

INFIX

POSTFIX

$$3 + 4$$

$$3\ 4\ +$$

$$4 \times 2$$

$$4\ 2\ \times$$

$$4 + 3 \times 2$$

$$4\ 3\ 2\ \times\ +$$

$$\begin{array}{c} \downarrow \\ 4\ (+)\ 3\ 2\ \times \end{array}$$

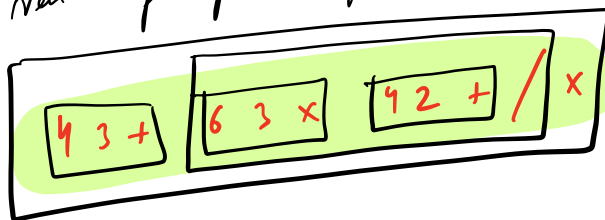
$$4/3 \times 2 + 6 \times 3 \rightarrow$$

$$\downarrow$$
$$4\ 3\ / \times\ 2\ +\ 6\ \times\ 3$$

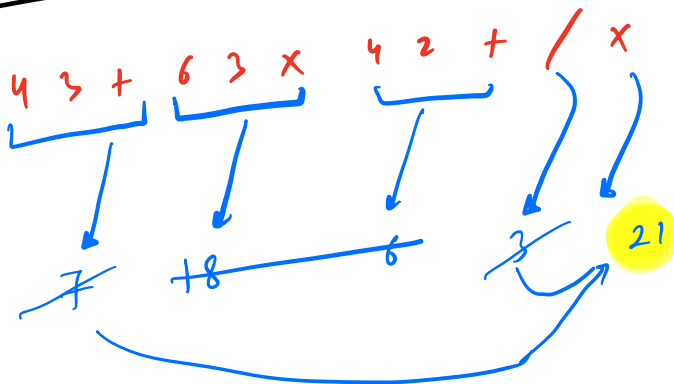
$$4\ 3\ / \ 2\ \times\ +\ 6\ 3\ \times$$

$$4\ 3\ / \ 2\ \times\ 6\ 3\ \times\ +$$

Q Given postfix expression. Evaluate it!

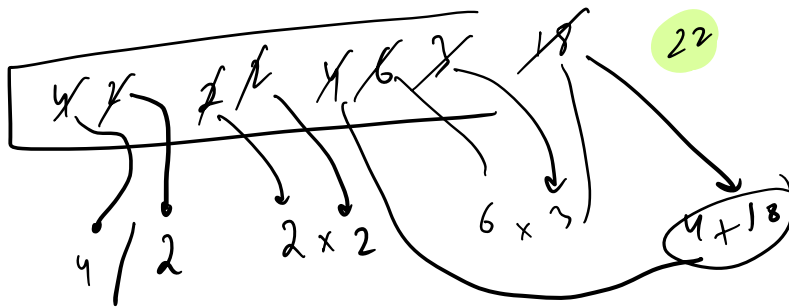


$$(4 + 3) \times ((6 \times 3) / (4 + 2))$$



DS: Stack →

$$4^2 / 2 \times 6^3 \times + 3^2$$



I Operand

push it in a stack

II operator

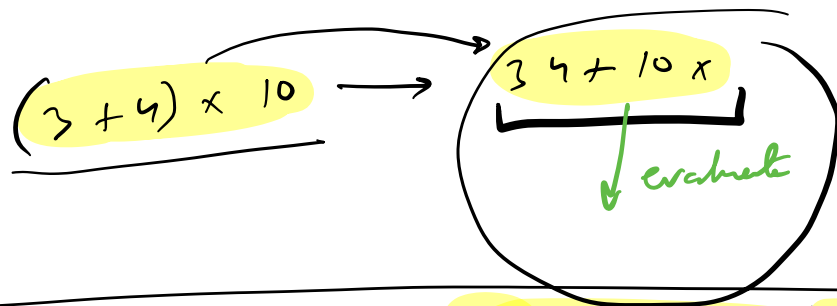
op2 → pop one item from stack

op1 →

push in stack →

op1 operator op2

ANS: Only item in the stack.



Q Given an array. Find the nearest smaller element on left of every element.

A: 4 5 2 10 8 2  
NSL: -1 4 -1 2 2 -1

A: 4 6 10 11 7 8 3 5  
NSL: -1 4 6 10 6 7 -1 3

1) BF

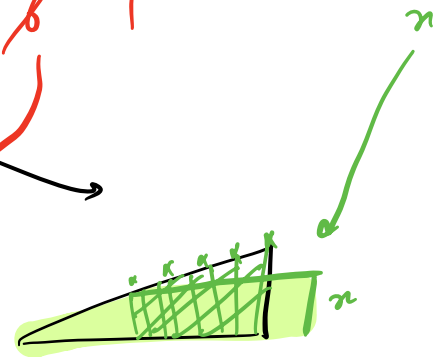
f(i: 0  $\rightarrow$  N-1) {  
f(j: i-1  $\rightarrow$  0)  
if ( $A[j] < A[i]$ )

$TC = O(N^2)$

$SC = O(1)$

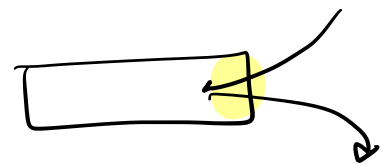
$A : 5 \quad 2 \quad 8 \quad 10 \quad 12 \quad 6 \quad 1$   
 $NSL : -1 \quad -1 \quad 2 \quad 8 \quad 10 \quad 2 \quad -1$

$CL : 5 \quad 2 \quad 8 \quad 10 \quad 12 \quad 6 \quad 1$



Requirements of DS [CL] ?

- 1) Insert at END
- 2) Remove elements from end
- 3) Read element at that end
- 4) Maintain insertion order



STACK



CODE : // A(N)

stack <int> CL;

ANS[N];

f(i: 0; i < N; i++) {

while(!CL.is\_empty() && CL.top() >= A[i]) {

CL.pop();

}

if(!CL.is\_empty())

ANS[i] = CL.top();

else ANS[i] = -1;

CL.push(A[i]);

}

ret ANS[];

N

DEL:  $\leq N$

CL

INS: N

~~T~~TC =  $O(N)$

~~S~~SC =  $O(N)$

WC for Space

1	2	3	4	5
-1	1	2	3	4

CL: 1 2 3 4 5

Q Given an Array . for every element find the index of the Nearest Smaller element on left  
 $\downarrow$  NSL

A:  $\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 2 & 7 & 6 & 3 & 1 & 5 \end{matrix}$   
 NSL<sub>i</sub>  $\rightarrow$   $\begin{matrix} -1 & 0 & 0 & 0 & -1 & 4 \end{matrix}$

CL: [0 X 2 ...]

CODE : A(N)

stack <int> CL;

ANS[N];

for (i: 0; i < N; i++) {  
 while (!CL.is Empty() &&  $A[CL.top()] \geq A[i]$ ) {  
 CL.pop();

}  
 if (!CL.is Empty())  
 ANS[i] = CL.top();

else ANS[i] = -1;

CL.push(i);

}

ret ANS[];

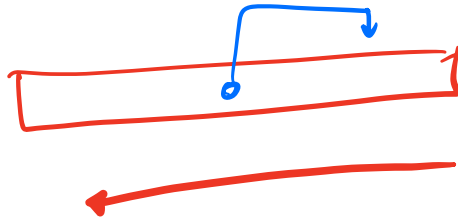
$TL = O(N)$   
 $SC = O(N)$

Q

Given  $A[]$ .

find NS on Right ?

NSR



CODE :  $A[N]$

stack <int> CL;

ANS[N];

for ( $i: N-1; i \geq 0; i--$ ) {

while (!CL.isEmpty() &&  $A[CL.top()] \geq A[i]$ ) {

CL.pop();

}

if (!CL.isEmpty())

ANS[i] = CL.top();

else ANS[i] = -1;

CL.push(i);

}

ret ANS[];

TC  $\rightarrow O(N)$   
SC  $\rightarrow$

Q Given Arr. find NG L. ?  
↓  
greater

CODE : Arr

stack <int> CL;

Ans[N];

f(i: 0; i < N; i++) {

while(!CL.is\_empty() && A[CL.top()] <= A[i]) {

CL.pop();

}

if(!CL.is\_empty())

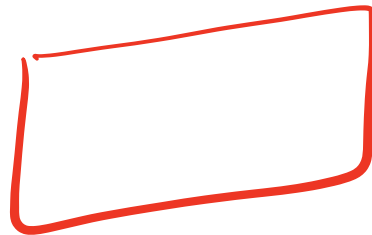
Ans[i] = CL.top();

else Ans[i] = -1;

CL.push(i);

}

ret Ans[];



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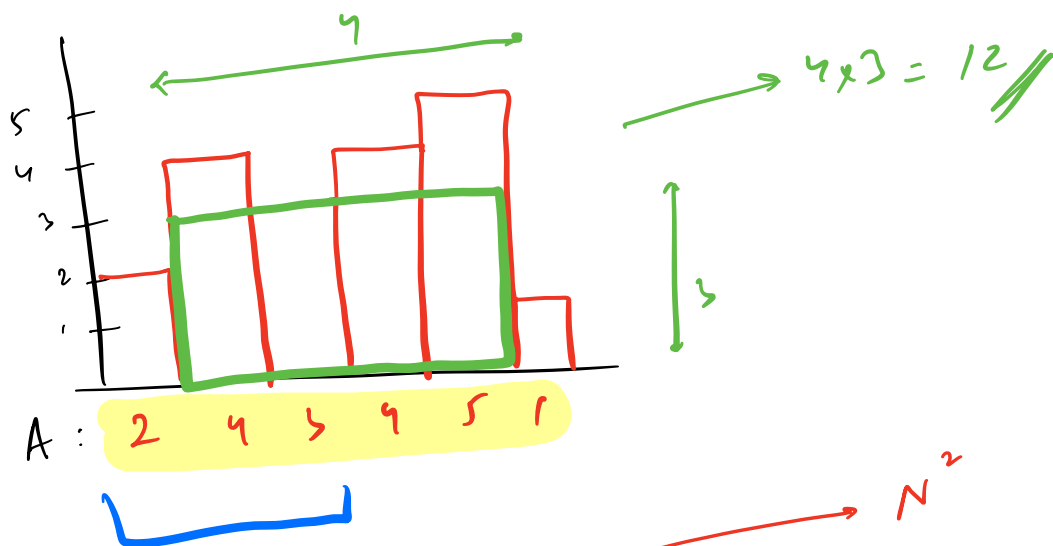
Q NGR ?

SAME AS ABOVE

f.(N-1 → 0)



Q Given continuous blocks of histogram.  
Find the maximum rectangular area.



1) BF

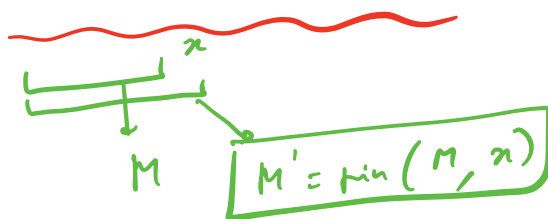
fin the S.A to choose as width  
→  $[L, R]$   $N^2$

$h \rightarrow \min(A[L] \dots A[R])$   
 $w \rightarrow R - L + 1$   
 $\text{MAX} \leftarrow \begin{matrix} h \\ w \end{matrix}$   
 $\downarrow$   
 ANS

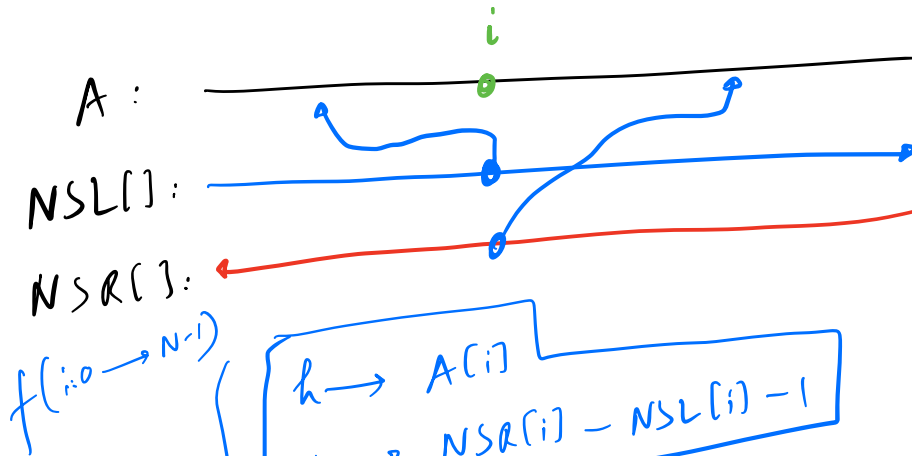
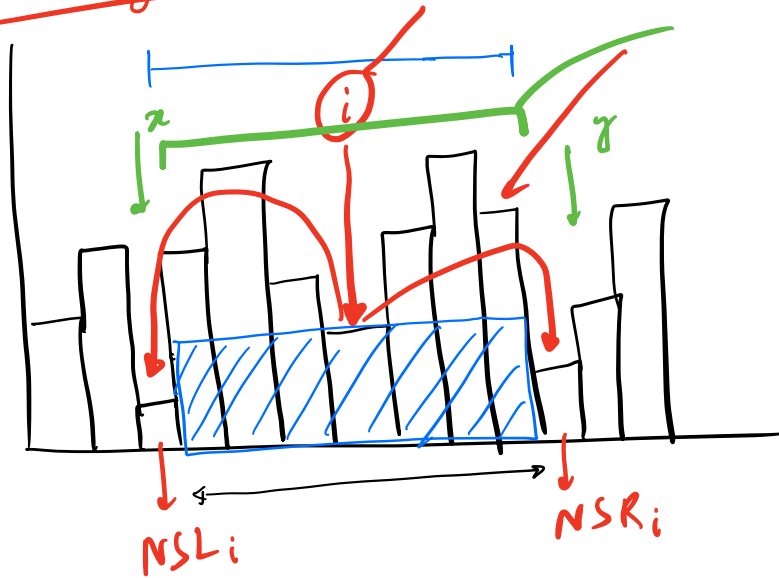
**$TC = O(N^2)$**

2) Carry forward

**$TC = O(N^2)$**



3) find the height



$O(N)$   
 $O(N)$

$O(N)$

$$\begin{aligned} h &\rightarrow A[i] \\ w &\rightarrow NSR[i] - NSL[i] - 1 \end{aligned}$$

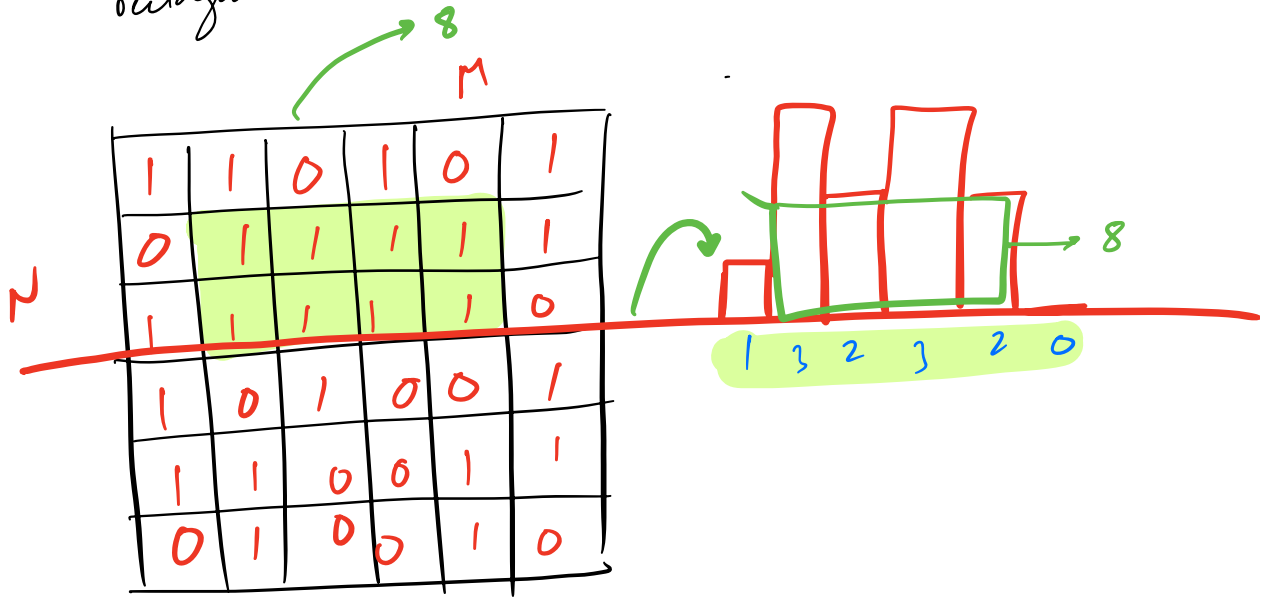
$$Area = h \times w$$

$$ANS = \max(ANS, Area);$$

$$TC = O(N)$$

$$SC = O(N)$$

Q Given a binary matrix. Find the MAX rectangular area with all 1's.



1) BF

#SM =  $N^2 M^2$

$O(1)$  ps

$TC = O(N^2 M^2)$

M

N

1	1	0	1	0	1
0	1	1	1	1	1
1	1	1	1	1	0
1	0	1	0	0	1
1	1	0	0	1	1
0	1	0	0	1	0

Columnwise ps :

1	1	0	1	0	1
0	2	1	2	1	2
1	3	2	3	2	0
2	0	3	0	0	1
3	1	0	0	1	2
0	2	0	0	2	0

Q Given an array. find the sum of MAX of all SAs.

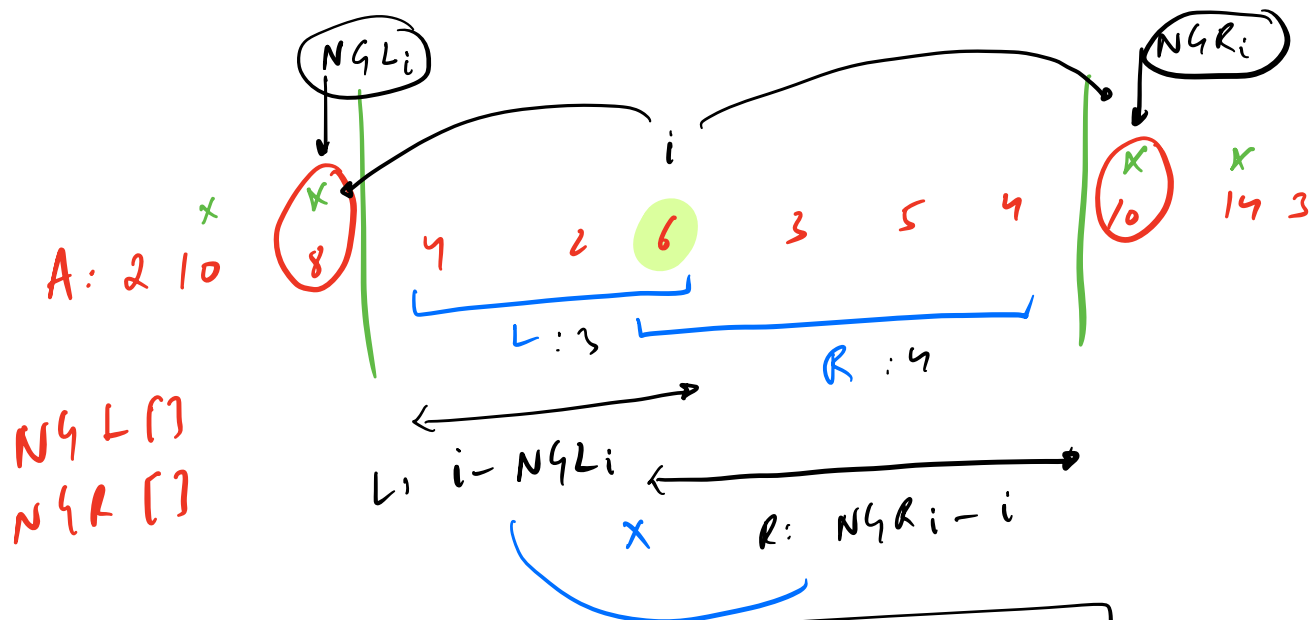
A : [1, 4, 3]

Contribution of every element

SA	MAX
(1)	1
(1, 4)	4
(1, 4, 3)	4
(4)	4
(4, 3)	4
(3)	3

element	# SAs
1	1
4	4
3	1

20



$$\text{\#SA with } A[i] \text{ as MAX} = (i - NGLi) \times (NGRi - i)$$

$$\text{Contribution by } A[i] = (i - NGLi) \times (NGRi - i) \times A[i]$$

$$\text{ANS} = \sum_{i=0}^{N-1}$$

$$TC = O(N)$$

$$SL = O(N)$$

