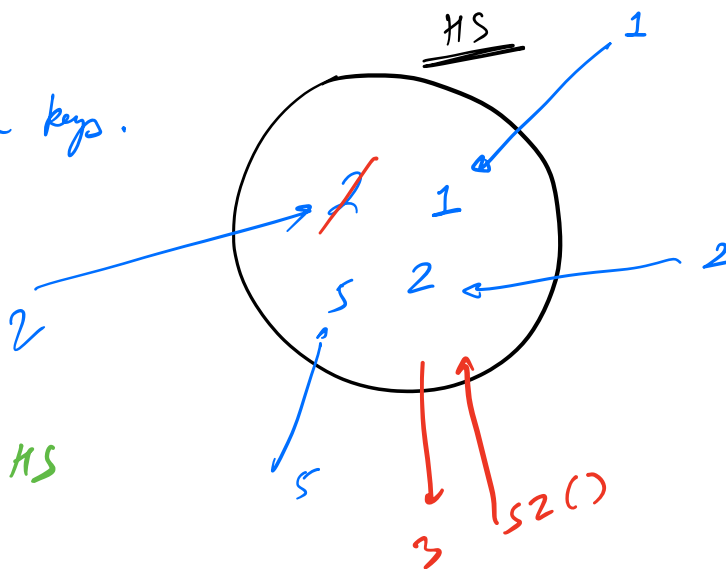


## Hashing - 1

① HashSet < Key >

→ D.S. contains unique keys.



fns

- 1) Insert(Key)
- 2) check if some key is in HS
- 3) Remove(Key)
- 4) Size → # of Keys!

TC = O(1) for ops.

HS does NOT maintain ANY order!

Tree Set : Maintains ORDER (SORTED: ASC)

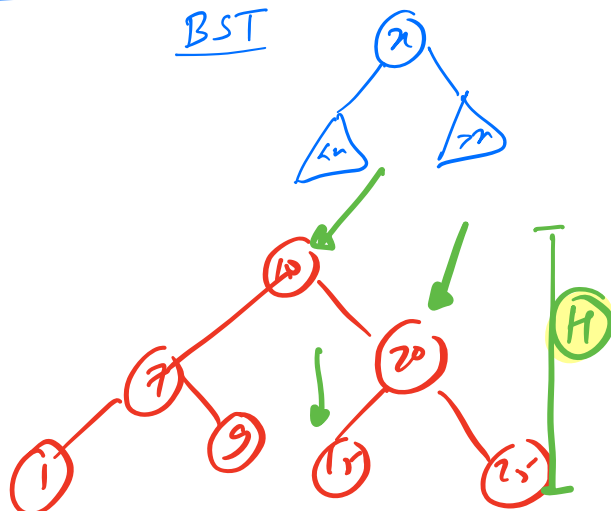
fns

SAME AS ABOVE

TC = O(log N)

Search,  
Insert,  
delete

BST



B B S T [Balanced B S T]

- AVL
- Red Black tree

$$H \rightarrow \frac{\log N}{2}$$

Internally uses ~ B S T !

Hash Map < key, value >

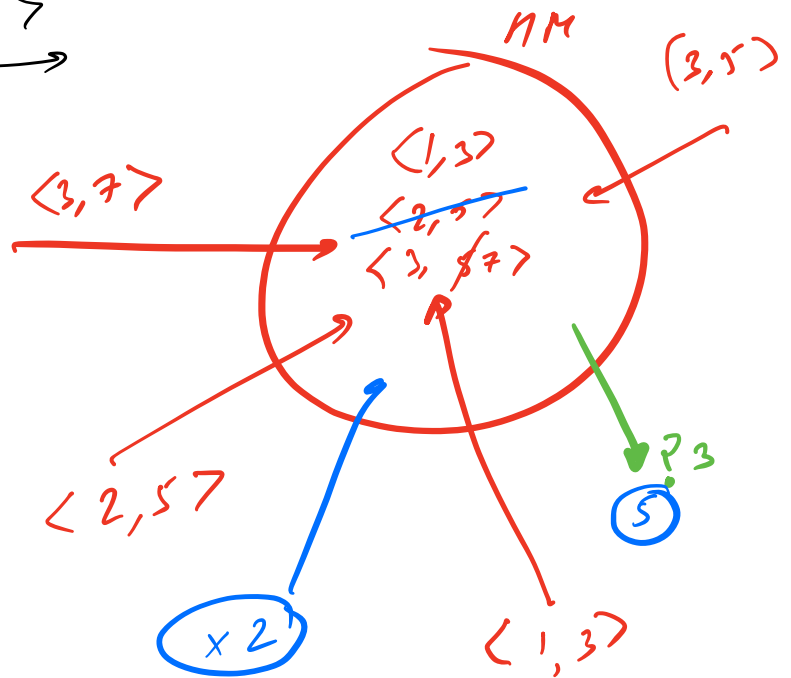
→ DS which contains  
<K, V> pair.  
Keys are UNIQUE.

fns

- insert(K, V)
- get(K)
- del(K)
- size()

TC = O(1) ops

Keys are NOT ordered!

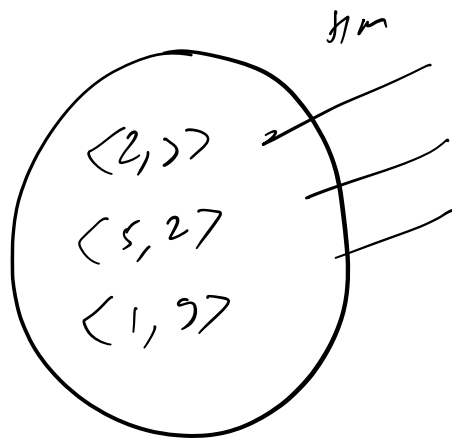


Tree Map  $\langle k, v \rangle$

Keys are ordered!

sorted: ASC

$\langle 1, 3 \rangle$   
 $\langle 2, 3 \rangle$   
 $\langle 5, 2 \rangle$



f''

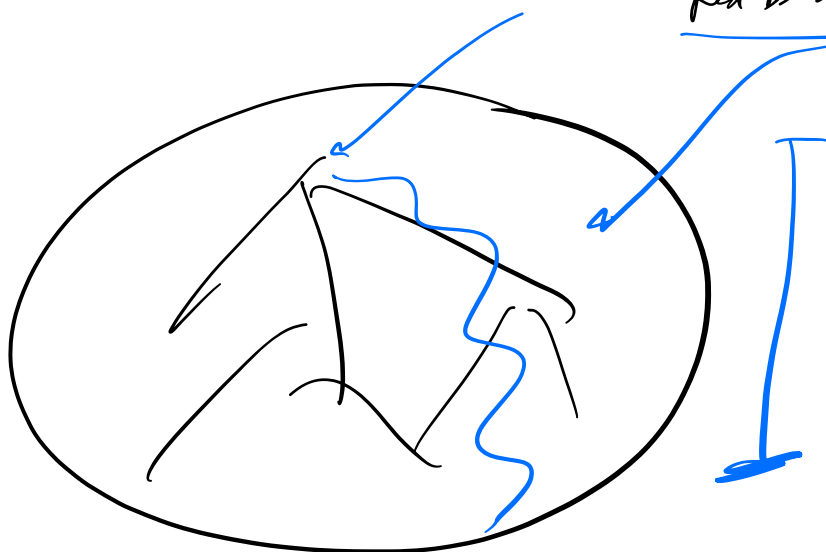
ALL SAME as ABOVE

$TC = O(\log N)$

In  
die  
get

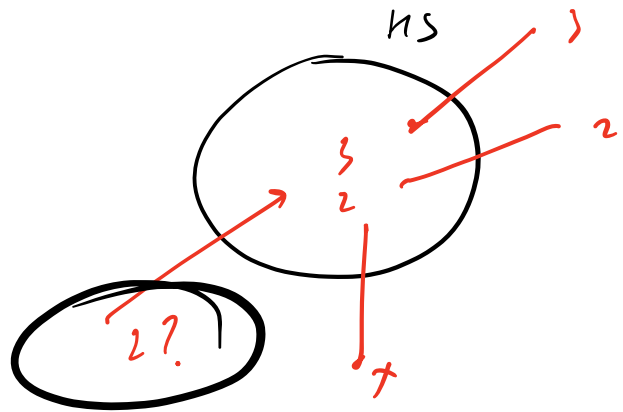
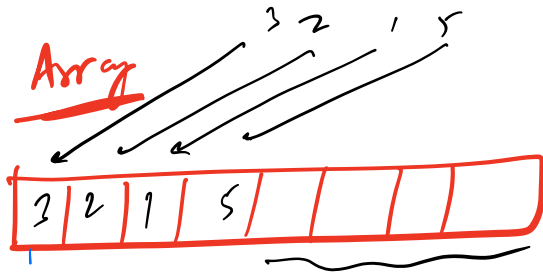
Internal implementation is **BST**

Red black tree.

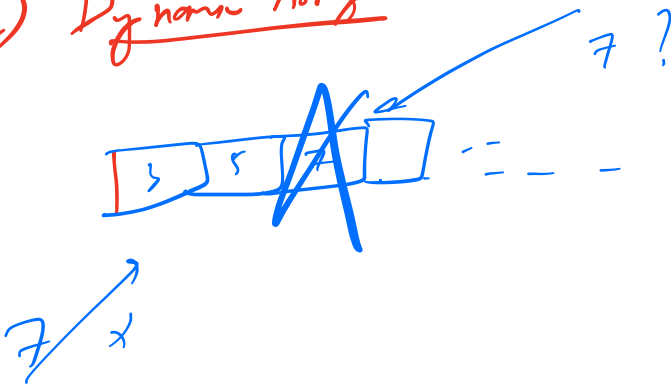


Implement HS

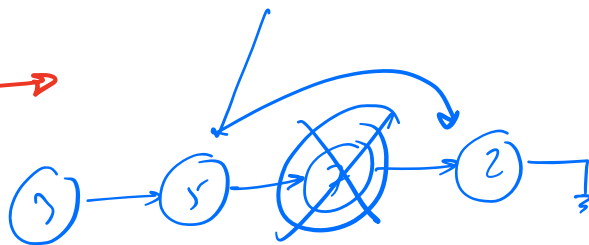
1) Array



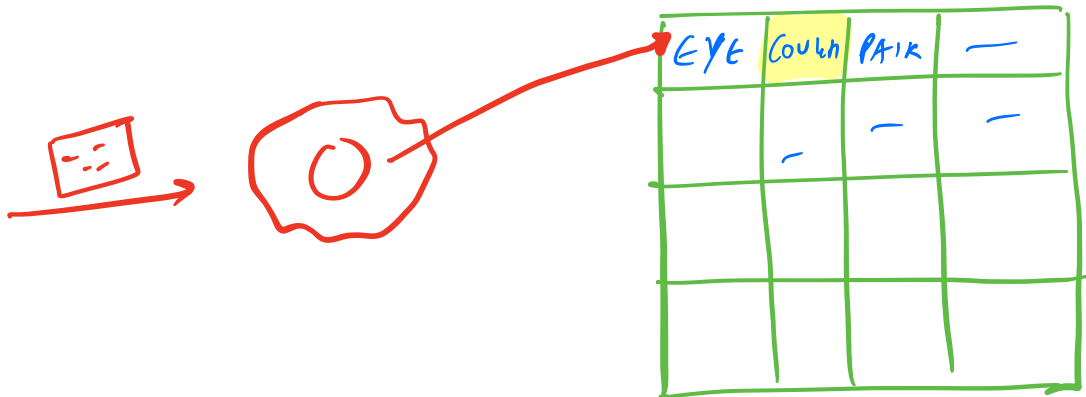
2) Dynamic Array



3) LL



CHEMIST



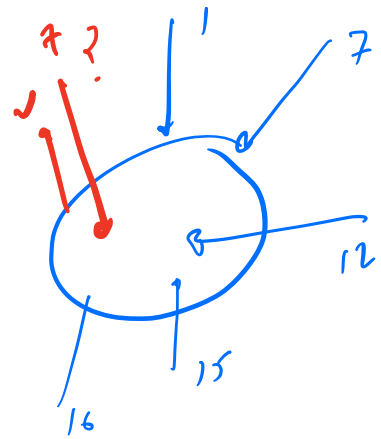
HASH TABLE

1) LL 2) BBST

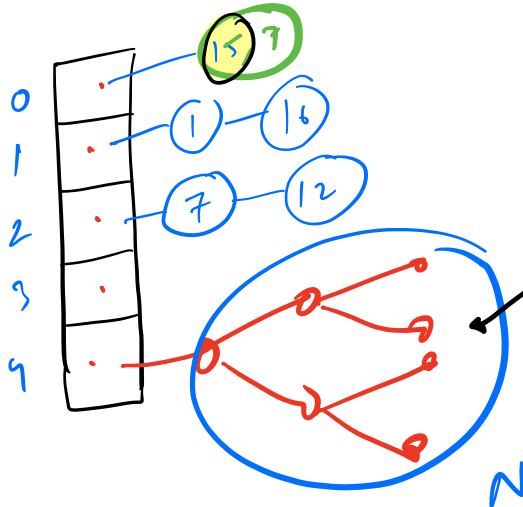
Hash function



$\% 5$   
[0-4]



M=5



$\log(N/M)$

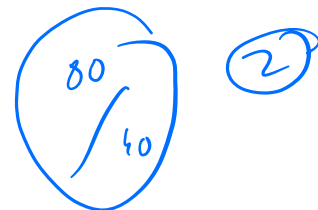
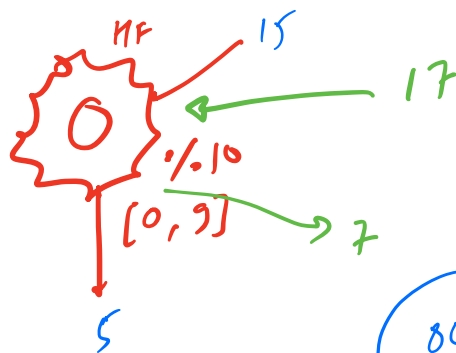
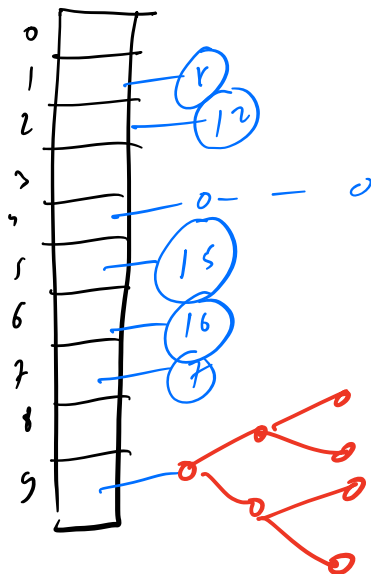
TC ↑

$\frac{a(1)}{b(1)}$

Load factor : (0.5)

RE-HASHING

$M=10$

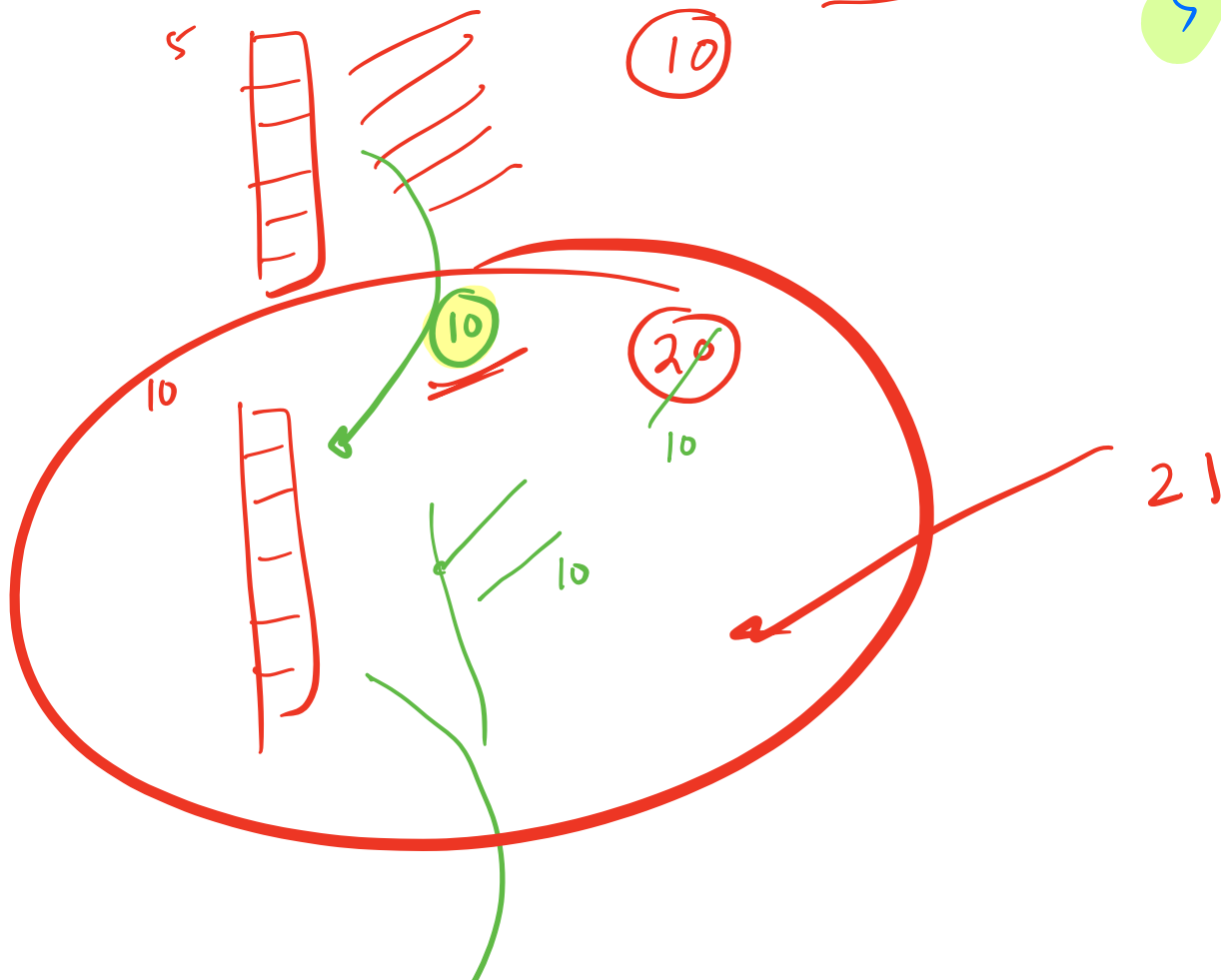


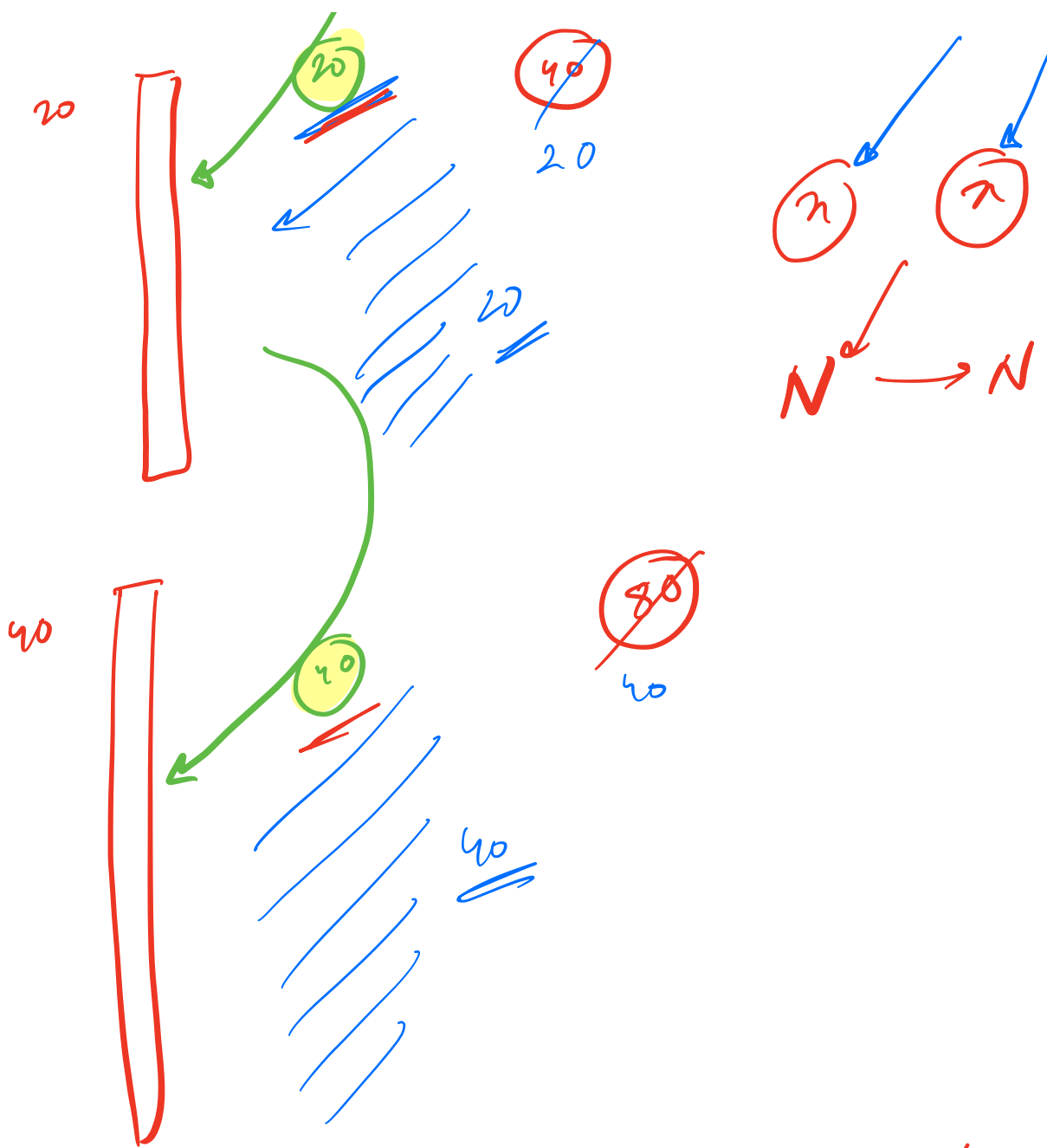
$\lg \left( \overset{9 \uparrow}{N/m} \right)$

$O(\lg(\overset{1 \uparrow}{N/m}))$



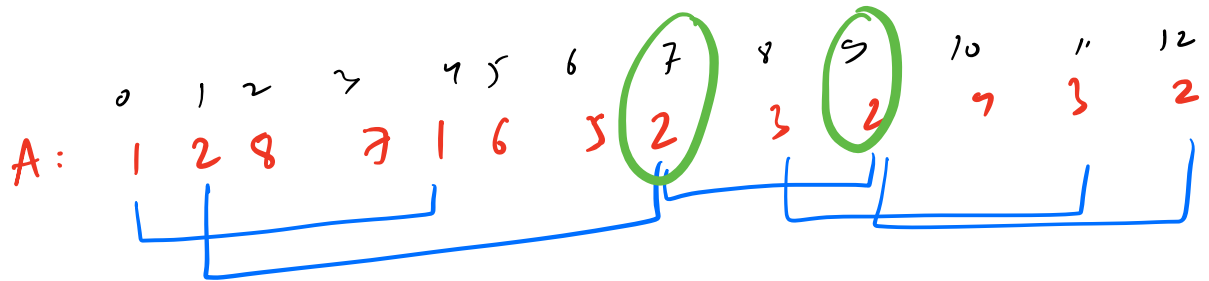
(10)



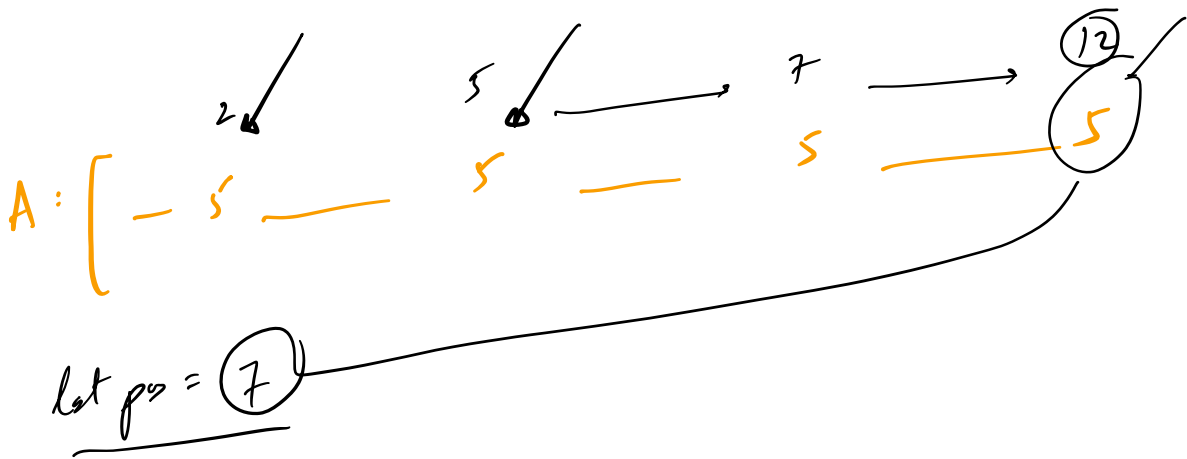
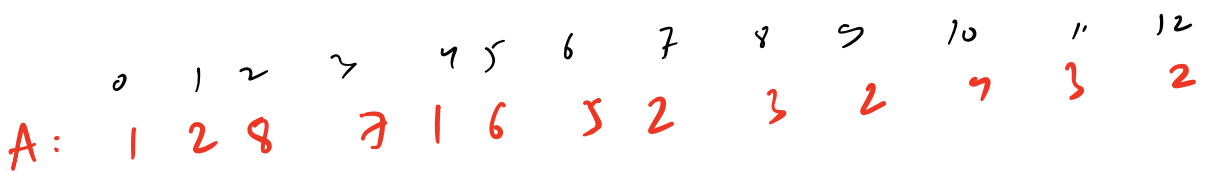


$$1 + 2 + 4 + 8 + \dots + \frac{N}{2} = N$$

Q Given an Array  $A[]$ .  
 Find pair  $(i, j)$  :  $A_i = A_j$  &  $\text{abs}(j-i)$  is MINIMUM



$(7, 9)$





$$A: \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 \\ 1 & 2 & 8 & 7 & 1 & 6 & 5 & 2 & 3 & 2 & 7 & 3 & 2 \end{matrix}$$

ANS  
 ~~$\infty$~~   
~~2~~  
 $(i, j)$   
 ~~$(1, 1)$~~   
 ~~$(0, 4)$~~   
 $(7, 9)$

HM [last pos]

$\langle 1, 4 \rangle$   
 $\langle 2, 7 \rangle$   
 $\langle 8, 2 \rangle$   
 $\langle 7, 3 \rangle$   
 $\langle 6, 5 \rangle$   
 $\langle 5, 6 \rangle$   
 $\langle 3, 8 \rangle$

HashMap < int, int > hm;  
 ANS =  $\infty$ , p = -1, q = -1;  
 for (i: 0  $\rightarrow$  N-1) {  
     if (hm.contains(A[i])) {  
         lastpos = hm[A[i]];  
         diff = i - lastpos;  
         if (diff < ANS) {  
             ANS = diff;  
             p = lastpos, q = i;  
         }  
     }  
 }

$\boxed{TC = O(N)}$   
 $\boxed{SC = O(N)}$

$$\} \text{hm}[A[i]] = i;$$

$\} \text{ret}(p, q);$

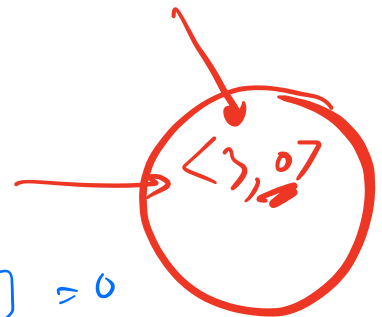
Q Given an Array: Longest S.A with sum = 0

	0	1	2	3	4	5	6
A:	3	6	4	-10	11	-11	0
PS:	3	9	13	3	14	3	3

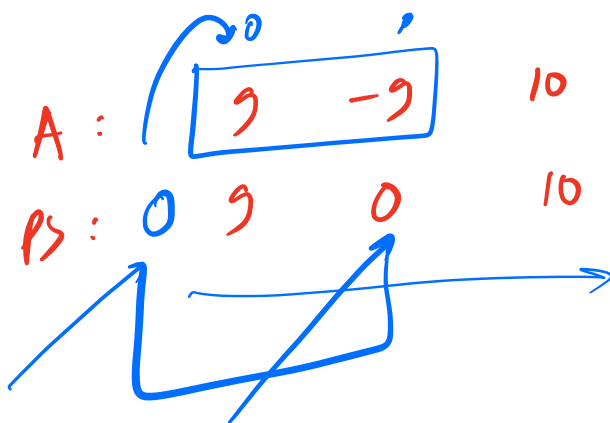
$S=0$

$$\text{sum}[L, R] = \text{PS}[R] - \text{PS}[L-1] = 0$$

$$\Rightarrow \boxed{\text{PS}[R] = \text{PS}[L-1]}$$



idea: Store the 1st occ..



HashMap < int, int > hm;

hm[0] = -1;

ANS = -∞, p = -1, q = -1; ps = 0

f ( i: 0 → N-1 ) {

if ( hm.containsKey ( ps ) ) {

first pos = hm[ ps ];

diff = i - first pos;

if ( diff > ANS ) {

ANS = diff;

p = first pos + 1, q = i;

}

}

else hm[ ps ] = i;

return ( p, q );

TC = O(N)

SC = O(N)

Q

Given an array. Find the length of the longest consecutive sequence!

A: [100, 4, 200, 1, 3, 2] → 4

$n, n+1, n+2, \dots$

A: [10, 5, 17, 7, 3, 6, 1, 2, 8] → 4

1) Sort

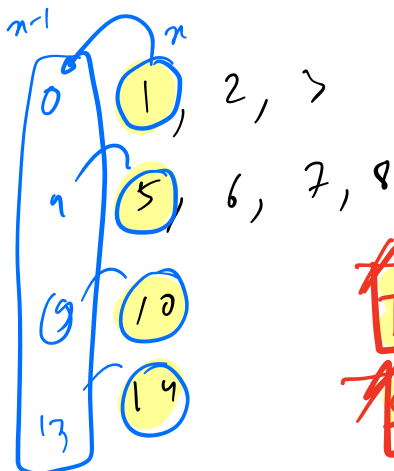
TC =  $O(N \log N)$

Ans  
4

[1, 2, 3, 5, 6, 7, 8, 10, 14]

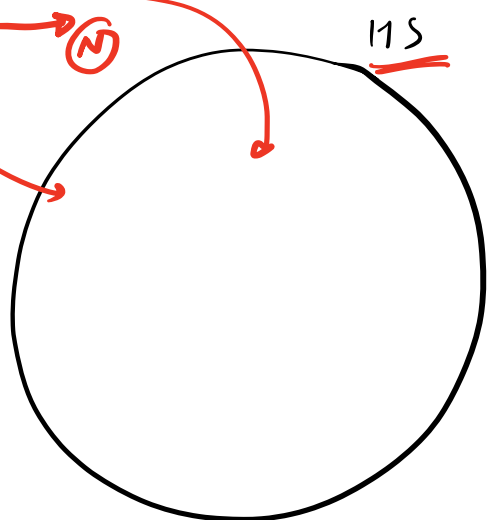
A: [10, 5, 17, 7, 3, 6, 1, 2, 8]

$O(N)$



TC =  $O(N)$

SL =  $O(N)$



Q Flip & find Nearest  
 Given a Binary Array of size  $N$ .

Q queries

- Q 1 X  $\longrightarrow$   
 Q 2 X  $\longrightarrow$

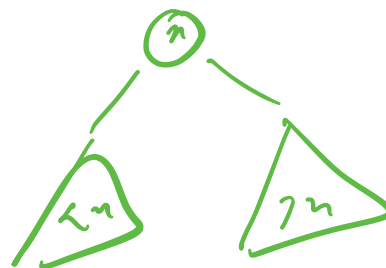
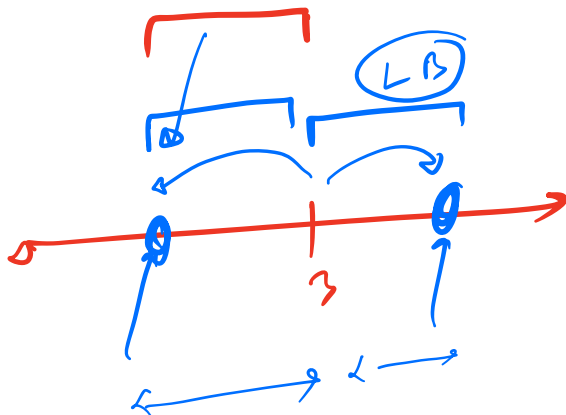
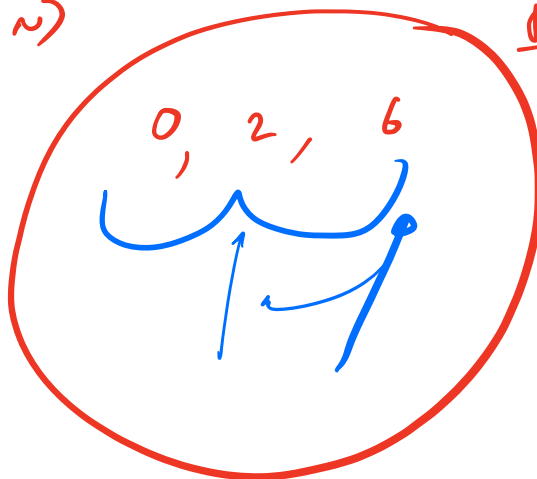
flip the bit at  $x^{\text{th}}$  pos  
 find the index of the  
 nearest 1 from X.

A:      0    1    2    3    4    5    6    7  
          1    0    1    0    0    0    1    0

2 3  $\longrightarrow$  2  
 1 3  
 2 3  $\longrightarrow$  3

LO(3)

True Set <int>  
 pos



lower\_bound(n) → first element  $\geq n$

→  $O(\log N)$

$$TC = O(N \log N + \log \log N)$$

lower\_bound(n) → first no:  $\geq n$   
Upper\_bound(n) → \_\_\_\_\_:  $> n$

