

Assignment-3

Data Structures and Algorithms Heaps and AVL Trees

Due Date: 16th March, 2025 11:59 PM

Important Notes

- You are only allowed to use **C** for this assignment.
- You are **not allowed** to use the inbuilt `qsort` function in C.
- You are not allowed to copy the exact code given in class. You are allowed to note the logic, but you need to implement the code by yourself.
- We are providing a [boilerplate](#) for AVL tree. This will **not** be considered for MOSS. You may still choose to implement it yourself.
- [Plagiarism Policy](#). Please read this before you start the assignment.

TOTAL: [100 PTS]

1 The Chocolate Dispute [25 PTS]

1.1 Problem Statement

Aayush and Aniket are embroiled in a dispute over a collection of chocolates. Initially, Aayush possesses n chocolates, each laid out along the $X - axis$. The i^{th} chocolate covers a segment starting at position l_i and ending at position r_i (both inclusive). The size of a chocolate is defined as,

$$size = r_i - l_i + 1$$

Aniket chooses a point k on the $X - axis$. If there are multiple chocolates covering that point, Aayush, being greedy, will hand over the chocolate with the smallest size to Aniket. If no chocolate covers the point k , then Aniket receives nothing. Your task is to determine, for each query point, the size of the chocolate that Aniket will obtain. If he doesn't receive a chocolate, output -1 .

1.2 Input Format

- The first line contains an integer n , the number of chocolates.
- Each of the next n lines contains two space-separated integers l_i and r_i , representing the starting and ending points of the i -th chocolate on the $X - axis$.
- The following line contains an integer q , the number of queries
- Each of the next q lines contains a single integer k , representing the query point on the $X - axis$.

1.3 Output Format

For each query, output a single integer — the size of the smallest chocolate covering the point k . If no chocolate covers the point, output -1 .

1.4 Example Testcases

1.4.1 Example 1

Sample Input	Sample Output
3 1 6 2 5 3 4 3 2 3 7	4 2 -1

- For $k = 2$, both the first and second chocolates cover the point; however, the second chocolate has a smaller size (4) compared to the first (6), so the output is 4. For $k = 3$, all three chocolates cover the point, and the smallest among them is the third chocolate ($size = 2$). For $k = 7$, no chocolate covers the point, hence the output is -1 .

1.5 Constraints

- $1 \leq n \leq 10^5$
- $1 \leq q \leq 10^5$
- $1 \leq l_i \leq r_i \leq 10^7$
- $1 \leq k \leq 10^7$

2 The Great Wall Reconstruction [40 PTS]

2.1 Problem Statement

A city is rebuilding its ancient Great Wall, which consists of multiple connected sections. Each section has a starting position, an ending position, and a specific height. Due to erosion and past reconstructions, some sections overlap, forming a continuous outer contour when viewed from a distance.

The government needs your help to determine the **visible outline** of the reconstructed wall, as seen from afar.

2.2 Input Format

- An integer n , representing the number of sections.
- n lines follow, each containing three integers: x_1 , x_2 , and h .

2.3 Output Format

The output should be a list of key points representing the visible outline of the reconstructed Great Wall. Each key point is a significant change in height along the structure.

- The list should be sorted in increasing order of the x -coordinate.
- Each key point should be represented as $[x, h]$, where:
 - x is the horizontal position.
 - h is the height of the wall at that position.
- The last key point should always have a height of 0, indicating the termination of the wall's visible structure.

2.4 Example Testcases

2.4.1 Example 1

Sample Input	Sample Output
5 2 9 10 3 7 15 5 12 12 15 20 10 19 24 8	2 10 3 15 7 12 12 0 15 10 20 8 24 0

- Figure A shows the given sections.
- Figure B depicts the visible outline.
- The marked points in Figure B represent key points in the final output.

Below is a visual representation of the input and expected output:

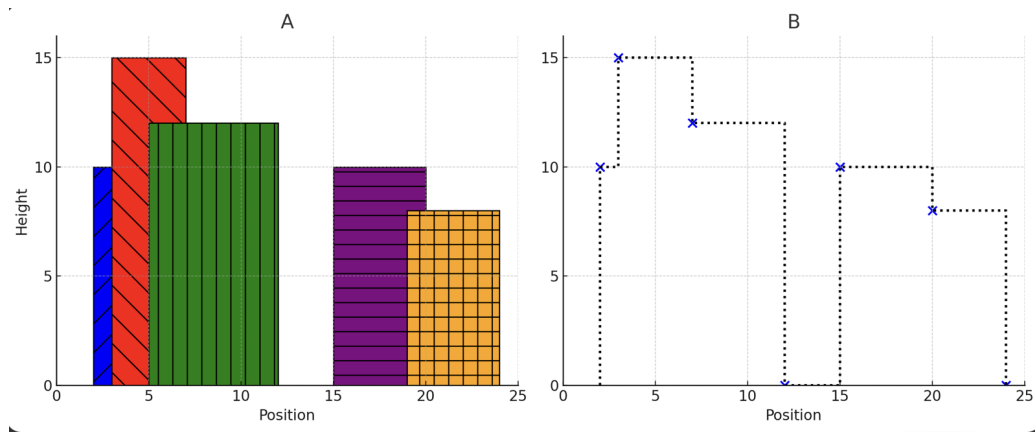


Figure A (left) represents the given sections, and Figure B (right) represents the visible outline.

2.4.2 Example 2

Sample Input	Sample Output
2 0 2 3 2 5 3	0 3 5 0

2.5 Constraints

- $1 \leq \text{sections.length} \leq 10^6$
- $0 \leq x_1 < x_2 \leq 2^{31} - 1$
- $1 \leq h \leq 2^{31} - 1$

3 The Canteen Cost Conundrum [35 PTS]

3.1 Problem Statement

With the rising prices in the college canteen, students are eager to find the most affordable way to assemble a meal.

Consider a dynamic menu where:

- New items are continuously added,
- Some items are removed, and
- Prices of certain items are updated.

A meal consists of k distinct food items or as many distinct items as available if there are fewer than k options.

3.2 Input Format

- The first line contains two integers n and k , representing the number of items initially on the menu and the number of items required to assemble a meal.
- The following line contains n space-separated integers which represent the prices of the items on the menu initially.
- The third line contains an integer u the number of updates to the menu.
- The following u lines contain updates of the form
 - 1 x : Add an item with price x to the menu
 - 2 x : Remove an item with price x from the menu. (It is guaranteed that there is an item with price x in the menu)
 - 3 x y : Update the price of an item with price x to y . (It is guaranteed that there is an item with price x in the menu)

3.3 Output Format

After every update operation output an integer on a separate line which is the minimum cost to assemble a meal.

3.4 Example Testcases

3.4.1 Example 1

Sample Input	Sample Output
8 3 1 2 3 4 5 6 7 8 4 1 9 1 2 2 1 3 2 1	6 5 7 6

- After adding an item of price 9 the cheapest meal costs $1 + 2 + 3 = 6$
- After adding an item of price 2 the cheapest meal costs $1 + 2 + 2 = 5$
- After removing an item of price 1 the cheapest meal costs $2 + 2 + 3 = 7$
- After changing the price of an item from 2 to 1 the cheapest meal costs $1 + 2 + 3 = 6$

3.4.2 Example 2

Sample Input	Sample Output
4 5 1 2 2 3 3 3 2 3 1 1 3 3 2	9 10 9

- After changing the price of an item from 2 to 3 the cheapest meal costs $1 + 2 + 3 + 3 = 9$ (Note that there are only 4 items available)
- After adding an item costing 1 the price of the cheapest meal becomes $1 + 1 + 2 + 3 + 3 = 10$
- After updating the cost of an item from 3 to 2 the cost of the cheapest meal becomes $1 + 1 + 2 + 2 + 3 = 9$

3.5 Constraints

- $1 \leq n \leq 2 \times 10^5$
- $1 \leq k \leq 10^5$
- $1 \leq p \leq 10^9$
- $1 \leq u \leq 2 \times 10^5$

Good Luck, have fun coding!