



Wind Field Generation

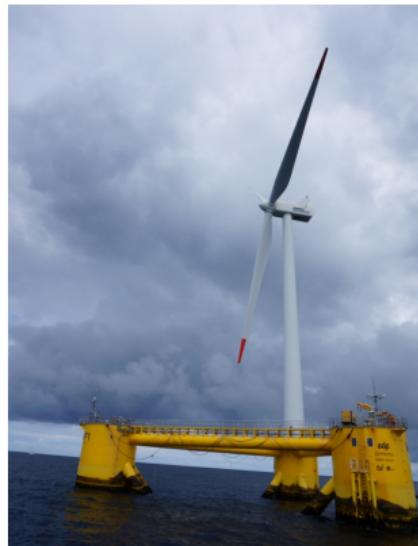
Prof. Dr.-Ing. David Schlipf

06.09.2024

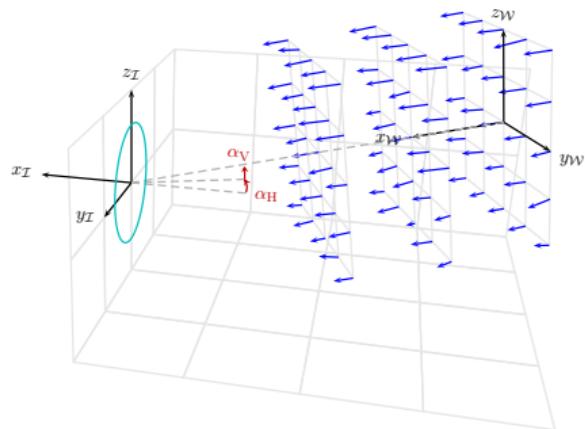
Lecture #7
Controller Design for Wind
Turbines and Wind Farms

Schedule

- 02.09. 1 Controller Design Objectives and Modeling
- 03.09. 2 Baseline Generator Torque Controller
- 04.09. 3 Collective Pitch Controller
- 05.09. 4 Filter Design
- 06.09. 7 Wind Field Generation**
- 09.09. 10 Lidar-Assisted Control I
- 10.09. 11 Lidar-Assisted Control II
- 11.09. 5 Tower Damper
- 12.09. 6 Advanced Torque Controller
- 12.09. 8 Steady State Calculations
- 16.09. 9 Individual Pitch Control
- 17.09. 12 Wind Farm Effects
- 18.09. 13 Wind Farm Control
- 19.09. 14 Floating Wind Control I
- 20.09. 15 Floating Wind Control II



Wind Field Generation



Motivation

- ▶ Wind is not totally random.
 - ▶ Understanding of wind is crucial in wind energy!

Main questions

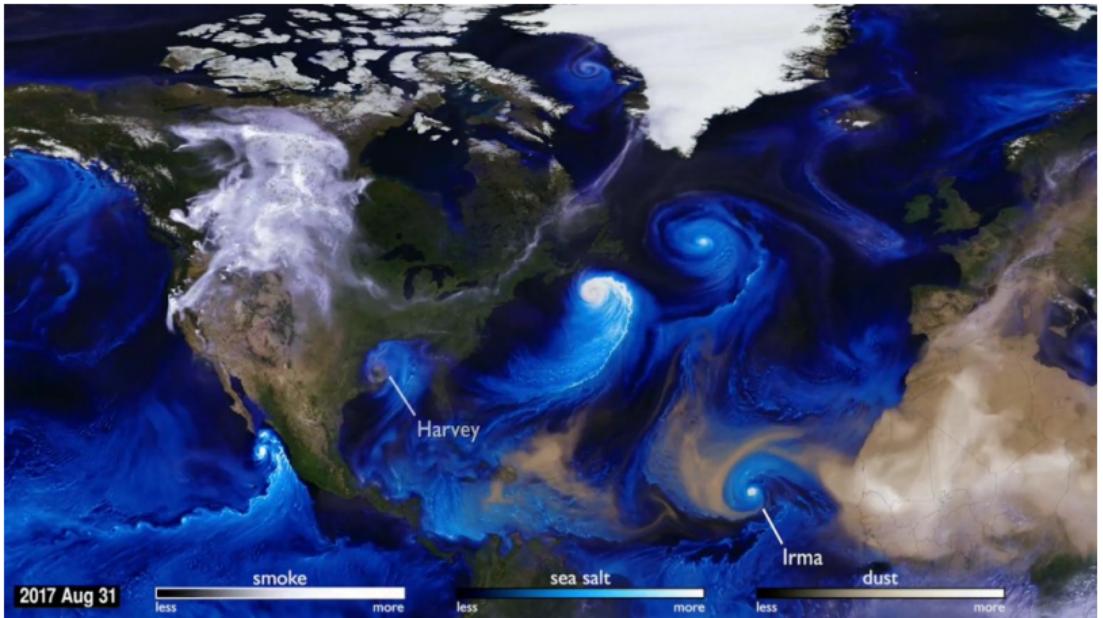
- ▶ How is a turbulent wind field generated?
 - ▶ How can we generate rotor-effective wind speed?

Content

1. Origin of Wind
2. Atmospheric Boundary Layer
3. Wind Field Generation
4. Research Challenges in Wind Energy
5. Conclusions

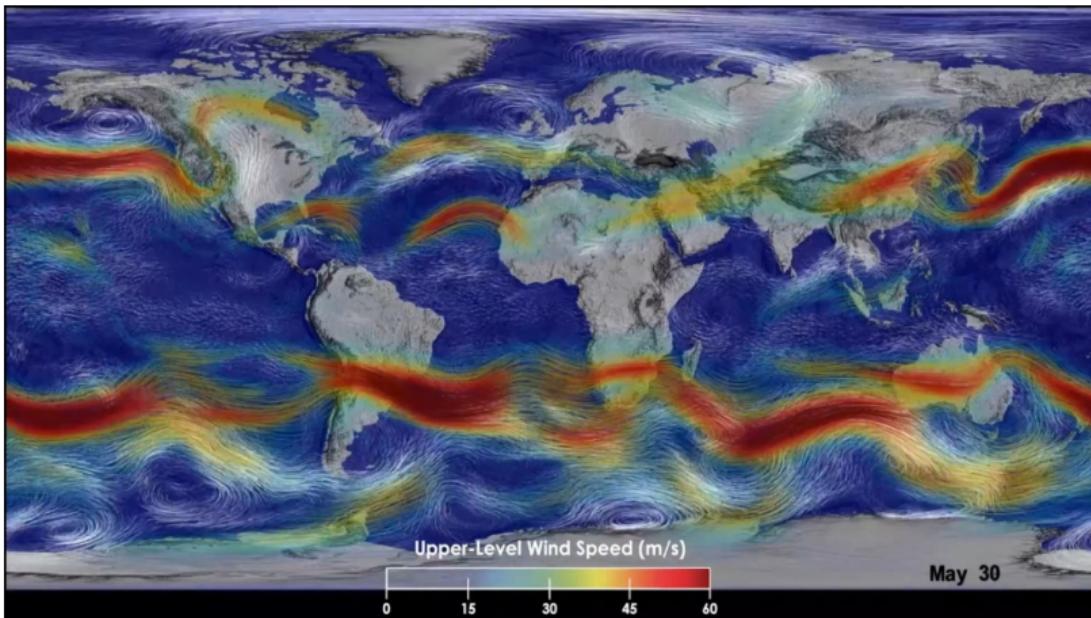


Dust in the Wind



- ▶ Saharan dust is swept into the outer cyclonic winds of tropical storm Irma.
- ▶ Rain at the center of the storm washes it out of the air.

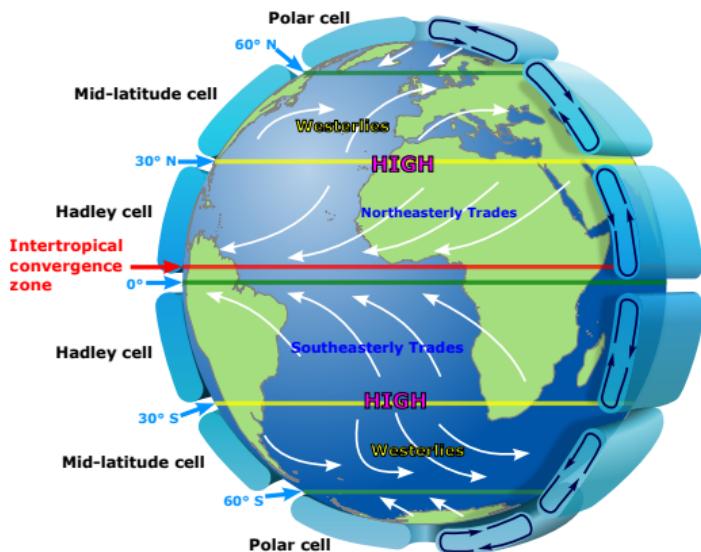
Global Wind



[Surface and Upper-level Winds]

- ▶ High altitude winds circumnavigate the earth in wave-like paths from west to east
 - ▶ Winds closer to the ground are trade winds, west winds and polar east winds

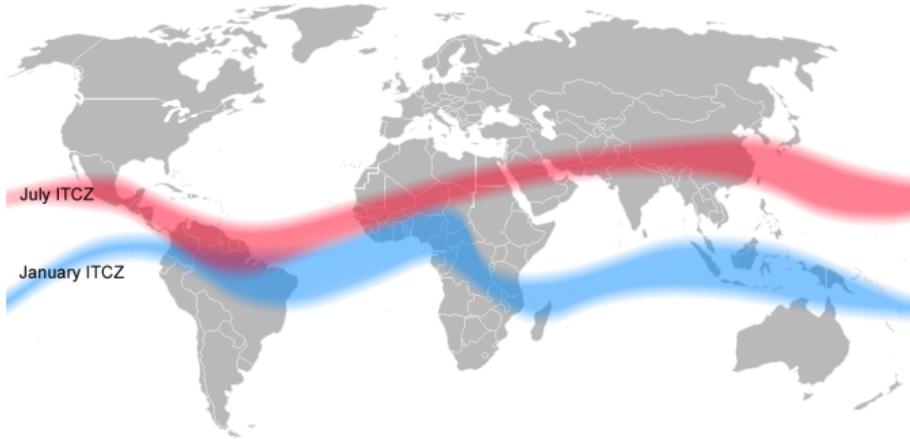
Atmospheric Circulation



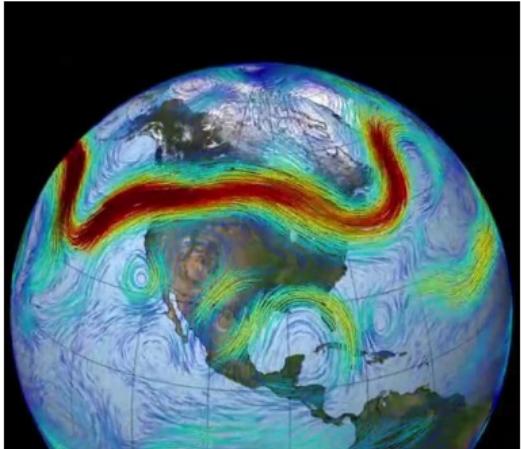
based on [wikipedia]

- ▶ As a result of different levels of solar heating, warm air rises at the equator and falls at the poles
 - ▶ Wind as a compensatory movement
 - ▶ Because of the rotation of the earth (Coriolis force), movements are deflected to the right in the northern hemisphere and to the left in the southern hemisphere
 - ▶ Three wind systems through surface convergence

Inter-tropical Convergence Zone



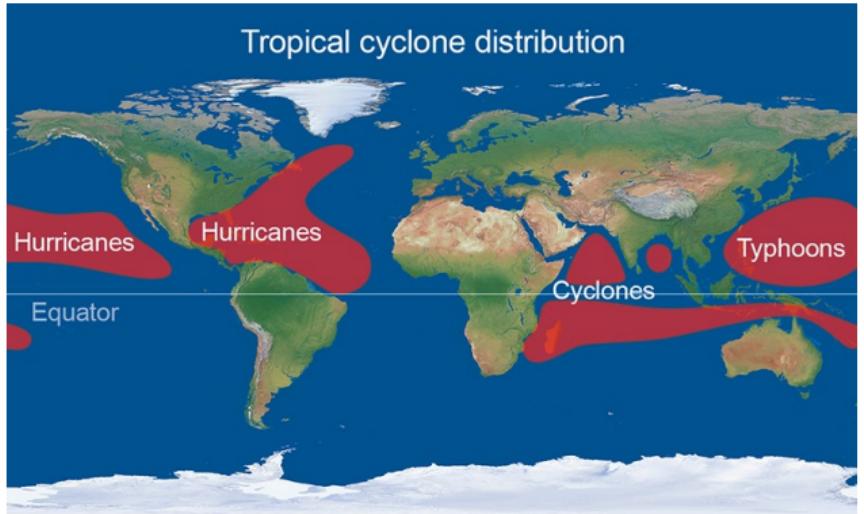
[wikipedia]



[NASA/Goddard Space Flight Center]

- ▶ Also equatorial low pressure belt or ITCZ (Inter-tropical Convergence Zone)
 - ▶ Due to different land mass distribution and solar warming it is not constantly 0°
 - ▶ Trade winds on both sides of the ITCZ for rapid ocean crossing
 - ▶ A hurricane, cyclone or typhoon often occurs here
 - ▶ Westerly winds to compensate: polar front jet stream (60°), subtropical jet stream (30°)

Location and naming of tropical cyclones



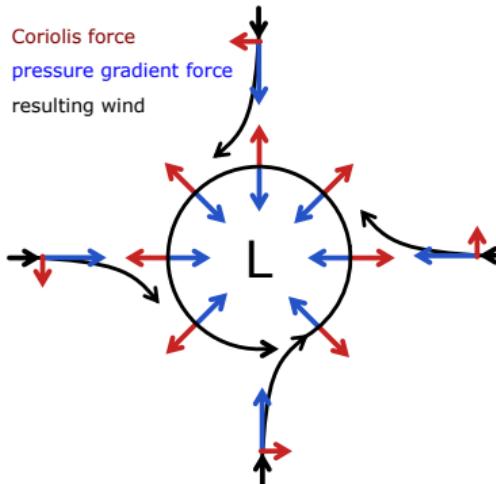
[www.metoffice.gov.uk]

- ▶ Hurricanes - Atlantic and North-East Pacific Oceans
 - ▶ Typhoons - North-West Pacific Ocean
 - ▶ Cyclones - South-West Pacific and Indian Ocean

Geostrophic wind



[NASA visible earth]

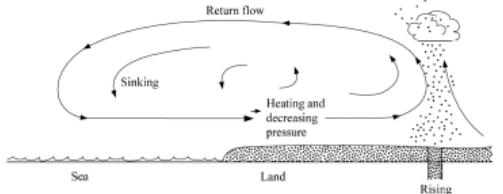


based on [wikipedia]

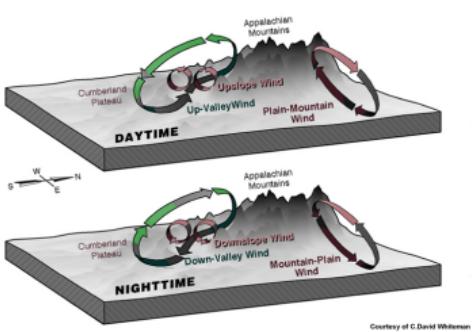
- ▶ Air flow at high altitudes unaffected by ground friction
 - ▶ Balance between gradient force and Coriolis force
 - ▶ Currents around low pressure areas in the northern hemisphere counterclockwise

Video: Coriolis force

Local winds



[1]



[wikipedia]

Sea-Land-circulation

- ▶ Daily cycle due to different heat capacity
- ▶ Sea wind during the day: land warms up faster
- ▶ Land wind at night: land cools down faster

Mountain-valley-circulation

- ▶ Daily cycle due to different proximity to the ground
- ▶ Valley wind during the day: the air on the mountain slope warms up
- ▶ Mountain wind at night: air on the mountain slope cools down

Formation of the Atmospheric Boundary Layer

Atmospheric Boundary Layer

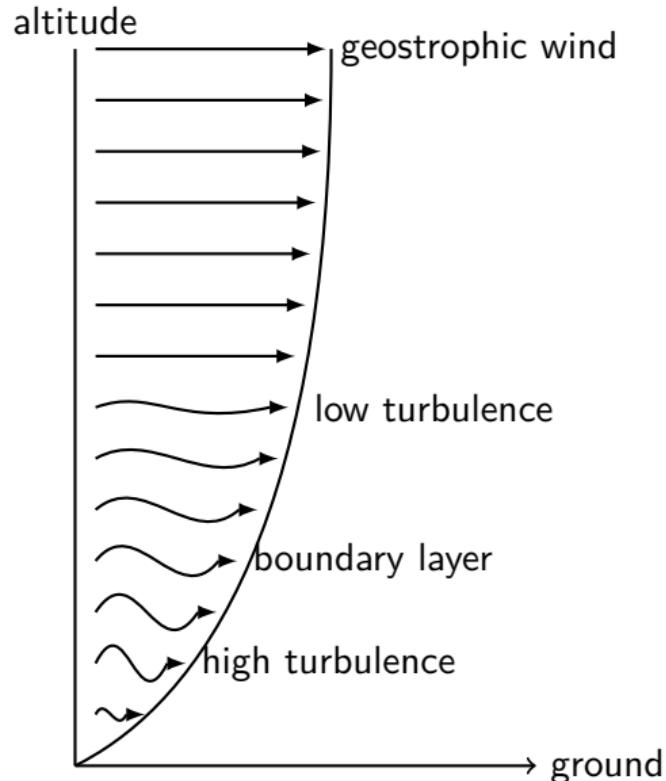
- ▶ High altitude → geostrophic wind
 - ▶ Ground → no wind speed

Energy extraction by ground roughness

- ▶ Vertical wind speed gradient
 - ▶ Turbulent momentum and mass exchange with higher air layers

Boundary layer thickness

- ▶ From 100 m on cold nights.
 - ▶ Up to 2000 m on warm summer days with low wind speed
 - ▶ On average approx. 1000 m



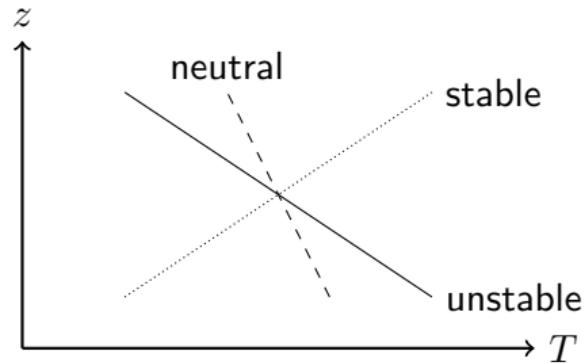
Vertical Temperature Profiles

Unstable

- ▶ Air near the ground is warmer than the air above.
 - There is more vertical mass transfer and thus increased turbulence

Stable

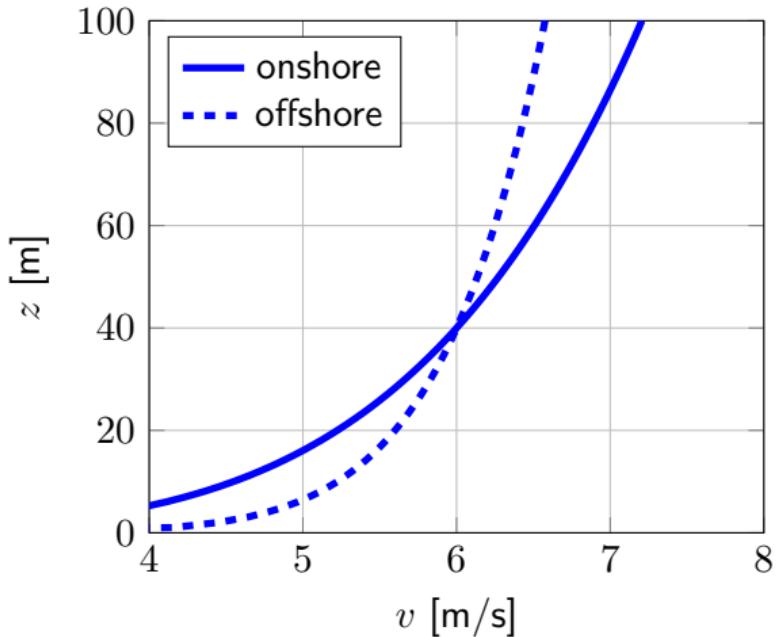
- ▶ Air near the ground is colder than the air above.
 - There is less vertical mass transfer and turbulence is suppressed



Neutral

- ▶ adiabatic temperature profile (no heat interaction, only caused by pressure)
 - ▶ Air temperature decreases by about 1°C per 100 m increase in altitude.
 - ▶ Often occurs at high wind speeds

Exponential Wind Profile



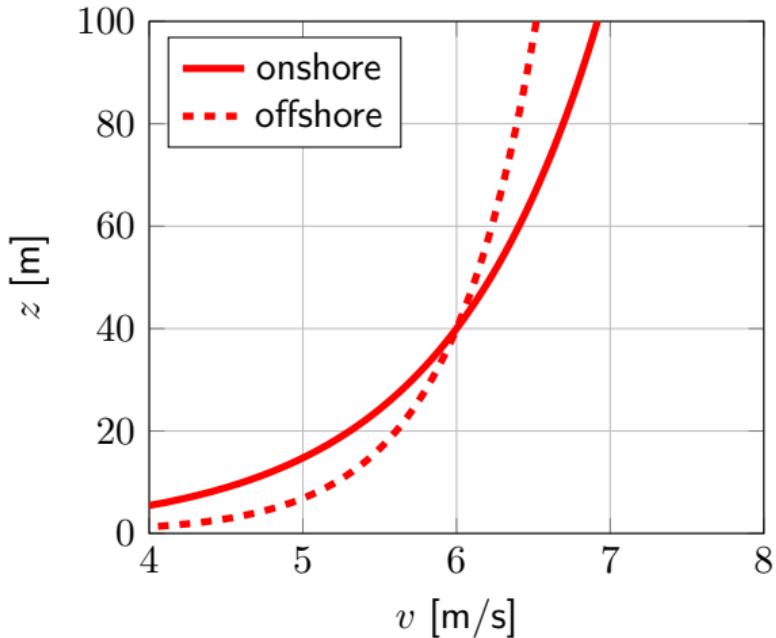
$$v_2 = v_1 \left(\frac{z_2}{z_1} \right)^\alpha$$

v_1 wind speed at height z_1
 v_2 wind speed at height z_2
 α roughness exponent

Roughness exponent α :

0.1	desert, open sea
0.15	meadows, pastures
0.2	little vegetation
0.37	cities, forest

Logarithmic Wind Profile



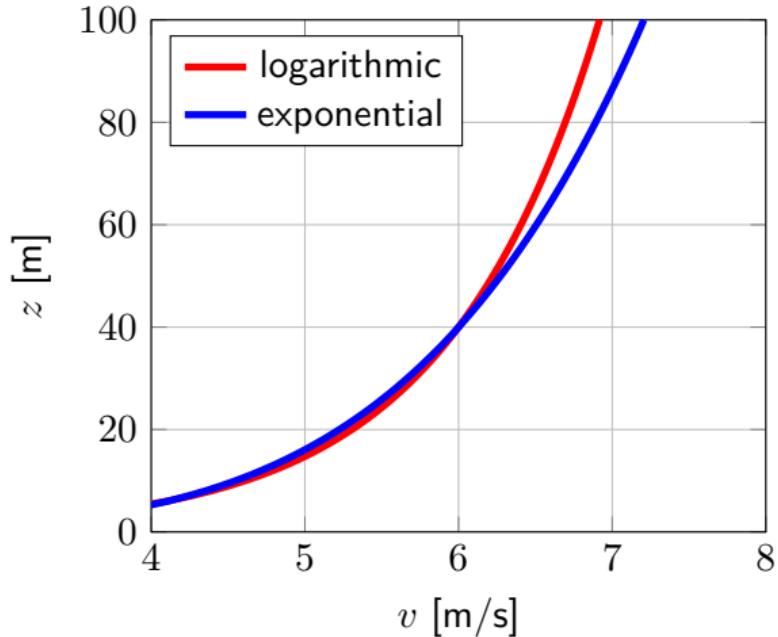
$$v_2 = v_1 \frac{\ln(z_2/z_0)}{\ln(z_1/z_0)}$$

v_1 wind speed at height z_1
 v_2 wind speed at height z_2
 z_0 roughness length

Roughness length z_0

0.001 m	desert, open sea
0.01 m	meadows, pasture
0.1 m	little vegetation
1 m	cities, forest

Logarithmic and Exponential Wind Profile



$$z = 40 \text{ m} \text{ and } v = 6 \text{ m/s}$$

$$z_0 = 0.1 \text{ m}$$

$$\alpha = 0.2$$

Influence of Stability on Wind Profile

Unstable thermal stratification

Rising air leads to strong vertical mass transfer and turbulence.

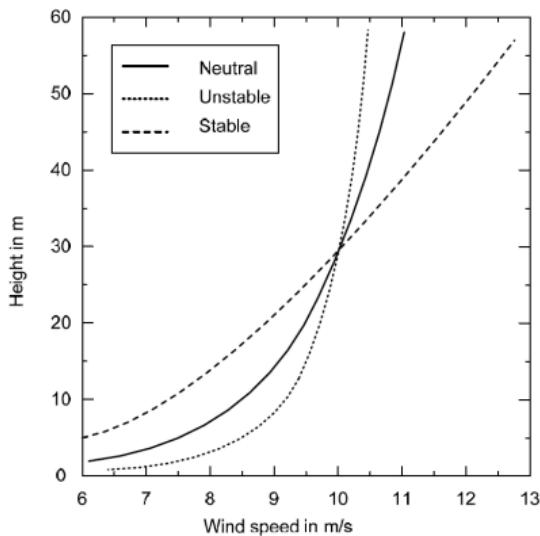
→ Slope of wind velocity with increasing altitude becomes smaller.

Stable thermal stratification

No vertical mass transfer and thus no turbulence.
→ Strong gradient of the wind profile.

Neutral thermal stratification

An adiabatic temperature profile is present.
→ Gradient of the wind profile decreases with the altitude.



[1]

Turbulence (Intensity)

Terminology:

- ▶ Turbulence describes a flow condition of the air that is characterized by disorder
 - ▶ Turbulence intensity describes the ratio of the standard deviation of the wind speed to the mean value of the wind speed related to a time interval of 10 minutes



[Leonardo da Vinci], ca. 1510-12

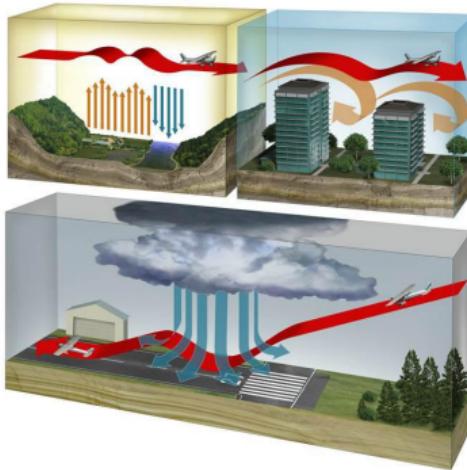


3D-Illustration von [Paolo Colagrossi]

Atmospheric Turbulence

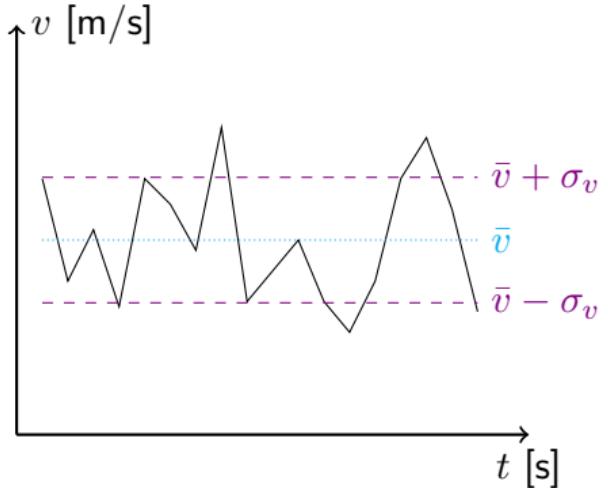
Causes

- ▶ Mechanical: caused by vertical shear and viscosity of the air, depends on local winds and roughness
- ▶ Thermal: caused by heat convection due to temperature differences



[Kevin Hand]

Turbulence Intensity



Mean wind speed \bar{v}

$$\bar{v} = \frac{1}{T} \int_0^T v(t) dt \quad \text{continuous}$$

$$= \frac{1}{n} \sum_{i=1}^n v_i \quad \text{discrete}$$

Variance σ_w^2 and standard deviation σ_w

$$\begin{aligned}\sigma_v^2 &= \frac{1}{T} \int_0^T (v(t) - \bar{v})^2 dt && \text{continuous} \\ \sigma_v^2 &= \frac{1}{n-1} \sum_{i=1}^n (v_i - \bar{v})^2 && \text{discrete, Bessel's corr.} \\ \sigma_v &= \sqrt{\sigma_v^2}\end{aligned}$$

Turbulence intensity I_V

$$I_V = \frac{\sigma_v}{\bar{v}}$$

WTG Classes acc. to IEC 61400-1 with Turbulence Classes

Wind Turbine Class	I	II	III	S
V _{ave} (m/s)	10	8.5	7.5	Values
	(m/s)	50	42.5	37.5
V _{ref}	Tropical (m/s)	57	57	specified
V _{ref,T} (m/s)		57		by the
A+		0.18		designer
A		0.16		
B		0.14		
C		0.12		

Extract from IEC 61400-1

V_{ref} reference wind speed

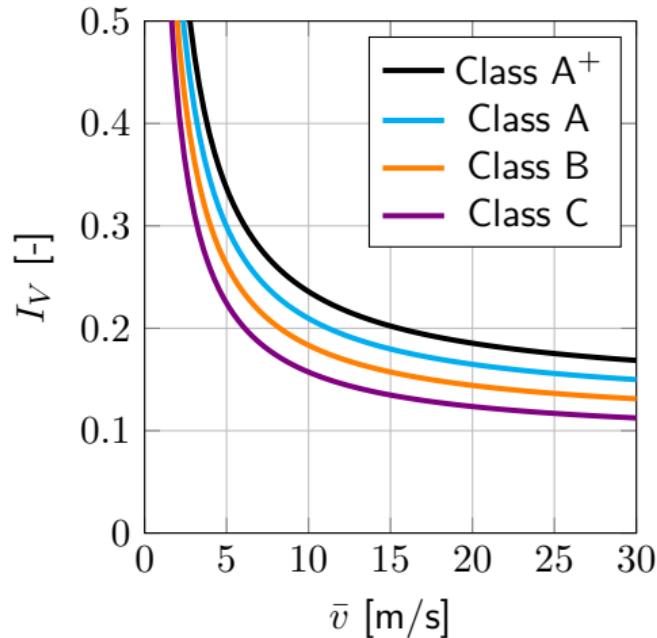
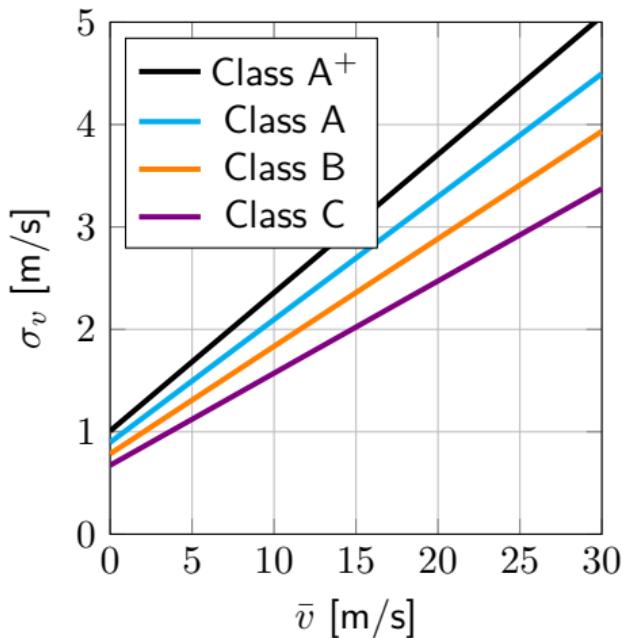
$V_{\text{ave}} = 0.2V_{\text{ref}}$ annual mean wind speed at hub height

I_{ref} expected value of the turbulence intensity at 15 m/s

A^+, A, B, C turbulence class

σ_v standard deviation of longitudinal wind component at hub height
 v_{hub} wind speed at hub height

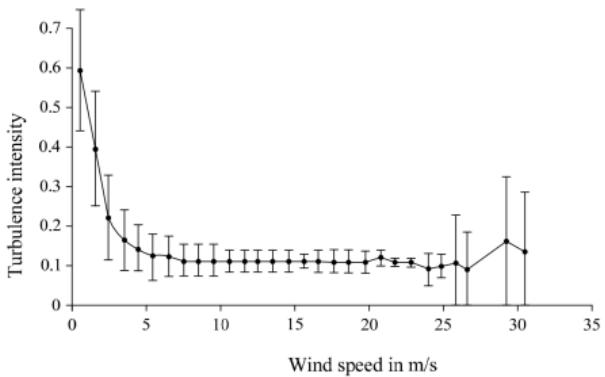
Normal Turbulence Model (NTM) acc. to IEC 61400-1



$$\sigma_v = I_{\text{ref}}(0.75\bar{v} + b) \text{ with } b = 5.6 \text{ m/s}$$

$$I_V = \frac{\sigma_v}{\bar{v}}$$

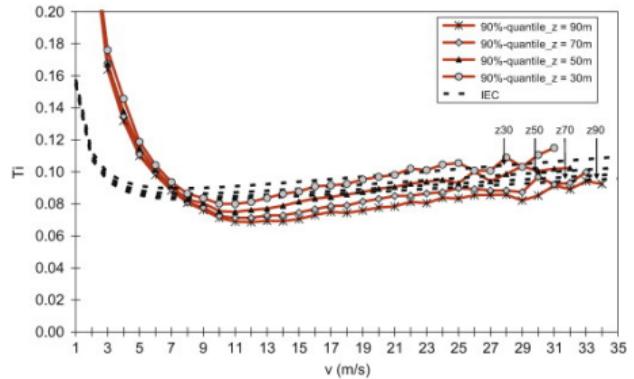
Turbulence intensity from measurements



[1]

Onshore

- ▶ I_V is reduced with increasing wind speed
- ▶ at low wind speeds I_V is strongly depending on the atmospheric stability

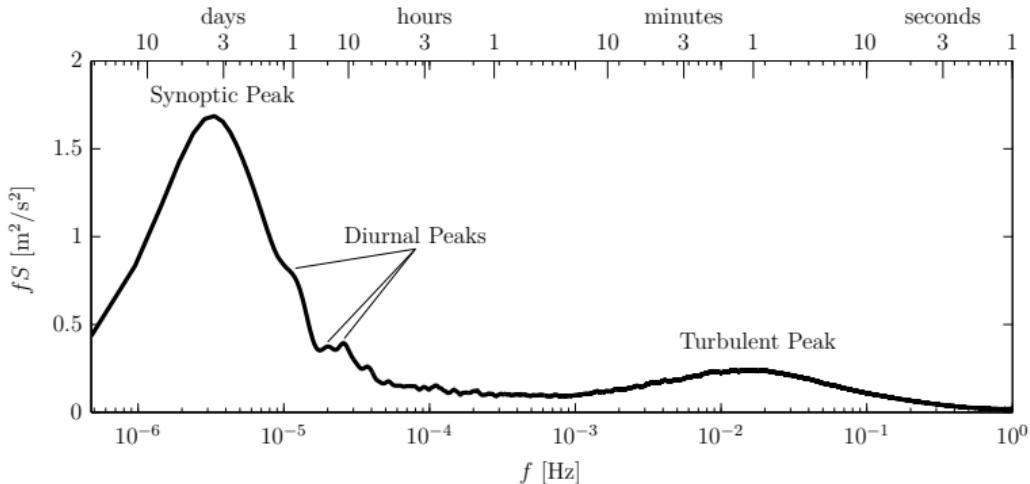


[Matthias Türk, Stefan Emeis]

Offshore

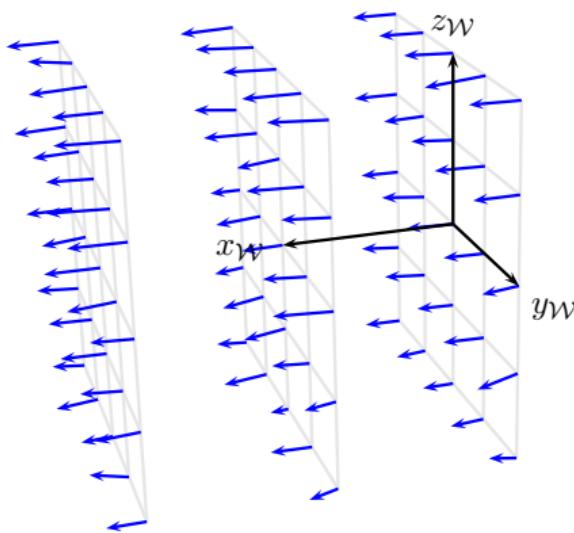
- ▶ Wind speed is influencing wave formation and by that the roughness
- ▶ Roughness and wave height are usually increasing with the wind speed → I_V is increasing

Spectral Gap



- ▶ Wind spectrum from Bremerhaven measured at 44 m, averaged over 4 months [2].
 - ▶ The peaks at around 10 and 14 hours are caused by land and sea breezes.
 - ▶ The wind speed variations with a timescale of minutes or less are known as turbulence.
 - ▶ The spectrum drops before the turbulence region as in [3].

Introduction to Turbulence Models



"When I meet God, I am going to ask him two questions: Why relativity? And why turbulence? I really believe he will have an answer for the first."
- Werner Heisenberg -

IEC Kaimal Spectral Model [4]

- ▶ spectra for each grid point i escala espacial L
 - ▶ longitudinal $S_{ii,u} = \frac{\sigma_u^2 4L_u / \bar{u}}{(1 + 6fL_u / \bar{u})^{5/3}}$
 - ▶ lateral $S_{ii,v} = \frac{\sigma_v^2 4L_v / \bar{u}}{(1 + 6fL_v / \bar{u})^{5/3}}$
 - ▶ vertical $S_{ii,w} = \frac{\sigma_w^2 4L_w / \bar{u}}{(1 + 6fL_w / \bar{u})^{5/3}}$
 - ▶ longitudinal coherence between point i and j :

$$\gamma_{ij,u} = \exp \left(-12 \sqrt{\left(\frac{f}{\bar{u}}\right)^2 + \left(\frac{0.12}{L_u}\right)^2} r_{ij} \right)$$

r_ij distancia entre puntos
solo se relaciona la componente u

Turbulent Wind Field Generation

wind

三

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Wind components without correlation to other points (lateral&vertical IEC Kaimal)

$$v_i(t) = \sum_{m=1}^{n_f} a_m \cos(2\pi f_m t + \theta_{i,m})$$

Amplitudes $a_m = \sqrt{2S_{ii,v}(f_m)\Delta f}$ defined by auto-spectrum $S_{ii,v}$ for each grid point i at frequency f_m and discretization Δf . Also single point longitudinal.

Wind components with correlation to other points (longitudinal IEC Kaimal)

$$u_i(t) = \bar{u} + \sum_{k=1}^i \sum_{m=1}^{n_f} a_{ik,m} \cos(2\pi f_m t + \theta_{k,m})$$

Amplitudes $a_{ik,m}$ defined by auto-spectra and coherence between point i and k .

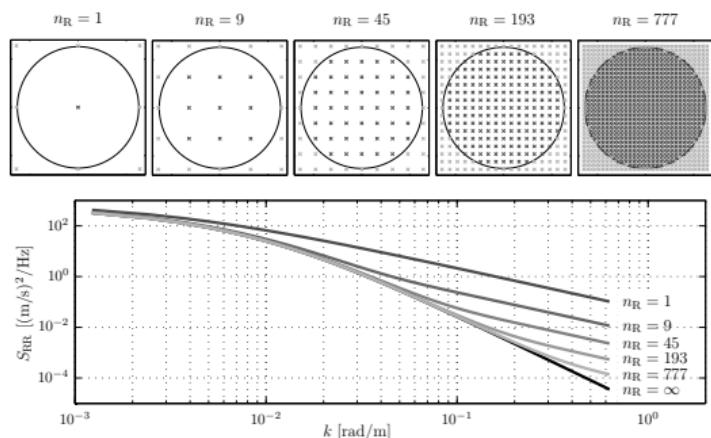
- ▶ Wind is “just” a sum of randomly shifted sinusoids with defined amplitudes.
 - ▶ This method is called the [Sandia Method](#) or Veers method [5].

Spectrum rotor effective wind speed

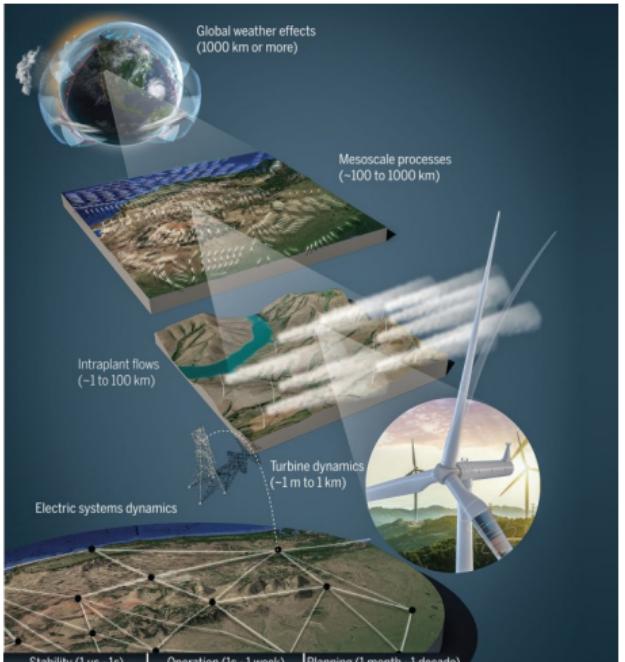
Auto-spectrum of $v_0 = \frac{1}{n} \sum_{i=1}^n u_i$

$$\begin{aligned} S_{\text{RR}} &= \mathcal{F}\{v_0\} \mathcal{F}^*\{v_0\} \\ &= \frac{1}{n^2} \sum_{i=1}^n \sum_{j=1}^n \underbrace{\mathcal{F}\{u_i\} \mathcal{F}^*\{u_j\}}_{S_{ij,u}} \\ &= \frac{S_{ii,u}}{n^2} \sum_{i=1}^n \sum_{j=1}^n \gamma_{ij,u} \end{aligned}$$

spectra $S_{ii,u}$ and coherence $\gamma_{ij,u}$ from turbulence model, e.g. Kaimal



Grand challenges in the science of wind energy 1/2



[7]

Speakers



*Paul Veers
National Renewable Energy Laboratory*



Julie Lundquist
University of Colorado, Boulder



Amy Robertson
National Renewable Energy Laboratory



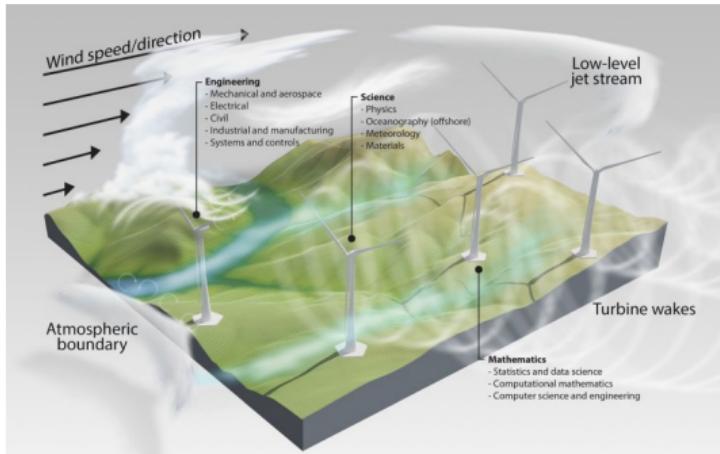
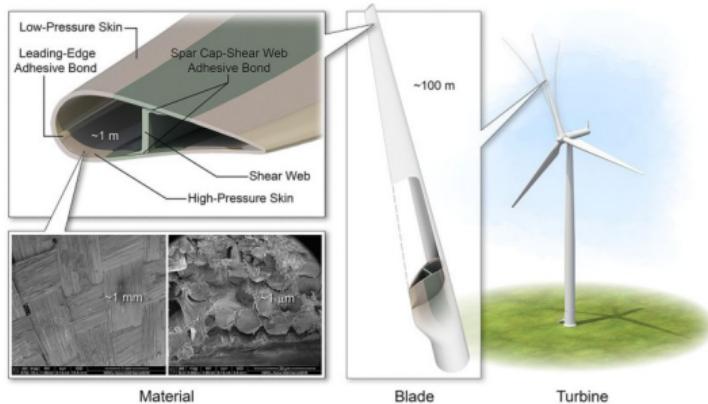
Eric Lantz
National Renewable Energy
Laboratory

[Video on YouTube]

Main challenges

- ▶ mastering the physics of resource from the atmosphere to the intra-plant flows

Grand challenges in the science of wind energy 2/2



[7]

- ▶ characterizing the structural, aero- and hydrodynamics of the largest rotating structures ever built coupled with access to the most advanced materials at commodity prices
 - ▶ controlling wind power plants to orchestrate wind turbine, plant, and grid formation operations for a stable, resilient, reliable and affordable energy system

Conclusion

Main questions

- ▶ How is a turbulent wind field generated?

$$\begin{aligned}
 & \text{wind} \\
 & = \\
 & + \\
 & + \\
 & + \\
 & + \\
 & \dots
 \end{aligned}$$

Sum of randomly shifted sinusoids with defined amplitudes

- ▶ lateral, vertical, single point longitudinal IEC Kaimal: amplitudes defined by auto-spectrum, one random phase angle per frequency

$$v_i(t) = \sum_{m=1}^{n_f} a_m \cos(2\pi f_m t + \theta_{i,m})$$

- ▶ longitudinal IEC Kaimal: amplitudes defined by auto-spectrum and coherence, phase angles from previous generated points are included

$$u_i(t) = \bar{u} + \sum_{k=1}^i \sum_{m=1}^{n_f} a_{ik,m} \cos(2\pi f_m t + \theta_{k,m})$$

Quick check on learning objectives

After this lectures you should be able to...

- ▶ linearize a reduced turbine model.
 - ▶ design a PI torque controller.
 - ▶ describe how the limits and reference values for the torque PI are obtained.
 - ▶ describe methods how the two PI controller can be coupled.
 - ▶ generate a time series of longitudinal wind following IEC standard.

References

- [1] R. Gasch and J. Twele. *Wind Power Plants : Fundamentals, Design, Construction and Operation*. Springer, 2012. ISBN: 978-3-642-22938-1.
- [2] D. Schlipf. "Lidar-Assisted Control Concepts for Wind Turbines". PhD thesis. University of Stuttgart, 2015. DOI: 10.18419/opus-8796.
- [3] I. Van der Hoven. "Power spectrum of horizontal wind speed in the frequency range from 0.0007 to 900 cycles per hour". In: *Journal of Meteorology* 14 (1957), pp. 160–164. DOI: 10.1175/1520-0469(1957)014<0160:PSOHWS>2.0.CO;2.
- [4] IEC 61400-1. *Wind turbines - Part 1: Design requirements*. International Electrotechnical Commission, 2005.
- [5] P. S. Veers. *Three-dimensional wind simulation*. Tech. rep. SAND88-0152. Sandia National Laboratory, 1988.
- [6] G. A. M. Van Kuik et al. "Long-term research challenges in wind energy – a research agenda by the european academy of wind energy". In: *Wind Energy Science* 1.1 (Feb. 2016), pp. 1–39. DOI: 10.5194/wes-1-1-2016.
- [7] P. Veers et al. "Grand challenges in the science of wind energy". In: *Science* 366.6464 (2019). DOI: 10.1126/science.aau2027.

Please let me know if you have further questions!

Prof. Dr.-Ing. David Schlipf
David.Schlipf@HS-Flensburg.de
www.hs-flensburg.de/go/WETI

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