

CFG \leftrightarrow PDA

Tuesday, October 15, 2019

6:54 PM

under

CF G

V: variables, $S \in V$

Σ : terminals

R: production rules $\subseteq V \rightarrow (\Sigma \cup \Sigma)^*$.

PDA

Q: states $q_0 \in Q$, $F \subseteq Q$.

Σ : input alphabet

Γ : stack alphabet

δ : transition relation $Q \times \Gamma$

$Q \times \Sigma \times \Gamma \rightarrow 2^{\text{Q} \times \Gamma}$

$$\delta(q, a, b) = \{ (q_1, b_1), (q_2, b_2), \dots \}$$

input top of stack.

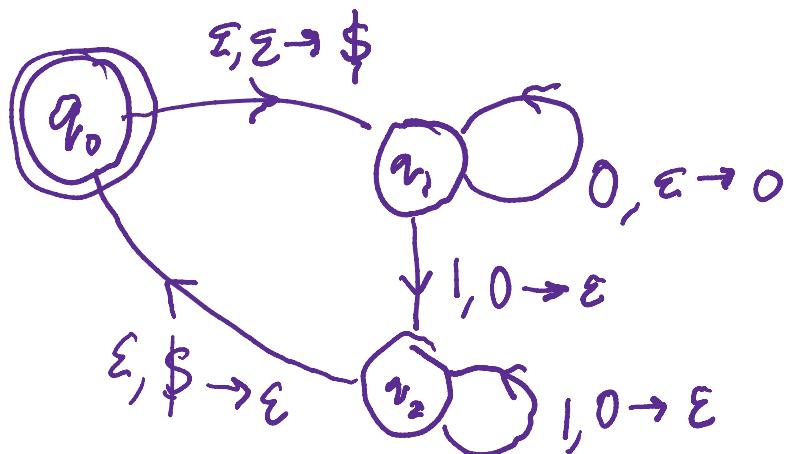
CF G for $(0^n 1^n)^*$

$$S \rightarrow SS$$

$$S \rightarrow \epsilon$$

$$S \rightarrow OS1$$

PDA:



Q. Is there always a PDA for a CFG and vice versa?

Given CFG, how to construct a PDA?

E.g.

$$S \rightarrow SS$$

input: (() (()))

$$S \rightarrow (S)$$

S

$$S \rightarrow \epsilon$$

(S)

(SS)

Q.1 At least in stack?

((S) S)

What to keep in stack?
 everything in current
 string to the right of
 (and including) first
 variable.

$((S) S)$
 $(() S)$
 $(() (S))$
 $(() ((S)))$
 $(() ((C)))$

- If top of stack is terminal, match with input.
- If _____ variable, apply rule

q_{start}

$\downarrow \epsilon, \epsilon \rightarrow \$$

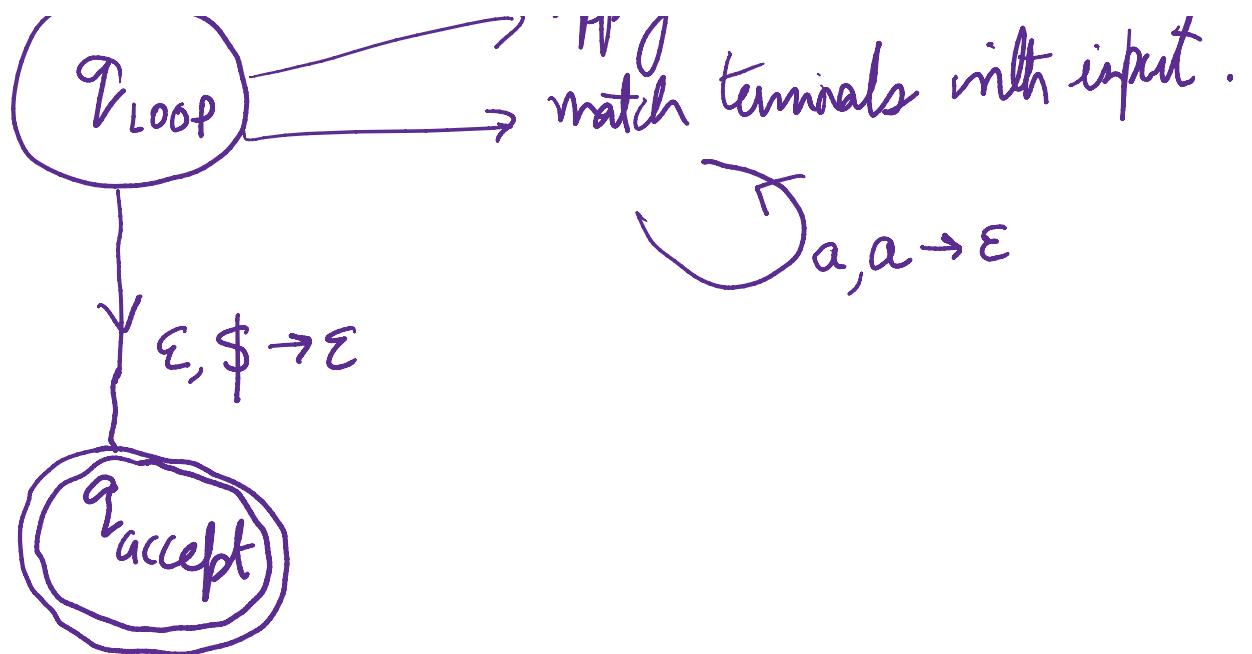
$\downarrow \epsilon, \epsilon \rightarrow S$

q_{final}

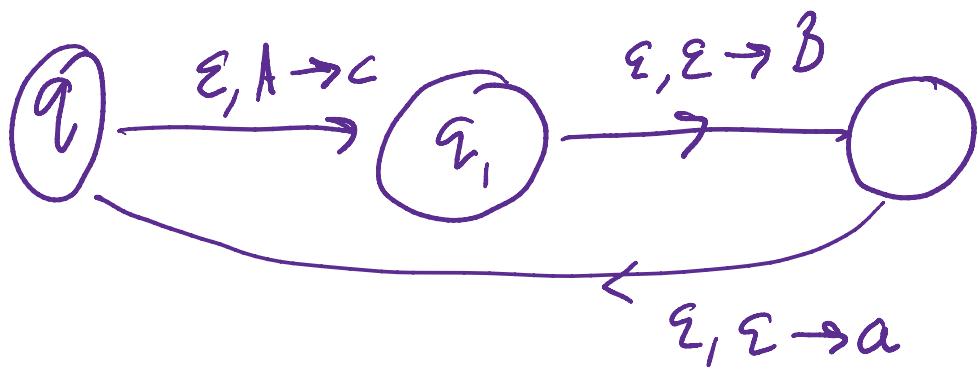
$A \rightarrow aBc$

$\epsilon, A \rightarrow aBc$

apply rules
 - match terminals with input.



$A \rightarrow aBC$



So, for "balanced parenthesis,"

