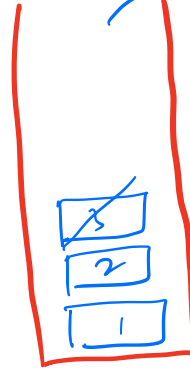
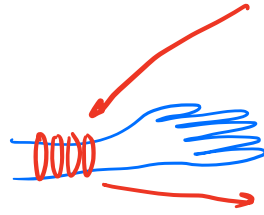
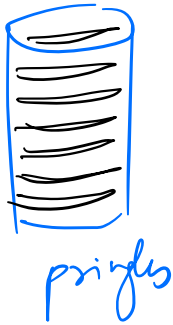
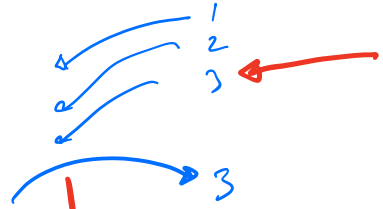


Stack

LIFO



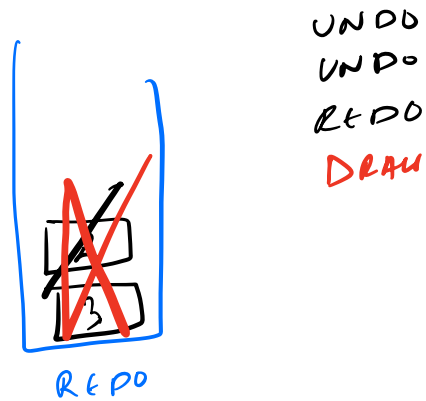
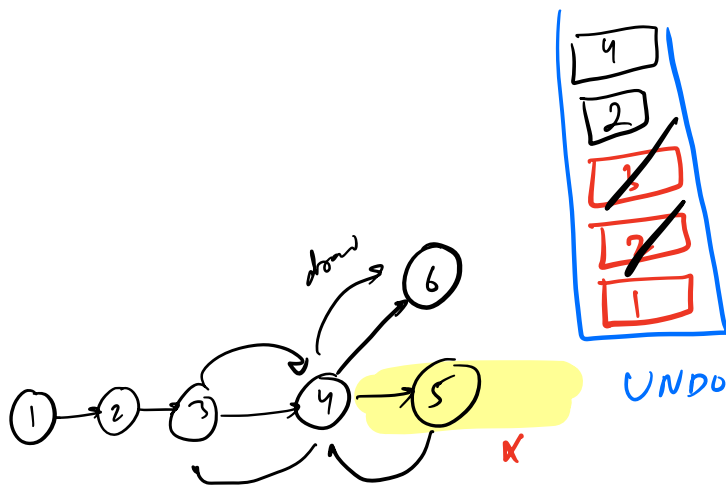
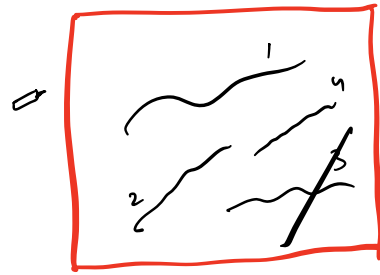
Ops of a stack

- ① push(x) → push x at the top of the stack
- ② pop() → remove the topmost —
- ③ top(), peek() → ret the topmost —
- ④ size() → ret the # of items —

$$TC = O(1)$$

Applications of Stack

- Recursion
- Undo / redo



UNDO
UNDO
REDO
DRAW

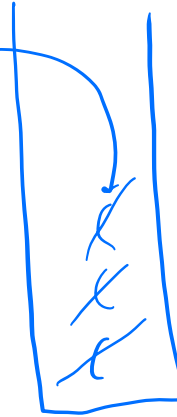
- ① back / fwd button : browser
- ① expression evaluation
- ① parenthesis check
- ① Reverse anything!



I Given an expression. Validate the parenthesis.

() (())

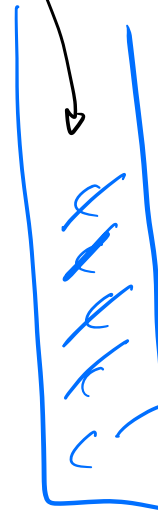
VALID



: stack empty

((())) (())

INVALID



: stack not empty!

$TC = O(N)$

$SC = O(N)$

II maintain an open variable

$(() (()))$
 $op = 0$ 1 2 1 2 3 2 1 0 $\xrightarrow{1) op = 0 \text{ At end}}$
 $\hookrightarrow \text{VALID}$

$(())) ()$
 $op = 0$ 1 2 1 0 \swarrow
NOT VALID!

$TC = O(N)$
 $SC = O(1)$

Q

SAME ques

$()$, $[]$, $\{ \}$

$(\{ () \} []) \{ () \}$

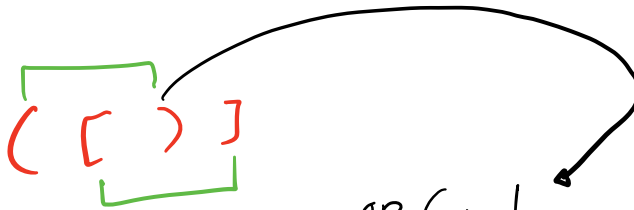
1) STACK

VALID!

$TC : O(N)$
 $SC : O(N)$

$\{$
 $\{$
 $\{$
 $\{$
 $\{$

2) 3 Variables
X

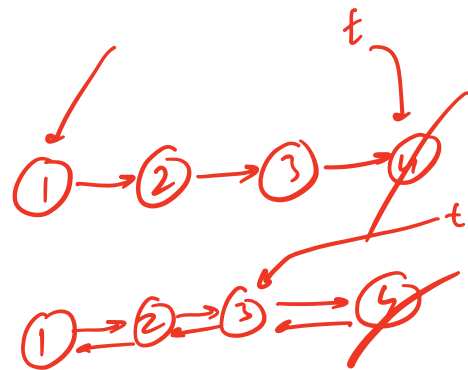


op [: 1
op [: 1
?

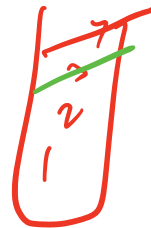
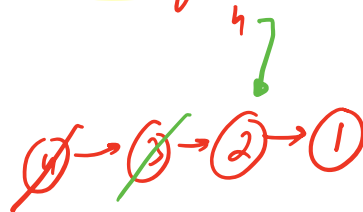
① Implementation of Stack

① Array → Static X
 → dynamic ✓

② LL → SLL → ✓✓
 → DLL → ✓



SLL: Adding & removing at head.



Q Given a string. Remove every consecutive duplicate pair of char until there are none left.

S: a c ~~b b~~ c k

a ~~c c~~ k

(a k)

S: a b c ~~k k~~ c b a ~~m m~~ d c

a b ~~c c~~ b a n c

a b ~~a a~~ n c

a b ~~n n~~ c

(b c)

c
~~a~~
m
~~k~~
~~c~~
~~b~~
~~a~~

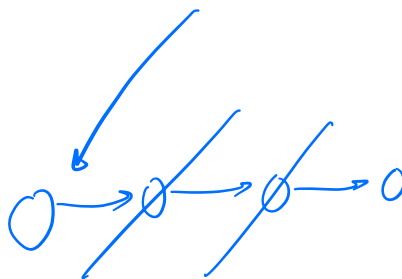
~~c~~
~~m~~

~~m~~
~~c~~

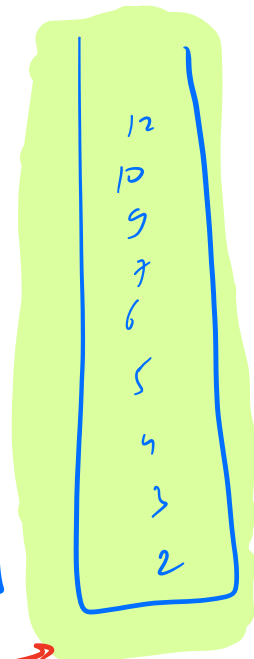
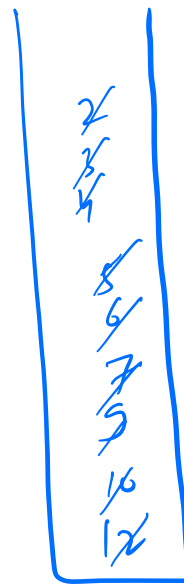
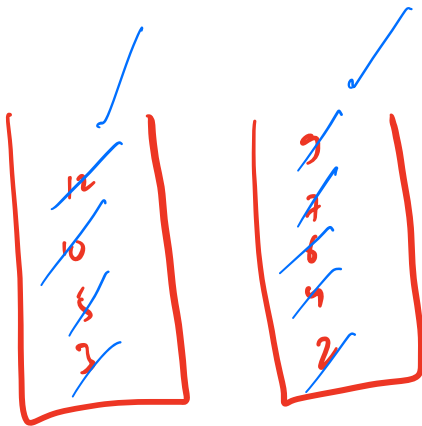
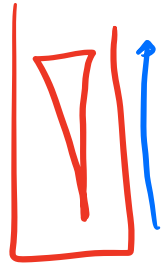
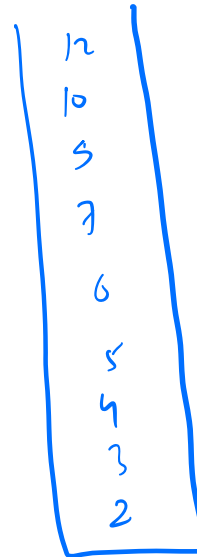
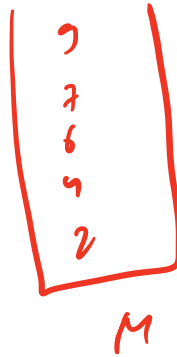
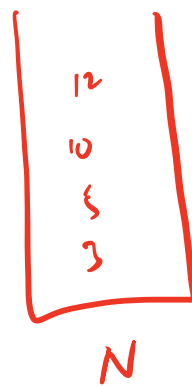
"m c"

TC = $O(N)$

SC = $O(N)$



Q Given 2 sorted stacks. Merge them into 1 sorted stack!

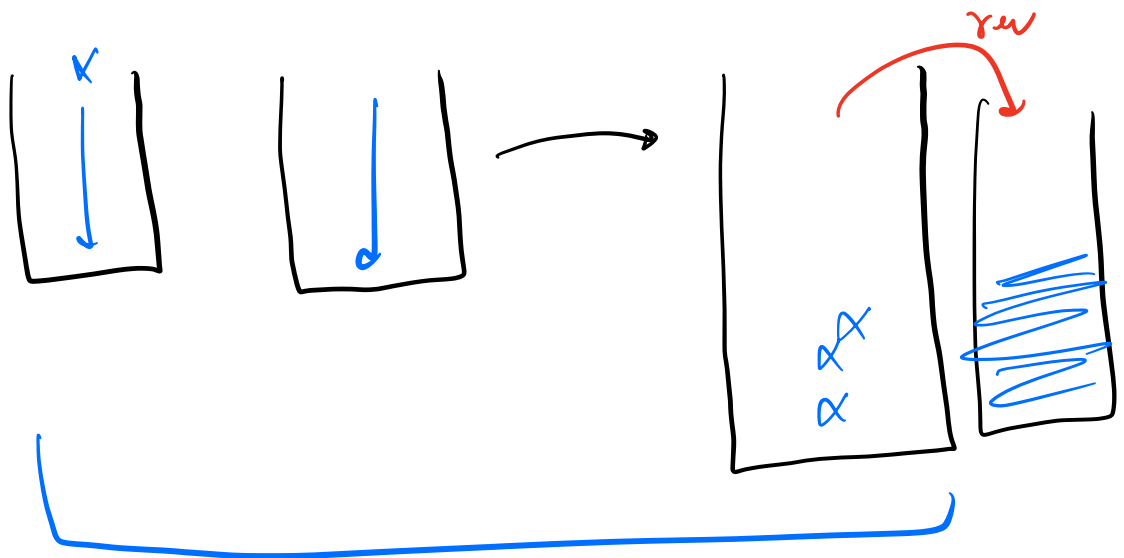


Reverse it

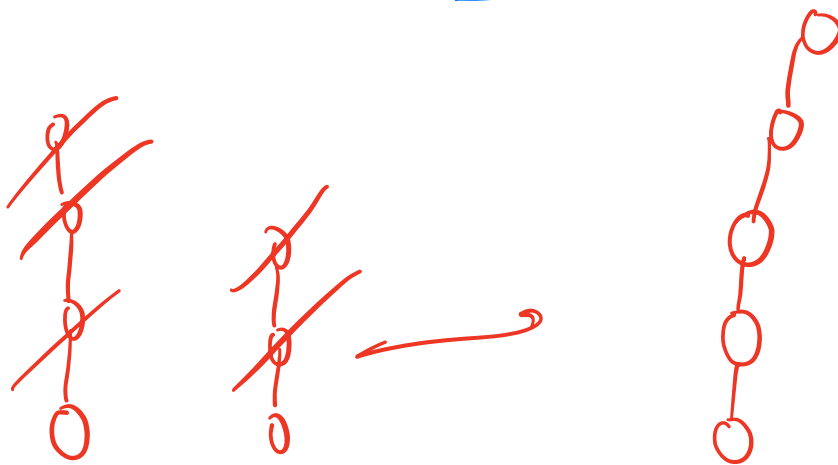
$$TC = O(N+M)$$

$$SC = O(N+M)$$

$$O(1)$$



N+M ?




```
stack < int > merge ( stack < int > s1, , stack < int > s2 ) {
```

```
    stack < int > s;
```

```
    while ( ! s1.isempty() && ! s2.isempty() ) {
```

```
        if ( s1.top() > s2.top() ) {
```

```
            s.push(s1.top());
```

```
            s1.pop();
```

```
        }
```

```
        else {
```

```
            s.push(s2.top());
```

```
            s2.pop();
```

```
        }
```

```
    } while ( ! s1.isempty() ) {
```

```
        s.push(s1.top());
```

```
        s1.pop();
```

```
    } while ( ! s2.isempty() ) {
```

```
        s.push(s2.top());
```

```
        s2.pop();
```

```
    } while ( ! s.isempty() ) {
```

```
        s1.push(s.top());
```

```
        s.pop();
```

```
    } return s1;
```

Q Given a stack! Sort it!

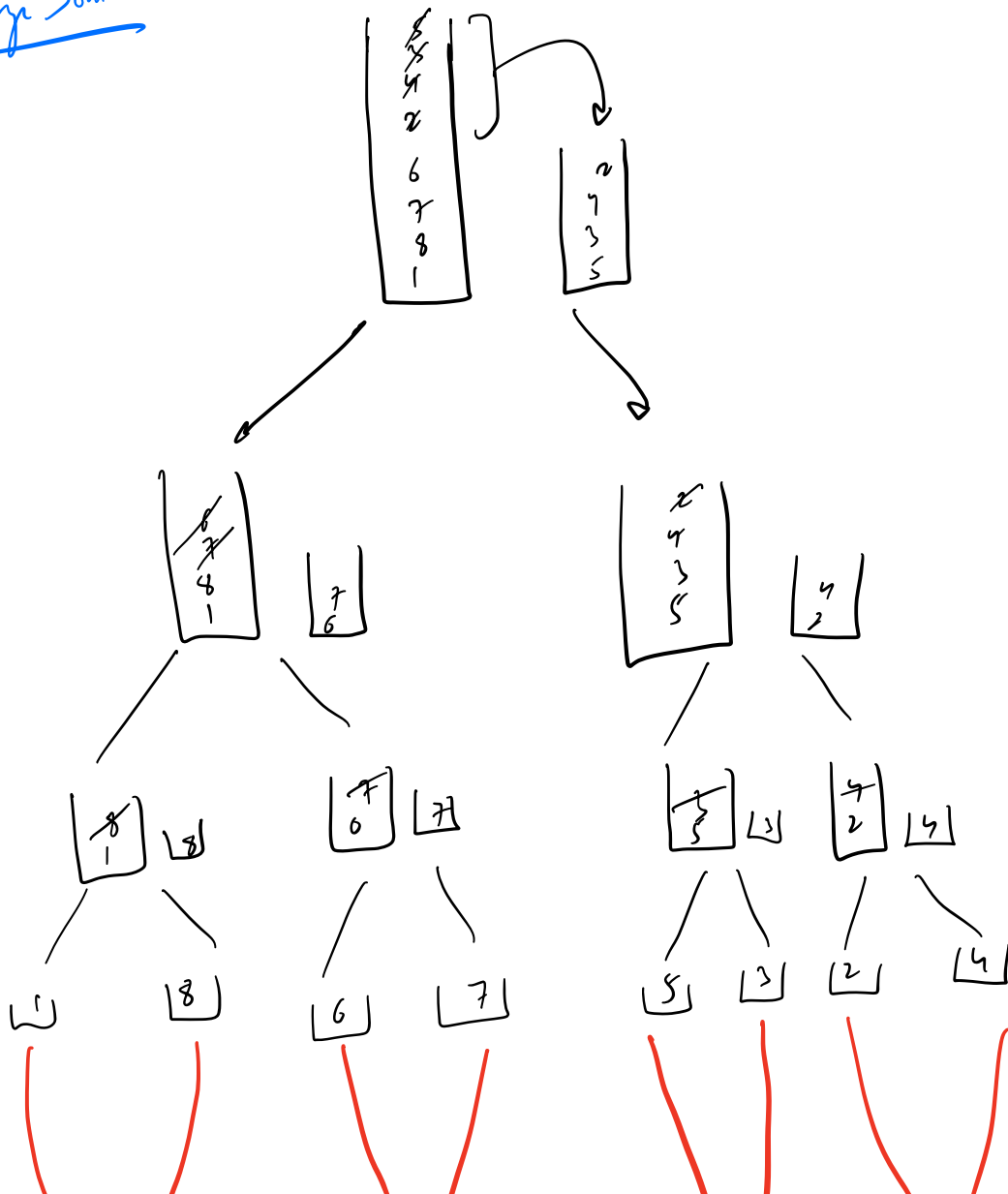
6
9
11
7
10

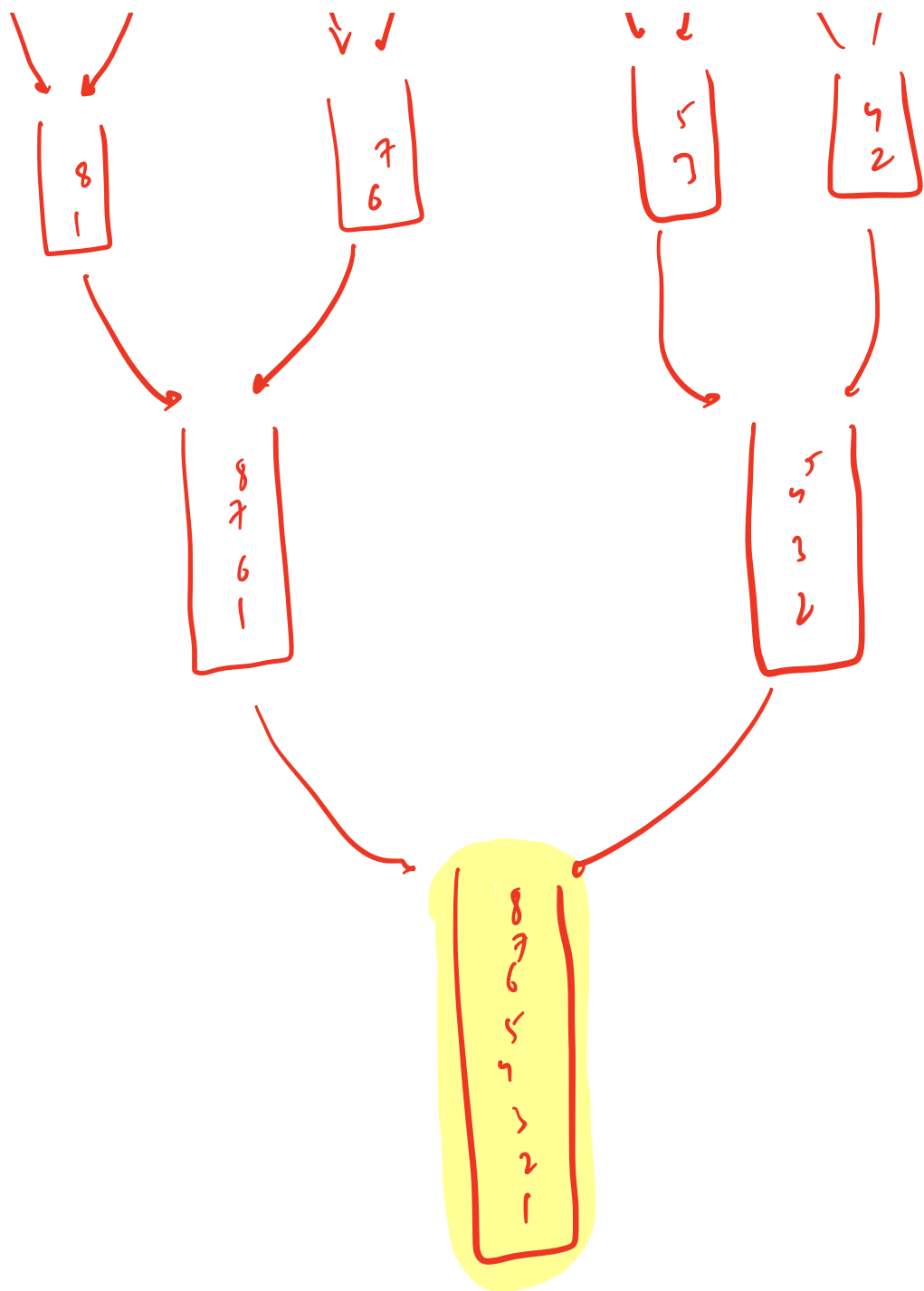
Sort

11
10
9
7
6

ASL

Merge Sort

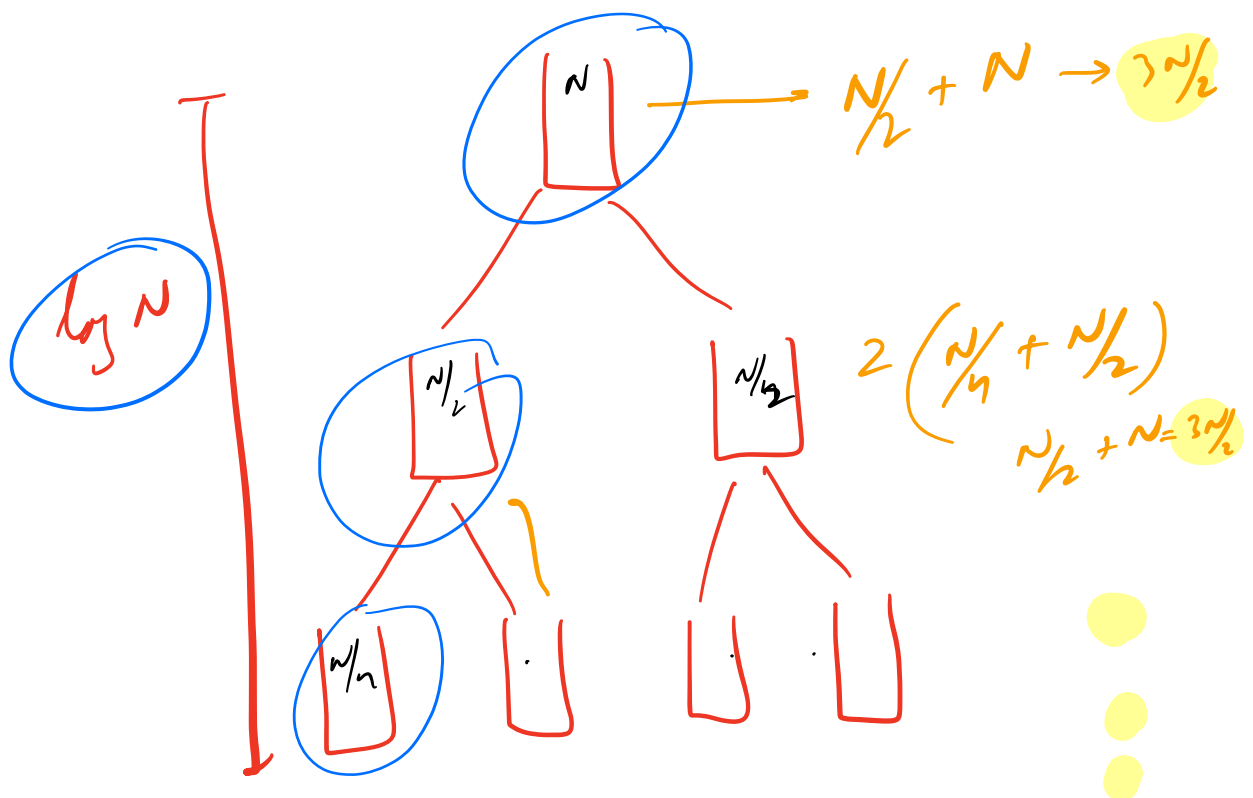
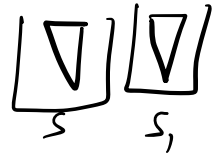




```

stack<int> mergeSort (stack<int> s) {
    if (s.size() <= 1) return s;
    stack<int> s1;    s2 = s.size()
    for (i=0; i < s2/2; i++) {
        s1.push(s.top());
        s.pop();
    }
    s = mergeSort(s);
    s1 = mergeSort(s1);
    return merge(s, s1);
}

```



$$TC = O(N \log(N))$$

$$SC = O(\log N)$$