

Ans 14 (a) let us consider a small elemental area ($dA = dx dy$) at a distance (x, y) from origin.

$$\therefore dF = \frac{G\sigma dx dy}{(x^2 + y^2 + z^2)^{3/2}}$$

$$F_z = \int dF \cos \theta = \iint \frac{G\sigma dx dy \cos \theta}{(x^2 + y^2 + z^2)^{3/2}}$$

$$\text{But } \cos \theta = \frac{z}{r} = \frac{z}{(x^2 + y^2 + z^2)^{1/2}}$$

$$\therefore F_z = \int_{-L/2}^{L/2} \int_{-L/2}^{L/2} \frac{G\sigma z dx dy}{(x^2 + y^2 + z^2)^{3/2}}$$

Proved.

