

Linear

Array



LL



stacks

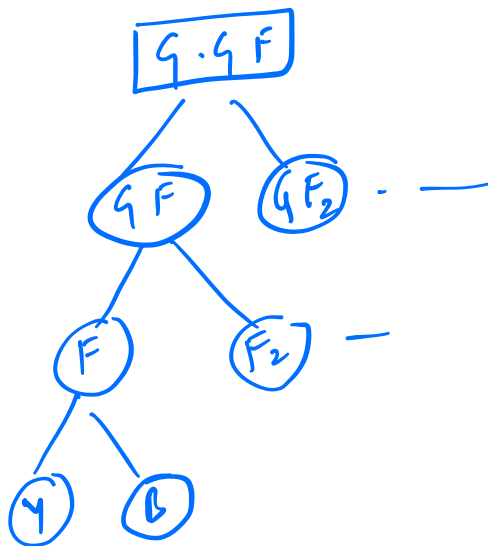


queues

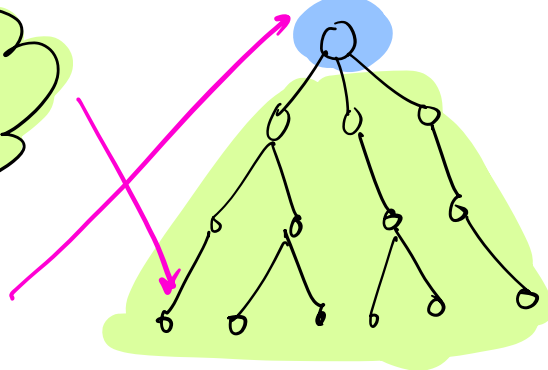
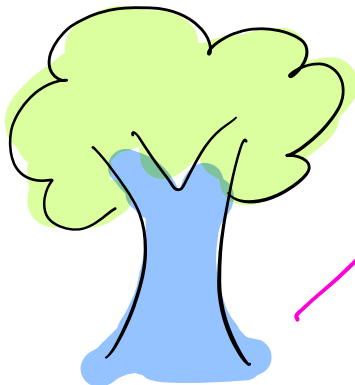
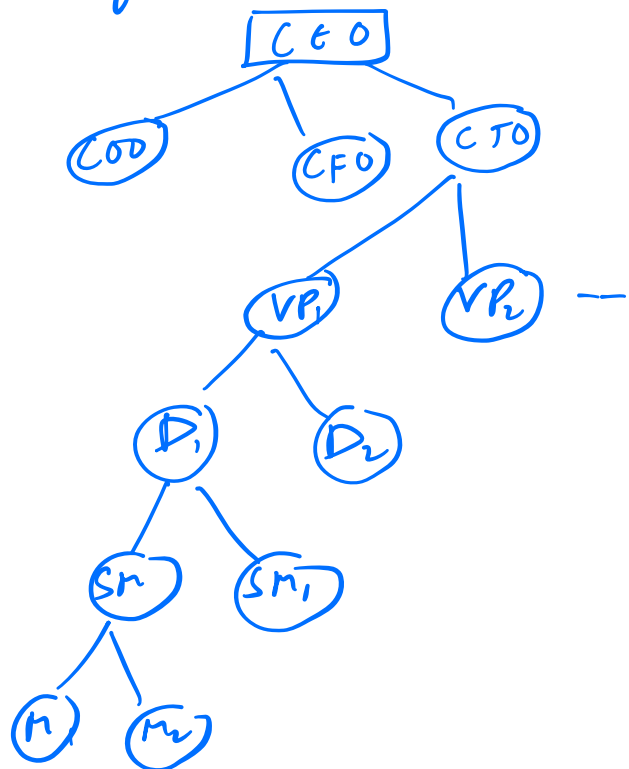


Hierarchical

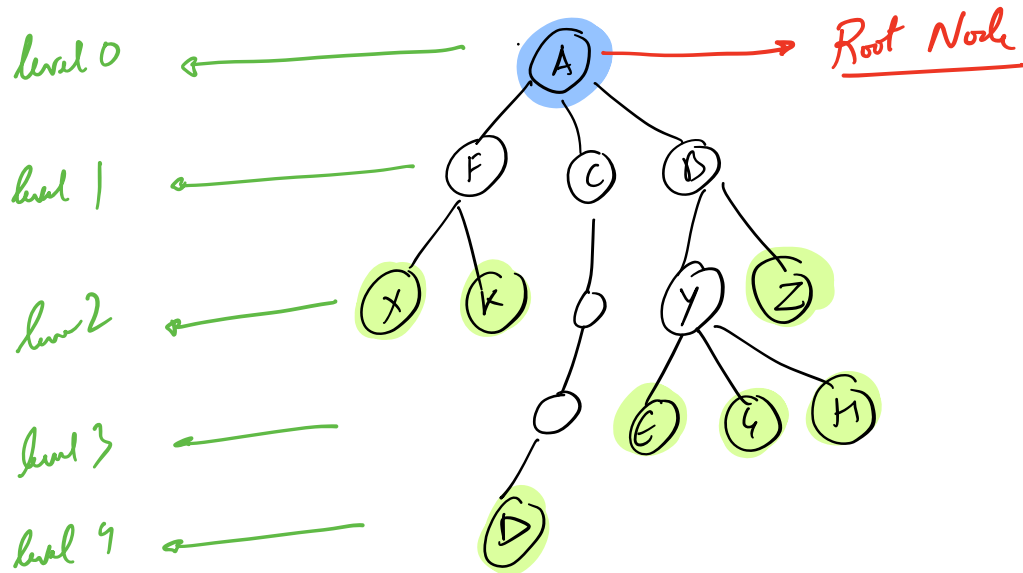
Family tree



Org. structure



UPSIDE  
DOWN!

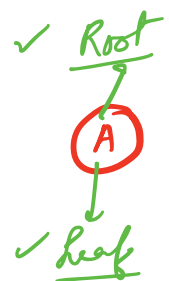


A is parent of B  
 B is child of A  
 F, C, B are siblings

Ancestors of H : Y, B, A.  
 Descendants : Y, Z, E, G, H  
 of B

Leaf Nodes: X, K, D, E, G, H, Z

→ Nodes with no child.  
 → having the SAME PARENT!

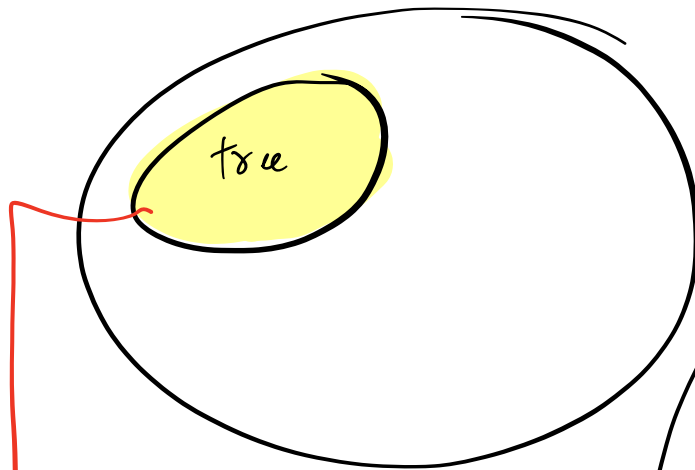


Tree : Hierarchical DS.

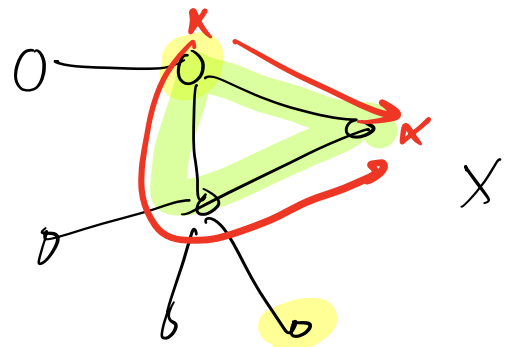
AT MAX 1 root!

Every node → exactly 1 parent!  
 except for the root node!

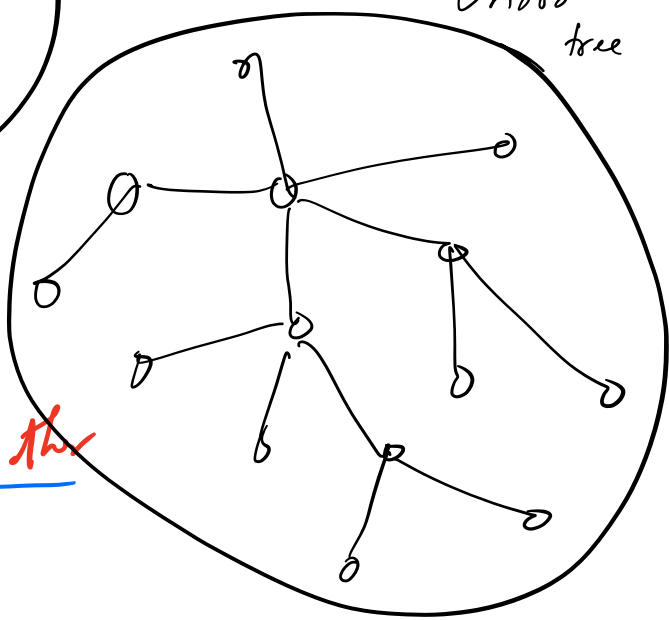
Graph



exactly 1 path  
from any node to any other  
node!



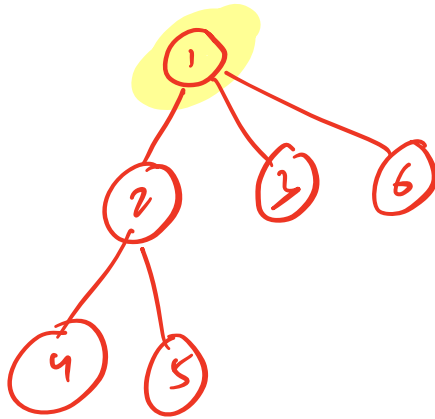
unrooted tree



tree



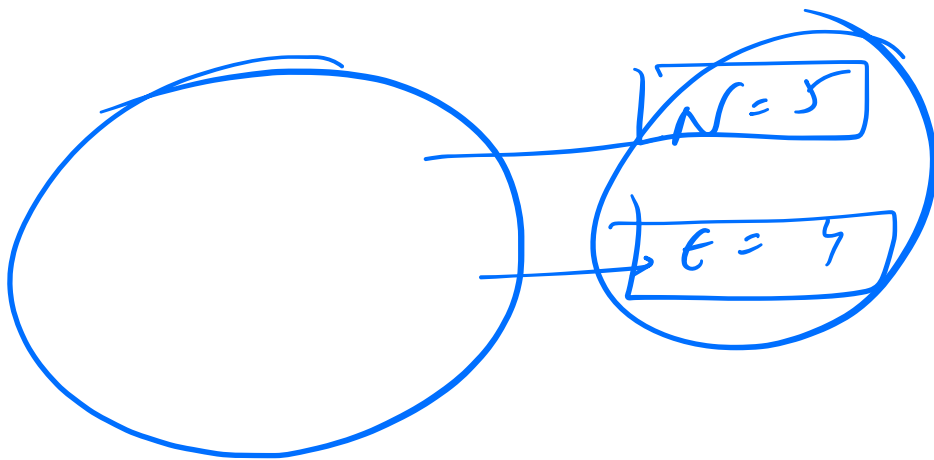
Q If a tree has  $N$  nodes.  
How many edges does it have?



x

Nodes	Edges
1	0
2	1 +1
3	2 +1
4	3 +1
5	4
6	5

$$\boxed{\# \text{ Edges} = \text{Nodes} - 1}$$



Height of a Node :

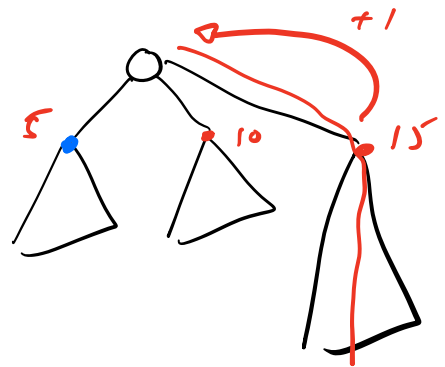
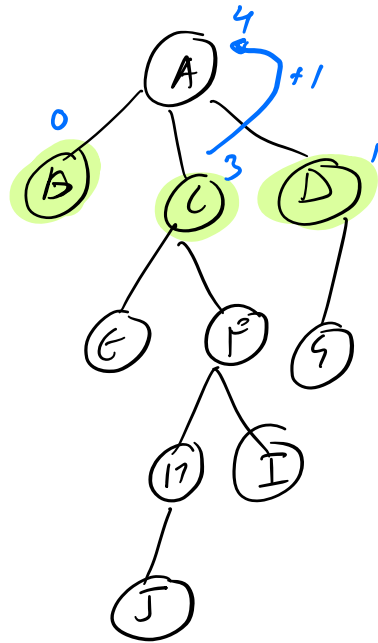
Length of the longest path  
from that node to any of  
it's descendants

$$h(C) = 3$$

$$h(B) = 0$$

$$h(D) = 1$$

$$h(A) = 4$$



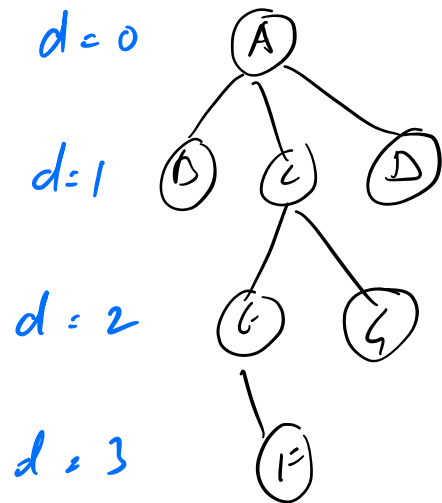
$$h(A) = 1 + \text{MAX}(h(B), h(D), h(C))$$

$$\underline{h(\text{node}) = 1 + \text{max height of it's children!}}$$

⑥ Depth of a Node

[ Distance from the root ]

Depth  $\equiv$  Level

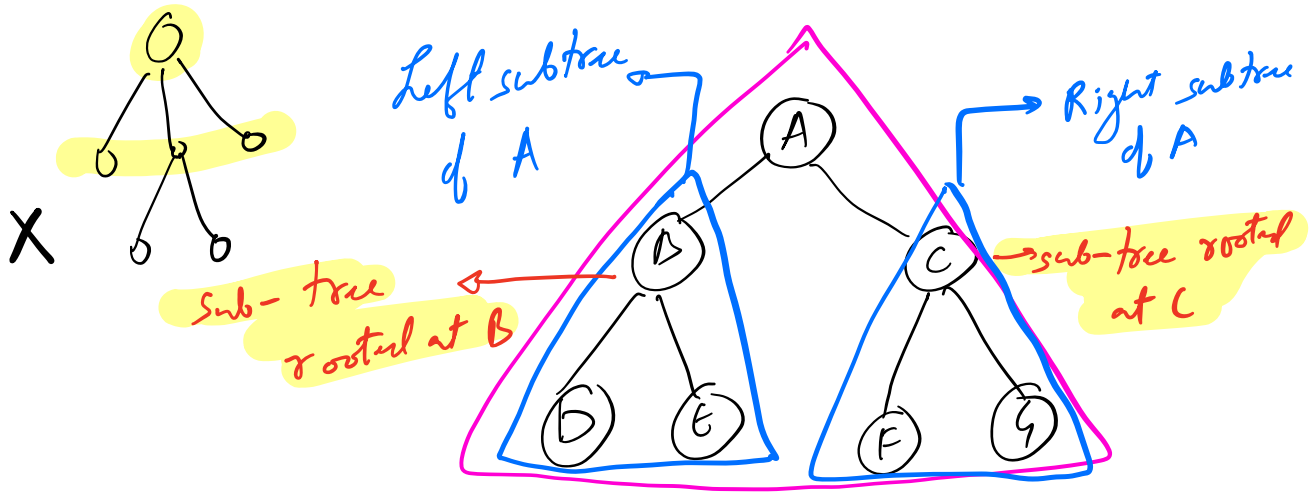
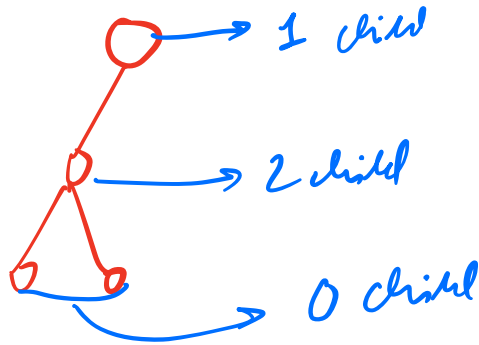


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⑦ Height of a tree ?

= height (root)

Binary Tree → [ Every node would have  
AT MAX 2 children ]

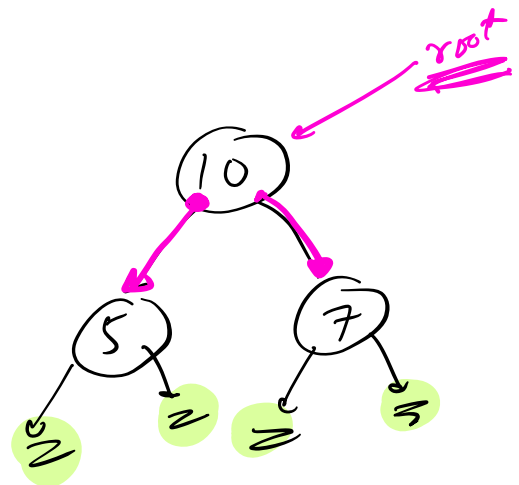
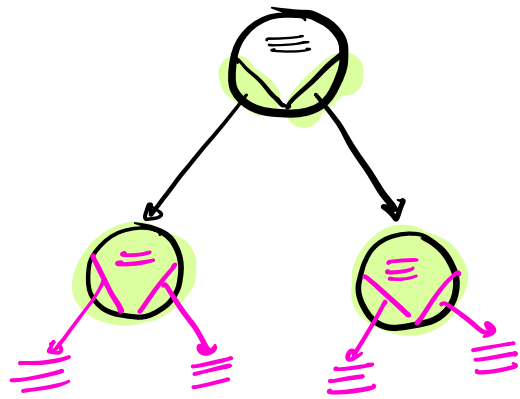


① subtree rooted at a node is:  
that Node & all its descendants!

```

class Node {
    int data;
    Node left;
    Node right;
    Node(val) {
        data = val;
        left = NULL;
        right = NULL;
    }
}

```



```

Node root = new Node(10);
root.left = new Node(5);
root.right = new Node(7);

```



Tree traversal →

PREORDER	INORDER	POSTORDER
<b>D</b> L R	L <b>D</b> R	L R <b>D</b>

① Preorder **D L R**

1. process the data of the current node!

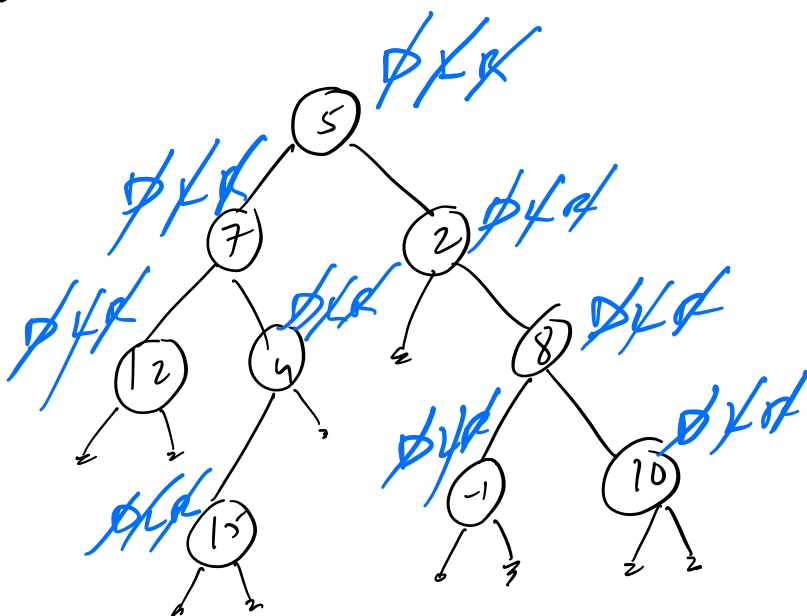
2. traverse the left subtree of the current node in preorder fashion

3. right

& print in preorder fashion!

5, 7, 12, 4, 15

2, 8, -1, 10

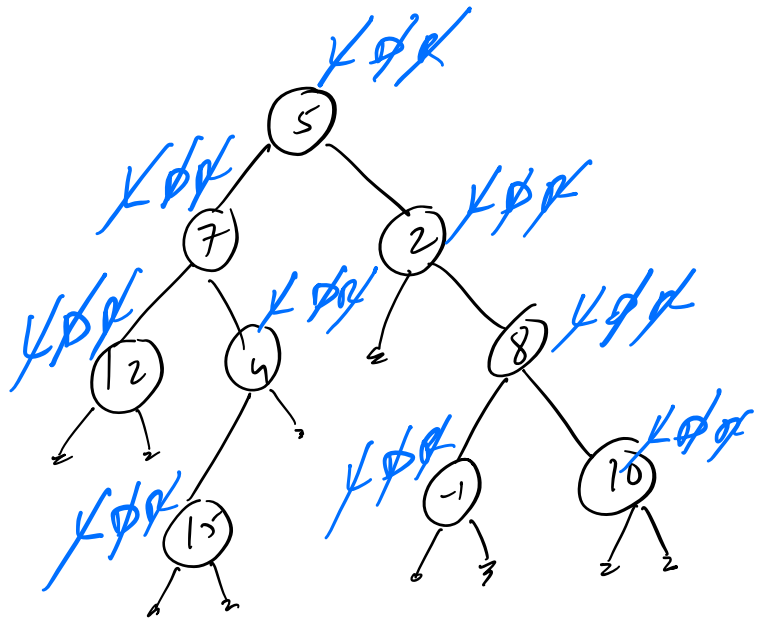


IN ORDER

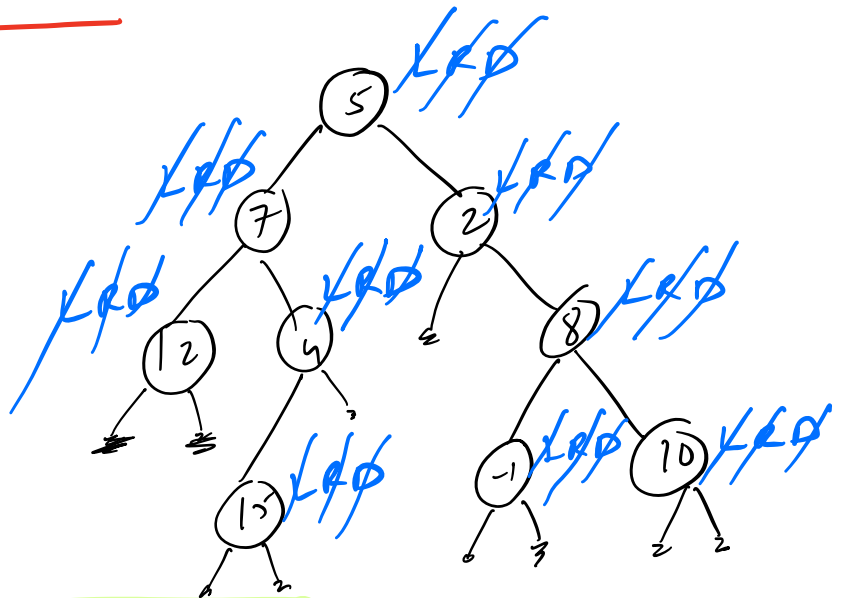
L D R

1. traverse the left subtree of the current node in inorder fashion
2. process the data of the current node!
3. right

12, 7, 15, 4, 5  
2, -1, 8, 10,



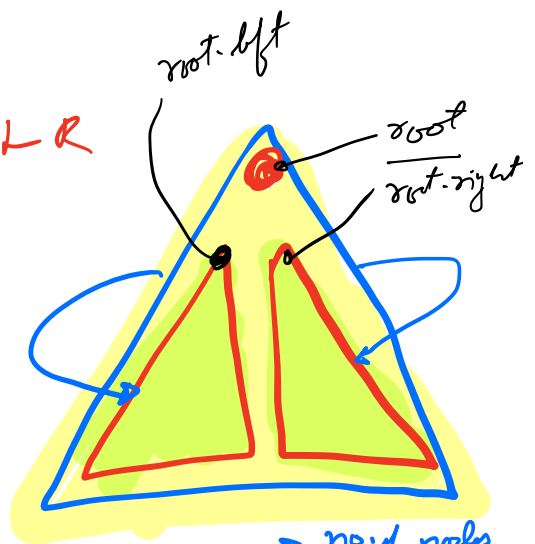
## POST ORDER [L R D]



12, 15, 4, 7, -1, 10, 8, 2, 5

## CODE : PREORDER DLR

```
void preorder (Node root) {
    // Ass: print the tree rooted at root
    // in preorder fashion
    if (root == NULL) return;
    print (root.data);
    preorder (root.left);
    preorder (root.right);
}
```

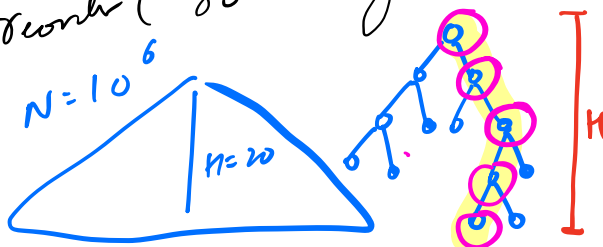


no. of nodes  
 $TC = N \times O(1)$

$TC = O(N)$

$SC = O(H)$

$H \rightarrow$  height of tree!



HW

Code for INORDER & POSTORDER!

Q Given a B.T. Find the no. of nodes!

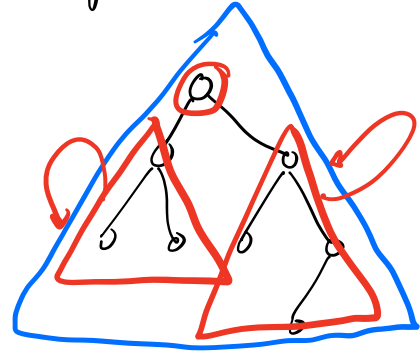
```
int cut(Node r) {
```

// Ans: ret the # nodes in  
tree rooted at 'r'

```
if (r == NULL) ret 0;
```

```
ret cut(r.left) + cut(r.right) + 1;
```

```
}
```



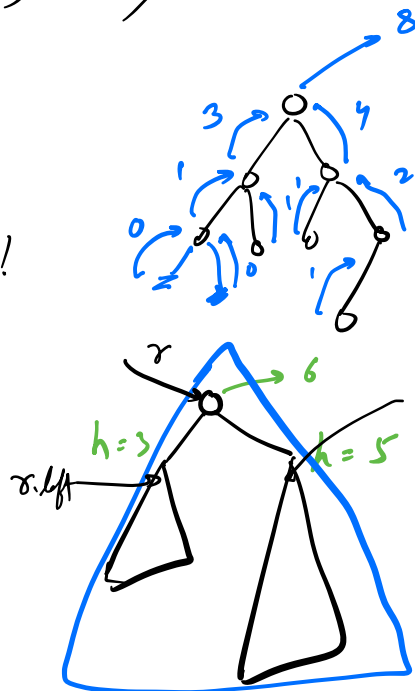
Q Given a B.T. Find the height!

```
int h(Node r) {
```

```
if (r == NULL) ret -1;
```

```
ret 1 + max { h(r.left),  
             h(r.right) };
```

```
}
```

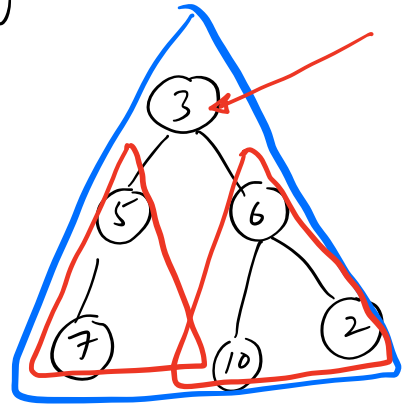


Q Given a B.T. Each node has a val.  
Find the sum of values of all nodes!

```
int sum(Node r) {  
    if (r == NULL) return 0;
```

```
    return (sum(r.left)  
            + sum(r.right)  
            + r.val);
```

```
}
```



~~TL~~  $TL = O(N)$

~~SL~~  $SL = O(N)$