# foundation of machine learning

November 21, 2018

- 1 lab1
- 2 Q1

```
In [ ]: # hebbian learning with signum function.....
        import numpy as np
        x=np.matrix([[1,-2,1.5,0],[1,-.5,-2,-1.5],[0,1,-1,1.5]])
        w0=np.array([1,-1,0,.5])
        n = .05
        #err =np.matlib.zeros([1,3])
        eps=.001
        while(1):
            for i in range(0,2):
                net=np.dot(w0,x[i].T)
                y=np.sign(net)
                del_w=n*y*x[1]
                w_nxt=w0+del_w
                err=np.linalg.norm(w_nxt-w0)
                if(err<eps):</pre>
                    break
                w0=w_nxt
        print(w0)
```

- 3 output the code is not converging
- 4 Q2

### 5 output - the code is not converging

### 6 Q3

```
In [11]: # by perceptron learning with noise data.....
         import numpy as np
         x=np.array([[1,-2,0,-1],[0,-1.5,-0.5,-1.0],[-1,1,0.5,-1]])
         d=np.array([[-1],[-1],[1]])
         w0=np.array([1,-1,0,0.5])
         no_data_pts,tmp=np.shape(x)
         iteration=0
         while(1):
             iteration=iteration+1
             cont=0
             for i in range(0,3):
                 net=np.dot(w0,x[i].T)
                 y=np.sign(net)
                 r=d[i]-y
                 w_nxt=w0+r*x[i]
                 tmp=w_nxt-w0
                 err=np.linalg.norm(tmp)
                 if(err<.001):</pre>
                     cont=cont+1
                 w0=w nxt
             if(cont==no_data_pts):
                 break
         print(w0)
         print('iteration is {}'.format(iteration))
         noisy_data=np.array([1,-2,0,-1.5])
         y=np.sign(np.dot(w0.T,noisy_data))
         noisy_data=np.array([-1,1.2,0.5,-1.2])
         y1=np.sign(np.dot(w0.T,noisy_data))
```

```
[-1. 3. 0. 2.5] iteration is 2
```

## 7 output - it converge in 2 iteration

### 8 Q4

```
In []: #train a neuron in a xy plane by habbian rule.....
        import numpy as np
        x=np.matrix([[5,10],[1,3],[2,4],[5,1],[1,-3],[2,-4]])
        y=np.array([[1],[1],[1],[-1],[-1],[-1]])
        w0=np.matrix([1,-1])
        n = .05
        #err =np.matlib.zeros([1,3])
        eps=.001
        while(1):
            cnt=0
            for i in range(0,2):
                net=np.dot(w0,x[i].T)
                y=np.sign(net)
                del_w=n*y*x[1]
                w_nxt=w0+del_w
                err=np.linalg.norm(w_nxt-w0)
                if(err<eps):</pre>
                    cnt=cnt+1
                w0=w_nxt
            if(cnt==2):
                break
        print(w0)
```

## 9 the code is not converging

```
In []: # train the neuron by perceptron rule ......
import numpy as np
    x=np.matrix([[5,10],[1,3],[2,4],[5,1],[1,-3],[2,-4]])
    d=np.array([[1],[1],[1],[-1],[-1],[-1]])
    w0=np.matrix([1,-1])
    no_data_pts,tmp=np.shape(x)
    iteration=0
    n=1
    while(1):
        iteration=iteration+1
        cont=0
```

```
for i in range(0,no_data_pts):
                net=np.dot(w0,x[i].T)
                y=np.sign(net)
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                if(err<.001):</pre>
                    cont=cont+1
                w0=w_nxt
            if(cont==no_data_pts):
                break
        print(w0)
        print('number of iteration is {}'.format(iteration))
10 OUTPUT= W0=[[-9 15]
    number of iteration is 3
11
12
    lab 2
13 O1
In [ ]: #single discrete perceptron training algorithm keeping eta=1
        import numpy as np
        x=np.matrix([[0.8,0.5,0],[0.9,0.7,0.3],[1,0.8,0.5],[0,0.2,0.3],[0.2,0.1,1.3],[0.2,0.7,0.3]
        d=np.array([[1],[1],[1],[-1],[-1],[-1]])
        w0=np.array([0,0,0])
        no_data_pts,tmp=np.shape(x)
        iteration=0
        n=1# ete=1
        while(1):
            iteration=iteration+1
            cont=0
            for i in range(0,no_data_pts):
                net=np.dot(w0,x[i].T)
                y=np.sign(net)
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                if(err<.001):
                    cont=cont+1
```

```
w0=w_nxt
if(cont==no_data_pts):
    break
print(w0)
print(iteration)
```

- 14 output
- 15 W0=[[ 0.8 0.1 -0.6]]
- 16 number of iteration=12
- 17 Q2

```
In [ ]: #delta learning rule for a single contineous perceptron......
        import numpy as np
        x=np.matrix([[0.8,0.5,0],[0.9,0.7,0.3],[1,0.8,0.5],[0,0.2,0.3],[0.2,0.1,1.3],[0.2,0.7,0.3]
        d=np.array([[1],[1],[1],[-1],[-1],[-1]])
        w0=np.array([0,0,0])
        no_data_pts,tmp=np.shape(x)
        iteration=0
        n=.001#eta=.001
        while(1):
            iteration=iteration+1
            cont=0
            for i in range(0,no_data_pts):
                net=np.dot(w0,x[i].T)
                y=1/(1+np.exp(-net))
                dy=0.5*(1-y**2)
                r=d[i]-y
                w_nxt=w0+n*r*dy*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                if(err<.001):</pre>
                    cont = cont + 1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cont==no_data_pts):
                break
        print(w0)
        print(iteration)
```

- 18 output is =  $w0=[[0.84816134\ 0.52973658\ -0.00122033]]$
- 19 number of iteration is 6
- 20 Q3

```
In [ ]: #WIDROW-HOFF LEARNING ALGORITHM.....
        import numpy as np
        x=np.matrix([[1,2],[1,-1],[-1,2],[-2,-1]])
        d=np.array([[-1],[1],[1],[-1]])
        w0=np.array([0.1,-0.3])
        no_data_pts,tmp=np.shape(x)
        n=0.001
        iteration=0
        while(1):
            cnt=0
            for i in range(0,no_data_pts):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                r=d[i]-net
                w0_nxt=w0+n*r*x[i]
                tmp=w0_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w0_nxt/np.linalg.norm(w0_nxt)
            if(cnt==no_data_pts):
                break
        print(w0)
        print(iteration)
```

- 21 output is w0=[[ 0.70574373 -0.70846721]]
- 22 number of iteration is 4
- 23 LAB 3
- 24 q1- AND operation

```
In [1]: #and operation bipolar input by perceptron learning
    import numpy as np
    x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
    d=np.array([[1],[-1],[-1],[-1]])
```

```
w0=np.array([0.5,-0.5])
        n = .002
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                y=1/(1+np.exp(-net))
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
0.0014142135623730963
0.00510369660012198
0.0033815847870624803
0.0042406372076714705
[[ 0.71150818 -0.70267782]]
In [2]: #AND operation by signum function using widrow-hoff learning rule
        import numpy as np
        x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
        d=np.array([[1],[-1],[-1],[-1]])
        w0=np.array([0.5,-0.5])
        n=.002
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                r=d[i]-net
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
```

```
err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
0.0028284271247461927
0.006828395125130148
0.0011715404341103351
0.0028122983536799876
[[ 0.71192993 -0.70225051]]
In [4]: #input AND operation using signum function done by perceptron learning
        import numpy as np
        x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
        d=np.array([[1],[-1],[-1],[-1]])
        w0=np.array([0.5,-0.5])
        n=.002
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                y=np.sign(net)
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:</pre>
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
```

```
0.005656854249492385
0.0
0.0
[[ 0.70994556 -0.70425656]]
```

### 25 OR operation

```
In [5]: #OR operation bipolar input by perceptron learning
        import numpy as np
        x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
        d=np.array([[1],[1],[1],[-1]])
        w0=np.array([0.5,-0.5])
        n=.004
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                y=1/(1+np.exp(-net))
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
0.0028284271247461927
0.0011063228501433527
0.004550531421590335
0.008477253770786631
[[ 0.71588352 -0.69821972]]
4
In [6]: #or operation bipolar input by widrow-hoff learning
        import numpy as np
        x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
```

```
d=np.array([[1],[1],[1],[-1]])
        w0=np.array([0.5,-0.5])
        n = .002
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                r=d[i]-net
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
0.0028284271247461927
0.0011715408756377626
0.0068283950500208496
0.002812298353674021
[[ 0.71192993 -0.70225051]]
```

## 26 xor operation

```
net=np.dot(w0,x[i].T)
                y=1/(1+np.exp(-net))
                r=d[i]-y
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
                break
        print(w0)
        print(iteration)
0.008485281374238578
0.0011064033924073154
0.004550451057256001
0.008509362117028373
[[ 0.7046052 -0.70959954]]
In [9]: #xor operation bipolar input by widrow-hoff learning rule
        import numpy as np
        x=np.matrix([[1,1],[1,-1],[-1,1],[-1,-1]])
        d=np.array([[-1],[1],[1],[-1]])
        w0=np.array([0.5,-0.5])
        n = .002
        iteration=0
        col,tmp=np.shape(x)
        while(1):
            cnt=0
            for i in range(0,col):
                iteration=iteration+1
                net=np.dot(w0,x[i].T)
                r=d[i]-net
                w_nxt=w0+n*r*x[i]
                tmp=w_nxt-w0
                err=np.linalg.norm(tmp)
                print(err)
                if err<10**-2:
                    cnt=cnt+1
                w0=w_nxt/np.linalg.norm(w_nxt)
            if(cnt==col):
```

```
break
       print(w0)
       print(iteration)
0.0028284271247461927
0.0011715408756377626
0.0068283950500208496
0.0028445558958183643
[[ 0.70626649 -0.70794607]]
27
   lab-6
In [10]: #lab=6.....
        import numpy as np
        my_data=np.array(('heli.csv','plane.csv','tank.csv'))
        w=np.zeros((144,144))
        image=[]
        for i in range(0,3):
            data=np.genfromtxt(my_data[i],delimiter=",")
            tmp=data.flatten()
            pattern=np.matrix(tmp)
             image.append(pattern)
            tmp=np.outer(pattern,pattern)
            w=w+tmp
         #Recall equation
        data=np.genfromtxt('testdata.csv',delimiter=",")
        input_pattern=data.flatten()
        no_clm=np.shape(input_pattern)[0]
        tmp1=np.matmul(input_pattern,w)
        y=np.sign(tmp1)
        for i in range(0,no_clm):
            if (y[i]==0):
                y[i]=input[i]
        dist_list=[]
        for i in range(0,3):
            sub=abs(y-image[i])
            dist=np.sum(sub)
            dist_list.append(dist)
        indx=dist_list.index(min(dist_list))
        print(indx)
```

1

## 28 output is helicopter

#### 29 lab 5

```
In [11]: # lab=5.....
                             import numpy as np
                              \#filename=np.array(('zero.csv', 'one.csv', 'two.csv', 'three.csv', 'four.csv', 'five.csv', 'five.csv
                             my_data=np.array(('four.csv','five.csv','six.csv','seven.csv','eight.csv','nine.csv')
                             w=np.zeros((35,35))
                             input_pattern=np.zeros((10,35))
                             n=6
                             img_arr=[]
                             for i in range(0,n):
                                          data=np.genfromtxt(my_data[i],delimiter=",")
                                          tmp=data.flatten()
                                          input_pattern[i]=tmp
                                          pattern=np.matrix(tmp)
                                          img_arr.append(pattern)
                                          tmp=np.outer(pattern,pattern)
                                          w=w+tmp
                                          #Recall equation
                             for k in range (0,n):
                                          no_clm=np.shape(input_pattern[k])[0]
                                          tmp1=np.matmul(input_pattern[k],w)
                                          y1=np.sign(tmp1)
                                          for i in range(0,no_clm):
                                                       if (y1[i]==0):
                                                                    y1[i]=input[i]
                                          dist_list=[]
                                          for i in range(0,n):
                                                       sub=abs(y1-img_arr[i])
                                                       dist=np.sum(sub)
                                                       dist_list.append(dist)
                                          indx=dist_list.index(min(dist_list))
                                          print(indx)
0
1
2
3
4
5
In [13]: import numpy as np
                             w=np.zeros((70,70))
```

```
img=[]
         input_pattern=np.zeros((5,70))
         my_data=np.array(('A.csv','B.csv','C.csv','D.csv','E.csv'))
         for i in range(0,5):
             data=np.genfromtxt(my_data[i],delimiter=",")
             tmp=data.flatten()
             input_pattern[i]=tmp
             pattern=np.matrix(tmp)
             img.append(pattern)
             tmp=np.outer(pattern,pattern)
             w=w+tmp
          #Recall
         for k in range (0,5):
             x=np.shape(input_pattern[k])[0]
             mem=np.matmul(input_pattern[k],w)
             y=np.sign(mem)
             for i in range(0,x):
                 if (y[i]==0):
                     y[i]=input_pattern[k][i]
             dist_list=[]
             for i in range(0,5):
                 diff=np.abs(y[i]-img[i])
                 dist=np.sum(diff)
                 dist_list.append(dist)
             indx=dist_list.index(min(dist_list))
             print(indx)
3
3
3
3
3
    OUTPUT = index is 3
30
31
    lab 8
32
    Q1
In [12]: import numpy as np
         w=np.zeros((144,120))
         A_vector=[]
         B_vector=[]
```

```
a=np.array(('heli.csv','plane.csv','tank.csv'))
b=np.array(('three.csv','one.csv','two.csv'))
for i in range(0,3):
    data a=np.genfromtxt(a[i],delimiter=",")
    data_b=np.genfromtxt(b[i],delimiter=",")
    tmp=data a.flatten()
    pattern_a=np.array(tmp)
    A_vector.append(pattern_a)
    tmp2=data_b.flatten()
    pattern_b=np.array(tmp2)
    B_vector.append(pattern_b)
    tmp=np.outer(pattern_a,pattern_b)
    w=w+tmp
#Recall equation
data=np.genfromtxt('testdata.csv',delimiter=",")
x=data.flatten()
tmp1=np.matmul(x,w)
new B=np.sign(tmp1)
new B[new B==0] = 1
first time=0
iteration=0
limit_pts=[]
while(1):
    iteration=iteration +1
    for i in range (0,3):
        if(new_B==B_vector[i]).all():
            print("Value corresponding to pattern index - :",i)
            break
    if(first_time !=0):
        if any((new_B == x).all() for x in limit_pts):
            #print('Limit pt...')
            break
    else:
        first_time=1
    limit pts.append(new B)
    tmp2=np.matmul(new_B,w.T)
    update_A=np.sign(tmp2)
    update_A[update_A==0] = x[update_A==0]
    new_A=update_A
    tmp1=np.matmul(new_A,w)
    B=new_B
    new_B=np.sign(tmp1)
    new_B[new_B==0] = B[new_B==0]
print(iteration)
```

-----

Value corresponding to pattern index -: 1 Value corresponding to pattern index -: 1

#### 33 Q2

```
In [7]: import numpy as np
        weight_vector=np.zeros((5,4))
        A_vector=[]
        B_vector=[]
        def compute_hamming_dist(u,v):
            tmp=abs(u-v)
            dist=np.sum(tmp)
            return dist
        def transfer_func(weight_vector,input):
            global A_vector,B_vector
            limit_pts=[]
            new_A=input
            tmp1=np.matmul(input,weight_vector)
            new_B=np.sign(tmp1)
            new_B[new_B==0] = -1
            first_time=0
            iteration=0
            while(1):
                for i in range (0,2):
                    if(new_B==B_vector[i]).all():
                        print("Value corresponding to pattern - :",i)
                        print("iterations=",iteration)
                        print("hammind dist from 0-",compute_hamming_dist(new_B,B_vector[0]))
```

```
print("hammind dist from 1-",compute_hamming_dist(new_B,B_vector[1]))
                return
        if(first_time !=0):
            if any((new_B == x).all() for x in limit_pts):
                print("iterations=",iteration)
                print('Limit pt...')
                print("hammind dist from 0-",compute_hamming_dist(new_B,B_vector[0]))
                print("hammind dist from 1-",compute_hamming_dist(new_B,B_vector[1]))
                return
        else:
            first\_time=1
        limit_pts.append(new_B)
        tmp2=np.matmul(new_B,weight_vector.T)
        update_A=np.sign(tmp2)
        update_A[update_A==0] = new_A[update_A==0]
        new_A=update_A
        tmp1=np.matmul(new_A,weight_vector)
        B=new_B
        new_B=np.sign(tmp1)
        new B[new B==0] = B[new B==0]
        iteration=iteration +1
a1 = np.matrix([0, 1, 0, 1, 0])
a2 = np.matrix([1, 1, 0, 0, 0])
b1 = np.matrix([1, 0, 0, 1])
b2 = np.matrix([0, 1, 0, 1])
a1[a1 == 0] = -1
a2[a2 == 0] = -1
b1[b1 == 0] = -1
b2[b2 == 0] = -1
A_vector.append(a1)
B_vector.append(b1)
tmp=np.outer(a1,b1)
weight_vector=weight_vector+tmp
A_vector.append(a2)
B_vector.append(b2)
tmp=np.outer(a2,b2)
weight_vector=weight_vector+tmp
input_pattern=np.array([-1,1,1,1,-1])
transfer_func(weight_vector,input_pattern)
input_pattern=np.array([-1,-1,1,1,-1])
transfer_func(weight_vector,input_pattern)
```

```
Value corresponding to pattern - : 0 iterations= 0 hammind dist from 0- 0.0 hammind dist from 1- 4.0 iterations= 1 Limit pt... hammind dist from 0- 4.0 hammind dist from 1- 8.0
```

#### 34 LAB 9

```
In [8]: import numpy as np
        weight_vector=np.zeros((15,10))
        A_vector=[]
        B_vector=[]
        def transfer_func(weight_vector,input):
            global A_vector,B_vector
            limit_pts=[]
            new_A=input
            tmp1=np.matmul(input,weight_vector)
            new_B=np.sign(tmp1)
            new_B[new_B==0] = 1
            first time=0
            iteration=1
            while(1):
                for i in range (0,4):
                    if(new_B==B_vector[i]).all():
                        print("Value corresponding to pattern index - :",i)
                        print("Number of iterations",iteration)
                        return
                if(first_time !=0):
                    if any((new_B == x).all() for x in limit_pts):
                        print('Limit pt...')
                        print("Number of iterations",iteration)
                        return
                else:
                    first\_time=1
                limit_pts.append(new_B)
                tmp2=np.matmul(new_B,weight_vector.T)
                update_A=np.sign(tmp2)
```

```
update_A[update_A==0] = new_A[update_A==0]
              new_A=update_A
              tmp1=np.matmul(new_A,weight_vector)
              B=new_B
              new_B=np.sign(tmp1)
              new_B[new_B==0] = B[new_B==0]
              iteration=iteration +1
       data_a=np.genfromtxt('input_data.csv',delimiter=",")
      data_b=np.genfromtxt('output_data.csv',delimiter=",")
       for i in range (0,4):
          A_vector.append(data_a[i])
          B_vector.append(data_b[i])
          tmp=np.outer(data_a[i],data_b[i])
          weight_vector=weight_vector+tmp
       transfer_func(weight_vector,input_pattern)
Limit pt...
Number of iterations 3
```