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package myMath;

import java.util.Iterator;

/** This interface represents a simple function of type  $y=f(x)$ , where both  $y$ 
and  $x$  are real numbers.
**/
public interface function {
    public double f(double x);
}

* The interface represents a continuance function.
public interface cont_function extends function{
    /**
    * Compute a Riman's integral from  $x_0$  to  $x_1$  in eps steps.
    * @param  $x_0$  starting pooint
    * @param  $x_1$  end point
    * @param eps positive step value
    * @return the approximated area above X-axis below this function
    bounded in the range of  $[x_0, x_1]$ 
    */
    public double area(double  $x_0$ , double  $x_1$ , double eps);
}

* Does the sorting process, using the equation
public class Monom_Comperator implements Comparator<Monom> {

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* This class represents a simple "Monom" of shape  $a \cdot x^b$ , where a is a real
number and a is an integer (summed a none negative),
* see: https://en.wikipedia.org/wiki/Monomial
* The class implements function and support simple operations as:
construction, value at x, derivative, add and multiply.
* @author Raam Banin
* @version 1.0
*/
public class Monom implements function{

    private double _coefficient; //
    private int _power;
    private static Monom init_from_string = null;

    /**
     * Define string with non-capital letter. define two variables. if the
     string is empty return error message. Define index = x
     * if x = -1 return a= string, else a is a * x and b= 1 define p_power
     as power index. if p_power is real so b is all the numbers after the
     power.
     * @param s - get monom in string.
     * @return - return a new monom.
     */
    private Monom init_from_string(String s)

    /**
     * create a new monom according to string and get it in to the original
     monom.
     * @param s - monom in the string
     */
    public Monom(String s)

    /**
     * constructor with parameterized.
     * @param a - coefficient.
     * @param b - power.
     */
    public Monom(double a, int b)

    /**
     * copy constructor
     * @param ot - copy parameterized
     */
    public Monom(Monom ot)

    /**
     * The function return the y value if the power is not negative.
     */
    public double f(double x)

    /**
     * Monom derivative - if power is 0 return 0, else do power * monom
     coefficient and -1 from monom power.
     * @return new monom after a derived method.
     */
    public Monom derivative()

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/**
 * addition between two monom. if powers of the monoms is equal sum the
monoms coefficients.
 * @param m - the monom we want to add.
 */
public void add(Monom m)

/**
 * subtraction between two monom - if the monoms coefficients are equal
subtract between the monoms.
 * @param m - the monom we want to subtract.
 */
public void subtract(Monom m)

/**
 * multiply between two monoms and sum the powers.
 * @param m - the monom we want to multiply.
 */
public void multiply(Monom m)

/**
 * comparison between two monoms - if the monom is not empty and the
coefficients are equal
and the powers are equals as well so the monoms are equal.
 * @param m - the monom we want to make comparison.
 * @return - if equal or no.
 */
public boolean equals(Monom m)

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/**
 * This interface represents a general Polynom:  $f(x) = a_1x^{b_1} + a_2x^{b_2} + \dots + a_nx^{b_n}$ ,
 * where:  $a_1, a_2 \dots a_n$  are real numbers and  $b_1 < b_2 < \dots < b_n \geq 0$  are none
negative integers (naturals)
 * For formal definitions see: https://en.wikipedia.org/wiki/Polynomial
 *
 * Such polygon has the following functionality:
 * 1. Init:
 * 1.1 Init(String)
 * 1.2 Init() // zero Polygon
 * 1.3 Polynom copy() // deep copy semantics
 *
 * 2. Math:
 * 2.1 void add(Polygon p) // add p to this Polynom
 * 2.2 void subtract(Polygon p) // subtract p from this Polygon
 * 2.3 void multiply(Polygon p) // multiply this Polygon by p
 *
 * 3. Utils
 * 3.1 isZero()
 * 3.2 Polynom derivative() // returns a new Polygon of the derivative
("NIGZERET").
 * 3.3 double f(x) // return this Polygon value at p(x)
 * 3.4 boolean equals(Polygon p) // returns true iff for any x: this.f(x) ==
p.f(x)
 * 3.5 double root(double x0, double x1, double eps) // assuming
(f(x0)*f(x1)<=0, returns f(x2) such that:
 *
//      (i)  $x_0 \leq x_2 \leq x_1$  & (ii)  $|f(x_2)| < \epsilon$ 
 * 3.6 String toString() // returns a String such that it can be used for init
an equal(s) Polygon.

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public interface Polynom_able extends cont_function{
    /**
     * Add p1 to this Polynom
     * @param p1
     */
    public void add(Polynom_able p1);
    /**
     * Add m1 to this Polynom
     * @param m1 Monom
     */
    public void add(Monom m1);
    /**
     * Subtract p1 from this Polynom
     * @param p1
     */
    public void substract(Polynom_able p1);
    /**
     * Multiply this Polynom by p1
     * @param p1
     */
    public void multiply(Polynom_able p1);
    /**
     * Test if this Polynom is logically equals to p1.
     * @param p1 - other polynom.
     * @return true iff this polynom represents the same function ans p1
     */
    public boolean equals (Polynom_able p1);
    /**
     * Test if this is the Zero Polynom
     * @return Boolean true or false.
     */
    public boolean isZero();
    /**
     * Compute a value  $x'$  ( $x_0 \leq x' \leq x_1$ ) for with  $|f(x')| < \text{eps}$ 
     * assuming  $(f(x_0) * f(x_1) \leq 0)$ , returns  $f(x_2)$  such that:
     * * (i)  $x_0 \leq x_2 \leq x_1$  && (ii)  $f(x_2) < \text{eps}$ 
     * @param x0 starting point
     * @param x1 end point
     * @param eps step (positive) value
     * @return The resulting approximation of the root according to epsilon
     */
    public double root(double x0, double x1, double eps);
    /**
     * create a deep copy of this Polynom
     * @return polynom.
     */
    public Polynom_able copy();
    /**
     * Compute a new Polynom which is the derivative of this Polynom
     * @return derivative polynom.
     */
    public Polynom_able derivative();
    /**
     * Compute Riemann's Integral over this Polynom starting from x0 till
     x1 using eps size steps,

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    * see: https://en.wikipedia.org/wiki/Riemann\_integral
    * @return the approximated area above the x-axis below this Polynom and
    between the [x0,x1] range.
    */
    public double area(double x0,double x1, double eps);
    /**
    * @return an Iterator (of Monoms) over this Polynom.
    */
    public Iterator<Monom> iteretor();
}

```