

Q: Given a binary array. Sort it!

A: [0, 1, 1, 0, 0, 1, 0] $\xrightarrow{\text{Q. sort (N log N)}}$
 \rightarrow [0, 0, 0, 0, 1, 1, 1]

cnt 0 \rightarrow 4

cnt 1 \rightarrow 3

find cnt 0
find cnt 1.

place 0's & then 1's

0000111 ✓
 $O(N)$

Q: Given an array.
Sort the array.

$0 \leq A[i] \leq 4$

A: [4, 1, 2, 1, 1, 3, 4]

\rightarrow cnt 0, cnt 1, cnt 2, cnt 3, cnt 4
X
0 3 1 1 2
| / | / | /
x 1 1 1 2 3 4 7

✓ HM < int, int > freq: → freq HM

HM
<2, 1>
<1, 3>
<3, 1>
<4, 2>

f(i:0 → 4)

[1 1 1 2 3 4 4]

i:0 → 0

1 → +

2 → +

3 → +

4 → +

→ 2

N

HolMap < int, int > freq;

f(i:0 → N-1) {
 freq[A[i]]++;

→ O(N)

 k=0

f(i:0; i<4; i++) {
 fo = freq[i];

→ 5

f(j=0; j<fo; j++) {

 A[k] = i;

 k++;

} → N

}


N + **N+5**

~ O(N)

Q Given an array. $a \leq A[i] \leq b$
Sort the array.

HashMap <int, int> freq;

f(i: 0 \rightarrow N-1) { $\rightarrow O(N)$
freq[A[i]]++;

 K = 0
 f(i: a; i \leq b; i++) { A 
 fo = freq[i]; $\rightarrow (b-a+1)$

 f(j: 0; j < fo; j++) {
 A[K] = i;
 K++;
 } $\rightarrow N$

 }

$N + N + b - a + 1$

COUNT
SORT }

$O(N + b - a)$

TC: $O(N + \text{Range})$

Range = $(b - a)$

SC: $O(\text{Distinct})$

Count Sort
is better
when

$$N + Range < N \log N$$

$$Range < N \log N - N$$

$$+ \leq N$$

$$0 \leq A[i] \leq 10^9$$

$$1 \leq N \leq 10^5$$

$$N \log N$$

$$10^5 \cdot \log(10^5)$$

$$10^5 \cdot 17$$

$$1.7 \times 10^6 \text{ ops}$$

$$N + R$$

$$10^5 + 10^9$$

$$\sim 10^9 \text{ ops}$$

Given a string $S_i \in \{a-z\}$

$$N \leq 10^6$$

$$R \rightarrow 26$$

$$TC = (N + 26)$$

$$O(N)$$

$$N \log N$$

$$2 \cdot 10^7$$

$$10^6 + 26$$

$$10^6$$

(*)

RADIX SORT →

MSD ← LSD

923
950
012
001
100
150
650
688
752
399
659

0	1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---	---

950 001 012 923 688 399
100 452 659



950, 100, 150, 650, 001, 012, 452, 923, 688, 399, 659

0	1	2	3	4	5	6	7	8	9
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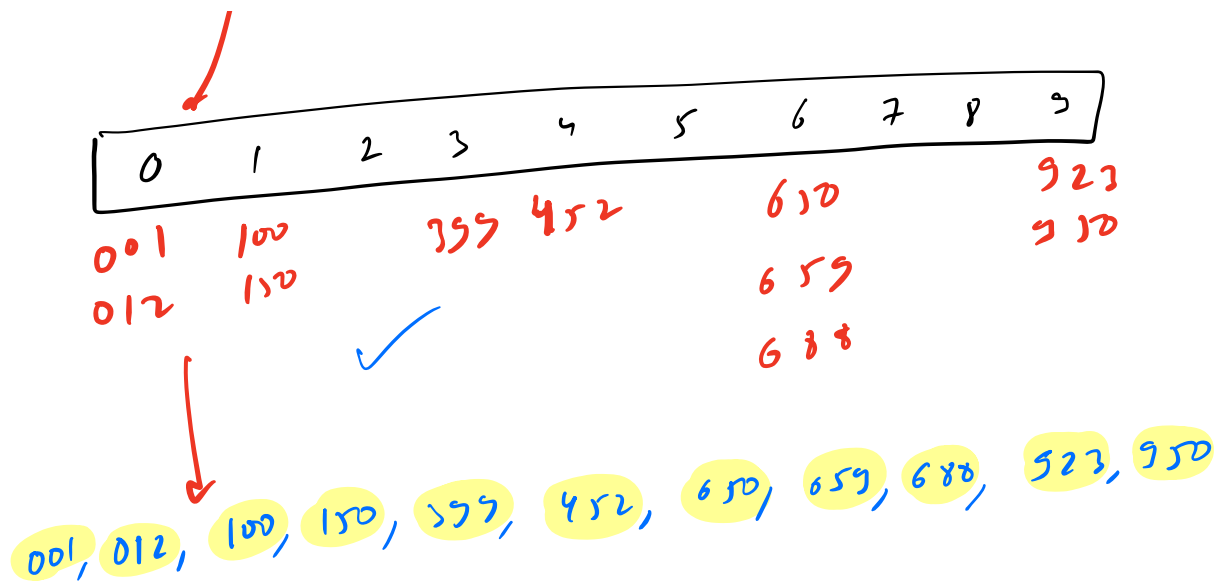
100 012 923
001

950 688 399
150
650
452
659



100 001 012 923 950 150 650 452 659 688 399

~ 5% 10 → 9



of digits of Max(A)

~~$(N + 10)$~~

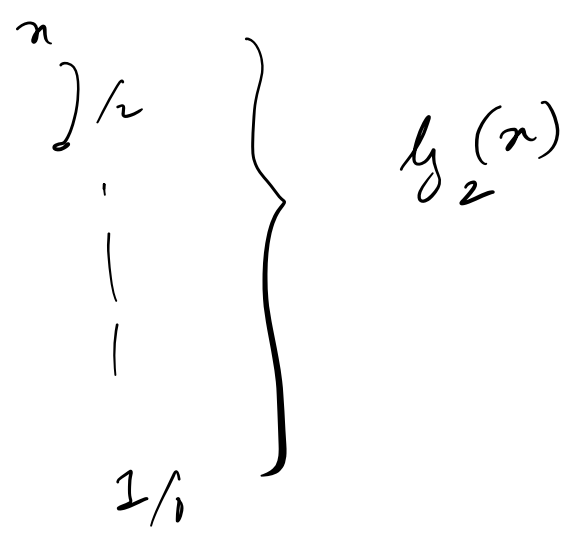
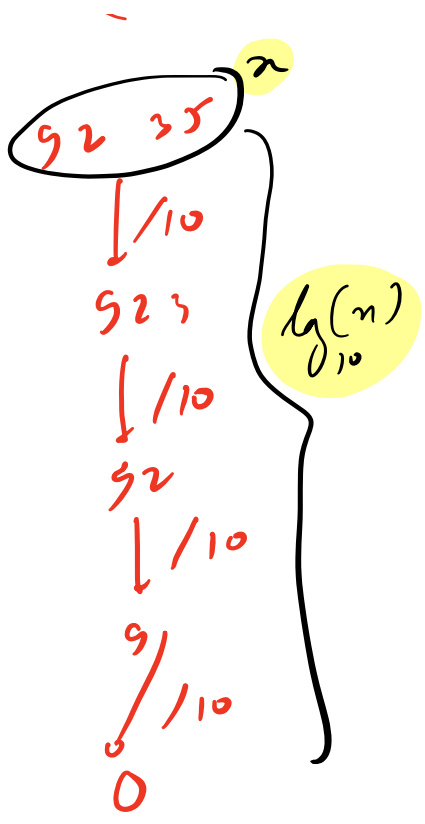
$N \log_2 N$

n
of digits
 $\log_{10}(n)$

$TC = O(N \times \log_{10} \text{Max}(A))$

$SC = O(N)$

- I $(9235 / 10^0) \% 10 \rightarrow 5$
 II $(9235 / 10^1) \% 10 \rightarrow 3$
 III $(9235 / 10^2) \% 10 \rightarrow 2$
 IV $(9235 / 10^3) \% 10 \rightarrow 9$



$1 \leq N \leq 10^5$
 $1 \leq A[i] \leq 10^9$

$N \lg_2 N$
 $N \cdot \lg_2 10^5$

$\lg_{10}(\max(A[i])) \rightarrow \sim 10$

$N \cdot 17$

$N \times 10$

X ✓

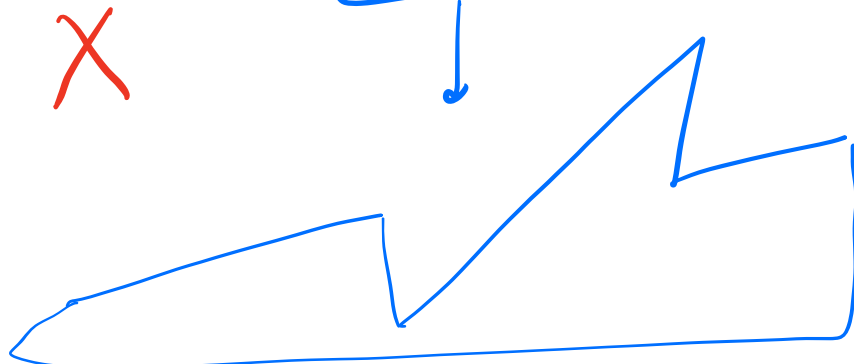
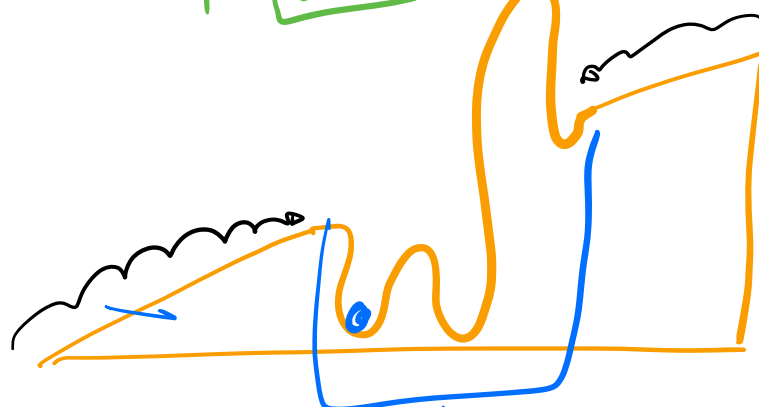
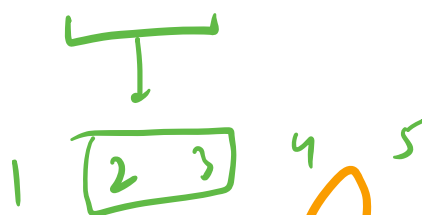
Handling -ve no's:

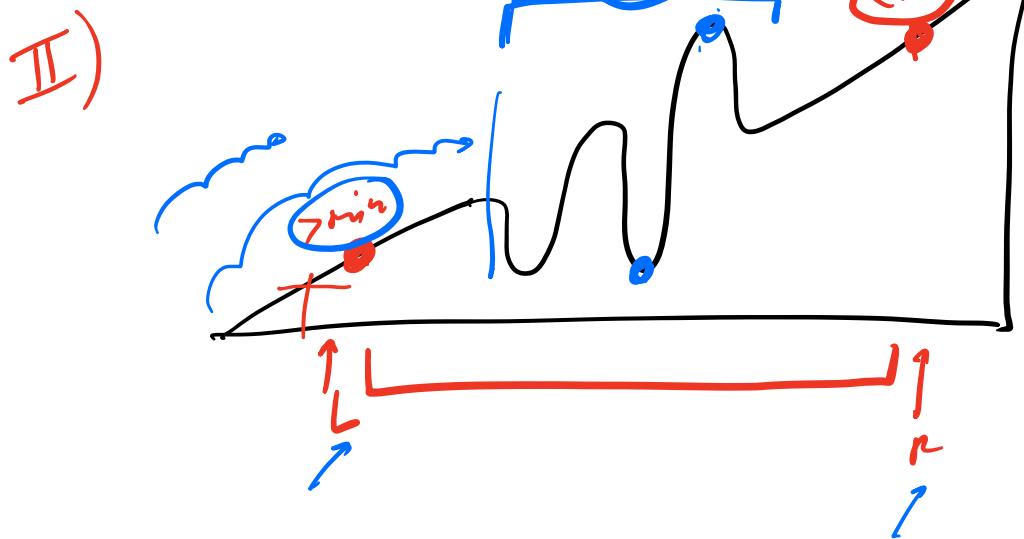
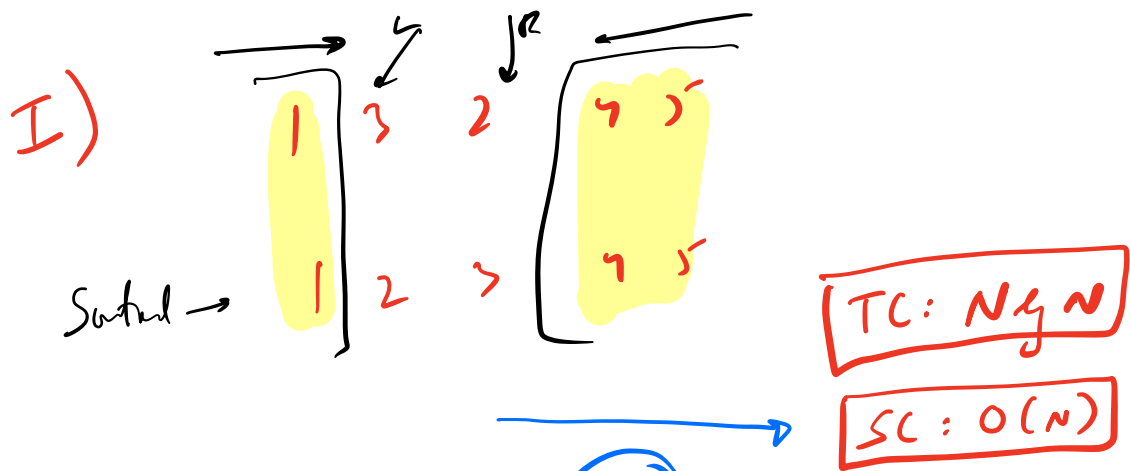
-10	-14	4	5	11
+14	+14	+14	+14	+14
4	0	18	19	25

$$\begin{array}{rcccccc}
 & 0 & 9 & 19 & 19 & 25 \\
 -14 & \hline
 -14 & -10 & 9 & 5 & 11
 \end{array}$$

Q Given an array. Find the minimum sized S.A. s.t if you sort it, then whole array is sorted (1N order)

A: 1, 3, 2, 4, 5 $\rightarrow 2$



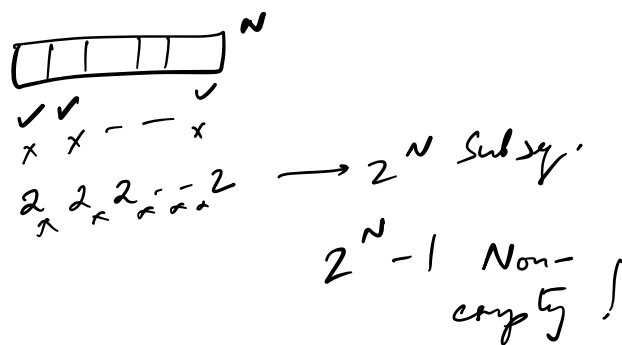
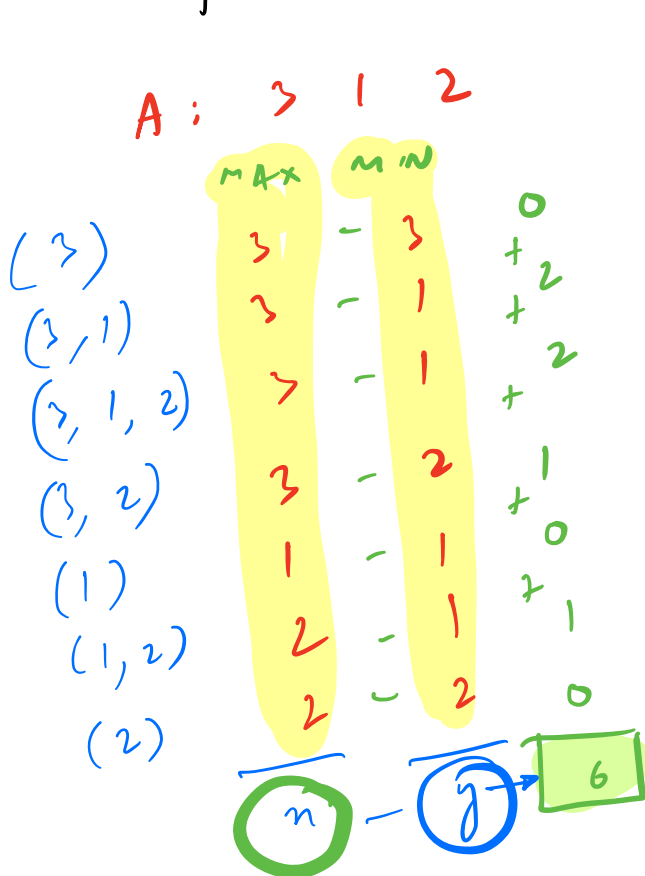


TC: $O(N)$

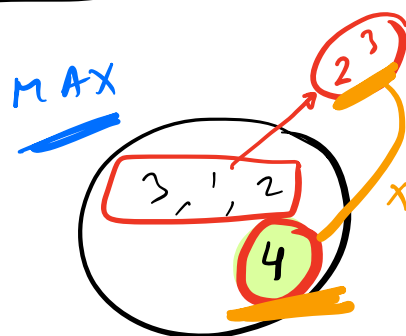
SC: $O(1)$



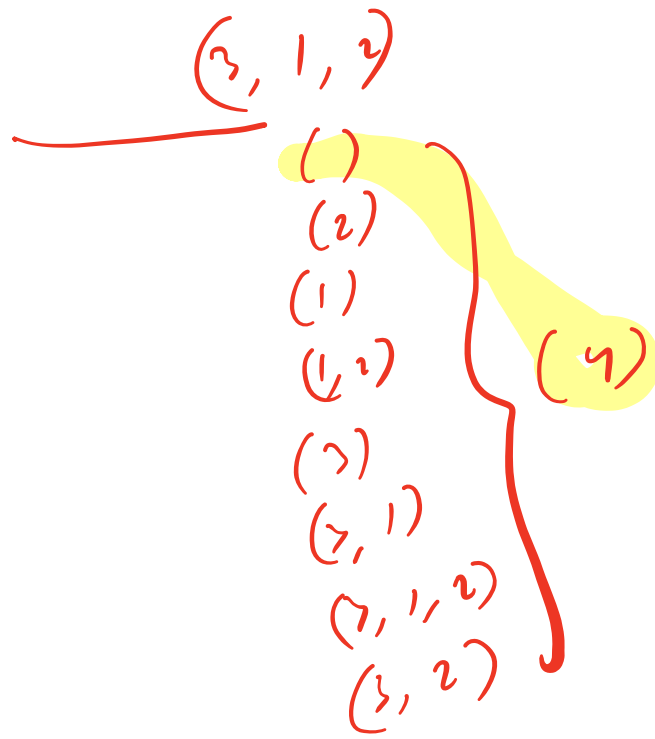
Q Given an Array.
 find all possible non-empty subsequences of
 the array, then for every subsequence find
 the diff b/w the smallest & the largest
 element.
 find the sum of such differences!



$$1 \leq N \leq 10^5$$



A: 3 1 2 6 4



A: 0 1 2 3 4

 3 1 2 6 4

Sort (A): 1 2 3 4 6

$\times 2^0$ $\times 2^1$ $\times 2^2$ $\times 2^3$ $\times 2^4$

subseq

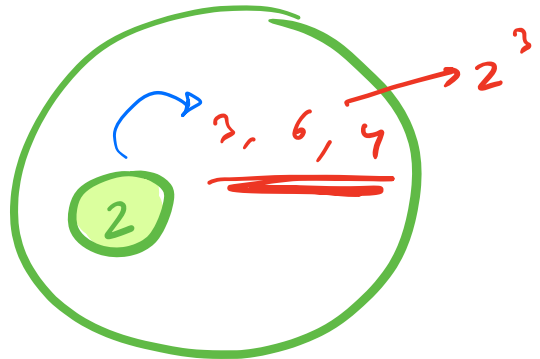
Contribution: 1 4 12 32 96

 + + + +

_____ \rightarrow n

MIN

A: 3 1 2 6 4



Sort(A): 1 2 3 4 6

#SA: 2^7 2^3 2^2 2^1 2^0

$$16 + 16 + 12 + 8 + 6 \rightarrow 7$$

$$\text{Ans} = n - 7$$

~~TC = $O(N \log N)$~~

~~SC = $O(1)$~~

Heap Sort!