

Q Given N array elements
 Check if there exists a pair (i, j)
 s.t. $A[i] + A[j] = K$ ($i \neq j$)

2-SUM

$A: \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 8 & 9 & 1 & -2 & 4 & 5 & 11 & -6 & 7 & 5 \end{matrix}$

$K=11 \rightarrow (4, 8) : 4 + 7 = 11 \rightarrow \text{true!}$

$K=22 \rightarrow \text{false!}$

1) BF

```

for (i: 0 → N-1) {
  for (j: i+1 → N-1) {
    if (A[i] + A[j] == K) {
      return true;
    }
  }
}
return false;

```

$TC = O(N^2)$
 $SC = O(1)$

2) HM

A: ⁰8 ¹9 ²1 ³-2 ⁴4 ⁵5 ⁶11 ⁷-6 ⁸7 ⁹5

$$K - A_j$$

$$11 - 5$$

$$= 6$$

$$A_i + A_j = K$$

$$A_i = K - A_j$$

$$K = 11$$

HashSet < int > hs;

for (i: 0 → N-1) {

find = K - A[i];

if (hs.contains(find) == true) {

return true;

} hs.insert(A[i]);

} return false;

TL = O(N)

SL = O(N)

Q Given an arr. Find the no. of pairs (i, j)
: $A_i + A_j = K$ $(i < j)$

I) BF

TL: $O(N^2)$
SL: $O(1)$

II) HM

A:

0	1	2	3	4	5	6	7	8	9
0	5	2	5	5	8	8	6	10	5

K=10

$\langle 0:1 \rangle$
 $\langle 2:1 \rangle$
 $\langle 5:3 \rangle$

$10 - 5$
 $= 5$

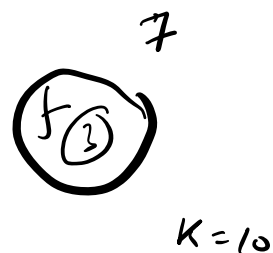
High Map < int, int > hm; $ANS = 0$

```

for (i: 0 → N-1) {
    find = K - A[i];
    ANS += hm[find];
    hm[A[i]]++;
}
return ANS;

```

$O(1)$



$TC = O(N)$

$SL = O(N)$

A: 0 1 2 3 4 5 6 7 8 9

 0 5 2 5 5 8 8 6 10 5

$K=10$

HM

<0, 1>

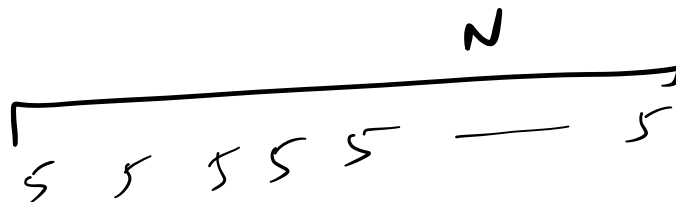
<5, 3>

<2, 1>

$K=10$

ANS

~~0~~ / 3



$N C_2$ $\frac{MAX}{ANS}$

$N(N-1)/2$

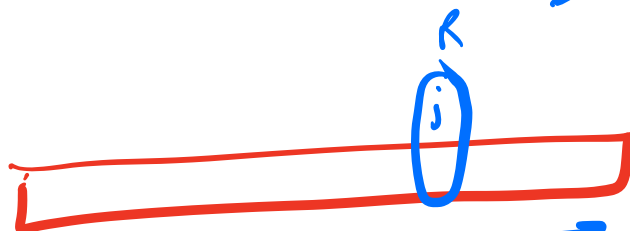
Q

Given an Array.

Find # pair (i, j) :

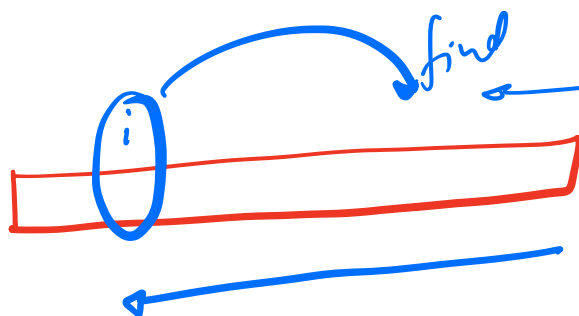
$$A_i - A_j = k$$

$$i < j$$



find

$$A_i = k + A_j$$



find

$$A_j = A_i - k$$

$$TC = O(N)$$

$$SC = O(N)$$

Q Given an Array. find the # of Sub-Arrays
where $SUM == K$

$K=2$

A:

1	2	1	0	1	0	1	0	1	1
---	---	---	---	---	---	---	---	---	---

PS:

--	--	--	--	--	--	--	--	--	--

$$sum(L, R) = K$$

$$PS[R] - PS[L-1] = K$$

$K=2$

A:

1	2	1	0	1	0	1	0	1	1
---	---	---	---	---	---	---	---	---	---

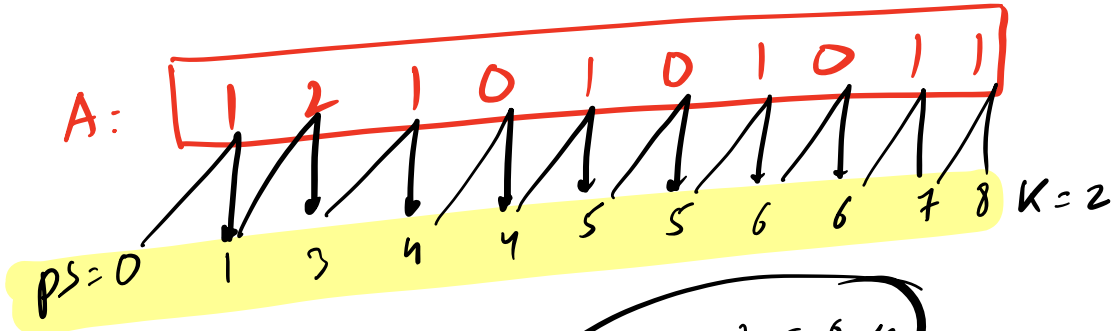
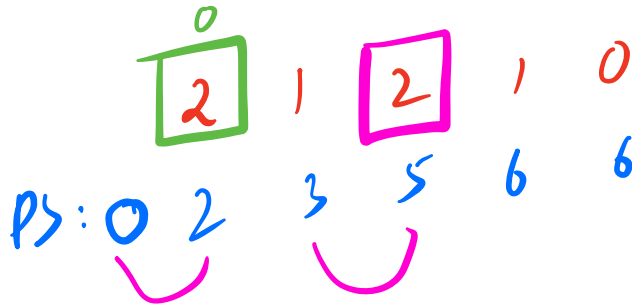
PS:

1	3	4	4	5	5	6	6	7	8
---	---	---	---	---	---	---	---	---	---

Idea: find the # of pair (i, j) in PS
: $A_j - A_i = K$ $i < j$

$R \rightarrow PS[R]$

Corner →
Car →

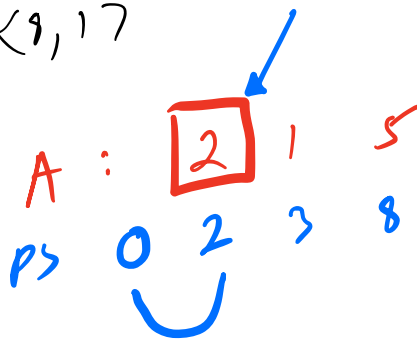


$$8 - 2 = 6 //$$

- HM
- <0, 17
 - <1, 17
 - <2, 17
 - <3, 27
 - <4, 27
 - <5, 27
 - <6, 27
 - <7, 17
 - <8, 17

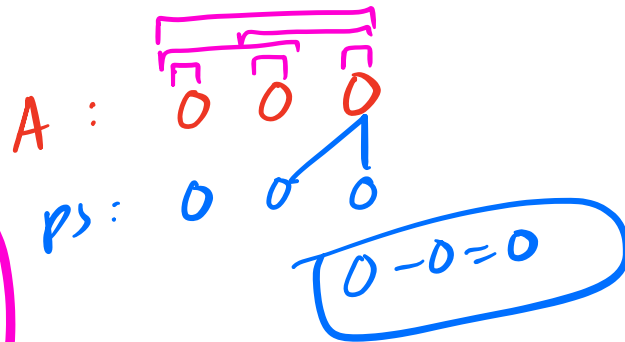
ANS

X Z 7 4 7 5
11



K=2

HM
 $\langle 0, 4 \rangle$



$K = 0$

Ans
 6

Q Given an array. Calculate the no. of **DISTINCT** elements in every subarray of size K .

A: 2 4 3 8 3 5 4 9 7 10 $K = 7$

#SA of size $K = N - K + 1$

1) BF

\checkmark S.A $\rightarrow (N - K + 1)$

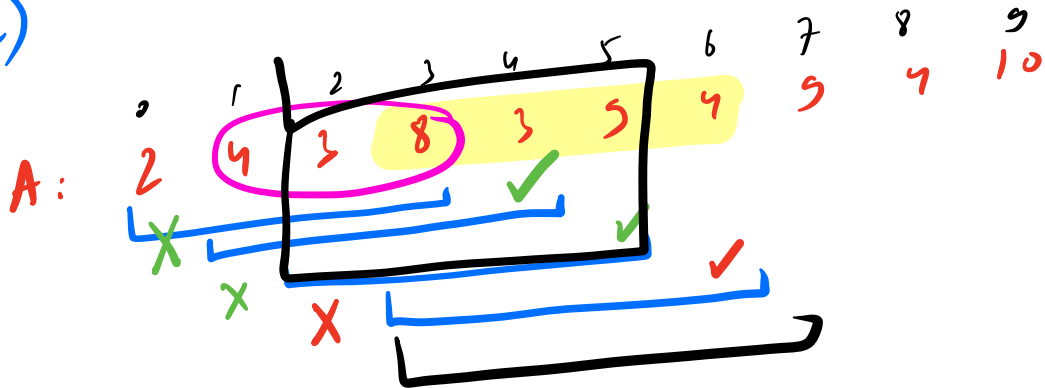
insert in HS
 find size!

$O(K)$
 $SC = O(K)$
 $TC = O(K(N - K))$

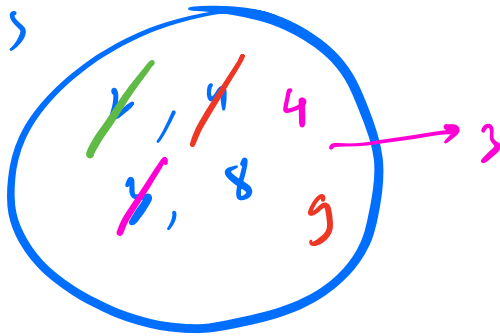
$K = N/2$

$\approx O(N^2)$

2)



ns



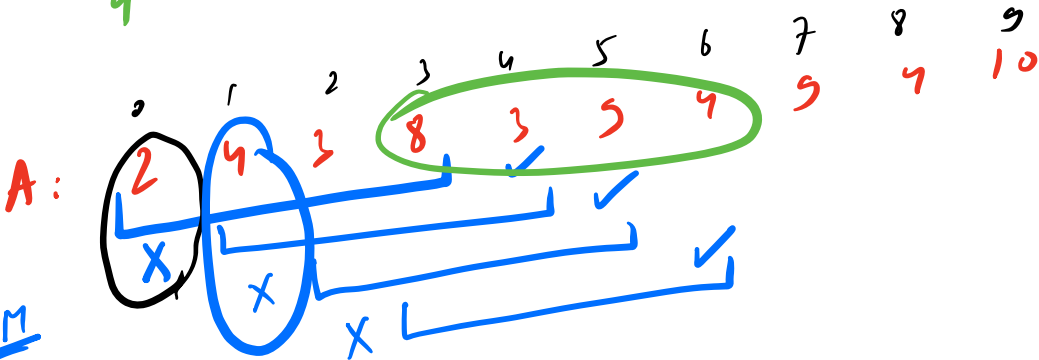
WRONG APPROACH

freq of element
MATTERS!

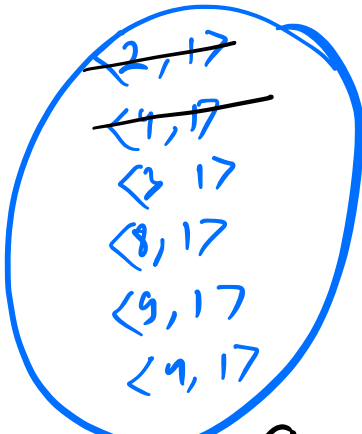
S2

4

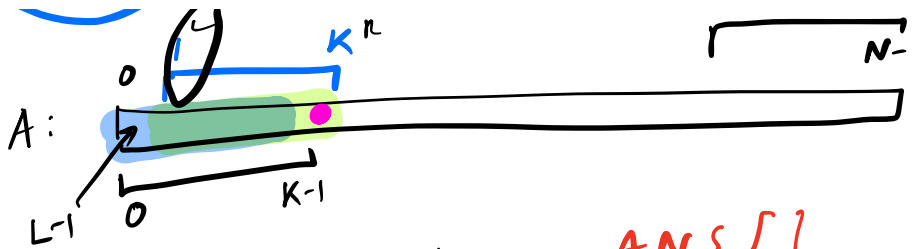
II



nm



S2: 4, 3, 3, 4



HashMap <int, int> hm; ANS[]

for ($i=0 \rightarrow k-1$) { $\rightarrow O(k)$
 $hm[A[i]]++$;

}
 $ANS.add(hm.size());$

$L=1, R=k;$

while ($R < N$) { $\rightarrow O(N-k)$
 $// [L, R] \rightarrow S.A$

$hm[A[R]]++$;

if ($hm[A[L-1]] == 1$) {
 $hm.remove(A[L-1]);$

}
 else $\rightarrow hm[A[L-1]]--$;

$ANS.add(hm.size());$

$L++, R++;$

}

return ANS;

$O(k + N - k)$

$TC = O(N)$

$SC = O(k)$