

(2)

$$U_1 = \frac{1}{3}$$

↓

$$r = \frac{3}{10}$$

$$m = \frac{1}{10}$$

$$v = \frac{6}{10}$$

$$U_2 = \frac{2}{3}$$

$$r = \frac{2}{10}$$

$$m = \frac{2}{10}$$

$$v = \frac{6}{10}$$

ahora

(a) Sea roja $P(r) = 1/2$

$$\Rightarrow \text{Para } U_1 = \frac{1}{3} \cdot \frac{3}{10} = \frac{1}{10} = P_1(r)$$

$$\text{Para } U_2 = \frac{2}{3} \cdot \frac{6}{10} = \frac{2}{5} = P_2(r)$$

$$\text{entonces } P_r = P_1(r) + P_2(r) = \frac{1}{10} + \frac{2}{5} = \boxed{\frac{1}{2}}$$

(b) Sea negra $P(n) = 1/6$

$$\Rightarrow \text{Para } U_1 = \frac{1}{3} \cdot \frac{1}{10} = \frac{1}{30} \rightarrow P_1(n)$$

$$\text{Para } U_2 = \frac{2}{3} \cdot \frac{2}{10} = \frac{2}{15} \rightarrow P_2(n)$$

$$\text{entonces } P(n) = P_1(n) + P_2(n) = \frac{1}{30} + \frac{2}{15} = \boxed{\frac{1}{6}}$$

c) Sea de la urna 1 si se ha obtenido una bola negra

$$P(1/n) = \frac{1}{5} \Rightarrow \frac{P(1) \cdot P(n)}{P(n)} = \frac{P_1(n)}{P(n)} = \frac{\frac{1}{30}}{\frac{1}{6}} = \boxed{\frac{1}{5}}$$

d) Sea de la urna 2 si se ha obtenido una bola negra

$$P(2/n) = \frac{4}{5} \Rightarrow \frac{P(2) \cdot P(n)}{P(n)} = \frac{P_2(n)}{P(n)} = \frac{\frac{2}{15}}{\frac{1}{6}} = \boxed{\frac{4}{5}}$$