

Q.12a) 
$$I(\omega) = \frac{\hbar}{4\pi^2 c^2} \frac{\omega^3}{(e^{\hbar\omega/kT} - 1)}$$

Now 
$$W = \int_0^{\infty} I(\omega) d\omega.$$

change of variable.  $\Rightarrow \frac{\hbar\omega}{kT} = x.$

$\therefore \frac{\hbar d\omega}{kT} = dx.$

$d\omega = \left(\frac{kT}{\hbar}\right) dx$

$\omega^3 = \left(\frac{kT}{\hbar}\right)^3 x^3.$

Substituting we get

$$\int_0^{\infty} I(\omega) d\omega = \frac{\hbar (kT)^4}{4\pi^2 c^2 \hbar^3} \int_0^{\infty} \frac{x^3 dx}{e^x - 1}$$

Proved.