

$$y_i \text{ (i=1,..., n)}$$

e4.1

$$y_i = x_i^{(1)}\beta_1 + ... + x_i^{(p)}\beta_p + \varepsilon_i$$

e4.2

$$\varepsilon \approx N(0,\sigma^2)$$

$$\begin{array}{l} x_i^{(1)},...,x_i^{(p)} \text{ (} p < n \\ \beta_1,...,\beta_p \\ \mathbf{x}_i = (x_i^{(1)},...,x_i^{(p)})' \\ \beta = (beta_1,...,\beta_p)' \end{array}$$

e4.3

$$y_i = \mathbf{x_i}'\beta + \varepsilon_i$$

e4.4

$$\begin{array}{l} E(y_i) = \mu_i = \mathbf{x_i}'\beta \\ Var(y_i) = \sigma^2 \end{array}$$

$$\mathbf{y} \equiv \left(\begin{array}{c} y_1 \\ \vdots \\ y_n \end{array} \right)$$

e4.6

$$\mathbf{X} \equiv \begin{pmatrix} x_1' \\ \vdots \\ x_n' \end{pmatrix} = \begin{pmatrix} x_1^{(1)} & x_1^{(2)} & \dots & x_1^{(p)} \\ \vdots & \vdots & \dots & \vdots \\ x_n^{(1)} & x_n^{(2)} & \dots & x_n^{(p)} \end{pmatrix} \equiv (\mathbf{x}^{(1)} \mathbf{x}^{(2)} \dots \mathbf{x}^{(p)})$$

e4.7

$$\mathbf{y} = \mathbf{X}\beta + \varepsilon$$

e4.8

$$\varepsilon \approx N_n(\mathbf{0}, \mathbf{R})$$

4.3 Offset

e4.9

$$y_i = x_i^{(0)} + x_i^{(1)}\beta_1 + \dots + x_i^{(p)}\beta_p + \varepsilon_i,$$

4.10

$$\mathbf{x}^{(0)} \equiv (x_1^{(0)}, \dots, x_n^{(0)})$$

4.4 Estimation

4.4.1 Ordinary Least Squares

4.11

$$\sum_{i=1}^n (y_i - \mathbf{x}_i' \beta)^2$$