Recommended Sistem

In this project i use a dataset about 904765 Musical Instruments that had been sold in Amazon, and i'm going to design a Similarity-Based Recommender based on the users who purchased the products and the items that had been purchased.

The dataset is able https://s3.amazonaws.com/amazon-reviews-pds/tsv/index.txt) downloading the document named: https://s3.amazonaws.com/amazon-reviews-

pds/tsv/amazon_reviews_us_Musical_Instruments_v1_00.tsv.gz (https://s3.amazonaws.com/amazon-reviews-pds/tsv/amazon_reviews_us_Musical_Instruments_v1_00.tsv.gz)

Useful Libraries

```
In [2]: import gzip
    from collections import defaultdict
    import random
    import numpy as np
    import scipy.optimize
```

Reading de data

```
In [3]: path = "amazon_reviews_us_Musical_Instruments_v1_00.tsv.gz"
In [4]: file = gzip.open(path, 'rt', encoding="utf-8")
In [5]: header = file.readline() header = header.strip().split('\t')
```

```
Now, let's see the content of the dataset
In [6]: header
Out[6]: ['marketplace',
          'customer_id',
          'review id',
          'product id',
          'product_parent',
          'product_title',
          'product_category',
          'star_rating',
          'helpful_votes',
          'total votes',
          'vine',
          'verified_purchase',
          'review_headline',
          'review body',
          'review date']
```

Useful data Structures

To perform set intersections/unions efficiently, we first build data structures representing the set of items for each user and users for each item

```
In [9]: usersPerItem = defaultdict(set)
itemsPerUser = defaultdict(set)

In [10]: itemNames = {}

In [11]: for d in dataset:
    user, item = d['customer_id'], d['product_id']
    usersPerItem[item].add(user) # Ui: Save the item and add the users that purchased that itemsPerUser[user].add(item) # Iu: Save the user and add the items that have been purch itemNames[item] = d['product_title']
```

Recommendation

Jaccard Similarity

$$\operatorname{Jaccard}(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

```
In [13]: def Jaccard(s1, s2):
    numerator = len(s1.intersection(s2))
    denominator = len(s1.union(s2))
    return numerator/denominator
```

We want a recommendation function that return items similar to a candidate item i.

- Find the set of users who purchased i
- · Iterate over all other items other than i
- For all other items, compute their similarity with i (and store it)
- · Sort all other items by (Jaccard) similarity
- · Return the most similar

```
In [15]: def mostSimilar(i):
             similarities = []
             users = usersPerItem[i] # Scroll the users in each item
             for i2 in usersPerItem: # Scroll the items that have been purchased by this user
                 if i2 == i: continue # Skip if is the current item
                 sim = Jaccard(users, usersPerItem[i2])
                 similarities.append((sim,i2))
             similarities.sort(reverse = True)
             return similarities[:10]
In [16]: dataset[2]
Out[16]: {'marketplace': 'US',
          'customer_id': '6111003',
          'review id': 'RIZR67JKUDBI0',
          'product id': 'B0006VMBHI',
          'product parent': '603261968',
          'product title': 'AudioQuest LP record clean brush',
          'product_category': 'Musical Instruments',
          'star_rating': 3,
          'helpful votes': 0,
          'total votes': 1,
          'vine': 'N',
          'verified purchase': 'Y',
          'review headline': 'Three Stars',
          'review_body': 'removes dust. does not clean',
          'review date': '2015-08-31'}
In [18]: # The query is just a product ID
         query = dataset[2]['product_id']
         query
Out[18]: 'B0006VMBHI'
In [19]: mostSimilar(query)
Out[19]: [(0.028446389496717725, 'B00006I5SD'),
          (0.01694915254237288, 'B00006I5SB'),
          (0.015065913370998116, 'B000AJR482'),
          (0.014204545454545454, 'B00E7MVP3S'),
          (0.008955223880597015, 'B001255YL2'),
          (0.008849557522123894, 'B003EIRVO8'),
          (0.00821917808219178, 'B00006I5UH'),
          (0.008021390374331552, 'B00008BWM7'),
          (0.007656967840735069, 'B000H2BC4E')]
```

Inefficient:

The slowest component is the iteration over all other items.

In fact is sufficient to iterate over those items purchased by one of the users who purchased i

Efficient Implementation

(0.01420454545454545454, 'B00E7MVP3S'), (0.008955223880597015, 'B001255YL2'), (0.008849557522123894, 'B003EIRVO8'), (0.0083333333333333333, 'B0015VEZ22'), (0.00821917808219178, 'B00006I5UH'), (0.008021390374331552, 'B00008BWM7'), (0.007656967840735069, 'B000H2BC4E')]

```
In [24]: def mostSimilarFast(i):
             similarities = []
             users = usersPerItem[i] # Scroll the users in each item
             candidateItems = set()
             for u in users:
                 candidateItems = candidateItems.union(itemsPerUser[u])
             for i2 in usersPerItem: # Scroll the items that have been purchased by this user
                 if i2 == i: continue # Skip if is the current item
                 sim = Jaccard(users, usersPerItem[i2])
                 similarities.append((sim,i2))
             similarities.sort(reverse = True)
             return similarities[:10]
In [25]: mostSimilarFast(query)
Out[25]: [(0.028446389496717725, 'B00006I5SD'),
          (0.01694915254237288, 'B00006I5SB'),
          (0.015065913370998116, 'B000AJR482'),
```

Rating Predictor based on Similarity

Heuristic:

- The user (u)'s rating for an item i is a weighted combination of all of their previous ratings for items j
- The weight for each rating is given by the Jaccard similarity between i and j

This can be written as:

$$r(u,i) = \frac{1}{Z} \sum_{\substack{j \in I_u \setminus \{i\}}} r_{u,j} \cdot \mathrm{sim}(i,j)$$
 Normalization constant all items the user has rated other than i
$$Z = \sum_{\substack{j \in I_u \setminus \{i\}}} \mathrm{sim}(i,j)$$

```
In [27]: reviewsPerUser = defaultdict(list)
reviewsPerItem = defaultdict(list)

In [28]: for d in dataset:
    user, item = d['customer_id'], d['product_id']
    reviewsPerUser[user].append(d)
    reviewsPerItem[item].append(d)
```

```
In [29]: # This will be our baseline for comparison
         ratingMean = sum(d['star_rating'] for d in dataset) / len(dataset)
         ratingMean
Out[29]: 4.251102772543146
In [30]: def predictRating(user, item):
             ratings = []
             similarities = []
             for d in reviewsPerUser[user]:
                  i2 = d['product id']
                  if i2 == item: continue
                  ratings.append(d['star_rating']) # r_u,j
                  similarities.append(Jaccard(usersPerItem[item], usersPerItem[i2])) # sim(i,j)
             if (sum(similarities) > 0):
                  weightedRatings = [(x*y) \text{ for } x,y \text{ in } zip(ratings, similarities)]
                  return sum(weightedRatings) / sum(similarities)
                  # User hasn't rated any similar items
                  return ratingMean
```

As an example, select a rating for prediction

```
In [31]: dataset[1]
Out[31]: {'marketplace': 'US',
           'customer_id': '14640079',
          'review id': 'RZSLOBALIYUNU',
           'product id': 'B003LRN53I',
           'product_parent': '986692292',
          'product title': 'Sennheiser HD203 Closed-Back DJ Headphones',
           'product_category': 'Musical Instruments',
          'star rating': 5,
          'helpful votes': 0,
           'total_votes': 0,
          'vine': 'N',
          'verified_purchase': 'Y',
          'review headline': 'Five Stars',
           'review_body': 'Nice headphones at a reasonable price.',
          'review_date': '2015-08-31'}
In [32]: |u,i = dataset[1]['customer_id'], dataset[1]['product_id']
In [33]: predictRating(u, i)
Out[33]: 5.0
```

Similarly, we can evaluate accuracy across the entire corpus

```
In [34]: def MSE(predictions, labels):
    differences = [(x-y)**2 for x,y in zip(predictions, labels)]
    return sum(differences) / len(differences)
```

```
In [35]: alwaysPredictMean = [ratingMean for d in dataset]
In [36]: cfPredictions = [predictRating(d['customer_id'], d['product_id']) for d in dataset]
In [37]: labels = [d['star_rating'] for d in dataset]
In [38]: MSE(alwaysPredictMean, labels)
Out[38]: 1.4796142779564334
In [39]: MSE(cfPredictions, labels)
Out[39]: 1.6146130004291603
```

- In fact in this case it did worse (in terms of the MSE) than always predicting the mean
- · We could adapt this to use:
 - 1) A different similarity function (e.g. cosine)
 - 2) Similarity based on users ratiher than items
 - 3) A different weighting scheme

Latent Factor Model.

Bias Only Model

$$\arg\min_{\alpha,\beta} \frac{1}{N} \sum_{u,i} (\alpha + \beta_u + \beta_i - R_{u,i})^2 + \lambda \left[\sum_u \beta_u^2 + \sum_i \beta_i^2 \right]$$

In this section is the code for the gradient equations; and after that a library is used to optimize the model

```
In [40]: N = len(dataset)
    nUsers = len(reviewsPerUser)
    nItems = len(reviewsPerItem)
    users = list(reviewsPerUser.keys())
    items = list(reviewsPerItem.keys())
```

Note: Alpha and Beta (userbiases) are parameter we'll fit. This code sets their initial values (alpha to the mean rating, and beta u / beta i to zero)

```
In [ ]: alpha = ratingMean
In [41]: # Beta_u & Beta_i
userBiases = defaultdict(float)
itemBiases = defaultdict(float)
```

Our prediction function in this case just implements the bias only model:

$$f(u,i) = \alpha + \beta_u + \beta_i$$
 user item user bias item bias

function = offset + UserBias + ItemBias

```
In [42]: def prediction(user, item):
    return alpha + userBiases[user] + itemBiases[item]
```

The first complex function to implement is this "unpack" function. The gradient descent library we'll use expects a single vector of parameters (θ), which we have to unpack to produce alpha and beta:

```
In [43]: def unpack(theta):
    global alpha
    global userBiases
    global itemBiases
    alpha = theta[0]
    userBiases = dict(zip(users, theta[1:nUsers+1]))
    itemBiases = dict(zip(items, theta[1+nUsers:]))
```

Full cost function

$$\frac{1}{N} \sum_{u,i} (\alpha + \beta_u + \beta_i - R_{u,i})^2 + \lambda \left[\sum_u \beta_u^2 + \sum_i \beta_i^2 \right]$$

```
In [44]:

def cost(theta, labels, lamb):
    unpack(theta)
    predictions = [prediction(d['customer_id'], d['product_id']) for d in dataset]
    cost = MSE(predictions, labels)
    print("MSE = " + str(cost))
    for u in userBiases:
        cost += lamb*userBiases[u]**2
    for i in itemBiases:
        cost += lamb*itemBiases[i]**2
    return cost
```

Derivative term for each parameter

```
\frac{\partial \text{obj}}{\partial \beta_u} = \frac{1}{N} \sum_{u,i} 2(\alpha + \beta_u + \beta_i - R_{u,i}) + 2\lambda \beta_u
```

```
In [46]: | def derivative(theta, labels, lamb):
             unpack(theta)
             N = len(dataset)
             d alpha = 0
             d_UserBiases = defaultdict(float)
             d_ItemBiases = defaultdict(float)
             for d in dataset:
                 u,i = d['customer_id'], d['product_id']
                 pred = prediction(u, i)
                 diff = pred - d['star_rating']
                 d_alpha += 2/N*diff
                 d_UserBiases[u] += 2/N*diff
                 d ItemBiases[i] += 2/N*diff
             for u in userBiases:
                 d_UserBiases[u] += 2*lamb*userBiases[u]
             for i in itemBiases:
                 d_ItemBiases[i] += 2*lamb*itemBiases[i]
             d_theta = [d_alpha] + [d_UserBiases[u] for u in users] + [d_ItemBiases[i] for i in iter
             return np.array(d_theta)
```

In [47]: MSE(alwaysPredictMean, labels)

Out[47]: 1.4796142779564334

Using Library from Scipy (lbfgs)

Cost function (returns scalar)

Initial parameter values (as vector)

Derivative function (returns vector)

Other arguments to be passed to the cost and derivative functions

```
In [48]: | scipy.optimize.fmin_l_bfgs_b(cost, [ratingMean] + [0.0]*(nUsers+nItems), derivative, args
         MSE = 1.4796142779564334
         MSE = 1.468686355953835
         MSE = 2.6961687181992064
         MSE = 1.4681419018494124
         MSE = 1.4523523347391192
         MSE = 1.4513575397272933
         MSE = 1.4476987674765316
         MSE = 1.4421925605951182
         MSE = 1.4415262672088056
         MSE = 1.4413460037417523
         MSE = 1.441397612244047
         MSE = 1.4414066017099236
Out[48]: (array([ 4.24278450e+00, -1.37216332e-03, 5.73953696e-03, ...,
                  8.31051679e-04, -2.15966373e-03, -2.67061773e-04]),
          1.4574364057349305,
          {'grad': array([-4.52665785e-07, 8.64056712e-09, -2.76548829e-08, ...,
                  -5.06227031e-09, 1.10178064e-08, 1.37544741e-09]),
           'task': b'CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL',
           'funcalls': 12,
           'nit': 9,
           'warnflag': 0})
```

Complete Latent Factor Model

```
\arg\min_{\alpha,\beta,\gamma} \frac{1}{N} \sum_{u,i} (\alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i - R_{u,i})^2 + \lambda \left[ \sum_u \beta_u^2 + \sum_i \beta_i^2 + \sum_i \|\gamma_i\|_2^2 + \sum_u \|\gamma_u\|_2^2 \right]
```

```
In [50]: alpha = ratingMean
alpha
Out[50]: 4.251102772543146
In [51]: userBiases = defaultdict(float)
    itemBiases = defaultdict(float)
In [52]: userGamma = {}
    itemGamma = {}

In [53]: K = 2 # Numbre of Latent factors(i.e. dimensionality of gamma)
In [54]: for u in reviewsPerUser:
    userGamma[u] = [random.random()*0.1 - 0.05 for k in range(K)]
In [55]: for i in reviewsPerItem:
    itemGamma[i] = [random.random()*0.1 - 0.05 for k in range(K)]
```

```
In [56]: def unpack(theta):
             global alpha
             global userBiases
             global itemBiases
             index = 0
             alpha = theta[index]
             index += 1
             userBiases = dict(zip(users, theta[index:index+nUsers]))
             index += nUsers
             itemBiases = dict(zip(items, theta[index:index+nItems]))
             index += nItems
             for u in users:
                 userGamma[u] = theta[index:index+K]
                 index += K
             for i in items:
                 itemGamma[i] = theta[index:index+K]
                 index += K
In [57]: def inner(x, y):
             return sum([a*b for a,b in zip(x, y)])
In [59]: def prediction(user, item):
             return alpha + userBiases[user] + itemBiases[item] + inner(userGamma[user], itemGamma[:
In [60]: def cost(theta, lafbels, lamb):
             unpack(theta)
             predictions = [prediction(d['customer_id'], d['product_id']) for d in dataset]
             cost = MSE(predictions, labels)
             print("MSE = " + str(cost))
             for u in users:
                 cost += lamb*userBiases[u]**2
                 for k in range(K):
                     cost += lamb*userGamma[u][k]**2
             for i in items:
                 cost += lamb*itemBiases[i]**2
                 for k in range(K):
                     cost += lamb*itemGamma[i][k]**2
             return cost
```

the video have a really bad Quality so de derivative can't be seen.

```
In [ ]:
```