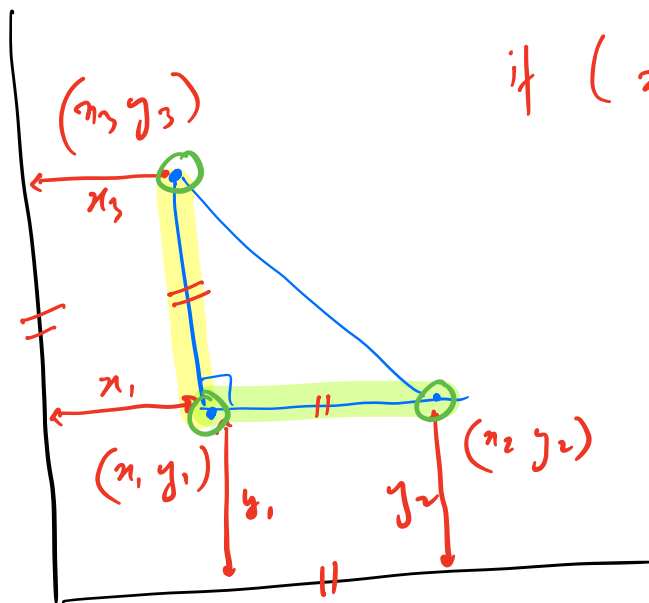
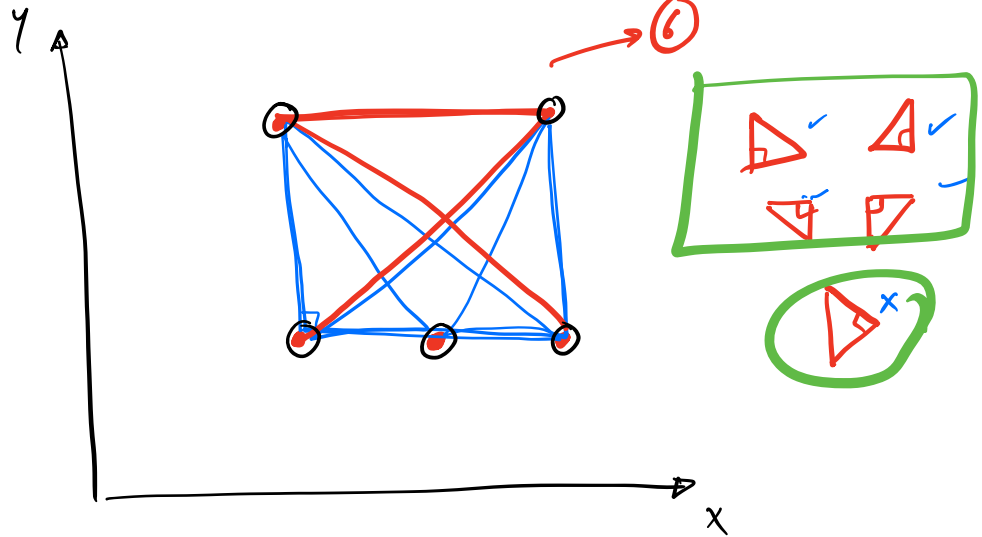


Q Given  $N$  points on a 2D plane.  
 Find the no. of right angled  $\Delta$  s.t  
 1 side is  $\parallel$  to  $x$ -axis  
 ———  $\parallel$  to  $y$ -axis

$(x_i, y_i)$   
 $x[], y[]$



if  $(x_1 == x_3 \text{ \& \& } y_1 == y_2)$   
 $\Rightarrow$  right angled  $\Delta$   
 with sides  
 $\parallel$  to  $x$  &  $y$  axis!

1) BF

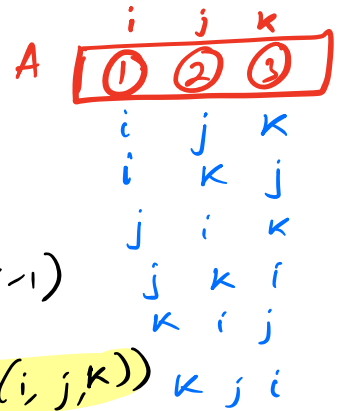
$TC = O(N^3)$   
 $SC = O(1)$

$f(i: 0 \rightarrow N-1)$

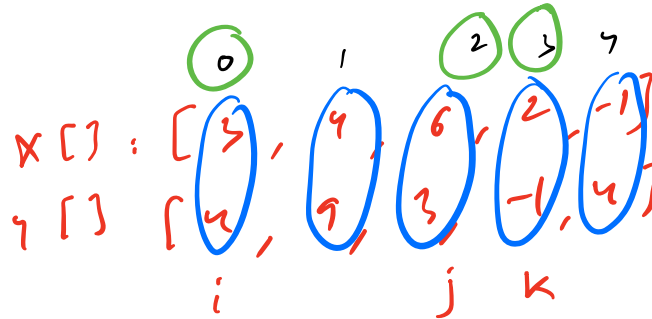
$f(j: \cancel{0}^{i+1} \rightarrow N-1)$

$f(k: \cancel{0}^{j+1} \rightarrow N-1)$

if (check(i, j, k))  
 cnt++

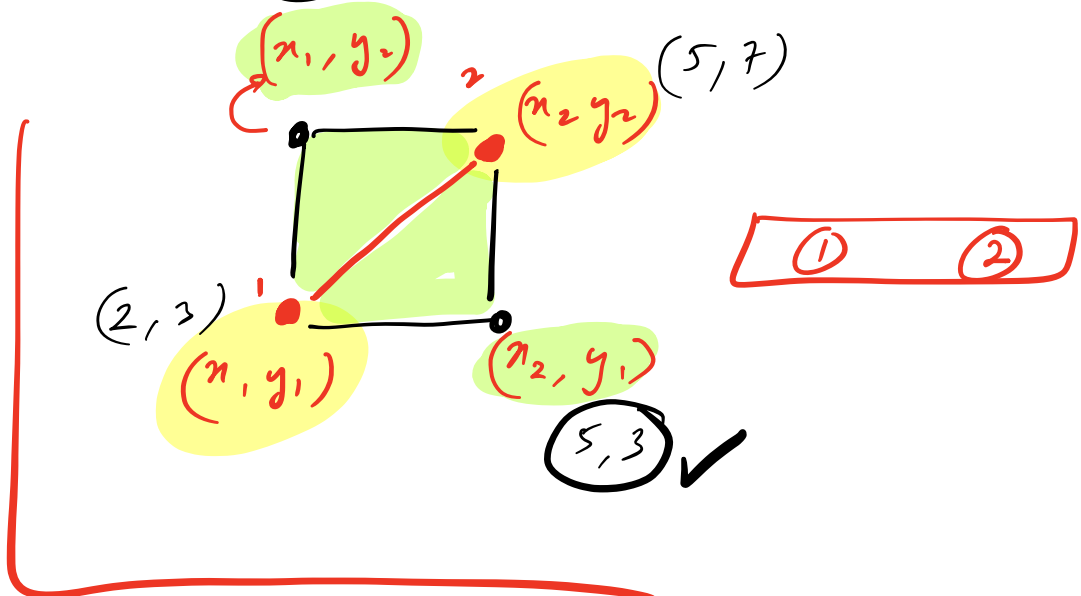


ret cnt;



(2, 7) ✓

11)



```

HashSet < pair <int, int> > hs;
f(i: 0 → N-1) {
    hs.insert( X[i], Y[i]);
}

```

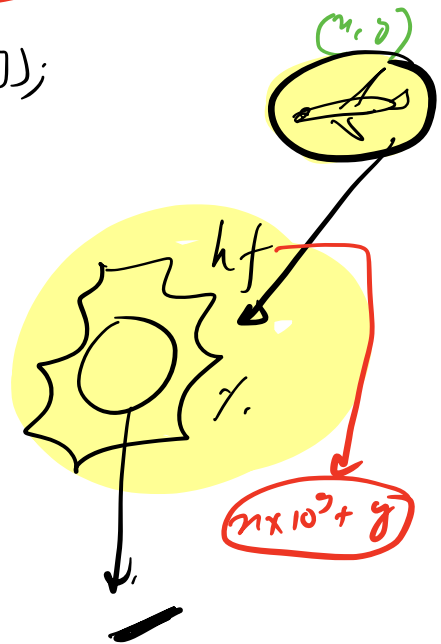
$O(N)$

```

f(i: 0 → N-1) {
    f(j: 0 i+1 → N-1) {
        if (hs.contains( {Xi, Yj} ))
            cnt++;
        if (hs.contains( {Xj, Yi} ))
            cnt++;
    }
}

```

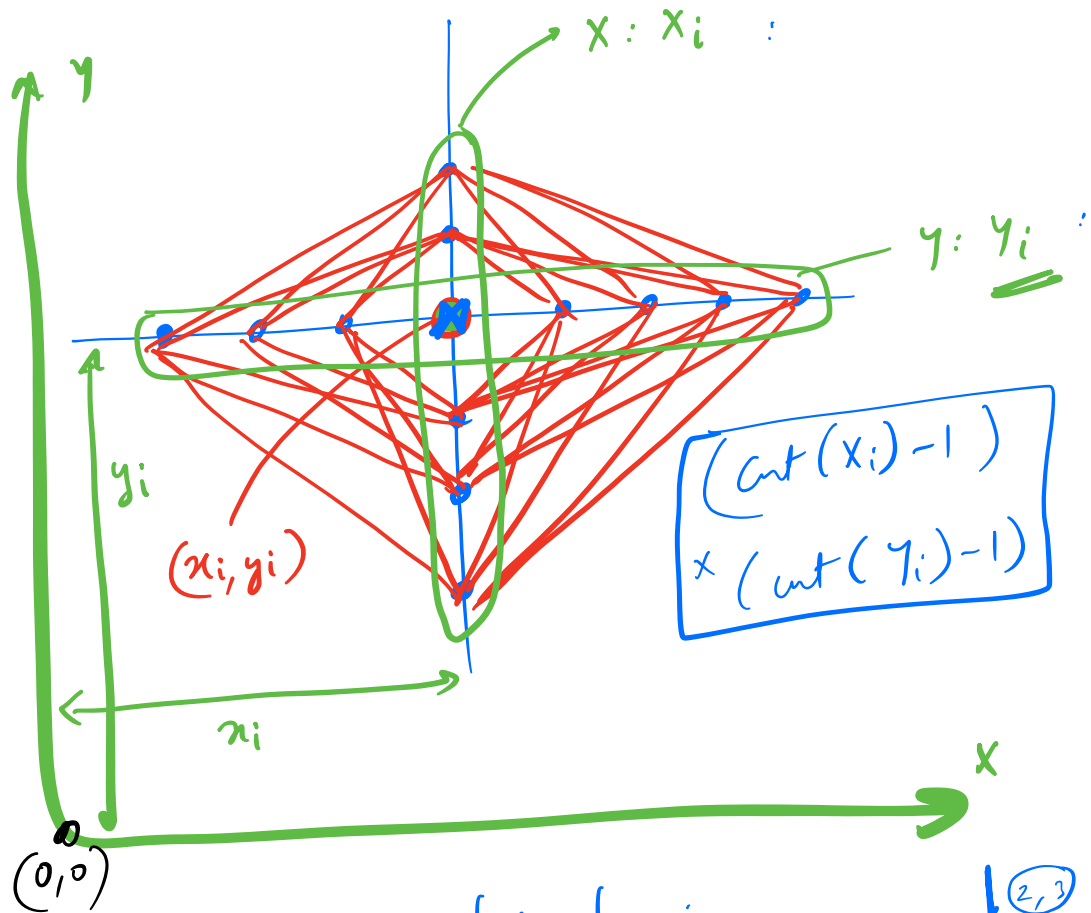
$N^2$



**$TC = O(N^2)$**

**$SC = O(N)$**

III



HashMap < int, int > fx, fy;

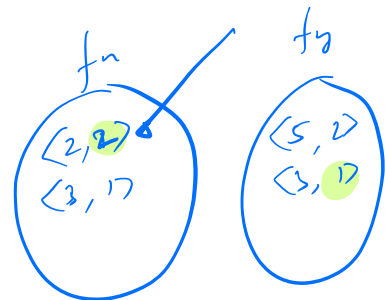
f(i:0 → N-1) {  
 fx[x[i]]++;  
 fy[y[i]]++;  
}

ANS = 0;

f(i:0 → N-1) {  
 ANS += (fx[x[i]] - 1) \* (fy[y[i]] - 1);  
}

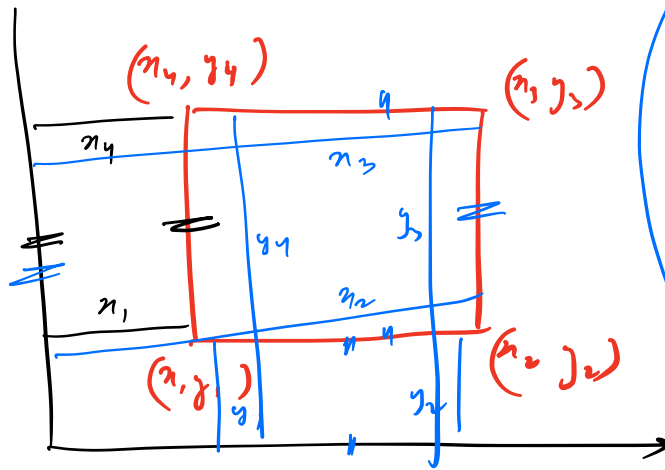
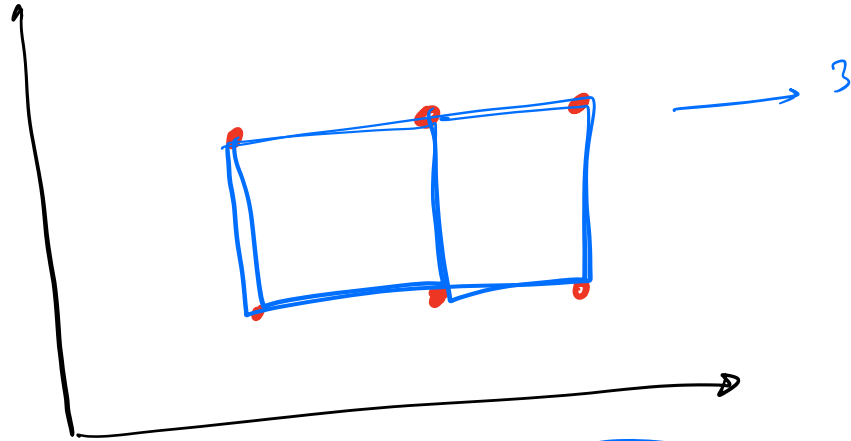
ret ANS;

(2,3)  
 x [2, 3, 2]  
 y [5, 5, 3]



TC = O(N)  
 SC = O(N)

Q Give  $N$  points on a 2D plane  
Find the no. of rectangles having sides  
|| to  $x$  &  $y$  axis!



if  $(x_1 == x_3$   
 $\&\& x_2 == x_4$   
 $\&\& y_1 == y_3$   
 $\&\& y_2 == y_4)$

→

i) BF

$f(i: 0 \rightarrow N-1)$

$f(j: i+1 \rightarrow N-1)$

$f(k: j+1 \rightarrow N-1)$

$f(l: k+1 \rightarrow N-1)$

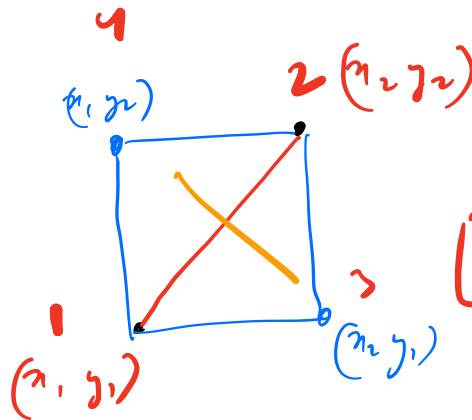
if (check(i, j, k, l))  
    cnt++;

1 2 3 4  
i j k l

TC =  $O(N^4)$

SC =  $O(1)$

ii)



1 2 3 4  
i j

Idea: SAME AS  $\Delta$  problem

$f(i: 0 \rightarrow N-1)$

$f(j: i+1 \rightarrow N-1)$

if (hs.contains((x<sub>i</sub>, y<sub>j</sub>)) &&  
    hs.contains((x<sub>j</sub>, y<sub>i</sub>)))

cnt++;

ret cnt/2;

(i, j): D/AGS  
NAVS

TC =  $O(N^2)$   
SC =  $O(N)$

Q Given 2 strings A & B.  
Find the # of substrings of A which are permutations of B.

A: N

B: M

$1 \leq M \leq N \leq 10^5$

A: a b a x a b a c d c x x b a a → 5

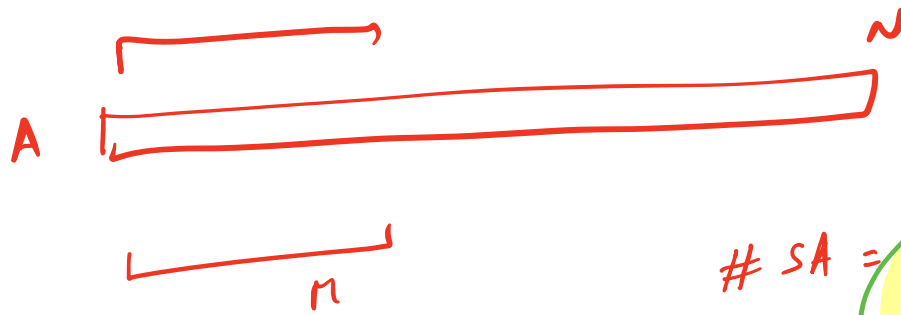
B: a b x a

A: a b a x a b a c d c x x b a a

HM<sub>A</sub>  
a: 2  
b: 1  
x: 1

B: a b x a

HM<sub>B</sub>  
a: 2  
b: 1  
x: 1



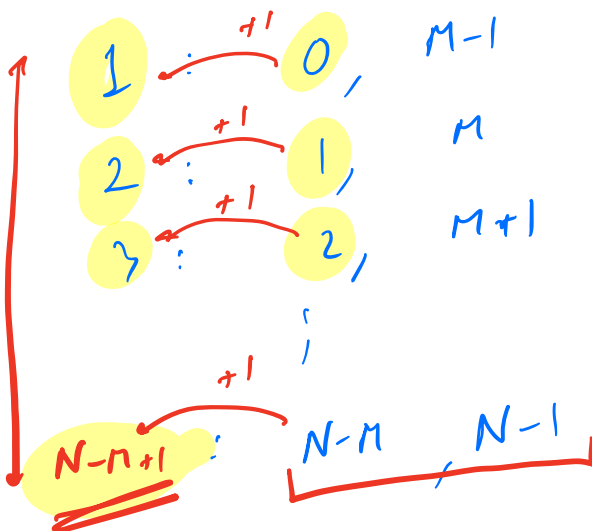
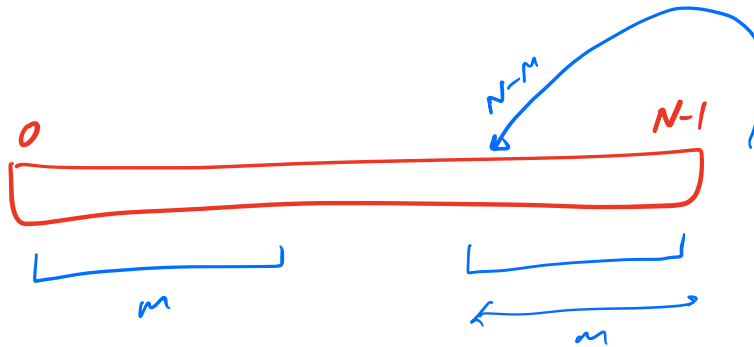
$HM_B \rightarrow O(m)$   
 $HM_A \rightarrow O(m)$

$+$   
 $\downarrow$   
 $TC$

$\# SA = \frac{(N-m+1)}{k}$   
 $\downarrow x$   
 $k$

26

$SC : O(k)$





Q Given 2 strings A & B.  
Find the length of the **shortest** substring of A  
which is having all characters of B.

A: a c x b d a

B: a b x a

A: a b d a x g a b a d c x x f b a a

$\underbrace{\hspace{10em}}_5$   
 $\underbrace{\hspace{10em}}_R$   
 $\underbrace{\hspace{10em}}_i$

(NK)  $\rightarrow$  window

HMA

a: 2  
b: 1  
d: 0  
x: 1  
a: 1

ANS  
= ~~5~~  
5

B: a b x a

HMB

a: 2  
b: 1  
x: 1

$O(n)$

**TC =  $O(NK + M)$**

$\xrightarrow{i} \xrightarrow{j}$   
 $\xrightarrow{i} \xrightarrow{j}$   
 $\xrightarrow{i} \xrightarrow{j}$

$O(N)$

N

