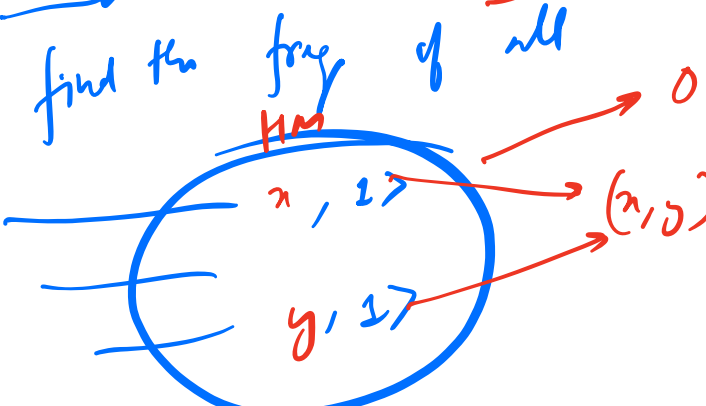


Q Given N elements.
 Every element repeats twice except 2 elements,
 which occur exactly once!
 find these 2 elements!

A: [3, 6, 4, 4, 3, 8] \rightarrow (6, 8) ^{ANS}

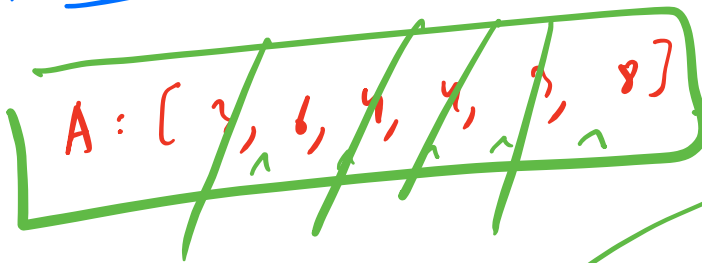
1) HM
 find the freq of all

 $O(N)$
 $O(N)$
 $(x, 0)$
 $(y, 0)$
 $TC = O(N)$
 $SC = O(N)$

2) Sort

Sorted A: [3, 3, 4, 4, 6, 8]

$TC = O(N \log N)$
 $SC = O(1)$

3) XOR →



$$6 \wedge 8$$

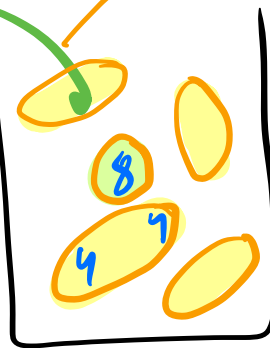
$$\begin{array}{r} 110 \\ \wedge 1000 \\ \hline 1110 \rightarrow 14 \end{array}$$

14
x = 0
XOR: 8

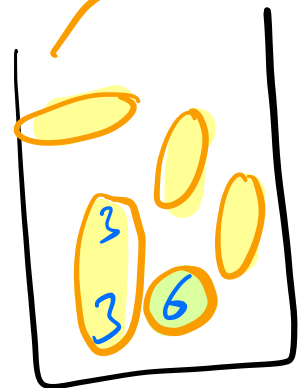
70
XOR: 6

3	:	0011
6	:	0110
4	:	0100
3	:	0011
4	:	0100
8	:	1000

XOR
 $\wedge 1110$



jth bit is
UNSET



jth bit is
SET

$xor = 0;$

$f(i: 0 \rightarrow N-1) \{$
 $xor = xor \wedge A[i];$

$\rightarrow O(N)$

$\}$

$pos = -1;$

$f(i: 0; i < 31; i++) \{$
 $if (xor \& (1 << i)) > 0 \{$

$pos = i; break;$
 $\}$

$\}$

$x = 0, y = 0;$

$f(i: 0 \rightarrow N-1) \{$
 $if (A[i] \& (1 << pos)) > 0 \{$

$y = y \wedge A[i];$

$\}$

$else \{$

$x = x \wedge A[i];$

$\}$

$\}$

$ret(x, y)$



$\rightarrow O(1)$

$\rightarrow O(N)$

$T.C = O(N)$

$S.C = O(1)$

Q Given an Array of size N .
 Array contains all elements in $[1, N+2]$
 except 2 elements. Find the 2 missing elements.

$N = 4$ $[1, 4+2] \rightarrow [1, 6]$

$A : [3, 6, 1, 4] \rightarrow (2, 5)$

1) HM

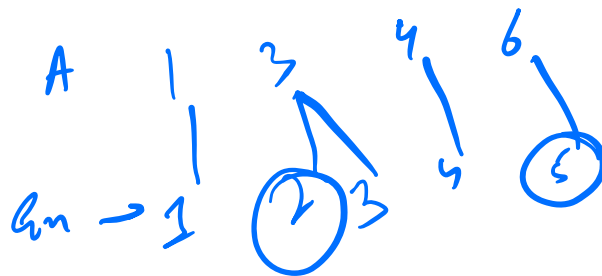
TC $O(N)$

SC $O(N)$

2) Sort

TC $= O(N \log N)$

SC $= O(1)$

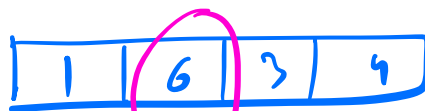


3) SEND HOME TECHNIQUE

TC $= O(N)$

SC $= O(N)$

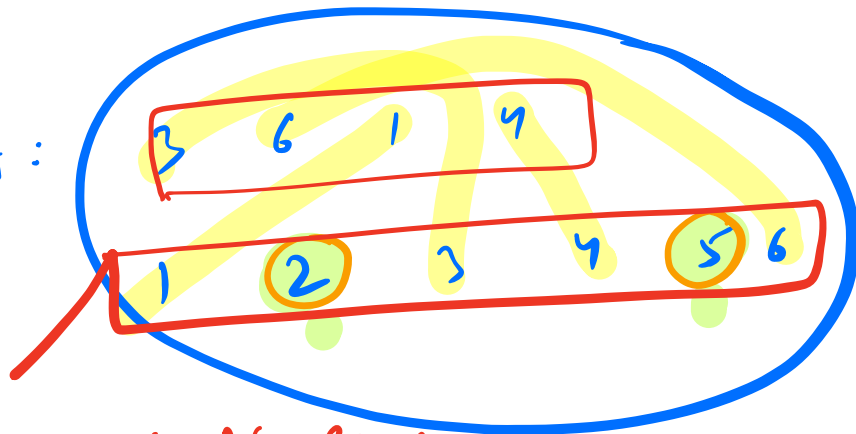
$\rightarrow O(1)$ SAME ARRAY



CASE WORK

n) ~~N=4~~ A:

[1, N+2]



SAME AS PREV !!!

xor = 0

```
f (i: 0 → N-1) {  
    xor = xor ^ A[i]
```

```
}
```

```
f (i: 1 → N+2) {  
    xor = xor ^ i;
```

```
}
```

...

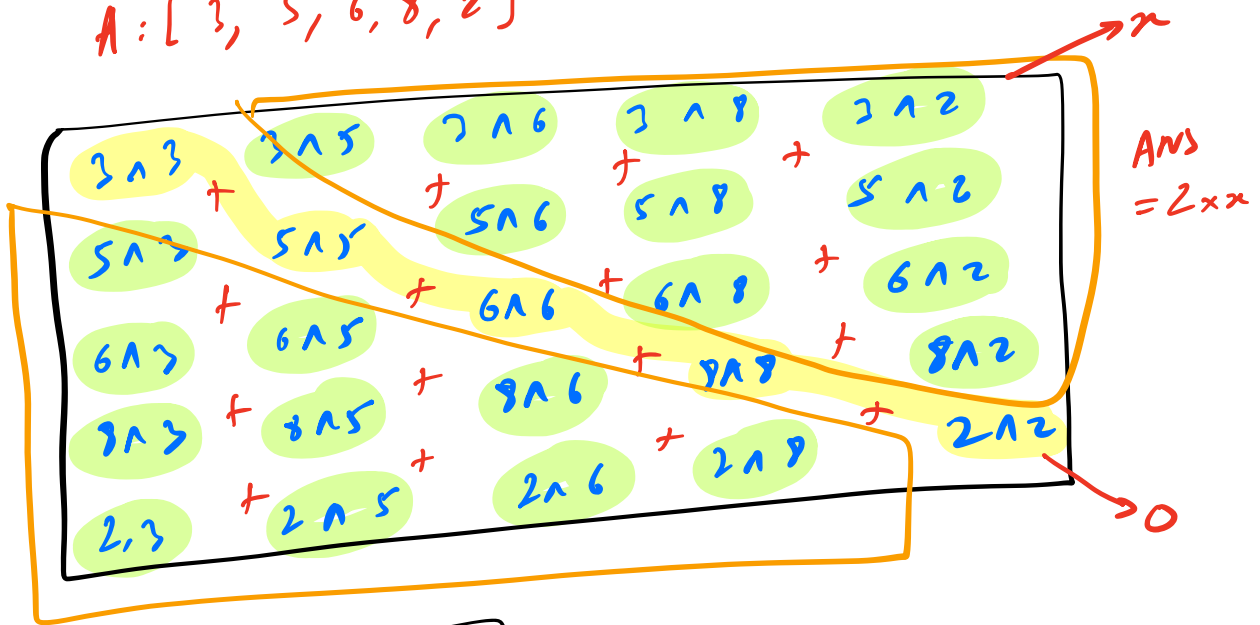
SAME ..

~~TC~~ $TC = O(N)$

$SC = O(1)$

Q Given N elements.
Calculate the XOR sum of all pairs.

$A: [3, 5, 6, 8, 2]$

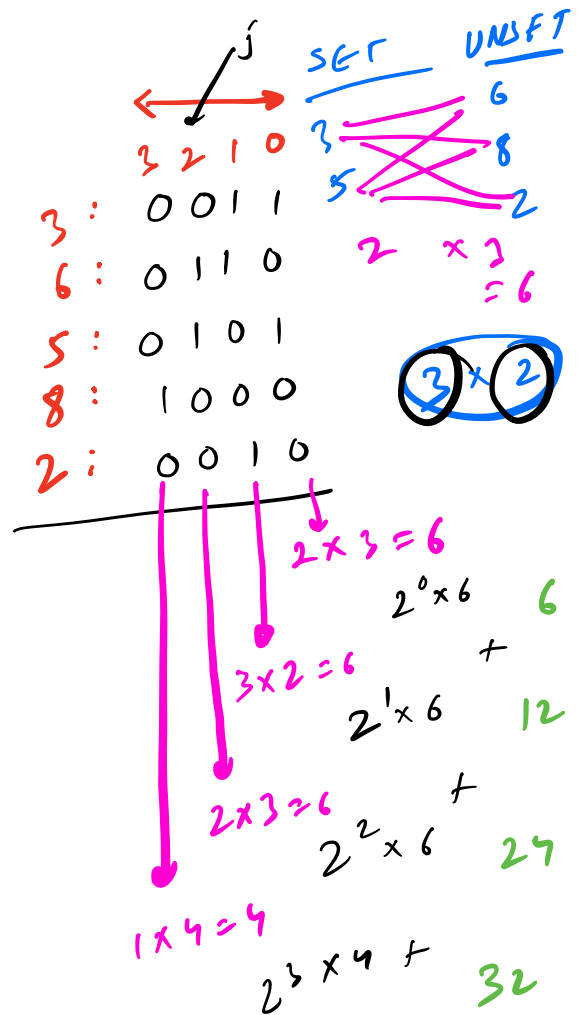


I) BF $TC O(n^2)$
 $SC O(1)$

II)

$3 \wedge 5$:	6	:	0	1	1	0
$3 \wedge 6$:	5	:	0	1	0	1
$3 \wedge 8$:	11	:	1	0	1	1
$3 \wedge 2$:	1	:	0	0	0	1
$5 \wedge 6$:	3	:	0	0	1	1
$5 \wedge 8$:	13	:	1	1	0	1
$5 \wedge 2$:	7	:	0	1	1	1
$6 \wedge 8$:	14	:	1	1	1	0
$6 \wedge 2$:	4	:	0	1	0	0
$8 \wedge 2$:	10	:	1	0	1	0

74



ANS : 148 $\times 2 = 74$

$m\text{-bits} \rightarrow \sim \log_2(\text{MAX}(A)) \rightarrow N$: 3

```
ANS = 0
f(j: 0  $\rightarrow$  m-bits) {
    cZero = 0, cOne = 0
    f(i: 0  $\rightarrow$  N-1) {
        if ((A[i] & (1 << j)) > 0) cOne++;
        else cZero++;
    }
}
```

$ANS += (1 << j) \times cZero \times cOne;$

```
}
return (ANS << 1);
```

$TC = O(\log(\text{Max}(A)) \times N)$

$SC = O(1)$

Q Given an array.
find the MAX value of $(A[i] \& A[j])$ $\forall (i, j)$
 $i \neq j$

$A: [27, 18, 20]$

27: 11011

18: ~~10010~~

10010 → 18

18: 10010

20: ~~10100~~

10000 → 16

27: 11011

20: ~~10100~~

10000 → 16

MAX

18 AND

$A: [26, 13, 23, 28, 27, 7, 25]$

MSB → 210 LSB

26: 11010

~~13: 01101~~

~~23: 10111~~

~~28: 11100~~

27: 11011

~~7: 00111~~

~~25: 11001~~

AND: 11010 → 26

1000
0111

1. find $\text{MAX}(A)$

2. $\text{max-bits} = \sim \log(\text{MAX}(A))$: 7

$\text{ANS} = 0;$

$f(j = \text{max-bits}; j \geq 0; j--) \{$

$\text{cnt} = 0;$

$f(i: 0 \rightarrow N-1) \{$

$\text{if}((A[i] \& (1 << j)) > 0) \{$

$\text{cnt}++;$

$\}$

$\}$

$\text{if}(\text{cnt} \geq 2) \{$

$\text{ANS} = (\text{ANS} | (1 << j));$

$f(i: 0 \rightarrow N-1) \{$

$\text{if}((A[i] \& (1 << j)) == 0) \{$

$A[i] = 0;$

$\}$

$\}$

$\}$

$\text{out ANS};$

$\text{TC} = O(N \cdot \log(\text{MAX}(A)))$

$\text{SC} = O(1)$