75 significant variables. The model summary is as follows:

We check for multicollinearity in our model by checking for Variance Inflation Factors:

```
vif(model_sig_scaled)[(sqrt(vif(model_sig_scaled)) > 10) == TRUE]
```

```
## GarageQualPo GarageCondPo
## 184.2926 171.8100
```

We see that there are two variables with VIF values > threshold = 10. This tells us there is multicollinearity present in the dataset. We verify this by checking the Singular Value Criteria for multicollinearity:

```
coll_out = colldiag(model_sig, scale = TRUE, center = FALSE, add.intercept = TRUE)
coll_out$condindx[(coll_out$condindx > 30) == TRUE]
```

```
## [1] 32.49461 36.98012 41.51708 50.60676 56.13318 71.42520
## [7] 93.12395 271.11407 306.50195 915.64842 1232.96408
```

We see that there are several entries > threshold = 30, and hence we conclude that multicollinearity exists. In order to identify which variables are multicollinear:

```
coll_out = colldiag(model_sig, scale = TRUE, center = FALSE, add.intercept = TRUE)
unlist(coll_out[1], use.names = F) > 30
```

```
## [1] FALSE FALSE
```

```
colnames(coll_out$pi)[unlist(coll_out[1], use.names = F) > 30]
##
    [1] "GarageQualGd"
                                 "GarageQualPo"
                                                        "GarageCondEx"
##
    [4] "GarageCondFa"
                                 "GarageCondGd"
                                                         "GarageCondPo"
   [7] "WoodDeckSF"
                                "ScreenPorch"
                                                         "PoolArea"
## [10] "SaleTypeNew"
                                "SaleConditionNormal"
dim(as.matrix(coll_out$pi[unlist(coll_out[1], use.names = F) > 30,
    ]))
## [1] 11 76
# 11 variabels with pi > 30
pi = coll_out$pi[unlist(coll_out[1], use.names = F) > 30, ]
pi[pi < 0.75] <- NA
рi
##
         intercept MSSubClass120 MSSubClass160 MSZoningFV MSZoningRH
    [1,]
##
                 NA
                                NA
                                                NA
                                                           NA
##
    [2,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
   [3,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
##
   [4,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
##
   [5,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
    [6,]
##
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
##
   [7,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
##
   [8,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
##
    [9,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
## [10,]
                 NA
                                NA
                                                NA
                                                            NA
                                                                       NA
   [11,] 0.9912576
                                NA
                                                NA
                                                            NA
                                                                       NA
##
##
         MSZoningRL MSZoningRM LotArea StreetPave LandContourLow
##
    [1,]
                  NA
                              NA
                                       NA
                                                   NA
##
    [2,]
                              NA
                                       NA
                                                   NA
                                                                   NA
                  NA
   [3,]
##
                  NA
                              NA
                                       NA
                                                   NA
                                                                   NA
##
   [4,]
                  NA
                              NA
                                       NA
                                                   NA
                                                                   NA
##
    [5,]
                  NA
                              NA
                                       NA
                                                   NA
                                                                   NA
##
   [6,]
          0.8622203
                                       NA
                                                   NA
                                                                   NA
                      0.8254915
    [7,]
                  NA
                              NA
                                       NA
                                           0.9470744
                                                                   NA
##
    [8,]
                  NA
                              NA
                                       NA
                                                                   NA
                                                   NA
##
    [9,]
                  NA
                              NA
                                       NA
                                                   NA
                                                                   ΝA
## [10,]
                              NA
                                       NA
                                                   NA
                  NA
                                                                   NA
## [11,]
                  NA
                              NA
                                       NA
                                                   NA
                                                                   NΑ
##
         LotConfigCulDSac LandSlopeSev NeighborhoodCollgCr
##
    [1,]
                         ΝA
                                       NA
##
   [2,]
                         ΝA
                                       NA
                                                             NA
##
   [3,]
                         NA
                                       NA
                                                            NA
##
   [4,]
                                       NA
                         NA
                                                            NA
##
   [5,]
                         NA
                                       NA
                                                            NA
   [6,]
##
                         NA
                                       NA
                                                            NA
##
   [7,]
                         NA
                                       NA
                                                            NA
##
    [8,]
                         NA
                                       NA
                                                            NA
  [9,]
                         NA
                                       NA
                                                            NA
##
## [10,]
                         NA
                                       NA
                                                            NA
## [11,]
                         NA
                                       NA
         NeighborhoodCrawfor NeighborhoodEdwards NeighborhoodGilbert
```

##	[1,]	NA		N	Δ	NA		
##	[2,]			N		NA NA		
##	[3,]	NA NA		N	NA			
		NA NA		N	NA			
##	[4,]							
##	[5,]	NA		N		NA		
##	[6,]	NA NA		N		NA		
##	[7,]	NA		N		NA		
##	[8,]	NA		N		NA		
##	[9,]	NA		N		NA		
##	[10,]	NA			A	NA		
##	[11,]	NA		N		NA		
##	F4 7	NeighborhoodMitchel	Nei	-	Neighborhoo	<u>.                                    </u>		
##	[1,]	NA		NA		NA		
##	[2,]	NA		NA		NA		
##	[3,]	NA		NA		NA		
##	[4,]	NA		NA		NA		
##	[5,]	NA		NA		NA		
##	[6,]	NA		NA		NA		
##	[7,]	NA		NA		NA		
##	[8,]	NA		NA		NA		
##	[9,]	NA		NA		NA		
##	[10,]	NA		NA		NA		
##	[11,]	NA		NA		NA		
##		${\tt NeighborhoodNridgHt}$	Neig	=	_			
##	[1,]	NA		NA		NA		
##	[2,]	NA		NA		NA		
##	[3,]	NA		NA		NA		
##	[4,]	NA		NA		NA		
##	[5,]	NA		NA		NA		
##	[6,]			NA		NA		
##	[7,]			NA		NA		
##	[8,]			NA		NA		
##	[9,]	NA	NA			NA		
##	[10,]	NA		NA		NA		
##	[11,]	NA		NA		NA		
##		${\tt NeighborhoodStoneBr}$	Cond	dition1Norm Con	dition1RRAe	Condition2RRAe		
##	[1,]	NA		NA	NA	NA		
##	[2,]	NA		NA	NA	NA		
##	[3,]	NA		NA	NA	NA		
##	[4,]	NA		NA	NA	NA		
##	[5,]	NA		NA	NA	NA		
##	[6,]	NA		NA	NA	NA		
##	[7,]	NA		NA	NA	NA		
##	[8,]	NA		NA	NA	NA		
##	[9,]	NA		NA	NA	NA		
##	[10,]	NA		NA	NA	NA		
##	[11,]	NA		NA	NA	NA		
##		OverallQual Overall				-		
##	[1,]	NA	NA	NA	NA	NA		
##	[2,]	NA	NA	NA	NA	NA		
##	[3,]	NA	NA	NA	NA	NA		
##	[4,]	0.8455787	NA	NA	NA	NA		
##	[5,]	NA	NA	NA	NA	NA		
##	[6,]	NA	NA	NA	NA	NA		

```
[7,]
                    NA
                                  NA
                                             NA
                                                            NA
                                                                            NA
    [8,]
##
                    NA
                                  NΑ
                                             NΑ
                                                            NΑ
                                                                            NΑ
    [9,]
                    NA
                                             NA
                                                                            NA
##
                                  NA
                                                            NA
## [10,]
                    NA
                                  NA
                                             NA
                                                            NA
                                                                            NA
##
   [11,]
                                  NA
                                             NA
                                                                            NA
##
          RoofMatlCompShg RoofMatlMembran RoofMatlMetal RoofMatlRoll
##
    [1,]
    [2,]
##
                         NA
                                           NA
                                                           NA
                                                                          NΑ
    [3,]
##
                         NA
                                           NA
                                                           NA
                                                                          NA
##
   [4,]
                         NA
                                           NA
                                                           NA
                                                                          NA
    [5,]
                         NA
                                           NA
                                                           NA
                                                                          NA
##
                         NA
                                           NA
                                                           NA
                                                                          NA
    [6,]
    [7,]
                         NA
                                                                          NA
                                           NA
                                                           NA
   [8,]
                                                                          NA
##
                 0.9365405
                                           NA
                                                           NA
##
   [9,]
                         NA
                                           NA
                                                           NA
                                                                          NA
## [10,]
                         NA
                                           NA
                                                           NA
                                                                          NA
##
   [11,]
                         NA
                                           NA
                                                           NA
                                                                          NA
##
          RoofMatlTar&Grv
                            RoofMatlWdShake RoofMatlWdShngl Exterior1stBrkFace
##
    [1,]
                         NA
                                           NA
                                                             NA
    [2,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
##
##
    [3,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
##
   [4,]
                         NA
                                                                                   NA
##
   [5,]
                        NA
                                           NA
                                                             NA
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##
    [6,]
                         NA
                                           NA
                                                                                   NA
##
   [7,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
    [8,]
                 0.8711354
                                   0.7908965
                                                     0.8161536
                                                                                   NA
##
    [9,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
## [10,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
##
  [11,]
                         NA
                                           NA
                                                             NA
                                                                                   NA
##
          Exterior1stWd Sdng Exterior2ndWd Sdng MasVnrTypeStone MasVnrArea
    [1,]
##
                            NA
                                                  NA
                                                                    NA
##
    [2,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
    [3,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
   [4,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
                            NA
    [5,]
                                                  NA
                                                                    NA
                                                                                 NA
##
    [6,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
    [7,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
    [8,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NΑ
                            NA
##
    [9,]
                                                  NA
                                                                    NA
                                                                                 NA
##
  [10,]
                            NA
                                                  NA
                                                                    NA
                                                                                 NA
##
   [11,]
          ExterQualGd ExterQualTA BsmtQualEx BsmtQualFa BsmtQualGd
##
##
    [1,]
                    NA
                                  NA
                                              NA
                                                           NA
##
    [2,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
    [3,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
##
    [4,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
##
    [5,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
##
   [6,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
    [7,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
##
    [8,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
##
   [9,]
                    NA
                                  NA
                                              NA
                                                           NA
                                                                       NA
## [10,]
                    NA
                                  NA
                                              NA
                                                           NA
## [11,]
                    NA
                                  NA
                                              NA
                                                           NA
          BsmtExposureAv BsmtFinType1BLQ BsmtFinSF1 BsmtFinSF2 BsmtUnfSF
##
```

	F4 7		37.4		37.4		3.T.A	37			3.T. A
##	[1,]		NA		NA		NA	NA			NA
##	[2,]		NA		NA		NA	NA			NA
##	[3,]		NA		NA		NA	NA			NA
##	[4,]		NA		NA		NA	NA			NA
##	[5,]		NA		NA		NA	NA			NA
##	[6,]		NA		NA		NA	NA			NA
##	[7,]		NA		NA		NA	NA			NA
##	[8,]		NA		NA		NA	NA			NA
##	[9,]		NA		NA		NA	NA			NA
##	[10,]		NA		NA		NA	NA			NA
##	[11,]		NA		NA		NA	NA			NA
##		X1stFlrSF X2		Bedroo		Kitche		Kitche	enQua		
##	[1,]	NA	NA		NA		NA			NA	
##	[2,]	NA	NA		NA		NA			NA	
##	[3,]	NA	NA		NA		NA			NA	
##	[4,]	NA	NA		NA		NA			NA	
##	[5,]	NA	NA		NA		NA			NA	
##	[6,]	NA	NA		NA		NA			NA	
##	[7,]	NA	NA		NA		NA			NA	
##	[8,]	NA	NA		NA		NA			NA	
##	[9,]	NA	NA		NA		NA			NA	
##	[10,]	NA	NA		NA		NA			NA	
##	[11,]	NA	NA		NA		NA			NA	
##		KitchenQualG	d Kitche	enQualT	'A TotRr	nsAbvGı	d Func	tional	Гур (	arag	eCars
##	[1,]	N	ΙA	N	Α	1	JA		NA		NA
##	[2,]	N	ΙA	N	Α	1	JA		NA		NA
##	[3,]	N	ΙA	N	Α	1	JA		NA		NA
##	[4,]	N	ΙA	N	Α	1	JA		NA		NA
##	[5,]	N	ΙA	N	(A )	.772008	31		NA		NA
##	[6,]	N	ΙA	N	Α	1	JA		NA		NA
##	[7,]	N	ΙA	N	Α	1	JA		NA		NA
##	[8,]	N	ΙA	N	Α	1	JA		NA		NA
##	[9,]	N	ΙA	N	Α	1	JA		NA		NA
##	[10,]	N	ΙA	N	Α	1	JA		NA		NA
##	[11,]	N	ΙA	N	A	1	JA.		NA		NA
##		GarageQualEx	Garage	QualFa	Garage	QualGd	Garage	QualPo	Gara	ageCo	ndEx
##	[1,]	NA	1	NA		NA		NA			NA
##	[2,]	NA	1	NA		NA		NA			NA
##	[3,]	NA	1	NA		NA		NA			NA
##	[4,]	NA	L	NA		NA		NA			NA
##	[5,]	NA	L	NA		NA		NA			NA
##	[6,]	NA	L	NA		NA		NA			NA
##	[7,]	NA		NA		NA		NA			NA
##	[8,]	NA		NA		NA		NA			NA
##	[9,]	0.9655115		307149		NA	0.98	362853	(	.959	
##	[10,]	NA		NA		NA		NA			NA
##	[11,]	NA		NA		NA		NA			NA
##	_ ,_	GarageCondFa			Garage		WoodDe		creer	Porc	
##	[1,]	NA	_	NA		NA		NA		N	
##	[2,]	NA		NA		NA		NA			A
##	[3,]	NA		NA		NA		NA			A
##	[4,]	NA		NA		NA		NA			A
##	[5,]	NA		NA		NA		NA		N	
##	[6,]	NA		NA		NA		NA		N	
••	,1	232.									

```
[7,]
##
                     NA
                                    NA
                                                   NA
                                                               NA
                                                                             NA
##
    [8,]
                     NΑ
                                    NΑ
                                                   NΑ
                                                               NΑ
                                                                             NΑ
##
    [9,]
              0.898874
                            0.8206515
                                           0.9873676
                                                               NA
                                                                             NA
## [10,]
                     NA
                                    NA
                                                   NA
                                                               NA
                                                                             NA
##
   [11,]
                     NA
                                    NA
                                                   NA
                                                               NA
                                                                             NA
          PoolArea SaleTypeNew SaleConditionNormal
##
    [1,]
##
                NA
                              NA
    [2,]
##
                NA
                              NA
                                                     NA
##
    [3,]
                NA
                              NA
                                                     NA
##
   [4,]
                                                     NA
                NA
                              NA
##
   [5,]
                NA
                              NA
                                                     NA
##
   [6,]
                 NA
                                                     NA
                              NA
##
   [7,]
                NA
                              NA
                                                     NA
##
   [8,]
                 NA
                              NA
                                                     NA
## [9,]
                NA
                              NA
                                                     NA
## [10,]
                 NA
                              NA
                                                     NA
## [11,]
                              NA
                                                     NA
                NA
```

Based on results, we drop the Garage Condition variables since they are collinear with the Garage Quality variables.

```
# Drop GarageCondition variables since they are correlated with
# Garage Quality variables
drop = c("GarageCondEx", "GarageCondFa", "GarageCondGd", "GarageCondPo")
new_sig_var_bic = sig_var_bic[!sig_var_bic %in% drop]
```

We then rerun the model and recheck for multicollinearity using VIFS:

## named numeric(0)

Using our rule of thumb, we conclude that there is no more multicollinearity in our model since there are no VIF values > 10. We print the summary of our model below:

```
summary(new_model)
```

```
##
## Call:
## lm(formula = new_model_formula, data = workingDF)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                         Max
  -131485
           -10264
##
                          0
                              10154
                                     141543
##
## Coefficients:
                               Estimate
                                             Std. Error t value
                         -1501264.91302
                                           112244.24739 -13.375
## (Intercept)
```

	MSSubClass120	-16220.08951	2850.38356	-5.690
	MSSubClass160	-22075.21962	3347.75394	-6.594
	MSZoningFV	38156.25052	8036.88635	4.748
	MSZoningRH	19652.20647	8926.62798	2.202
	MSZoningRL	23371.47826	7386.62559	3.164
	MSZoningRM	19051.08011	7420.13904	2.567
	LotArea	0.75227	0.08234	9.137
	StreetPave	38663.50280 -10195.83610	9376.39492 4254.25975	4.123 -2.397
	LandContourLow	8779.72336	2388.54431	3.676
##	LotConfigCulDSac	-41595.28359	8804.48586	-4.724
##	LandSlopeSev NeighborhoodCollgCr	258.49691	2358.95728	0.110
##	NeighborhoodCrawfor	19613.85511	3417.66256	5.739
##	NeighborhoodEdwards	-8495.28154	2511.56384	-3.382
##	NeighborhoodGilbert	-2895.07052	3018.05498	-0.959
##	NeighborhoodMitchel	-13388.23766	3378.24743	-3.963
##	NeighborhoodNAmes	-8194.95954	2039.33105	-4.018
##	NeighborhoodNoRidge	27488.21640	4167.77030	6.595
##	NeighborhoodNridgHt	19051.93042	3380.96462	5.635
##	NeighborhoodNWAmes	-12512.36145	2915.34823	-4.292
##	NeighborhoodOldTown	-5529.93302	2983.95330	-1.853
##	NeighborhoodStoneBr	40921.72927	4719.78982	8.670
##	Condition1Norm	6622.88542	1762.88860	3.757
	Condition1RRAe	-17398.07438	6705.93805	-2.594
	Condition2RRAe	-95060.05239	33065.48249	-2.875
##	OverallQual	6688.31950	804.96840	8.309
##	OverallCond	5355.15268	668.09521	8.016
##	YearBuilt	312.30718	46.27090	6.750
##	YearRemodAdd	108.54151	44.41420	2.444
##	RoofStyleShed	64239.54318	25119.21237	2.557
##	RoofMatlCompShg	647160.04869	26054.58228	24.839
##	RoofMatlMembran	721671.17292	35301.90723	20.443
##	RoofMatlMetal	690777.89068	35169.27755	19.642
##	RoofMatlRoll	634745.46777	33587.18762	18.898
##	`RoofMatlTar&Grv`	637476.78963	26681.46875	23.892
##	RoofMatlWdShake	641591.64489	28100.88317	22.832
	RoofMatlWdShngl	683006.14049	27586.87806	24.758
##	Exterior1stBrkFace	16337.84226	3365.15389	4.855
	`Exterior1stWd Sdng`	-7630.98849	3370.11676	-2.264
	`Exterior2ndWd Sdng`	7733.43621	3344.56420	2.312
	MasVnrTypeStone	7204.58508	2323.17645	3.101
	MasVnrArea	12.07108	3.97553	
	ExterQualGd	-20087.06918	3524.14146	-5.700
	ExterQualTA	-22829.76580	3712.79583	-6.149
	BsmtQualEx	-12273.92721	4728.68724	
	BsmtQualFa	-20428.76983	2476.52955	-8.249
	BsmtQualGd	-16048.79772	2840.07243	-5.651
	BsmtExposureAv	19595.59377	2273.19595	8.620
	BsmtFinType1BLQ	4137.92986	1750.48172	2.364
	BsmtFinSF1	37.75769	3.05222	12.371
	BsmtFinSF2	25.80156	4.40669	5.855
	BsmtUnfSF X1stFlrSF	22.51566 52.28720	2.93701	7.666
	X2ndFlrSF	52.28720 56.91686	3.81987 2.79574	13.688 20.358
##	V7II(IL II OL	50.91000	2.19014	20.338

```
## BedroomAbvGr
                            -6118.75256
                                             1094.29142
                                                         -5.592
## KitchenAbvGr
                                             3016.82367
                                                         -8.419
                           -25400.14493
## KitchenQualFa
                           -19644.45816
                                             4918.27287
                                                         -3.994
## KitchenQualGd
                           -22306.88810
                                             2943.12682
                                                         -7.579
## KitchenQualTA
                           -22836.34400
                                             3323.75948
                                                         -6.871
## TotRmsAbvGrd
                             2483.27537
                                              782.09095
                                                          3.175
## FunctionalTyp
                                             2469.94324
                                                          5.998
                            14814.79638
## GarageCars
                             9240.14566
                                             1288.45962
                                                          7.171
  GarageQualEx
                           -15039.17858
                                             4315.98810
                                                         -3.485
## GarageQualFa
                            -1456.50341
                                             6588.04379
                                                         -0.221
## GarageQualGd
                           -16857.98707
                                            12738.07414
                                                         -1.323
## GarageQualPo
                                                         -3.144
                           -10156.77637
                                             3230.28881
  WoodDeckSF
                               15.11486
                                                4.93408
                                                          3.063
## ScreenPorch
                                                          4.029
                               41.82895
                                               10.38260
## PoolArea
                                                          2.650
                               46.54277
                                               17.56247
  SaleTypeNew
                            22639.33785
                                             3056.75435
                                                          7.406
## SaleConditionNormal
                                             1988.58730
                             6635.61415
                                                          3.337
##
                                     Pr(>|t|)
   (Intercept)
                         < 0.0000000000000000 ***
##
## MSSubClass120
                         0.000000015441952884 ***
## MSSubClass160
                         0.000000000060744262 ***
## MSZoningFV
                         0.000002271756534403 ***
## MSZoningRH
                                     0.027863 *
## MSZoningRL
                                     0.001590 **
## MSZoningRM
                                     0.010348 *
## LotArea
                         < 0.0000000000000000 ***
## StreetPave
                         0.000039538361591505 ***
## LandContourLow
                                     0.016679 *
## LotConfigCulDSac
                                     0.000246 ***
## LandSlopeSev
                         0.000002543849781085 ***
   NeighborhoodCollgCr
                                     0.912758
  NeighborhoodCrawfor
                         0.00000011688777608 ***
   NeighborhoodEdwards
                                     0.000738 ***
  NeighborhoodGilbert
                                     0.337600
   NeighborhoodMitchel
                         0.000077768287814754 ***
                         0.000061736078775388 ***
  NeighborhoodNAmes
   NeighborhoodNoRidge
                         0.000000000060196556 ***
## NeighborhoodNridgHt
                         0.000000021177336753 ***
## NeighborhoodNWAmes
                         0.000018948718917523 ***
## NeighborhoodOldTown
                                     0.064063 .
## NeighborhoodStoneBr
                         < 0.000000000000000 ***
## Condition1Norm
                                     0.000179 ***
  Condition1RRAe
                                     0.009575 **
## Condition2RRAe
                                     0.004103 **
                         0.000000000000000228 ***
## OverallQual
## OverallCond
                         0.00000000000002313 ***
## YearBuilt
                         0.000000000021756978 ***
## YearRemodAdd
                                     0.014656 *
  RoofStyleShed
                                     0.010652 *
  RoofMatlCompShg
                         < 0.0000000000000000 ***
## RoofMatlMembran
                         < 0.0000000000000000 ***
## RoofMatlMetal
                         < 0.0000000000000000 ***
## RoofMatlRoll
                         < 0.0000000000000000 ***
## `RoofMatlTar&Grv`
                         < 0.0000000000000000 ***
```

```
## RoofMatlWdShake
                        < 0.00000000000000000002 ***
## RoofMatlWdShngl
                        < 0.0000000000000000 ***
## Exterior1stBrkFace
                        0.000001340618306495 ***
## `Exterior1stWd Sdng`
                                    0.023709 *
## `Exterior2ndWd Sdng`
                                    0.020911 *
## MasVnrTypeStone
                                    0.001966 **
## MasVnrArea
                                    0.002439 **
## ExterQualGd
                        0.00000014636523040 ***
## ExterQualTA
                        0.00000001018871882 ***
## BsmtQualEx
                                    0.009542 **
## BsmtQualFa
                        0.00000000000000368 ***
                        0.00000019361569651 ***
## BsmtQualGd
                        < 0.0000000000000000 ***
## BsmtExposureAv
## BsmtFinType1BLQ
                                    0.018222 *
## BsmtFinSF1
                        < 0.000000000000000 ***
## BsmtFinSF2
                        0.000000005947144042 ***
## BsmtUnfSF
                        0.00000000000033196 ***
## X1stFlrSF
                        < 0.00000000000000000002 ***
## X2ndFlrSF
                        < 0.0000000000000000 ***
## BedroomAbvGr
                        0.00000027086389464 ***
## KitchenAbvGr
                        < 0.000000000000000 ***
## KitchenQualFa
                        0.000068334389684203 ***
## KitchenQualGd
                        0.00000000000063342 ***
## KitchenQualTA
                        0.000000000009635832 ***
## TotRmsAbvGrd
                                    0.001530 **
## FunctionalTyp
                        0.00000002545803481 ***
## GarageCars
                        0.00000000001204751 ***
## GarageQualEx
                                    0.000508 ***
## GarageQualFa
                                    0.825061
## GarageQualGd
                                    0.185910
## GarageQualPo
                                    0.001701 **
## WoodDeckSF
                                    0.002231 **
                        0.000059123036763314 ***
## ScreenPorch
## PoolArea
                                    0.008138 **
## SaleTypeNew
                        0.000000000000224875 ***
## SaleConditionNormal
                                    0.000870 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20860 on 1383 degrees of freedom
## Multiple R-squared: 0.9293, Adjusted R-squared: 0.9257
## F-statistic: 256.1 on 71 and 1383 DF, p-value: < 0.0000000000000000022
```

At first glance, the multiple R-squared value of 0.9293 indicates that 92.93% of the variability in SalePrice around its mean is explained by the mode, i.e. by the predictor variables that have been included. This suggests a high-performing explanatory model.

Let Before welcoming this conclusion, we validate the linearity and normality assumptions of our model by checking our residuals as follows:

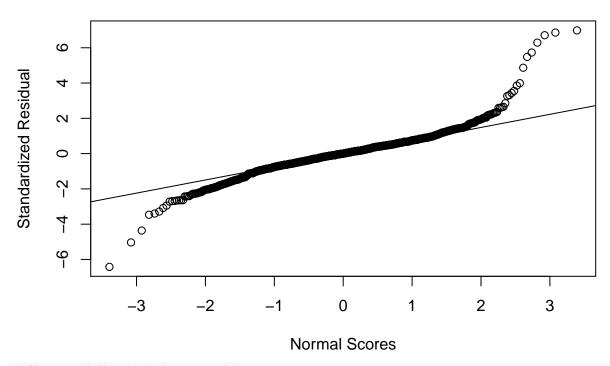
```
# Residual plots

res = resid(new_model) # residuals

stdres = rstandard(new_model) # standardized residuals
```

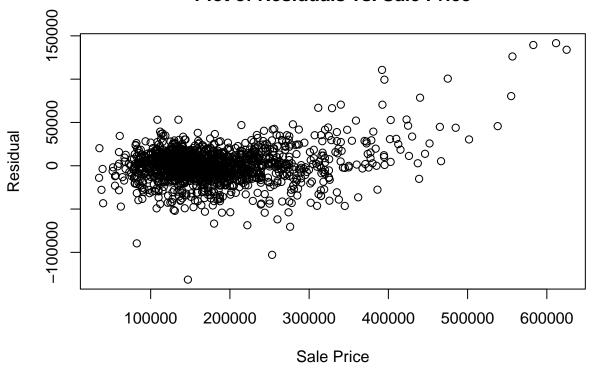
```
# QQ Plot of Residuals - for normality
qqnorm(stdres, main = "QQ Plot of Standardized Residuals", xlab = "Normal Scores",
    ylab = "Standardized Residual")
qqline(stdres)
```

## **QQ Plot of Standardized Residuals**



```
# Shapiro-Wilks test for normality
shapiro.test(res)
```

## Plot of Residuals vs. Sale Price

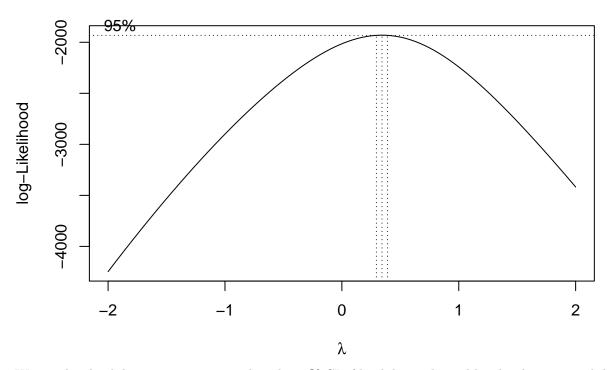


# abline(h=c(0,0), col = 'red') abline(v=350000, col = 'blue')

The plot of residuals against fitted values shows that for the most part, the residuals are evenly distributed across the y=0 line. However, we see that as Sale Price increases, the residuals start to deviate homoscedasticity. More specifically, we see this deviation happen at approximately Sale Price = \$350K, which our earlier summary showed to be between the variable's 3rd quartile and maximum. This suggets that for the last quartile of high-priced houses, the fitted regression model is not as adequate as it is for the reset of the population. The normal probability (QQ) plot corroborates this finding: it shows deviance from linearity at both tail ends of the residual rang, which suggests a heavy tailed distribution. This occurs at both ends of the distribution, i.e. both extremely low-priced houses and extremely high-priced houses are pulling the distribution away from normality. Indeed, the formal Shapiro-Wilks test for normality produces a p-value of  $\sim$ 0, which leads us to reject the null hypothesis, at the alpha = 0.05 level, that the residuals are normally distributed.

As a remedial measure, we consider performing a transformation on Sale Price. We use the boxcox() function to determine the transformation under which the maximum likelihood [of?] is attained.

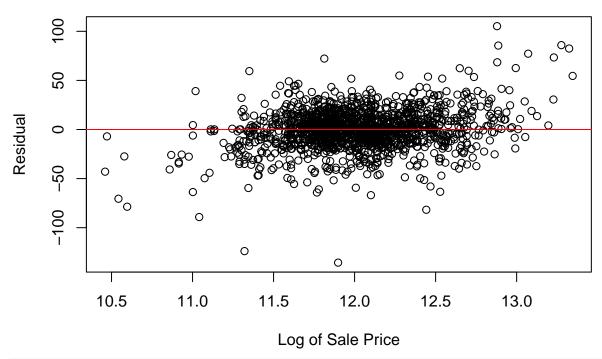
boxcox(new\_model)



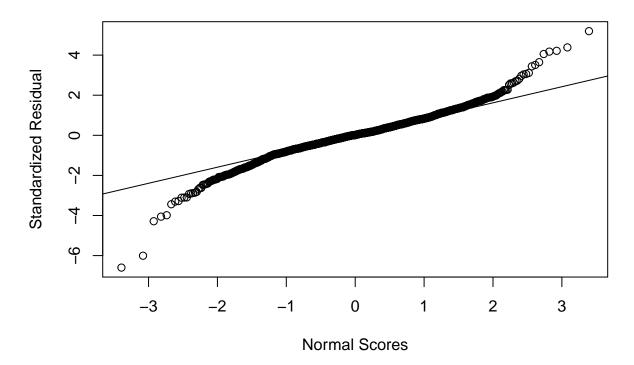
We see that lambda = 1 is not captured in the 95% CI of lambdas, indicated by the three vertical dashed lines. This means a transformation is necessary. We choose lambda =  $\sim 0.5$  since this is an interpretable transformation value. Below, we apply a square root transformation to Sale Price, refit the model, and revalidate our model assumptions with residual plots as above.

```
# Log Transformation
log_model_formula <- as.formula(paste("sqrt(SalePrice) ~ ", paste(new_sig_var_bic,</pre>
    collapse = "+")))
log_model <- lm(formula = log_model_formula, data = workingDF)</pre>
res_log = resid(log_model) # residuals
stdres_log = rstandard(log_model) # standardized residuals
shapiro.test(res)
##
##
   Shapiro-Wilk normality test
##
## data: res
## W = 0.91064, p-value < 0.0000000000000022
# Plot of Residuals from Log Model vs. Fitted Values
plot(log(workingDF$SalePrice), res_log, main = "Plot of Log Model Residuals vs. Log of Sale Price",
    xlab = "Log of Sale Price", ylab = "Residual")
abline(h = c(0, 0), col = "red")
abline(v = 350000, col = "blue")
```

## Plot of Log Model Residuals vs. Log of Sale Price



## **QQ Plot of Standardized Log Model Residuals**



Our new model produces an R-squared value of 0.9411, indicating that 94.11% of the variance in Sale Price is captured by the model. Our residuals vs. fitted values plot shows a better pattern of homoscedasticity, which suggests that our linear regression model adequately captures the trend in the log-transformed data. The normal probability plot of the standardized residuals also shows better adherence to a linear pattern, which suggests that our assumption of normality is better.

Accepting our new model, we provide its summary as follows:

#### summary(log\_model)

```
##
## Call:
  lm(formula = log_model_formula, data = workingDF)
##
##
##
  Residuals:
##
        Min
                   1Q
                        Median
                                      30
                                              Max
   -135.567
                         0.261
                                  11.306
##
             -10.635
                                          105.225
##
## Coefficients:
##
                               Estimate
                                             Std. Error t value
##
   (Intercept)
                         -1671.18357282
                                           112.58872806 -14.843
                                                          -3.724
## MSSubClass120
                           -10.64752125
                                             2.85913147
  MSSubClass160
                           -26.18081164
                                             3.35802829
                                                          -7.796
## MSZoningFV
                            65.46041153
                                             8.06155177
                                                           8.120
## MSZoningRH
                            42.89043937
                                             8.95402404
                                                           4.790
## MSZoningRL
                            48.03525028
                                             7.40929535
                                                           6.483
## MSZoningRM
                            38.45017202
                                             7.44291165
                                                           5.166
## LotArea
                                             0.00008259
                                                           8.902
                             0.00073517
## StreetPave
                            31.53534731
                                             9.40517134
                                                           3.353
## LandContourLow
                            -7.17666556
                                             4.26731619
                                                          -1.682
## LotConfigCulDSac
                             8.15820547
                                             2.39587482
                                                           3.405
## LandSlopeSev
                           -39.91544398
                                             8.83150706
                                                          -4.520
## NeighborhoodCollgCr
                            -0.01011682
                                             2.36619698
                                                          -0.004
## NeighborhoodCrawfor
                            24.00687376
                                             3.42815146
                                                           7.003
## NeighborhoodEdwards
                                             2.51927190
                                                          -4.181
                           -10.53432796
## NeighborhoodGilbert
                            -1.28573035
                                             3.02731747
                                                          -0.425
## NeighborhoodMitchel
                           -12.26751912
                                             3.38861536
                                                          -3.620
   NeighborhoodNAmes
                            -7.48489934
                                             2.04558981
                                                          -3.659
  NeighborhoodNoRidge
                            17.29709181
                                             4.18056130
                                                           4.138
## NeighborhoodNridgHt
                            15.42677210
                                             3.39134089
                                                           4.549
## NeighborhoodNWAmes
                           -11.21336222
                                             2.92429552
                                                          -3.835
## NeighborhoodOldTown
                            -5.14713279
                                             2.99311114
                                                          -1.720
## NeighborhoodStoneBr
                            32.00644840
                                             4.73427499
                                                           6.761
## Condition1Norm
                                                           4.232
                             7.48316286
                                             1.76829895
## Condition1RRAe
                           -20.11004958
                                                          -2.990
                                             6.72651876
## Condition2RRAe
                          -102.75611865
                                            33.16696136
                                                          -3.098
## OverallQual
                             8.93921706
                                             0.80743887
                                                          11.071
## OverallCond
                             7.15741893
                                             0.67014561
                                                          10.680
## YearBuilt
                             0.40385545
                                             0.04641291
                                                           8.701
## YearRemodAdd
                             0.16358008
                                             0.04455051
                                                           3.672
## RoofStyleShed
                            72.49869955
                                            25.19630392
                                                           2.877
## RoofMatlCompShg
                           674.45031929
                                            26.13454451
                                                          25.807
## RoofMatlMembran
                           755.12050273
                                            35.41024975
                                                          21.325
## RoofMatlMetal
                           730.65450605
                                            35.27721303
                                                          20.712
## RoofMatlRoll
                           663.16972068
                                            33.69026761
                                                          19.684
```

```
## `RoofMatlTar&Grv`
                           668.08268748
                                            26.76335491
                                                          24.963
## RoofMatlWdShake
                                                          23.651
                           666.66645567
                                            28.18712555
                           703.17079135
                                            27.67154294
## RoofMatlWdShngl
                                                          25.411
## Exterior1stBrkFace
                                             3.37548164
                                                           4.901
                            16.54367684
   `Exterior1stWd Sdng`
                            -8.22155502
                                             3.38045974
                                                          -2.432
   `Exterior2ndWd Sdng`
                             7.74299867
                                             3.35482876
                                                           2.308
## MasVnrTypeStone
                             7.35971115
                                             2.33030634
                                                           3.158
## MasVnrArea
                             0.00715501
                                             0.00398773
                                                           1.794
  ExterQualGd
                           -10.85790351
                                             3.53495715
                                                          -3.072
## ExterQualTA
                           -14.04465027
                                             3.72419051
                                                          -3.771
   BsmtQualEx
                            -7.65520773
                                             4.74319971
                                                          -1.614
  BsmtQualFa
                                                          -5.603
                           -13.91804704
                                             2.48413009
   BsmtQualGd
                           -10.71663639
                                             2.84878869
                                                          -3.762
                                                           7.334
   BsmtExposureAv
                            16.72368119
                                             2.28017245
   BsmtFinType1BLQ
                                                           2.444
                             4.29191348
                                             1.75585399
   BsmtFinSF1
                             0.04088735
                                             0.00306158
                                                          13.355
  BsmtFinSF2
                                             0.00442021
                                                           6.542
                             0.02891711
## BsmtUnfSF
                             0.02397144
                                             0.00294602
                                                           8.137
                                                          15.661
## X1stFlrSF
                             0.06000525
                                             0.00383159
## X2ndFlrSF
                             0.06310356
                                             0.00280432
                                                          22.502
## BedroomAbvGr
                            -3.90758206
                                             1.09764983
                                                          -3.560
## KitchenAbvGr
                                             3.02608238
                                                          -8.134
                           -24.61391838
## KitchenQualFa
                                                          -3.689
                           -18.19947694
                                             4.93336719
## KitchenQualGd
                                                          -6.299
                           -18.59497607
                                             2.95215936
## KitchenQualTA
                           -19.88106371
                                             3.33396019
                                                          -5.963
  TotRmsAbvGrd
                             2.06333085
                                             0.78449120
                                                           2.630
## FunctionalTyp
                                                           6.546
                            16.21671425
                                             2.47752357
   GarageCars
                            10.52823232
                                             1.29241394
                                                           8.146
   GarageQualEx
                           -10.17295582
                                             4.32923399
                                                          -2.350
   GarageQualFa
                             8.48332330
                                             6.60826268
                                                           1.284
   GarageQualGd
                           -16.49507217
                                            12.77716764
                                                          -1.291
   GarageQualPo
                            -2.39845798
                                             3.24020265
                                                          -0.740
   WoodDeckSF
                             0.01810918
                                             0.00494922
                                                           3.659
## ScreenPorch
                                                           4.878
                             0.05080009
                                             0.01041447
  PoolArea
                             0.04605799
                                             0.01761637
                                                           2.614
                                                           7.764
  SaleTypeNew
                            23.80567847
                                             3.06613561
   SaleConditionNormal
                             9.87327013
                                             1.99469032
                                                           4.950
##
                                      Pr(>|t|)
   (Intercept)
                         < 0.0000000000000000 ***
  MSSubClass120
                                      0.000204 ***
  MSSubClass160
                         0.00000000000012444 ***
## MSZoningFV
                         0.00000000000001021 ***
  MSZoningRH
                         0.000001846634598217 ***
  MSZoningRL
                         0.000000000124711745 ***
## MSZoningRM
                         0.000000274125859981 ***
## LotArea
                         < 0.0000000000000000 ***
## StreetPave
                                      0.000821 ***
## LandContourLow
                                      0.092838 .
  LotConfigCulDSac
                                      0.000680 ***
   LandSlopeSev
                         0.000006722390861845 ***
## NeighborhoodCollgCr
                                      0.996589
## NeighborhoodCrawfor
                         0.00000000003901696 ***
## NeighborhoodEdwards
                         0.000030779955347722 ***
## NeighborhoodGilbert
                                      0.671115
```

```
## NeighborhoodMitchel
                                     0.000305 ***
## NeighborhoodNAmes
                                     0.000263 ***
                         0.000037228199946703 ***
  NeighborhoodNoRidge
  NeighborhoodNridgHt
                         0.000005865667023773 ***
  NeighborhoodNWAmes
                                     0.000131 ***
  NeighborhoodOldTown
                                     0.085718 .
## NeighborhoodStoneBr
                         0.000000000020210524 ***
## Condition1Norm
                         0.000024705134413399 ***
  Condition1RRAe
                                     0.002842 **
## Condition2RRAe
                                     0.001987 **
## OverallQual
                         < 0.0000000000000000 ***
## OverallCond
                         < 0.0000000000000000 ***
                         < 0.00000000000000002 ***
## YearBuilt
## YearRemodAdd
                                     0.000250 ***
## RoofStyleShed
                                     0.004072 **
  RoofMatlCompShg
                         < 0.0000000000000000 ***
## RoofMatlMembran
                         < 0.0000000000000000 ***
## RoofMatlMetal
                         < 0.0000000000000000 ***
## RoofMatlRoll
                         < 0.0000000000000000 ***
  `RoofMatlTar&Grv`
                         < 0.0000000000000000 ***
## RoofMatlWdShake
                         < 0.0000000000000000 ***
## RoofMatlWdShngl
                         < 0.0000000000000000 ***
## Exterior1stBrkFace
                         0.000001065352965006 ***
  `Exterior1stWd Sdng`
                                     0.015139 *
## `Exterior2ndWd Sdng`
                                     0.021145 *
## MasVnrTypeStone
                                     0.001621 **
## MasVnrArea
                                     0.072991 .
## ExterQualGd
                                     0.002171 **
## ExterQualTA
                                     0.000169 ***
## BsmtQualEx
                                     0.106770
## BsmtQualFa
                         0.000000025419586296 ***
## BsmtQualGd
                                     0.000176 ***
                         0.00000000000377958 ***
  BsmtExposureAv
  BsmtFinType1BLQ
                                     0.014636 *
## BsmtFinSF1
                         < 0.0000000000000000 ***
## BsmtFinSF2
                         0.000000000085228977 ***
## BsmtUnfSF
                         0.000000000000000895 ***
## X1stFlrSF
                         < 0.0000000000000000 ***
## X2ndFlrSF
                         < 0.0000000000000000 ***
## BedroomAbvGr
                                     0.000383 ***
## KitchenAbvGr
                         0.00000000000000916 ***
## KitchenQualFa
                                     0.000234 ***
## KitchenQualGd
                         0.000000000402233982 ***
## KitchenQualTA
                         0.000000003135879653 ***
## TotRmsAbvGrd
                                     0.008629 **
                         0.000000000083308288 ***
## FunctionalTyp
                         0.000000000000000832 ***
  GarageCars
  GarageQualEx
                                     0.018922 *
  GarageQualFa
                                     0.199446
  GarageQualGd
                                     0.196926
## GarageQualPo
                                     0.459293
## WoodDeckSF
                                     0.000263 ***
## ScreenPorch
                         0.000001196738264173 ***
## PoolArea
                                     0.009033 **
```

We conclude that the variables included above are most relevant in determining a house's sale price. In particular, those variables that are significant at the 0.01 level, i.e., are most significant.

## Task 2: Making recommendations

```
# morty <-
# read.csv('/Users/booranium/usf/601_regression/project/Morty.txt',
# stringsAsFactors = T)
morty <- read.csv("/Users/santhoshhari/Documents/Coursework/LinearRegression/IowaHousing/Data/Morty.txt
    stringsAsFactors = T)
sig_var_morty <- names(morty)[bool_bic == TRUE]</pre>
sig_var_morty
    [1] "MSSubClass"
                         "MSZoning"
                                                           "Street"
##
                                          "LotArea"
                                                           "LotConfig"
                         "LotShape"
##
   [5] "Alley"
                                          "Utilities"
   [9] "LandSlope"
                         "Neighborhood"
                                          "BldgType"
                                                           "OverallQual"
## [13] "OverallCond"
                         "YearBuilt"
                                                           "RoofStyle"
                                          "YearRemodAdd"
## [17] "RoofMatl"
                         "Exterior1st"
                                          "MasVnrType"
                                                           "MasVnrArea"
## [21] "ExterQual"
                         "Foundation"
                                          "BsmtCond"
                                                           "BsmtFinType1"
                                                           "X1stFlrSF"
  [25] "BsmtFinType2"
                         "CentralAir"
                                          "Electrical"
                                                           "BsmtHalfBath"
  [29] "X2ndFlrSF"
                         "GrLivArea"
                                          "BsmtFullBath"
## [33] "FullBath"
                         "HalfBath"
                                          "BedroomAbvGr"
                                                           "KitchenAbvGr"
## [37] "KitchenQual"
                         "TotRmsAbvGrd"
                                          "GarageYrBlt"
                                                           "GarageCars"
## [41] "GarageCond"
                         "PavedDrive"
                                          "WoodDeckSF"
                                                           "OpenPorchSF"
## [45] "X3SsnPorch"
                         "ScreenPorch"
                                          "PoolArea"
                                                           "MiscFeature"
## [49] "MoSold"
                         "YrSold"
                                          "SaleCondition" "SalePrice"
## [53] NA
                         NA
                                          NA
                                                           NA
## [57] NA
                         NA
                                          NA
                                                           MΔ
## [61] NA
                         NΑ
                                          NΑ
                                                           NA
## [65] NA
                         NA
                                          NΑ
                                                           NΑ
## [69] NA
                         NA
                                          NA
                                                           NΑ
## [73] NA
                         NA
                                          NΑ
```

To make a recommendation to Morty regarding the selling price of his house, we leverage the model built above to make a prediction of Sale Price based on select attributes as determined above.

```
morty <- c()
prediction <- predict(log_model, newdata = morty, type = "response",
    interval = "confidence", level = 0.95)
prediction</pre>
```

We see that the 95% CI for the predicted Sale Price of Morty's house, based on selected attributes, is ... As such, we recommend that Morty sell his house at a maximum of ..., which is more/less than the other firm's recommendation of \$143K.

In addition, we see that

# Part II: Predictive Modelling