Ecuaciones de Lotka-Volterra para tres especies con salto y retardo

Versión 1

April 4, 2025

$$dx_1(t) = (x_1(t) - \beta x_1(t)x_2(t) - \delta x_1(t)x_3(t - \tau) - Ax_1(t)u_1(t))dt + \alpha_1 dW_1(t)$$

$$dx_2(t) = (x_2(t) - \beta x_2(t)x_1(t) - \epsilon x_2(t)x_3(t - \tau) - Bx_2(t)u_2(t))dt + \alpha_2 dW_2(t)$$

$$dx_3(t) = (-x_3(t) + \delta x_3(t - \tau)x_1(t) + \epsilon x_3(t - \tau)x_2(t) - Cx_3(t)u_3(t))dt + \alpha_3 dW_3(t)$$

con las condiciones:

$$x_1(t) = 0.7$$

 $x_2(t) = 0.7$
 $x_3(t) = 0.5, -\tau \le t \le 0$

$$\begin{array}{lll} dp_1(t) & = & \left(x_1(t) - p_1(t) + \beta p_1(t) x_2(t) + A p_1(t) u_1(t) + \beta p_2(t) x_2(t) + \delta p_1(t) x_3(t-\tau) - \delta p_3(t) x_3(t)\right) dt \\ & + & p_1(t) dW_1(t) \\ dp_2(t) & = & \left(x_2(t) - p_2(t) + \beta p_1(t) x_1(t) + \beta p_2(t) x_1(t) + B p_2(t) u_2(t) + \epsilon p_2(t) x_3(t-\tau) - \epsilon p_3(t) x_3(t)\right) dt \\ & + & p_2(t) dW_2(t) \\ dp_3(t) & = & \left(x_3(t) + p_3(t) + \delta p_1(t) x_1(t) + \epsilon p_2(t) x_2(t) + C p_3(t) u_3(t) - \epsilon p_3(t) x_2(t) - \delta p_3(t) x_1(t)\right) dt \\ & + & p_3(t) dW_3(t) \\ p_1(t) & = & 0.5 \\ p_2(t) & = & 0.5 \\ p_3(t) & = & 0.7, & T - \tau \leq t \leq T \end{array}$$

$$\begin{array}{rcl} u_1(t) & = & -p_1(t)x_1(t) \\ u_2(t) & = & -p_2(t)x_2(t) \\ u_3(t) & = & -p_3(t)x_3(t) \end{array}$$