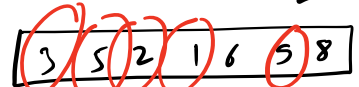
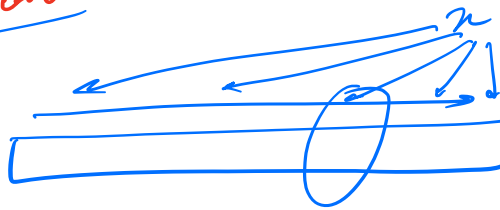


# of friends to look at to find a friend =  $N$

Linear Search



x

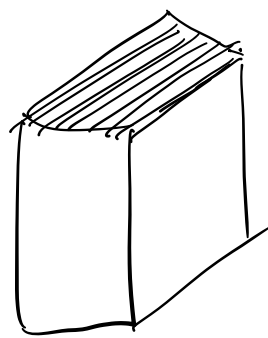
$O(N)$

```

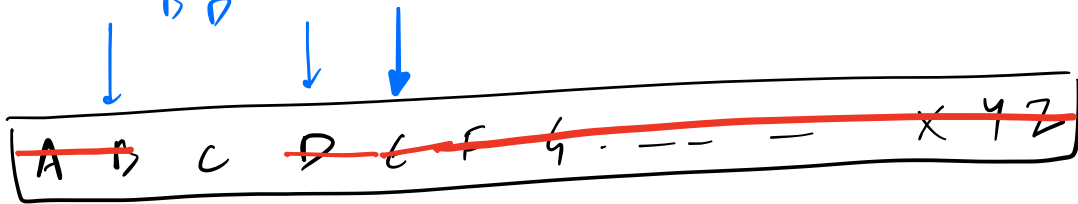
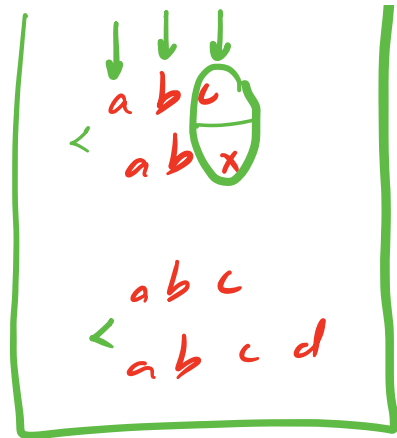
f(i = 0 → N-1) {
    if (A[i] == n) return i;
}
return -1;

```

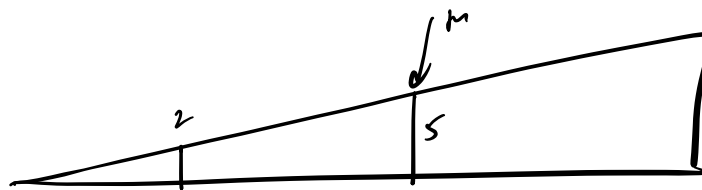
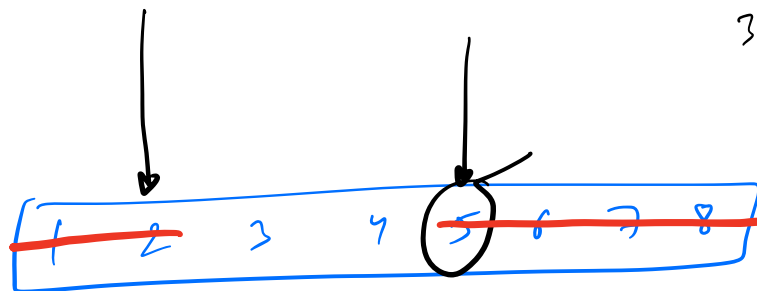
DICTIONARY



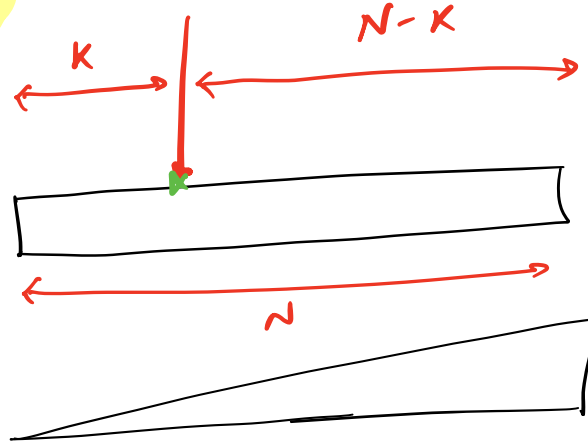
Lexicographical ordering  
Alphabetical order!



- Searching in a DICT is easier because of ORDERING.



Why MID ?



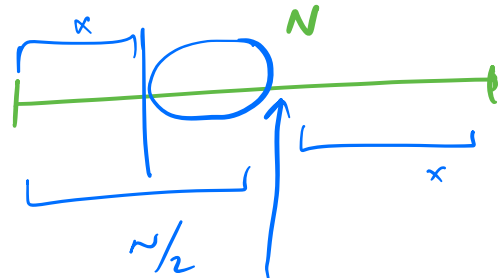
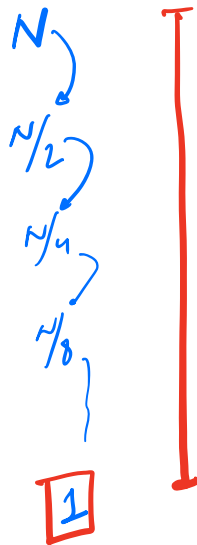
$$k < N-k$$

$$k = N-k$$

$$2k = N$$
$$k = \frac{N}{2}$$

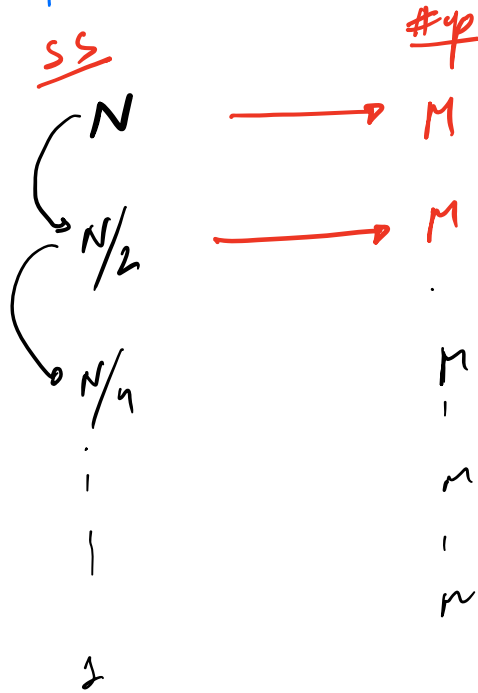
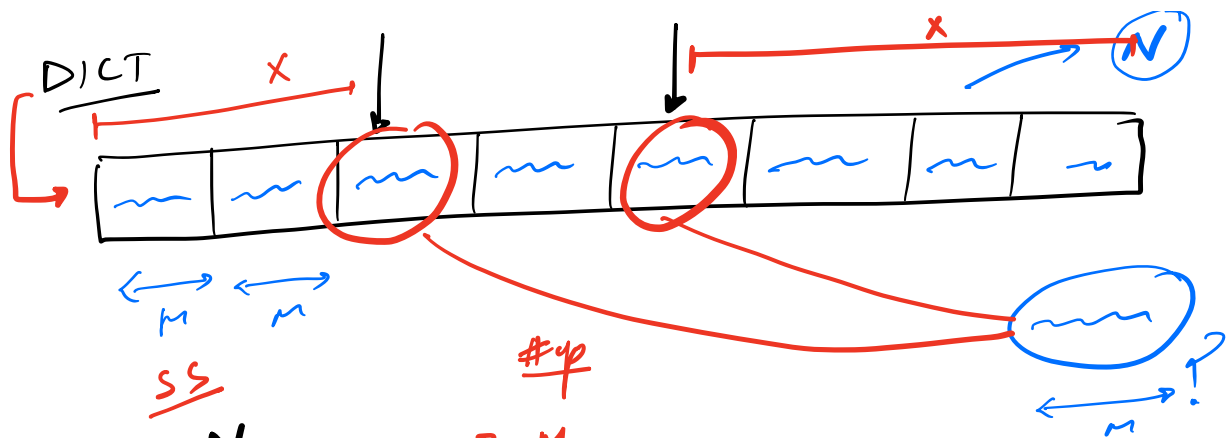
## Binary Search

Try to divide the search space into two halves  
& discard 1 half by using some condition.



$$\# \text{ of it of DS where } SS = N$$
$$= \log_2 N$$

$$\log_2 (\text{Search Space Size})$$



# of it of BS =  $\log(N)$

# of ops/it of BS  
=  $O(M)$

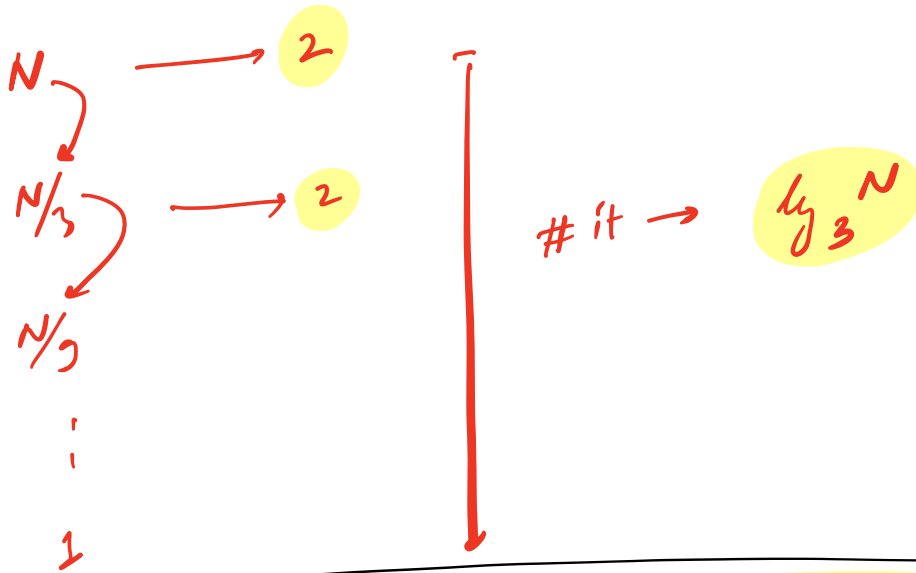
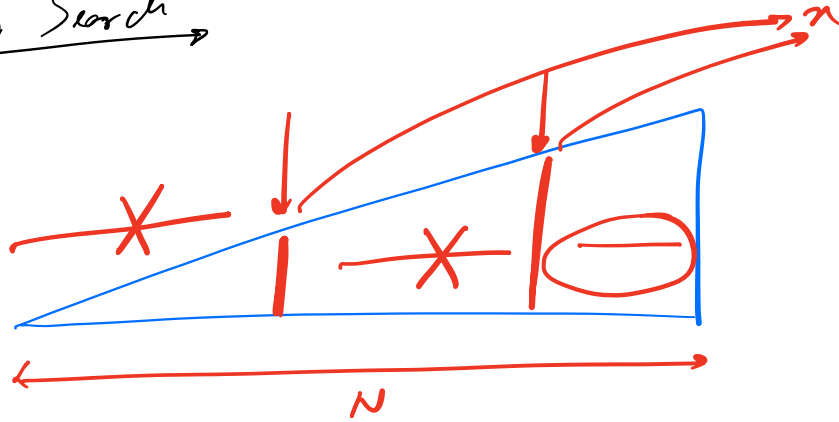
$$TC = O(M \cdot \log N)$$

Search Space Size

TC of BS

$\rightarrow O(\log(SS) \times \text{Time per it})$

Turnary Search →



Q Given a sorted array with DISTINCT element  
 Search for the index of the element  $K$ .  
 If  $K$  is not present, then ret -1.



↙

$A: [3, 6, 9, 12, 17, 19, 20, 23, 25, 27]$   $K=12$

↓  
3

1) Linear Search

$TC = O(N)$

$SC = O(1)$

$K=13$

↓  
-1

2) B.S.  $l=0, h=N-1$

CASES

I)  $A[mid] == K$  return mid

II)  $A[mid] < K$  go right  
 $l = m + 1;$

III)  $A[mid] > K$  go left  
 $h = m - 1$

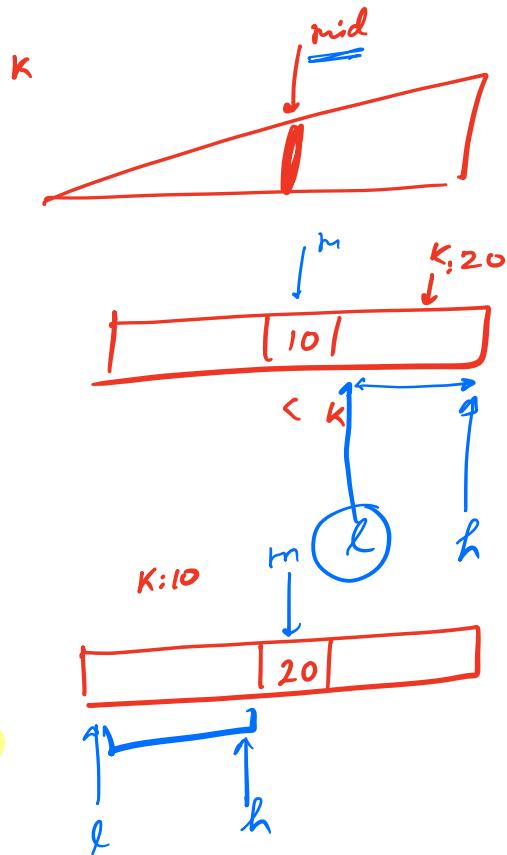


Diagram showing indices 0 to 9 with values 3, 6, 9, 12, 14, 17, 20, 23, 25, 27. A vertical line at index 3 is labeled  $l$  and  $h$ . A horizontal line above indices 0-2 is labeled  $x$ . A horizontal line above indices 3-9 is labeled  $K$ .

$A: [3, 6, 9, 12, 14, 17, 20, 23, 25, 27]$

$l$	$h$	$\text{mid} \rightarrow (l+h)/2$	$A[\text{mid}]$	
0	9	4	14	$14 > K$ ; go left
0	3	1	6	$6 < K$ ; go right
2	3	2	9	$9 < K$ ; go right
3	3	3	12	$12 == K$ ; set mid

$K = 12$

$K = 15$

Diagram showing the array  $A$  with indices 0 to 9. A vertical line at index 5 is labeled  $m$ . A vertical line at index 4 is labeled  $h$ . A vertical line at index 5 is labeled  $l$ .

$A: [3, 6, 9, 12, 14, 17, 20, 23, 25, 27]$

// A[], N, K

l = 0, h = N-1;

while (l <= h) {

    m = (l+h)/2

    if (A[m] == K) return m;

    else if (A[m] < K) l = m+1;

    else h = m-1;

}  
return -1;

SS  $\rightarrow$  N  
#it  $\rightarrow \log(N)$

o(1)

TC =  $O(\log N)$   
SC =  $O(1)$

### DIFF STYLES of BS

l = 0, h = N-1  
while (l <= h) {

    m = ...  
    return ...

}  
return

l = -1, h = N  
while (h - l > 1) {

    m = ...

    if l == m

        h = m

}  
return l;

l = 0, h = N-1  
while (l < h) {

    m = ...

    ...

    ...

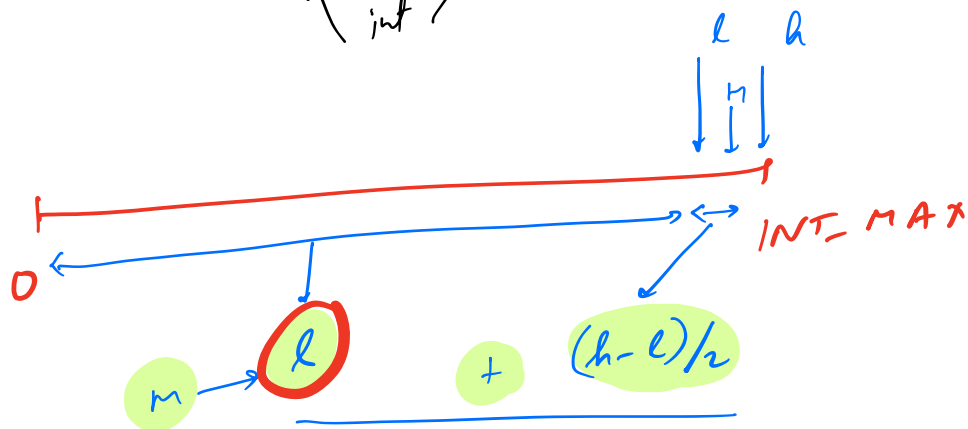
}  
return (l+1);



④

$$m = (l + h) / 2 ;$$

$$m = l + (h - l) / 2 ;$$



Q Given a sorted array. **DISTINCT.**  
Find the **floor** of a no.  $K$  in the array!  
↳ greatest element  $\leq K$

$A: [-5, 2, 3, 6, 9, 10, 11, 14, 18]$

$K = 5 \rightarrow 3$

$K = 4 \rightarrow 2$

$K = 6 \rightarrow 6$

$K = -7 \rightarrow \text{not INT\_MIN!}$

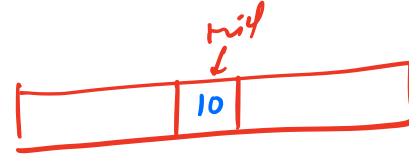
## CASES

I)  $A[mid] == k$  return  $k$



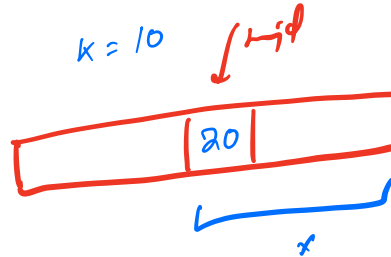
$k = 20$

II)  $A[mid] < k$   
 $ans = A[mid]$  go right  
 $l = mid + 1$



$k = 10$

III)  $A[mid] > k$  go left  
 $h = mid - 1$



$A: [-5, 2, 3, 6, 9, 10, 11, 14, 18]$   $k = 5$

$l$	$h$	$m$	$A[m]$	$ans$
				$-\infty$
0	8	4	$9 > k$	<div style="border-left: 2px solid red; padding-left: 5px; margin-left: 10px;"> <math>2</math>  <math>3</math>  <math>3</math> </div>
0	3	1	$2 < k$	
2	3	2	$3 < k$	
3	3	3	$6 > k$	
3	2			
			STOP!	

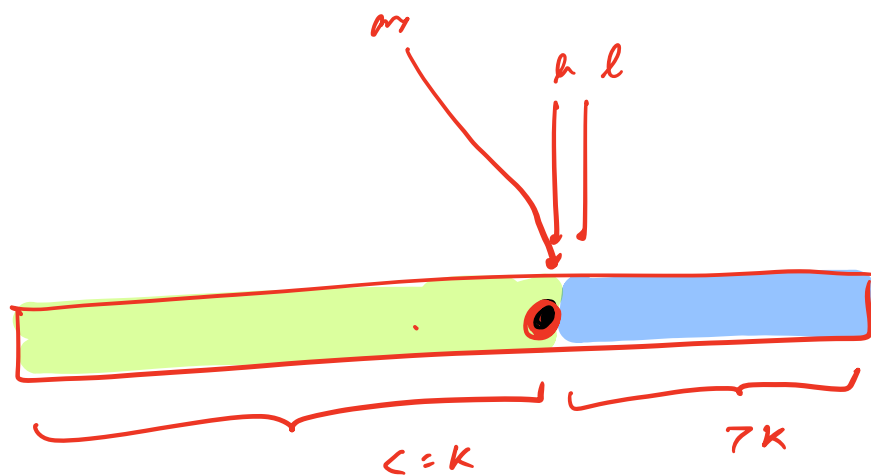
```

l = 0, h = N-1, ans = -∞
while (l <= h) {
    m = (l+h)/2;
    if (A[m] == k) return k;
    else if (A[m] < k) {
        ans = A[m], l = m+1;
    }
    else h = m-1;
}
return ans;

```

$$TC = O(\log N)$$

$$SC = O(1)$$



```

if (A[m] <= k) ans = A[m], l = m+1,
else h = m-1

```

Q Given a sorted Array & K.  
find the first occurrence of K. Ret the index!  
If it does not exist, ret -1;

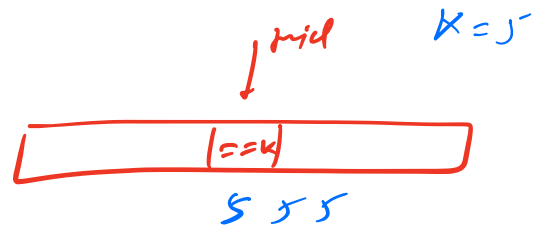
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14  
A: -5, -5, -3, 0, 0, 1, 1, 5, 5, 5, 5, 5, 8, 11, 11

$k = 5 \rightarrow 7$

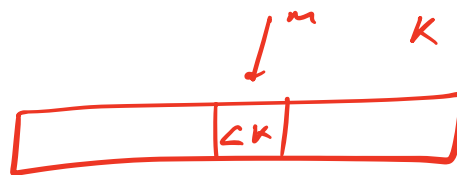
$k = 6 \rightarrow -1$

### CASES

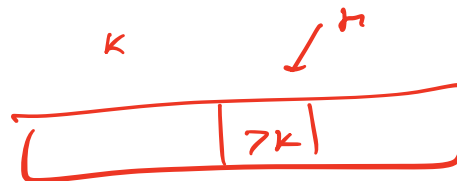
I)  $A[mid] == K$   
ans = mid  
go left,  $h = m - 1$

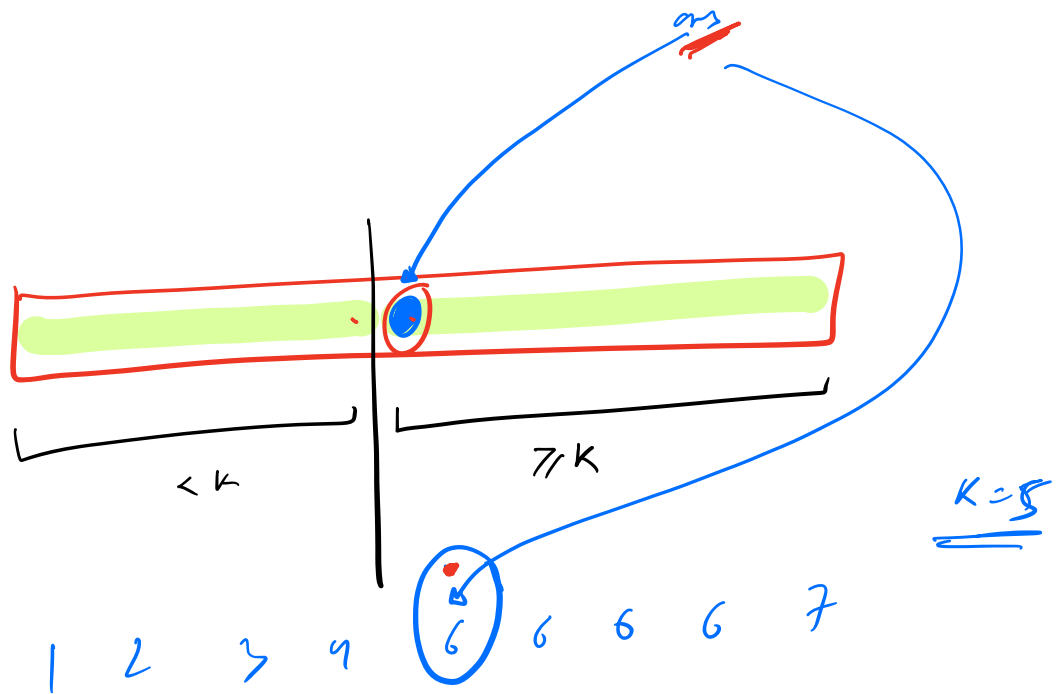


II)  $A[mid] < K$   
go right,  $l = m + 1$



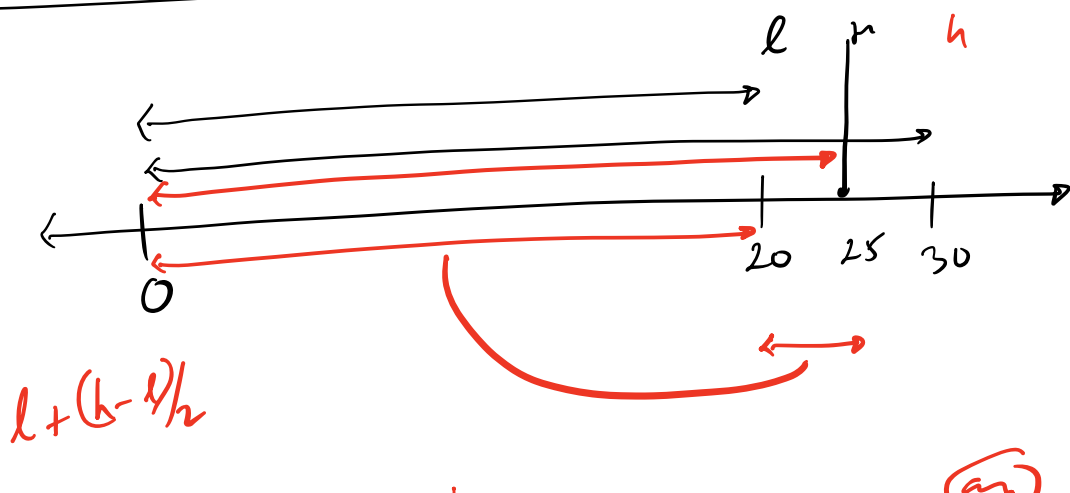
III)  $A[mid] > K$   
go left;  $h = m - 1$

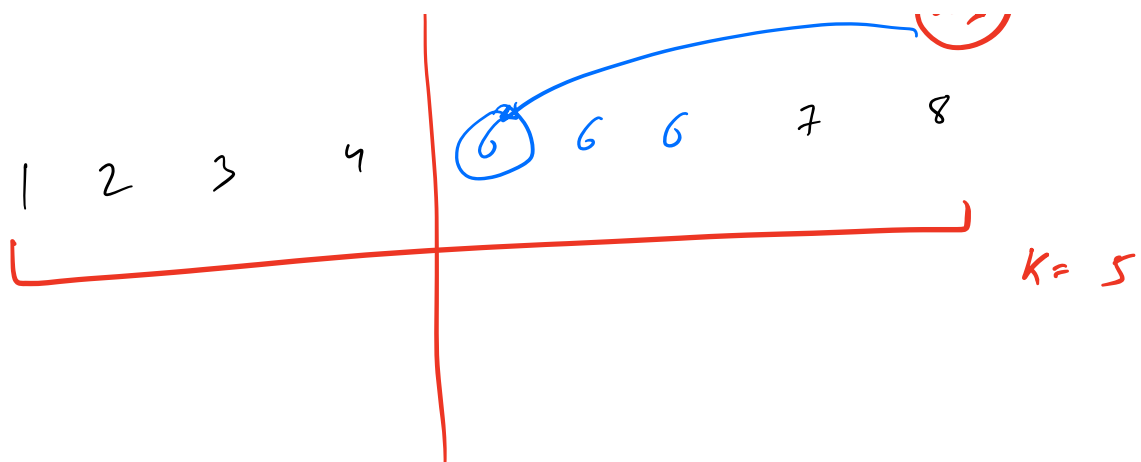




$A[m] \geq K \quad \text{ans} = m, \quad h = m - 1$   
 $A[m] < K \quad l = m + 1$

if  $(A[m] == K) \rightarrow \text{ret ans};$   
 ret -1;





$< k$

$$7 = k$$