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DMS INTERMEDIATE - II

Section - 1

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1) The difference between the permutation and combination are: given:

Permutation	Combination
<p>1) permutation means the selection of objects, where the order of selection matters.</p> <p>2) In other words, it is the arrangement of r objects taken out of n objects</p> <p>3) The formula for permutation is</p> ${}^n P_r = n! / (n-r)!$	<p>1) The combination means the selection of objects, in which the order of selection does not matter</p> <p>2) In other words, it is the selection of r objects taken out of n objects arrangement</p> <p>3) The formula for combination is</p> ${}^n C_r = n! / [r!(n-r)!]$

4) PBS Based on sumrule and product Rule:

" In how many ways can we draw a heart or a shade from an ordinary deck of playing cards? A heart or an ace? An ace or a king? A card number 2

though 10? A numbered card or a king?

Sol: (a) No. of heart = 13, No. of shade = 13

Sumrule: ways to draw heart (or) Shade = $13 + 13 = 26$ ways

b) No. of heart = 13, No. of Ace = 4

Sumrule: ways to draw heart (or) Ace = $13 + 4 = 17$ ways

c) No. of Ace = 4 ; No. of king = 4

Sumrule: way to draw heart (or) king = $4 + 4 = 8$ ways

d) No. of n 2 to 10 is 10

No. of way a card numbered 2 through 10 = $9 \times 4 = 36$ ways

e) No. of numbered card = 36

No. of king = 4

\therefore No. of ways to draw numbered card

(or) a king = $36 + 4$ ways.

= 40 ways

Section - II

6. Binomial Theorem:

Statement:

A Binomial Theorem describes the algebraic expansion of powers of a Binomial with two variables

Proof:

$$(x+y)^n = nC_0 \cdot x^n y^0 + nC_1 \cdot x^{n-1} \cdot y^1 + nC_2 \cdot x^{n-2} \cdot y^2 + \dots + nC_{n-1} \cdot x^1 \cdot y^{n-1} + nC_n \cdot x^0 \cdot y^n$$

It can be written as

$$(x+y)^n = \sum_{r=0}^n nC_r \cdot (x)^{n-r} \cdot y^r$$

$$\rightarrow (1+x)^n = nC_0 \cdot 1^n \cdot x^0 + nC_1 \cdot 1^{n-1} \cdot x^1 + nC_2 \cdot 1^{n-2} \cdot x^2 + nC_3 \cdot 1^{n-3} \cdot x^3 + \dots$$

$$= nC_0 \cdot x^0 + nC_1 \cdot x^1 + nC_2 \cdot x^2 + nC_3 \cdot x^3 + \dots$$

$$= 1 \cdot x^0 + \frac{n!}{(n-1)!1!} \cdot x + \frac{n!}{(n-2)!2!} \cdot x^2 + \frac{n!}{(n-3)!3!} \cdot x^3 + \dots$$

$$= 1 + \frac{n(n-1)!}{(n-1)!} \cdot x + n \cdot \frac{(n-2)!}{(n-2)!} \cdot x^2 + \frac{n(n-1)(n-2)!}{(n-3)!3!} \cdot x^3 + \dots$$

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!} \cdot x^2 + \frac{n(n-1)(n-2)}{3!} \cdot x^3 + \dots$$

8) Among 50 patients admitted to a hospital
 25 are diagnosed with pneumonia.
 30 with bronchitis
 10 with both pneumonia and bronchitis

Let $U = \{ \text{patients in the hospital} \} \Rightarrow |U| = 50$

$A = \{ \text{diagnosed with pneumonia} \} \Rightarrow |A| = 25$

$B = \{ \text{bronchitis} \} \Rightarrow |B| = 30$

$A \cap B = \{ \text{both pneumonia and bronchitis} \} \Rightarrow |A \cap B| = 10$

To find:

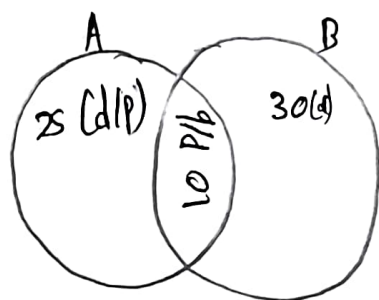
No. of patients neither
diagnosed with pneumonia } $|\overline{A \cup B}| = |U| - |A \cup B| = 0$

w.k.T

$$|A \cup B| = |A| + |B| - |A \cap B| = 25 + 30 - 10 = 45$$

$$\therefore \textcircled{1} \Rightarrow |\overline{A \cup B}| = 50 - 45$$
$$= 5$$

\therefore The 5 patients neither of hospital



(a) The number of patients diagnosed with
pneumonia (or) bronchitis

diagnosed pneumonia = 25

or

diagnosed bronchitis = 30

(b) The number of patients

not diagnosed pneumonia = 25

(c)

not diagnosed bronchitis = 20

(c) Number of patients

diagnosed with only pneumonia = 20

(d) Number of patient

diagnosed with only bronchitis = 25