PW1: CN2 algorithm

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## Chapter 1

## CN2 pseudo-code

In this chapter short, we see the pseudo-code of the CN2 algorithm. It is broken down into two procedures. The first one (see Algorithm 1) corresponds to the main loop of the algorithm where we obtain and save the rules. The second one (see Algorithm 2) corresponds to the procedure that generates the rules and finds the best current rule.

## Algorithm 1 CN2 Algorithm - Part 1

```
1: procedure CN2(E)
       Discretize E with user-defined \#bins
       Replace missing values in E with the mode of the feature
3:
       rules \leftarrow \text{Empty list of rules}
       selectors \leftarrow Set of all possible selectors
       default\_rule\_class \leftarrow Most common class in E
6:
       N \leftarrow |E|
7:
       (best\_cpx, covered\_examples,
8:
           most\_common\_class, precision) \leftarrow find\_best\_complex(E)
       while best\_cpx not nil and E not empty do
9:
           coverage \leftarrow |covered\_examples|/N
10:
           Remove covered\_examples from E
11:
           rules.append(best_cpx, most_common_class, precision, coverage)
12:
           (best\_cpx, covered\_examples,
13:
               most\_common\_class, precision) \leftarrow find\_best\_complex(E)
       end while
14:
15:
       precision \leftarrow \#instances \ with \ default\_rule\_class/|E|
       coverage \leftarrow |E|/N
16:
       rules.append(*, default_rule_class, precision, coverage)
18: end procedure
```

### **Algorithm 2** CN2 Algorithm - Part 2

```
1: procedure FIND_BEST_COMPLEX(E)
 2:
        best\_cpx \leftarrow nil
        best\_entropy \leftarrow \infty
 3:
 4:
        best\_significance \leftarrow -\infty
        best\_cpx\_covered\_examples \leftarrow nil
        best\_cpx\_class \leftarrow nil
 6:
        best\_cpx\_precision \leftarrow 0
 7:
 8:
        star \leftarrow The set containing the empty complex
 9:
        while star is not empty do
10:
            entropies \leftarrow []
            significances \leftarrow []
11:
            new\_star \leftarrow \{x \land y | x \in star, y \in selectors\}
12:
            Remove all complexes from new\_star that are either in star
13:
                or null
            for cpx in new_star do
14:
                E' \leftarrow \text{Set of covered examples by } cpx
15:
16:
                cpx\_entropy \leftarrow entropy(E')
                cpx\_significance \leftarrow significance(E')
17:
                entropies.append(cpx\_entropy)
18:
                significances.append(cpx\_significance)
19:
                if cpx\_significance > user defined significance then
20:
21:
                    if cpx\_entropy < best\_entropy and
                       cpx\_significance \ge best\_significance then
22:
                        best\_cpx \leftarrow cpx
                        best\_entropy \leftarrow cpx\_entropy
23:
                        best\_significance \leftarrow cpx\_significance
24:
                        best\_cpx\_covered\_examples \leftarrow E'
25:
                        best\_cpx\_class \leftarrow Most common class in E'
26:
27:
                        best\_cpx\_precision \leftarrow \#instances \ with \ most \ common \ class/|E'|
                    end if
28:
                end if
29:
            end for
30:
31:
            repeat
32:
                Remove from star the worst complex based on the entropies
                    and significances lists
            until size(new\_star) \le user defined maximum
33:
34:
            star \leftarrow new\_star
        end while
35:
36: end procedure
```

## Chapter 2

## Results

In this chapter, we will see the results of applying our implementation of the CN2 algorithm in three datasets of small, medium and large sizes.

Since the algorithm has a random component when computing the rule significance, the results have been obtained after running the algorithm 5 times for each dataset.

### 2.1 Iris dataset

The following section presents the results obtained from applying the algorithm to the Iris dataset<sup>1</sup>. This is a small-sized dataset with 150 instances and 4 real attributes plus the class attribute.

#### 2.1.1 Rules

In this ruleset, we can see how, in most cases, the algorithm can classify the instances only requiring one of the attributes. Another thing to note is how specific the rules are. This can be observed by looking at the precision, which usually is 1, and coverage, which is no greater than 0.125, of each rule. One last comment about this ruleset is how the algorithm can cover almost all the training data without needing the default rule, with only 3.3% of the training examples not being classified by any rule but the default.

Below we can see the ruleset (in brackets we can see each rule's coverage and precision respectively).

```
 \begin{split} \text{IF petal\_length} &= (5.61, 6.9] \implies \text{virginica} \ [0.125, 1.000] \\ \text{IF petal\_length} &= (0.99, 1.4] \implies \text{setosa} \ [0.125, 1.000] \\ \text{IF petal\_length} &= (3.76, 4.35] \implies \text{versicolor} \ [0.125, 1.000] \\ \text{IF petal\_length} &= (5.12, 5.61] \implies \text{virginica} \ [0.125, 1.000] \\ \text{IF sepal\_width} &= (3.5, 4.4] \implies \text{setosa} \ [0.075, 1.000] \\ \text{IF petal\_length} &= (4.8, 5.12] \land \text{sepal\_width} = (2.5, 2.8] \implies \text{virginica} \ [0.058, 0.857] \\ \end{split}
```

https://archive.ics.uci.edu/ml/datasets/iris

```
IF sepal_width = (3.3, 3.5] \land \text{petal\_length} = (1.4, 1.6] \implies \text{setosa} [0.050, 1.000]
IF petal_length = (1.4, 1.6] \implies \text{setosa} [0.050, 1.000]
IF petal_length = (1.6, 3.76] \land \text{petal\_width} = (0.3, 1.0] \implies \text{versicolor} [0.050, 0.833]
IF petal_width = (1.3, 1.5] \land \text{petal\_length} = (4.35, 4.8] \implies \text{versicolor} [0.042, 1.000]
IF petal_length = (4.8, 5.12] \implies \text{virginica} [0.033, 0.750]
IF sepal_length = (6.71, 7.7] \implies \text{versicolor} [0.025, 1.000]
IF sepal_width = (2.8, 2.9] \implies \text{versicolor} [0.025, 1.000]
IF sepal_width = (2.9, 3.0] \implies \text{virginica} [0.025, 1.000]
IF petal_width = (1.0, 1.3] \implies \text{versicolor} [0.017, 1.000]
IF sepal_length = (5.8, 6.14] \implies \text{versicolor} [0.017, 1.000]
IF \implies \text{virginica} [0.033, 0.500]
```

### 2.2 Heart dataset

The following section presents the results obtained from applying the algorithm to the Heart dataset<sup>2</sup>. This is a medium-sized dataset with 918 instances and 12 attributes both numerical and categorical.

#### 2.2.1 Rules

In this ruleset, we can see how the algorithm needs at least two attributes to classify the instances in contrast with the one seen before. Probably because this dataset contains more data both in terms of instances and attributes. Also, as in the previous ruleset, the rules are very specific which is demonstrated by their high precision and low coverage. The last point to note is that the algorithm was not able to produce any rule only for 0.1% of the instances.

Below we can see the ruleset (in brackets we can see each rule's coverage and precision respectively).

```
IF ChestPainType = ATA \land Age = (27.0, 42.0] \implies No [0.045, 1.000]
IF ST_Slope = Flat \land Oldpeak = (-2.61, 0.0] \land Age = (48.0, 53.0] \implies Yes [0.025, 1.000]
IF Oldpeak = (1.4, 2.0] \land MaxHR = (59.0, 110.0] \implies Yes [0.023, 1.000]
IF ChestPainType = ATA \land Cholesterol = (182.0, 212.0] \Longrightarrow No [0.018, 1.000]
IF Age = (59.0, 63.0] \land \text{RestingBP} = (79.0, 115.0] \implies \text{Yes} [0.018, 1.000]
IF MaxHR = (59.0, 110.0] \land \text{RestingBP} = (140.0, 150.0] \implies \text{Yes} [0.016, 1.000]
IF Age = (53.0, 56.0) \Longrightarrow No [0.016, 0.583]
IF Oldpeak = (2.0, 6.2) \land \text{RestingBP} = (135.0, 140.0) \implies \text{Yes } [0.014, 1.000]
IF FastingBS = 1 \land Age = (27.0, 42.0] \land ChestPainType = ASY \implies Yes [0.014, 1.000]
IF RestingBP = (115.0, 120.0] \implies \text{No} [0.014, 0.700]
IF Oldpeak = (2.0, 6.2] \land \text{Cholesterol} = (289.0, 603.0] \implies \text{Yes} [0.012, 1.000]
IF Oldpeak = (2.0, 6.2] \land \text{Age} = (53.0, 56.0) \implies \text{Yes} [0.012, 1.000]
IF ST_Slope = Up \land Cholesterol = (212.0, 233.0] \land Age = (42.0, 48.0] \implies No [0.012,
1.000
IF ExerciseAngina = Y \land FastingBS = 1 \implies Yes [0.012, 1.000]
IF ChestPainType = ATA \land RestingBP = (130.0, 135.0] \implies No [0.011, 1.000]
IF ChestPainType = ATA \land RestingBP = (79.0, 115.0] \implies No [0.011, 1.000]
```

<sup>&</sup>lt;sup>2</sup>https://www.kaggle.com/datasets/fedesoriano/heart-failure-prediction

```
IF ChestPainType = ATA \land Age = (48.0, 53.0] \Longrightarrow No [0.011, 1.000]
```

- IF ExerciseAngina = Y  $\land$  RestingBP = (140.0, 150.0]  $\land$  Age = (63.0, 77.0]  $\Longrightarrow$  Yes [0.011, 1.000]
- IF ExerciseAngina =  $Y \land FastingBS = 1 \land Age = (48.0, 53.0) \implies Yes [0.011, 1.000]$
- IF ChestPainType = ATA  $\land$  Cholesterol = (289.0, 603.0]  $\land$  Age = (53.0, 56.0]  $\Longrightarrow$  No [0.010, 1.000]
- IF Oldpeak =  $(2.0, 6.2] \land \text{Age} = (56.0, 59.0] \implies \text{Yes} [0.010, 1.000]$
- IF ST\_Slope = Up  $\land$  Sex = F  $\land$  Age = (53.0, 56.0]  $\Longrightarrow$  No [0.010, 1.000]
- IF ChestPainType = NAP  $\land$  Age = (27.0, 42.0]  $\land$  RestingBP = (120.0, 130.0]  $\Longrightarrow$  No [0.010, 1.000]
- IF ChestPainType = ATA  $\land$  Age = (53.0, 56.0]  $\implies$  No [0.010, 0.857]
- IF ST\_Slope = Up  $\land$  Age = (59.0, 63.0]  $\implies$  No [0.010, 0.857]
- IF ChestPainType = NAP  $\land$  MaxHR = (165.0, 202.0]  $\Longrightarrow$  No [0.010, 1.000]
- IF ExerciseAngina = Y  $\land$  Age = (59.0, 63.0]  $\land$  RestingBP = (115.0, 120.0]  $\Longrightarrow$  Yes [0.008, 1.000]
- IF ChestPainType = ATA  $\land$  RestingBP = (120.0, 130.0]  $\land$  Age = (42.0, 48.0]  $\implies$  No [0.008, 1.000]
- IF RestingBP =  $(150.0, 200.0] \land Age = (53.0, 56.0] \implies Yes [0.008, 1.000]$
- IF ST\_Slope = Up  $\land$  Cholesterol = (289.0, 603.0]  $\land$  Age = (27.0, 42.0]  $\implies$  No [0.008, 1.000]
- IF Sex = F  $\land$  Cholesterol = (260.0, 289.0]  $\land$  ChestPainType = NAP  $\implies$  No [0.008, 1.000]
- IF RestingECG = ST  $\land$  Age = (53.0, 56.0]  $\Longrightarrow$  Yes [0.008, 1.000]
- IF Oldpeak =  $(1.4, 2.0] \land \text{RestingBP} = (130.0, 135.0] \implies \text{Yes } [0.007, 1.000]$
- IF MaxHR = (165.0, 202.0]  $\land$  Resting ECG = ST  $\land$  Oldpeak = (-2.61, 0.0]  $\implies$  No [0.007, 1.000]
- IF ST\_Slope = Up  $\land$  ChestPainType = ATA  $\land$  RestingBP = (135.0, 140.0]  $\implies$  No [0.007, 1.000]
- IF MaxHR =  $(165.0, 202.0] \land \text{RestingBP} = (140.0, 150.0] \implies \text{No} [0.007, 1.000]$
- IF Oldpeak =  $(2.0, 6.2] \land RestingECG = Normal \implies Yes [0.007, 1.000]$
- IF Sex = F  $\land$  Age = (48.0, 53.0]  $\land$  Exercise Angina = N  $\land$  Oldpeak = (-2.61, 0.0]  $\implies$  No [0.007, 1.000]
- IF Resting BP =  $(140.0, 150.0] \land \text{Age} = (63.0, 77.0] \implies \text{Yes} [0.007, 1.000]$
- IF Resting BP = (130.0, 135.0)  $\implies$  No [0.007, 0.800]
- IF ST\_Slope = Up  $\land$  Cholesterol = (212.0, 233.0]  $\land$  ChestPainType = NAP  $\implies$  No [0.007, 1.000]
- IF ExerciseAngina =  $Y \land Oldpeak = (1.0, 1.4) \implies Yes [0.007, 1.000]$
- IF  $Sex = F \land Age = (42.0, 48.0) \implies No [0.007, 1.000]$
- IF Oldpeak =  $(1.4, 2.0] \land Age = (42.0, 48.0] \implies Yes [0.007, 1.000]$
- IF MaxHR =  $(110.0, 121.0] \land Age = (42.0, 48.0] \implies Yes [0.007, 1.000]$
- IF MaxHR = (110.0, 121.0]  $\land$  Resting BP = (120.0, 130.0]  $\land$  Exercise Angina = Y  $\implies$  Yes [0.007, 0.800]
- IF Cholesterol =  $(182.0, 212.0] \land \text{ChestPainType} = \text{ASY} \implies \text{No} [0.007, 0.800]$
- IF MaxHR = (59.0, 110.0]  $\wedge$  Sex = M  $\Longrightarrow$  Yes [0.007, 1.000]
- IF RestingBP =  $(120.0, 130.0] \implies \text{Yes } [0.007, 1.000]$
- IF Age =  $(48.0, 53.0] \implies \text{Yes} [0.007, 1.000]$
- IF Exercise Angina = Y  $\land$  Resting BP = (130.0, 135.0]  $\land$  Age = (59.0, 63.0]  $\implies$  Yes [0.005, 1.000]
- IF Sex = F  $\wedge$  ChestPainType = NAP  $\wedge$  RestingBP = (115.0, 120.0]  $\implies$  No [0.005, 1.000]
- IF ChestPainType = ATA  $\land$  Age = (42.0, 48.0]  $\implies$  No [0.005, 1.000]
- IF Exercise Angina = Y  $\land$  Oldpeak = (1.0, 1.4]  $\land$  Age = (53.0, 56.0]  $\implies$  Yes [0.005, 1.000]

```
IF ST_Slope = Flat \wedge Cholesterol = (260.0, 289.0] \wedge Age = (42.0, 48.0] \Longrightarrow \text{Yes} [0.005, 48.0] \mapsto \text{Yes} [0.00
IF ChestPainType = NAP \land Cholesterol = (260.0, 289.0] \Longrightarrow No [0.005, 1.000]
IF ExerciseAngina = Y \land Cholesterol = (-1.0, 182.0) \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \implies Yes [0.005, 182.0] \land Age = (53.0, 56.0) \land Age = (53.0, 56.
IF MaxHR = (121.0, 132.0] \land Oldpeak = (1.0, 1.4] \implies Yes [0.005, 1.000]
IF ChestPainType = TA \land RestingBP = (135.0, 140.0] \Longrightarrow Yes [0.005, 1.000]
IF Resting
BP = (140.0, 150.0] \land Age = (53.0, 56.0]
 \land Exercise
Angina = N \implies No
[0.005, 1.000]
IF FastingBS = 1 \land Age = (53.0, 56.0) \implies Yes [0.005, 1.000]
IF ExerciseAngina = Y \land MaxHR = (143.0, 153.0) \land Age = (42.0, 48.0) \implies Yes [0.005, 150.0] \land Age = (42.0, 48.0) \implies Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow Yes [0.005, 150.0] \land Age = (42.0, 48.0) \Rightarrow 
IF RestingBP = (140.0, 150.0] \land \text{ChestPainType} = \text{NAP} \implies \text{No} [0.005, 1.000]
IF FastingBS = 1 \land Age = (63.0, 77.0] \implies Yes [0.005, 1.000]
IF MaxHR = (165.0, 202.0] \implies \text{Yes} [0.005, 0.750]
IF Age = (59.0, 63.0] \land \text{ChestPainType} = \text{ASY} \implies \text{Yes} [0.005, 1.000]
IF FastingBS = 1 \land \text{Cholesterol} = (-1.0, 182.0) \implies \text{Yes} [0.005, 1.000]
IF RestingBP = (120.0, 130.0] \land Sex = F \implies No [0.005, 1.000]
IF Oldpeak = (0.0, 0.1] \land Age = (48.0, 53.0] \implies No [0.004, 1.000]
IF MaxHR = (165.0, 202.0] \land ST\_Slope = Down \implies No [0.004, 1.000]
IF Sex = F \wedge Age = (42.0, 48.0] \wedge ChestPainType = ATA \implies No [0.004, 1.000]
IF ExerciseAngina = Y \land Age = (53.0, 56.0) \land Sex = F \implies Yes [0.004, 1.000]
IF Sex = F \wedge Age = (42.0, 48.0] \wedge RestingECG = LVH \implies No [0.004, 1.000]
IF ExerciseAngina = Y \wedge Oldpeak = (2.0, 6.2] \wedge \text{RestingBP} = (140.0, 150.0] \implies \text{Yes}
[0.004, 1.000]
IF MaxHR = (110.0, 121.0] \land \text{RestingBP} = (130.0, 135.0] \implies \text{Yes } [0.004, 1.000]
IF ST_Slope = Down \land RestingBP = (115.0, 120.0] \Longrightarrow Yes [0.004, 1.000]
IF ST_Slope = Down \land ExerciseAngina = N \implies No [0.004, 1.000]
IF Age = (59.0, 63.0] \land \text{Cholesterol} = (260.0, 289.0] \implies \text{Yes} [0.004, 1.000]
IF Sex = F \wedge Age = (63.0, 77.0] \wedge RestingBP = (79.0, 115.0] \implies No [0.004, 1.000]
IF RestingBP = (130.0, 135.0] \land \text{ChestPainType} = \text{ASY} \land \text{ST\_Slope} = \text{Up} \implies \text{No}
[0.004, 1.000]
IF Resting BP = (130.0, 135.0] \land Age = (42.0, 48.0] \implies Yes [0.004, 1.000]
IF ChestPainType = NAP \land Oldpeak = (1.0, 1.4] \implies \text{No} [0.004, 1.000]
IF ChestPainType = ATA \land Age = (63.0, 77.0] \Longrightarrow No [0.004, 1.000]
IF MaxHR = (110.0, 121.0] \land \text{RestingBP} = (135.0, 140.0] \implies \text{Yes} [0.004, 1.000]
IF RestingBP = (150.0, 200.0] \land ST\_Slope = Up \land FastingBS = 1 \implies No [0.004, 1.000]
IF Age = (59.0, 63.0] \land RestingECG = LVH \land Sex = M \implies Yes [0.004, 1.000]
IF RestingBP = (140.0, 150.0] \land \text{RestingECG} = \text{ST} \implies \text{Yes} [0.004, 1.000]
IF MaxHR = (165.0, 202.0] \land \text{Cholesterol} = (182.0, 212.0] \implies \text{Yes} [0.004, 1.000]
IF Resting BP = (140.0, 150.0] \land Age = (59.0, 63.0] \implies Yes [0.004, 1.000]
IF FastingBS = 1 \land Age = (59.0, 63.0) \implies Yes [0.004, 1.000]
IF Cholesterol = (182.0, 212.0] \land Age = (42.0, 48.0] \implies No [0.004, 1.000]
IF Cholesterol = (182.0, 212.0] \land Age = (48.0, 53.0] \implies No [0.004, 1.000]
IF ST_Slope = Up \land RestingBP = (135.0, 140.0] \land Age = (48.0, 53.0] \implies No [0.004,
1.000
IF Cholesterol = (289.0, 603.0] \land \text{Oldpeak} = (1.4, 2.0] \land \text{Sex} = \text{M} \implies \text{Yes} [0.004, 1.000]
IF MaxHR = (59.0, 110.0] \land Age = (63.0, 77.0] \implies Yes [0.004, 1.000]
IF ST_Slope = Up \land MaxHR = (59.0, 110.0] \implies No [0.004, 1.000]
IF Sex = F \land Cholesterol = (-1.0, 182.0] \implies Yes [0.004, 1.000]
IF Age = (63.0, 77.0] \land Sex = F \implies No [0.004, 1.000]
IF Oldpeak = (0.0, 0.1] \land MaxHR = (153.0, 165.0] \implies Yes [0.003, 1.000]
IF Sex = F \wedge ChestPainType = NAP \wedge Age = (59.0, 63.0] \Longrightarrow No [0.003, 1.000]
```

IF ExerciseAngina =  $Y \land Oldpeak = (0.0, 0.1] \implies Yes [0.003, 1.000]$ 

```
IF Oldpeak = (0.0, 0.1] \implies \text{No} [0.003, 1.000]
IF ST_Slope = Up \land Oldpeak = (2.0, 6.2] \land \text{RestingBP} = (140.0, 150.0] \implies \text{Yes } [0.003, 1.00] \implies 
IF Sex = F \wedge Cholesterol = (212.0, 233.0] \wedge Age = (42.0, 48.0] \implies No [0.003, 1.000]
IF ExerciseAngina = Y \wedge Oldpeak = (2.0, 6.2] \wedge Age = (27.0, 42.0] \implies Yes [0.003,
IF Oldpeak = (2.0, 6.2] \land \text{RestingBP} = (130.0, 135.0] \implies \text{Yes} [0.003, 1.000]
IF ST_Slope = Up \land MaxHR = (143.0, 153.0] \land Age = (56.0, 59.0] \implies No [0.003, 1.000]
IF ExerciseAngina = Y \land ChestPainType = TA \implies No [0.003, 1.000]
IF MaxHR = (165.0, 202.0] \land Oldpeak = (0.1, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \implies No [0.003, 1.0] \land Age = (27.0, 42.0] \land Age = (27.0, 42.0) \land Age = (27.0, 42.
IF ST\_Slope = Flat \land ChestPainType = ATA \land Age = (59.0, 63.0] \implies Yes [0.003, 1.000]
IF ST_Slope = Down \land ChestPainType = TA \implies No [0.003, 1.000]
IF ST_Slope = Down \land Age = (42.0, 48.0] \implies Yes [0.003, 1.000]
IF Oldpeak = (2.0, 6.2] \land Sex = F \implies Yes [0.003, 1.000]
IF Oldpeak = (2.0, 6.2] \land \text{RestingBP} = (115.0, 120.0] \implies \text{Yes} [0.003, 1.000]
IF ChestPainType = NAP \land Oldpeak = (2.0, 6.2] \land Age = (63.0, 77.0] \implies Yes [0.003,
1.000
IF MaxHR = (59.0, 110.0] \land \text{RestingBP} = (130.0, 135.0] \implies \text{No} [0.003, 1.000]
IF ST\_Slope = Up \land ChestPainType = TA \land Age = (63.0, 77.0) \implies No [0.003, 1.000]
IF ST_Slope = Flat \wedge ChestPainType = TA \wedge Age = (42.0, 48.0] \Longrightarrow Yes [0.003, 1.000]
IF ExerciseAngina = Y \wedge Cholesterol = (182.0, 212.0] \wedge Age = (27.0, 42.0] \Longrightarrow Yes
[0.003, 1.000]
IF ST_Slope = Down \land Cholesterol = (260.0, 289.0) \implies \text{Yes } [0.003, 1.000]
IF RestingBP = (130.0, 135.0] \land Age = (53.0, 56.0] \implies No [0.003, 1.000]
IF Oldpeak = (1.4, 2.0] \land \text{ChestPainType} = \text{TA} \implies \text{No} [0.003, 1.000]
IF FastingBS = 1 \land \text{Cholesterol} = (260.0, 289.0) \land \text{RestingBP} = (150.0, 200.0) \implies \text{Yes}
[0.003, 1.000]
IF RestingBP = (130.0, 135.0] \land MaxHR = (121.0, 132.0] \implies Yes [0.003, 1.000]
IF MaxHR = (165.0, 202.0] \land Age = (59.0, 63.0] \implies Yes [0.003, 1.000]
IF ST_Slope = Down \land RestingBP = (120.0, 130.0] \Longrightarrow Yes [0.003, 1.000]
IF ST_Slope = Down \implies No [0.003, 1.000]
IF ChestPainType = TA \land RestingECG = LVH \land RestingBP = (150.0, 200.0] \implies Yes
[0.003, 1.000]
IF MaxHR = (165.0, 202.0] \land \text{Cholesterol} = (212.0, 233.0] \land \text{RestingECG} = \text{Normal} \land \text{Constant}
Resting BP = (135.0,\,140.0] \implies No \; [0.003,\,1.000]
IF ChestPainType = ATA \land ExerciseAngina = Y \land Sex = M \implies Yes [0.003, 1.000]
IF Oldpeak = (2.0, 6.2] \land MaxHR = (59.0, 110.0] \implies Yes [0.003, 1.000]
IF ChestPainType = TA \land Sex = F \Longrightarrow No [0.003, 1.000]
IF Oldpeak = (2.0, 6.2] \land \text{ExerciseAngina} = Y \implies \text{No} [0.003, 1.000]
IF Age = (27.0, 42.0] \land \text{RestingBP} = (120.0, 130.0] \implies \text{Yes } [0.003, 1.000]
IF Oldpeak = (1.4, 2.0] \land \text{FastingBS} = 1 \land \text{Age} = (59.0, 63.0] \implies \text{Yes} [0.003, 1.000]
IF MaxHR = (165.0, 202.0] \land Age = (56.0, 59.0] \implies Yes [0.003, 1.000]
IF Oldpeak = (2.0, 6.2] \land MaxHR = (143.0, 153.0) \implies Yes [0.003, 1.000]
IF ChestPainType = TA \wedge FastingBS = 0 \Longrightarrow No [0.003, 1.000]
IF ChestPainType = TA \land Cholesterol = (-1.0, 182.0] \Longrightarrow Yes [0.003, 1.000]
```

IF ST\_Slope = Up  $\land$  Oldpeak =  $(1.0, 1.4] \implies \text{No} [0.003, 1.000]$ 

IF Oldpeak =  $(2.0, 6.2] \land \text{FastingBS} = 1 \implies \text{No} [0.003, 1.000]$ 

IF Oldpeak =  $(1.0, 1.4] \land MaxHR = (165.0, 202.0] \implies No [0.003, 1.000]$ IF Cholesterol =  $(260.0, 289.0] \land Age = (42.0, 48.0] \implies No [0.003, 1.000]$ IF ChestPainType = ATA  $\land$  Cholesterol =  $(260.0, 289.0] \implies Yes [0.003, 1.000]$ 

IF ChestPainType = ATA  $\land$  RestingBP = (120.0, 130.0]  $\implies$  No [0.003, 1.000] IF MaxHR = (121.0, 132.0]  $\land$  Age = (53.0, 56.0]  $\implies$  Yes [0.003, 1.000] IF RestingECG = ST  $\land$  Age = (48.0, 53.0]  $\implies$  Yes [0.003, 1.000]

```
IF Cholesterol = (260.0, 289.0) \land Age = (63.0, 77.0) \implies Yes [0.003, 1.000]
IF MaxHR = (110.0, 121.0] \land \text{Cholesterol} = (260.0, 289.0] \implies \text{Yes} [0.003, 1.000]
IF MaxHR = (110.0, 121.0] \land \text{RestingBP} = (79.0, 115.0] \land \text{RestingECG} = \text{Normal} \implies
Yes [0.003, 1.000]
IF Sex = F \land FastingBS = 1 \implies No [0.003, 1.000]
IF Cholesterol = (260.0, 289.0] \land \text{RestingBP} = (79.0, 115.0] \implies \text{No} [0.003, 1.000]
IF FastingBS = 1 \land Age = (42.0, 48.0) \implies Yes [0.003, 1.000]
IF FastingBS = 1 \land Age = (48.0, 53.0] \implies Yes [0.003, 1.000]
IF Age = (59.0, 63.0] \land \text{Cholesterol} = (289.0, 603.0] \implies \text{No} [0.003, 1.000]
IF RestingBP = (140.0, 150.0] \land \text{Cholesterol} = (289.0, 603.0] \implies \text{Yes} [0.003, 1.000]
IF MaxHR = (165.0, 202.0] \land Sex = M \land ST\_Slope = Up \land Oldpeak = (-2.61, 0.0] \land
RestingECG = LVH \implies No [0.003, 1.000]
IF Age = (59.0, 63.0] \wedge Sex = M \wedge ST_Slope = Flat \wedge FastingBS = 0 \wedge Oldpeak = (1.4,
[2.0] \implies \text{No} [0.003, 1.000]
IF MaxHR = (121.0, 132.0] \land Age = (42.0, 48.0] \implies Yes [0.003, 1.000]
IF MaxHR = (110.0, 121.0] \land Age = (63.0, 77.0] \land Sex = M \implies No [0.003, 1.000]
IF Cholesterol = (182.0, 212.0] \land Age = (63.0, 77.0] \implies Yes [0.003, 1.000]
IF Cholesterol = (182.0, 212.0] \land Sex = F \implies No [0.003, 1.000]
IF FastingBS = 1 \land \text{RestingBP} = (135.0, 140.0] \implies \text{No} [0.003, 1.000]
IF Age = (42.0, 48.0] \land MaxHR = (143.0, 153.0] \implies Yes [0.003, 1.000]
IF Age = (42.0, 48.0] \land \text{Sex} = M \land \text{ChestPainType} = \text{NAP} \implies \text{No} [0.003, 1.000]
IF Cholesterol = (-1.0, 182.0] \land MaxHR = (143.0, 153.0] \implies No [0.003, 1.000]
IF MaxHR = (121.0, 132.0] \land \text{ChestPainType} = \text{NAP} \implies \text{Yes} [0.003, 1.000]
IF MaxHR = (110.0, 121.0] \land \text{Cholesterol} = (-1.0, 182.0] \land \text{FastingBS} = 0 \land \text{Sex} = \text{M} \land \text{Sex} = \text{M
ST\_Slope = Flat \implies Yes [0.003, 1.000]
IF RestingBP = (79.0, 115.0] \land Age = (56.0, 59.0] \implies No [0.003, 1.000]
IF RestingBP = (79.0, 115.0) \land Age = (63.0, 77.0) \implies Yes [0.003, 1.000]
IF Oldpeak = (1.4, 2.0] \land Age = (63.0, 77.0] \implies Yes [0.003, 1.000]
IF Resting
ECG = ST \land Cholesterol = (233.0, 260.0] \Longrightarrow No [0.003, 1.000]
IF Cholesterol = (233.0, 260.0] \land Age = (56.0, 59.0] \implies Yes [0.003, 1.000]
IF Cholesterol = (233.0, 260.0] \land MaxHR = (121.0, 132.0] \implies Yes [0.003, 1.000]
IF Cholesterol = (233.0, 260.0] \implies \text{Yes} [0.003, 1.000]
IF Age = (42.0, 48.0) \implies \text{Yes} [0.003, 1.000]
IF Age = (48.0, 53.0] \land \text{ChestPainType} = \text{NAP} \implies \text{Yes} [0.003, 1.000]
IF Age = (63.0, 77.0] \land \text{Cholesterol} = (212.0, 233.0) \implies \text{No} [0.003, 1.000]
\label{eq:energy} \text{IF MaxHR} = (110.0,\, 121.0] \implies \text{No} \; [0.003,\, 1.000]
IF MaxHR = (121.0, 132.0] \implies No [0.003, 1.000]
IF Cholesterol = (289.0, 603.0] \implies \text{Yes} [0.003, 1.000]
\label{eq:iff} \text{IF ChestPainType} = \text{NAP} \implies \text{No} \; [0.003, \, 1.000]
IF Oldpeak = (-2.61, 0.0] \implies \text{Yes} [0.003, 1.000]
IF MaxHR = (153.0, 165.0] \implies No [0.003, 1.000]
IF * \implies Yes [0.001, 1.000]
```

### 2.3 Rice dataset

The following section presents the results obtained from applying the algorithm to the Rice dataset<sup>3</sup>. This is a large-sized dataset with 3810 instances and 7 numerical attributes and the class.

<sup>&</sup>lt;sup>3</sup>https://www.kaggle.com/datasets/muratkokludataset/rice-dataset-commeo-and-osmancik

### 2.3.1 Rules

In this last ruleset, we see how happens the same as in the previous two. We have very specific rules again, which are characteristic of this algorithm. Also, we see how most of the rules are composed by the conjunction of multiple selectors. The most noticeable thing in this ruleset is the fact that the algorithm has not been able to classify 20.4% of the training instances. This is a considerable amount of instances, even more compared to the two previous cases. Moreover, by looking at the accuracy of the default rule we can see that most of the remaining instances are misclassified by this rule.

Below we can see the ruleset (in brackets we can see each rule's coverage and precision respectively).

```
IF Major_Axis_Length = (203.33, 239.01] \land \text{Minor_Axis_Length} = (90.01, 107.54] \implies
Cammeo [0.051, 0.981]
IF Major_Axis_Length = (203.33, 239.01] \land Minor_Axis_Length = (86.34, 90.01] \land Area
= (13932.0, 18913.0] \implies \text{Cammeo} [0.050, 1.000]
IF Eccentricity = (0.77, 0.87] \implies \text{Osmancik} [0.043, 0.931]
IF Major_Axis_Length = (203.33, 239.01] \land \text{Extent} = (0.64, 0.73] \land \text{Area} = (13932.0, 0.73)
18913.0] \implies Cammeo [0.042, 1.000]
IF Major_Axis_Length = (174.46, 185.63] \land Minor_Axis_Length = (82.65, 86.34) \implies
Osmancik [0.026, 0.886]
IF Major_Axis_Length = (203.33, 239.01] \land \text{Extent} = (0.49, 0.6] \land \text{Eccentricity} = (0.89, 0.6)
0.9] \implies Cammeo [0.025, 1.000]
IF Major_Axis_Length = (174.46, 185.63] \land \text{Extent} = (0.6, 0.64] \land \text{Convex\_Area} = (11627.75,
12676.5] \implies Osmancik [0.022, 0.941]
IF Major_Axis_Length = (203.33, 239.01] \land \text{Extent} = (0.73, 0.86] \land \text{Eccentricity} = (0.89, 0.89)
0.9] \implies Cammeo [0.018, 1.000]
IF Major_Axis_Length = (174.46, 185.63) \land \text{Eccentricity} = (0.77, 0.87) \land \text{Area} = (11375.25,
12405.5] \implies Osmancik [0.015, 0.979]
IF Perimeter = (359.090000000000003, 426.42] \land \text{Eccentricity} = (0.89, 0.9] \implies \text{Osmancik}
[0.011, 1.000]
IF Eccentricity = (0.77, 0.87] \land \text{Area} = (11375.25, 12405.5] \land \text{Extent} = (0.6, 0.64] \implies
Osmancik [0.011, 1.000]
IF\ Major\_Axis\_Length = (174.46,\,185.63] \, \land \, Minor\_Axis\_Length = (82.65,\,86.34] \, \land \, Extent = (174.46,\,185.63) \, \land \, Exte
= (0.64, 0.73] \implies \text{Osmancik} [0.011, 0.971]
IF Perimeter = (483.02, 548.45] \land Area = (12405.5, 13932.0] \land Minor_Axis_Length =
(82.65, 86.34) \implies \text{Cammeo} [0.010, 1.000]
IF Convex_Area = (14274.25, 19099.0] \land Extent = (0.73, 0.86] \implies Cammeo [0.008, 0.86]
IF Major_Axis_Length = (203.33, 239.01] \land Minor_Axis_Length = (82.65, 86.34] \land Con-
vex\_Area = (14274.25, 19099.0] \implies Cammeo [0.008, 1.000]
IF Major_Axis_Length = (203.33, 239.01] \land \text{Minor_Axis_Length} = (82.65, 86.34] \land \text{Area}
= (12405.5, 13932.0] \implies \text{Cammeo} [0.008, 1.000]
IF Perimeter = (359.090000000000003, 426.42] \land Minor_Axis_Length = (82.65, 86.34) \implies
Osmancik [0.008, 1.000]
IF Perimeter = (359.090000000000003, 426.42) \implies Osmancik [0.008, 0.957]
IF Convex_Area = (14274.25, 19099.0] \land \text{Extent} = (0.49, 0.6] \implies \text{Cammeo} [0.007, 1.000]
IF Perimeter = (359.09000000000003, 426.42] \land \text{Eccentricity} = (0.87, 0.89] \implies \text{Osmancik}
[0.007, 1.000]
```

```
IF Perimeter = (483.02, 548.45] \land \text{Extent} = (0.6, 0.64] \implies \text{Cammeo} [0.007, 1.000]
```

- IF Eccentricity =  $(0.9, 0.95] \land \text{Convex\_Area} = (12676.5, 14274.25] \land \text{Minor\_Axis\_Length}$  $= (82.65, 86.34) \land \text{Extent} = (0.64, 0.73) \implies \text{Cammeo} [0.006, 0.895]$
- IF Perimeter =  $(483.02, 548.45] \land \text{Minor\_Axis\_Length} = (59.52, 82.65] \implies \text{Cammeo}$ [0.006, 1.000]
- IF Major\_Axis\_Length =  $(203.33, 239.01] \land \text{Extent} = (0.6, 0.64] \land \text{Eccentricity} = (0.9, 0.9)$ 0.95]  $\implies$  Cammeo [0.006, 1.000]
- IF Major\_Axis\_Length =  $(203.33, 239.01] \land \text{Extent} = (0.73, 0.86] \land \text{Perimeter} = (448.66, 0.000)$ 483.02  $\implies$  Cammeo [0.005, 1.000]
- IF Eccentricity =  $(0.77, 0.87] \land Major\_Axis\_Length = (174.46, 185.63] \land Minor\_Axis\_Length$  $= (90.01, 107.54) \land Perimeter = (426.42, 448.66) \land Extent = (0.64, 0.73) \implies Osmancik$ [0.005, 1.000]
- IF Convex\_Area =  $(14274.25, 19099.0] \land Area = (12405.5, 13932.0] \implies Cammeo [0.005, 13932.0]$
- $IF\ Perimeter = (426.42, 448.66] \land Minor\_Axis\_Length = (82.65, 86.34] \land Major\_Axis\_Length$  $= (185.63, 203.33) \implies \text{Osmancik} [0.005, 1.000]$
- IF Area = (7550.99, 11375.25]  $\wedge$  Extent = (0.49, 0.6]  $\wedge$  Eccentricity = (0.89, 0.9]  $\Longrightarrow$ Osmancik [0.005, 1.000]
- IF Perimeter =  $(359.090000000000003, 426.42] \land \text{Extent} = (0.64, 0.73] \implies \text{Osmancik}$ [0.004, 1.000]
- IF Eccentricity =  $(0.77, 0.87] \land \text{Convex\_Area} = (11627.75, 12676.5] \land \text{Minor\_Axis\_Length}$  $= (90.01, 107.54) \implies Osmancik [0.004, 1.000]$
- IF Area =  $(13932.0, 18913.0] \land \text{Minor\_Axis\_Length} = (86.34, 90.01] \implies \text{Cammeo} [0.004,$ 1.000
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Minor_Axis\_Length} = (59.52, 82.65] \land \text{Eccenter}$ tricity =  $(0.87, 0.89] \land \text{Area} = (7550.99, 11375.25] \implies \text{Osmancik} [0.004, 1.000]$
- IF Perimeter =  $(483.02, 548.45] \land Major\_Axis\_Length = (185.63, 203.33] \land Minor\_Axis\_Length$ =  $(90.01, 107.54] \land \text{Convex\_Area} = (14274.25, 19099.0] \implies \text{Cammeo} [0.004, 0.667]$
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land Perimeter = (448.66, 483.02) \implies Osmancik$ [0.004, 0.917]
- IF Major\_Axis\_Length =  $(203.33, 239.01] \land \text{Minor_Axis\_Length} = (59.52, 82.65] \land \text{Extent}$  $= (0.49, 0.6] \implies \text{Cammeo} [0.004, 1.000]$
- IF Major\_Axis\_Length =  $(174.46, 185.63) \land \text{Eccentricity} = (0.77, 0.87) \land \text{Extent} = (0.49, 185.63)$ 0.6]  $\implies$  Osmancik [0.004, 1.000]
- IF Convex\_Area =  $(14274.25, 19099.0] \land \text{Eccentricity} = (0.87, 0.89) \land \text{Area} = (13932.0,$ 18913.0]  $\wedge$  Extent = (0.6, 0.64]  $\wedge$  Minor\_Axis\_Length = (90.01, 107.54]  $\Longrightarrow$  Cammeo [0.004, 0.818]
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land Extent = (0.6, 0.64] \implies Osmancik [0.004, 0.004]$ 0.818
- IF Major\_Axis\_Length =  $(203.33, 239.01] \land \text{Extent} = (0.49, 0.6] \land \text{Area} = (12405.5,$ 13932.0]  $\implies$  Cammeo [0.003, 1.000]
- IF Convex\_Area =  $(14274.25, 19099.0] \land Extent = (0.6, 0.64] \implies Cammeo [0.003, 0.900]$ IF Convex\_Area =  $(14274.25, 19099.0] \implies \text{Cammeo} [0.003, 0.900]$
- IF Minor\_Axis\_Length =  $(82.65, 86.34] \land \text{Eccentricity} = (0.9, 0.95] \land \text{Extent} = (0.6, 0.64]$  $\implies$  Cammeo [0.003, 0.900]
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land Minor_Axis_Length = (86.34, 90.01] \land Area$ =  $(11375.25, 12405.5] \land \text{Extent} = (0.73, 0.86] \implies \text{Osmancik} [0.003, 1.000]$
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Eccentricity} = (0.89, 0.9] \land \text{Extent} = (0.49, 0.9)$ 0.6]  $\Longrightarrow$  Osmancik [0.003, 1.000]
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Convex\_Area} = (7722.99, 11627.75] \land \text{Area} = (7722.99, 11627.75]$  $(11375.25, 12405.5] \implies \text{Osmancik} [0.003, 1.000]$
- IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Extent} = (0.49, 0.6] \land \text{Minor_Axis_Length} =$  $(86.34, 90.01) \land \text{Area} = (11375.25, 12405.5) \implies \text{Osmancik} [0.003, 1.000]$

```
IF Major_Axis_Length = (203.33, 239.01] \land Eccentricity = (0.77, 0.87] \implies Cammeo [0.002, 1.000]
```

IF Perimeter =  $(359.090000000000003, 426.42] \land Major_Axis_Length = (174.46, 185.63] \land Extent = (0.73, 0.86] \land Area = (7550.99, 11375.25] \implies Osmancik [0.002, 1.000]$ 

IF Major\_Axis\_Length = (174.46, 185.63]  $\land$  Extent = (0.6, 0.64]  $\land$  Area = (7550.99, 11375.25]  $\Longrightarrow$  Osmancik [0.002, 1.000]

IF Major\_Axis\_Length =  $(203.33, 239.01] \land Area = (12405.5, 13932.0] \land Minor_Axis_Length = (59.52, 82.65] \implies Cammeo [0.002, 0.857]$ 

IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Extent} = (0.6, 0.64] \land \text{Minor_Axis_Length} = (59.52, 82.65] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Perimeter =  $(483.02, 548.45] \land \text{Extent} = (0.6, 0.64] \land \text{Area} = (12405.5, 13932.0] \implies \text{Cammeo} [0.002, 1.000]$ 

IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Extent} = (0.6, 0.64] \land \text{Eccentricity} = (0.89, 0.9] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Minor_Axis_Length} = (59.52, 82.65] \land \text{Area} = (7550.99, 11375.25] \land \text{Extent} = (0.64, 0.73] \land \text{Eccentricity} = (0.9, 0.95] \land \text{Perimeter} = (426.42, 448.66] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Major\_Axis\_Length =  $(203.33, 239.01] \land \text{Area} = (11375.25, 12405.5] \implies \text{Cammeo} [0.002, 1.000]$ 

IF Eccentricity =  $(0.77, 0.87] \land \text{Area} = (11375.25, 12405.5] \land \text{Minor\_Axis\_Length} = (82.65, 86.34] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Minor_Axis_Length} = (90.01, 107.54] \land \text{Area} = (11375.25, 12405.5] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Perimeter = (426.42, 448.66]  $\land$  Area = (7550.99, 11375.25]  $\land$  Minor\_Axis\_Length = (82.65, 86.34]  $\implies$  Osmancik [0.002, 1.000]

IF Convex\_Area =  $(7722.99, 11627.75] \land \text{Extent} = (0.73, 0.86] \land \text{Major_Axis_Length} = (174.46, 185.63] \land \text{Eccentricity} = (0.9, 0.95] \implies \text{Osmancik} [0.002, 1.000]$ 

IF Perimeter = (483.02, 548.45]  $\land$  Eccentricity = (0.77, 0.87]  $\land$  Extent = (0.64, 0.73]  $\Longrightarrow$  Cammeo [0.001, 1.000]

IF Convex\_Area = (14274.25, 19099.0]  $\wedge$  Eccentricity = (0.89, 0.9]  $\implies$  Cammeo [0.001, 1.000]

IF Area =  $(7550.99, 11375.25] \land$  Eccentricity =  $(0.89, 0.9] \land$  Convex\_Area =  $(11627.75, 12676.5] \implies$  Osmancik [0.001, 1.000]

IF Major\_Axis\_Length = (174.46, 185.63]  $\land$  Perimeter = (448.66, 483.02]  $\land$  Area = (11375.25, 12405.5]  $\Longrightarrow$  Osmancik [0.001, 1.000]

 $IF\ Area = (13932.0,\ 18913.0] \implies Cammeo\ [0.001,\ 0.750]$ 

IF Major\_Axis\_Length = (174.46, 185.63]  $\land$  Perimeter = (448.66, 483.02]  $\land$  Extent = (0.49, 0.6]  $\implies$  Osmancik [0.001, 1.000]

IF Major\_Axis\_Length = (203.33, 239.01]  $\land$  Minor\_Axis\_Length = (59.52, 82.65]  $\land$  Extent = (0.6, 0.64]  $\Longrightarrow$  Cammeo [0.001, 1.000]

IF Major\_Axis\_Length = (203.33, 239.01]  $\land$  Eccentricity = (0.89, 0.9]  $\land$  Area = (12405.5, 13932.0]  $\implies$  Cammeo [0.001, 1.000]

IF Perimeter =  $(483.02, 548.45] \land \text{Minor\_Axis\_Length} = (86.34, 90.01] \land \text{Convex\_Area} = (12676.5, 14274.25] \land \text{Major\_Axis\_Length} = (185.63, 203.33] \implies \text{Cammeo} [0.001, 1.000]$  IF Eccentricity =  $(0.77, 0.87] \land \text{Convex\_Area} = (11627.75, 12676.5] \implies \text{Osmancik} [0.001, 1.000]$ 

$$\begin{split} & \text{IF Perimeter} = (426.42,\,448.66] \land \text{Minor\_Axis\_Length} = (86.34,\,90.01] \land \text{Major\_Axis\_Length} \\ & = (185.63,\,203.33] \implies \text{Osmancik} \; [0.001,\,1.000] \end{split}$$

IF Convex\_Area =  $(7722.99, 11627.75] \land \text{Area} = (11375.25, 12405.5] \implies \text{Cammeo} [0.001, 1.000]$ 

IF Major\_Axis\_Length =  $(174.46, 185.63] \land \text{Minor_Axis_Length} = (82.65, 86.34] \land \text{Eccentricity} = (0.89, 0.9] \land \text{Extent} = (0.64, 0.73] \land \text{Perimeter} = (426.42, 448.66] \implies \text{Osmancik} [0.001, 1.000]$ 

```
IF Perimeter = (483.02, 548.45] \land \text{Eccentricity} = (0.9, 0.95] \land \text{Major\_Axis\_Length} = (185.63, 203.33] \implies \text{Cammeo} [0.001, 1.000]
IF Major_Axis_Length = (203.33, 239.01] \land \text{Area} = (12405.5, 13932.0] \land \text{Extent} = (0.64, 0.73] \implies \text{Cammeo} [0.001, 1.000]
IF Major_Axis_Length = (174.46, 185.63] \land \text{Minor\_Axis\_Length} = (82.65, 86.34] \land \text{Eccentricity} = (0.89, 0.9] \land \text{Extent} = (0.73, 0.86] \implies \text{Osmancik} [0.001, 1.000]
IF Eccentricity = (0.9, 0.95] \land \text{Minor\_Axis\_Length} = (86.34, 90.01] \land \text{Extent} = (0.6, 0.64] \implies \text{Cammeo} [0.001, 1.000]
IF Eccentricity = (0.9, 0.95] \land \text{Convex\_Area} = (12676.5, 14274.25] \land \text{Area} = (11375.25, 12405.5] \implies \text{Cammeo} [0.001, 1.000]
IF * \implies \text{Osmancik} [0.204, 0.476]
```

## 2.4 Performance

In this section, we will briefly discuss the performance of the algorithm in the three datasets.

In Table 2.1 we can see how well the algorithm performs in the different datasets in terms of accuracy and training time. We can see that in all the datasets the best accuracy is between 70-80%, which is a fairly good result. However, the average accuracy is not so promising for the Rice dataset, which obtains a 53.5%. This could be due to the discretization step since all its features are numeric and we are grouping ranges of values in one category. Thus, it might be the case that two instances of different classes end up with the same feature values, leading to misclassifications.

In terms of time performance, we see how the greater the dataset the greater the time needed to train. One interesting thing is that the largest dataset needs less time to train than the medium one. This is probably due to two factors.

First, the Heart dataset has more features and different values per feature than the Rice dataset. This means that the number of selectors will be bigger in the former and that it will take more time to explore all the possible rules.

Second, it is possible that in the Rice dataset the algorithm can find rules surpassing the significance threshold more easily than in the Heart dataset. Thus, the algorithm will cover the whole set of examples faster than in the Heart dataset.

Table 2.1: Accuracy and training time for each dataset.

	Iris	Heart	Rice
Best accuracy	0.8	0.739	0.787
Avg. accuracy	0.767	0.701	0.535
Avg. training time (s)	3.152	72.048	28.972

## Chapter 3

## How to execute the code

## 3.1 Using the CN2 class

To create an instance of the CN2 class we can use the default parameters or we can specify the maximum star size, the significance threshold and seed used in the significance computation to make the results reproducible.

Once we have an instance of the algorithm we must call the fit method, which receives the training data without the labels, the labels, and the number of bins used in the discretization of numerical variables.

After training the algorithm we can use the **predict** method, which receives a set of examples without the labels and returns its predicted labels.

To obtain the ruleset we can access the rule\_list class attribute. Additionally, the CN2 class implements two methods to obtain the formatted rules. The print\_rules method displays the rules in the standard output and the save\_rules method, which receives a file name without the extension and a format (i.e. text or latex) and saves the rules in a folder named "results".

## 3.2 Using the runner script

To facilitate the testing of the algorithm the runner.py scrip is provided.

To run the test you need to create a python virtual environment and install in it the following dependencies:

```
pandas = "^1.4.1"
numpy = "^1.22.3"
scipy = "^1.8.0"
sklearn = "^0.0"
```

After the installation, you can run the test with the runner.py script.

WARNING: The runner.py must be in the same location that the source and data folders.

```
usage: runner.py [-h] [--short] [--medium] [--long] [--iterations ITERATIONS]
        [--seed SEED]
```

## optional arguments:

-h, --help show this help message and exit

--iterations ITERATIONS, -i ITERATIONS

number of times the algorithm is executed (default 5)

--seed SEED seed for reproducible results

#### Datasets:

By default all datasets are used

--short, -s run CN2 with short dataset
--medium, -m run CN2 with medium dataset
--long, -l run CN2 with long dataset