

## Number system

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+ Binary to decimal =  $\times 2$

Binary to octal

001101101.101100

Octal equivalent of binary value

001      101      100  
421      421      421

now representing above binary value into octal

$$(001101101.101100)_2 = (155.54)_8$$

# Binary to Hexadecimal

$$A=10, B=11, C=12, D=13$$

$$E=14, F=15$$

00101101.1011000

8 4 2 1

0 0 1 0  $\rightarrow 2$

1 1 - 1 0 1  $\rightarrow 8 + 4 + 1 = 13 = E$

1 0 1 1  $\rightarrow B$

1 0 0 0 - 8

$$(00101101.1011000)_2 = (2B.E8)_{16}$$

1011011.1101010

converting into decimal

$$\begin{aligned} &= 1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} \\ &+ 1 \times 2^{-4} + 0 \times 2^{-5} + 1 \times 2^{-6} + 1 \times 2^{-7} + 0 \times 2^{-8} \end{aligned}$$

$$= 64 + 0 + 16 + 8 + 0 + 2 + 1 + \frac{1}{2} + \frac{1}{4} + 0 + \frac{1}{8} + 0 + \frac{1}{16} + 0 + \frac{1}{32}$$

$$= 91.769$$

## Converting into octal

001011011.110101100

4 2 1

0 0 1 → 1

0 1 1 → 3

1 1 0 → 6

1 0 1 → 5

1 0 0 → 4

001 → 1

011 → 3

110 → 6

101 → 5

100 → 4

now, representing above binary into octal

$$(001011011.110101100)_2 = (133.654)_8$$

## Hexadecimal

01011011.11010110

0101	1011	1101	0110
8421	8421	8421	8421
5	11 → B	13 → D	6

now, representing above binary into hexadecimal.

$$(1011011.11010110)_2 = (5B.D6)_{16}$$

\*  $(567.348)_8 = (?)_{16}$

Converting octal into binary

5	6	7	3	4	6
421	421	421	421	421	421
101	110	111	011	100	110

Here

$$(567.348)_8 (1011011.01100110)_2$$

now,

$$\begin{array}{r}
 0001 \\
 8421
 \end{array}
 \quad
 \begin{array}{r}
 0111 \\
 8421
 \end{array}
 \quad
 \begin{array}{r}
 0011 \\
 8421
 \end{array}$$

3 7 3

Representing binary into hexadecimal.

$$(101110111.011100110)_2 = (177.73)_{16}$$

$$(567.348)_8 = (177.73)_{16}$$

$$+ (BFA.9BC)_{16} = (?)_8$$

$$\begin{array}{r}
 B \quad f \quad n \\
 11 \quad 15 \quad 10 \\
 8421 \quad 8421 \quad 8421 \\
 1011 \quad 1111 \quad 1010
 \end{array}$$

$$\begin{array}{r}
 9 \quad B \quad C \\
 8421 \quad 8421 \quad 8421 \\
 1001 \quad 1011 \quad 1100
 \end{array}$$

Here,  $(BFA.9BC)_{16} = (10111111.1010 \cdot 10011011100)_2$   
converting binary into octal.

$$\begin{array}{r}
 101 \quad 111 \quad 101 \quad 100 \quad 110 \\
 421. \quad 421 \quad 421 \quad 421 \quad 421 \\
 5 \quad 7 \quad 6 \quad 4 \quad 6
 \end{array}$$

now,

Representing binary value into octal.

$$\begin{aligned}
 (101111101101.100111100)_2 &= (5772.4674)_{16} \\
 (BFA.9BC)_{16} &= (5772.4674)_8
 \end{aligned}$$

## Decimal to Binary

$$(986.625)_{10} - (?)_2$$

SOL:

	2   986 → 0	↑ Decimal value	operational value	Result	integer
2   493 → 1.					
2   246 → 0.		0.625	0.625 × 2	1.25	1
2   123 → 1.		0.25	0.25 × 2	0.5	0
2   61 → 1.		0.5	0.5 × 2	1.0	1
2   30 → 0.					
2   15 → 1.					
2   7 → 1.					
2   3 → 1					

$$(986.625)_{10} = (1111011010)_2$$

decimal into octal

$$986.625$$

	8   986 → 2	↑ Decimal value	operation value	Result	integer
8   123 → 3					
8   15 → 7		0.625	0.625 × 8	5	5

$$(986.625)_{10} = (1732.5)_8$$

## Decimal to Hexadecimal

$$\begin{array}{r} 16 | 986 - 10 \\ 16 | 61 - 13 \\ \hline & 3 \end{array}$$

Decimal value	operational value	Result integer
0.625	$0.625 \times 16$	(0.8P·1A)H A

$$(986.625)_{10} = (38A.A)_{16}$$

\*  $(735.674)_8 = (?)_{10}$

Sol:

$$\begin{aligned}
 &= 7 \times 8 + 3 \times 8^1 + 5 \times 8^0 + 6 \times 8^{-1} + 7 \times 8^{-2} + 4 \times 8^{-3} \\
 &= 448 + 24 + 5 + 6/8 + 7/64 + 4/512 \\
 &= 477 + 0.75 + 0.10 + 0.0078 \\
 &= 477.85
 \end{aligned}$$

\*  $(AC9.2B)_{16} = (?)_{10}$

$$A = 10$$

$$C = 12$$

$$9$$

$$D = 15$$

$$B = 12$$

Here,

$$10 \times 16^2 + 12 \times 16^1 + 9 \times 16^0 + 15 \times 16^{-1} + 12 \times 16^{-2}$$

$$= 2560 + 192 + 9 + 15/16 + 12/256$$

$$= 2761 + 0.9375 + 0.046$$

$$= 2761.9835$$

1's complement

$$1011 - 0101$$

1's complement of 0101 = 1010

Adding it with 1011 = 101010

So, removing the carry and adding it with remaining.

$$\begin{array}{r} 0101 \\ + 1 \\ \hline 0110 \end{array}$$

∴ Difference is  $(0110)_2$

Subtract 1011 from 0101

1's complement of 1011 = 0100  
+ 0101

Adding it with 0101 = 0100.

$$\begin{array}{r} 0101 \\ + 0101 \\ \hline 1001 \end{array}$$

now, we do not have extra bit,

so

difference - 1's complement of result  
= -(0110)

$$+ 1011 \cdot 010 - 1000 \cdot 101$$

So

1's complement of 1000 · 101 = 0111 · 010

Adding it with 1011 · 010 = 0111 · 010

$$\begin{array}{r} 1011 \cdot 010 \\ + 0111 \cdot 010 \\ \hline 10010 \cdot 100 \end{array}$$

So, removing the carry and add it with remaining

$$\begin{array}{r} 0010 \cdot 100 \\ + 0010 \cdot 101 \\ \hline 0010 \cdot 111 \end{array}$$

Difference is  $(0010 \cdot 101)_2$

$\bar{1}$ 's complement of  $1011 \cdot 010$  is  $0100 \cdot 101$

$$\begin{array}{r} \text{Adding it with } 1000 \cdot 101 \\ + 0100 \cdot 101 \\ \hline 101 \cdot 010 \end{array}$$

Here, we don't have extra bit.

Hence

$$\begin{aligned} \text{Difference} &= -\bar{1}'\text{'s complement of result} \\ &= -(0010 \cdot 101) \end{aligned}$$

#  $1011 - 0101$

$$1\text{'s component of } 0101 = 1010$$

$$2\text{'s component of } 0101 = \overline{1010} + 1$$

$$\begin{array}{r} \text{Adding it with } 1011 - \\ 1011 \\ + 1011 \\ \hline 10110 \end{array}$$

Here we have carry so removing the carry  
difference is  $0110$

1)  $1011 \cdot 010$

$$1000 \cdot 101$$

So,

$$1\text{'s component of } 1000 \cdot 101 = 0111 \cdot 010$$

$$2\text{'s component of } 1000 \cdot 101 = 0111 \cdot 010 + 1$$

$$\underline{0111 \cdot 011}$$

$$\begin{array}{r} \text{Adding it with } 1011 \cdot 010 = \\ 0111 \cdot 011 \\ + 1011 \cdot 010 \\ \hline 1011011 \end{array}$$

so removing the extra bit and difference is 0010.10

is component of 10110.010 = 0100.101

2's component of 10110.010 = 0100.101

$$0100 \cdot 110$$

Adding it with 1000.101

$$1000 \cdot 101$$

$$1101 \cdot 011$$

Here we don't have extra bit

So,

$$\begin{aligned} \text{different} &= -2\text{'s complement} \\ &= -(1101 \cdot 011) \end{aligned}$$

$$101 \cdot 11 - 100 \cdot 01$$

SOL:

$$1\text{'s complement of } 100 \cdot 01 = 011 \cdot 10$$

Adding it with 101.11

$$\begin{array}{r} 101 \cdot 11 \\ + 011 \cdot 10 \\ \hline 1001 \cdot 01 \end{array}$$

So removing extra bit and adding with remaining

$$\begin{array}{r} 001 \cdot 01 \\ + 1 \\ \hline 001 \cdot 10 \end{array}$$

$$\text{Difference} = (001 \cdot 10)_2$$

$$101 \cdot 11 - 100 \cdot 01$$

$$1's \text{ complement} = 0 \ 11 \cdot 10$$

$$2's \text{ complement} = 0 \ 11 \cdot 10$$

$$\begin{array}{r} & +1 \\ 011 \cdot 10 & \hline 011 \cdot 11 \end{array}$$

Adding it with 101.11

$$\begin{array}{r} 0 \ 11 \cdot 11 \\ 1 \ 01 \cdot 11 \\ \hline 100 \cdot 11 \cdot 10 \end{array}$$

So removing the extra bit and difference is

$$001 \cdot 10$$

$$+ 100 \cdot 01 - 101 \cdot 11$$

Soly

$$1's \text{ complement of } 101 \cdot 11 = 010 \cdot 11$$

$$\begin{array}{r} & +1 \\ 010 \cdot 11 & \hline 011 \cdot 10 \\ 100 \cdot 01 & \hline 111 \cdot 00 \end{array}$$

Here we don't have extra bit

$$\begin{aligned} \text{Hence, Difference} &= - 1's \text{ complement of result} \\ &= -(000 \cdot 11)_2 \end{aligned}$$

$$1010 \cdot 110 - 1100 \cdot 101$$

Soly

$$1's \text{ complement of } 1100 \cdot 101 = 0011 \cdot 010$$

$$\text{Adding it with } 1010 \cdot 110 = 0011 \cdot 010$$

$$\begin{array}{r} 1010 \cdot 110 \\ \hline 1110 \cdot 000 \end{array}$$

We don't have extra bit  
 Hence, difference = - 1's complement of result  
 $= -(0001.111)_2$

$$1^{\text{st}}$$
 complement of  $1100.101 = 011.010$

$$2^{\text{nd}}$$
 complement of  $0011.010 = 0011.010$

$$\begin{array}{r} +1 \\ 0011.011 \end{array}$$

$$\text{Adding it with } 1010.110 = \begin{array}{r} 0011.011 \\ 1010.110 \\ \hline 1110.001 \end{array}$$

We don't have extra bit

$$1^{\text{st}}$$
 component =  $0001.110$

$$2^{\text{nd}}$$
 component  $\begin{array}{r} 0001.110 \\ +1 \\ \hline 0001.111 \end{array}$

For + value 1 write the binary value of it  
 $+8 = 1000$

Add 0 in remaining slot to make it of 8 bit  
 for - value (-1) write the binary of it.  
 $-8 = 10000$

$$1^{\text{st}}$$
 complement  $0111$

$$2^{\text{nd}}$$
 complement  $\begin{array}{r} 0111 \\ \cancel{0000} \\ +1 \\ \hline 1000 \end{array}$

Add 1 remaining slot to make it of 8 bit

$$-8 = 11.111000$$

	sign	operation
$[+] + [+]$	+	+
$[+] + [-]$	= greater	
$[-] + [+]$	= greater	
$[-] + [-]$	-	+

$$A = 8$$

$$B = 12$$

Sol/

$$A + B = (+8) + (+12)$$

$$\text{Binary value of } 8 = 1000$$

$$\text{Making it of 8bit} = 0001000$$

$$\text{Binary value of } 12 = 1100$$

$$\text{Making it of 8bit} = 0001100$$

now,

$$(A+B) = (+8) = 0001000$$

$$(A+B) = (+12) = \begin{array}{r} 0001100 \\ 00010100 \end{array}$$

$$A - B = (+A) + (-B)$$

$$\text{Binary value of } 8 = 1000$$

$$\text{Making it of 8bit} = 0001000$$

$$\text{Binary value of } 12 = 1100$$

$$1\text{'s complement} = 0011$$

$$2\text{'s complement} = \begin{array}{r} 0011 \\ +1 \\ \hline 0100 \end{array}$$

Making it 8 bit = 11110100

now,

$$\begin{array}{r} (+A) = +8 = 00001000 \\ (-B) = -12 \quad \underline{-4} \quad 11111000 \\ \hline \end{array}$$

$$\begin{array}{r} 1's \text{ component of result} \quad 00000011 \\ +1 \\ \hline 0000100 \end{array}$$

$$* A - B = -4$$

$$-A + B = (-A) + (+B)$$

$$\text{Binary value of } 8 = 1000$$

$$\begin{array}{r} 1's \text{ component} = 0111 \\ 2's \text{ component} = \underline{0111} \\ \hline 1000 \end{array}$$

$$\text{Making it 8 bit} = 11111000$$

$$\text{Binary value of } 12 = 1100$$

$$\text{Making it 8 bit} = 00001100$$

now,

$$\begin{array}{r} (-A) = -8 = 11111000 \\ (+B) = +12 \quad \underline{-4} \quad 00001100 \\ \hline 10000100 \end{array}$$

$$\text{Here, neglect the carry } -A + B = +4$$

Solutions

$$(total) as -A + B$$

$-A - B$ 

SOLY

$$(-A) + (-B)$$

Binary value of  $12 = 1100$

1's complement = 0011

2's complement = 0101

$$\begin{array}{r} 0011 \\ +1 \\ \hline 0100 \end{array}$$

Making it of 8 bit = 11111000

Binary value of  $12 = 1100$

1's complement = 0011

2's complement = 0100

Making it of 8 bit = 11110100  
now,

$$(-A) = -8 = 11110100$$

$$(-B) = -12 = 11110100$$

neglect the carry and

1's complement = 00010011

2's complement = 00010011

$$\begin{array}{r} \cancel{0} \\ +1 \\ \hline \end{array}$$

$$00010100$$

$$(-A) + (-B) = -20 (10100)$$

-  $54 + 65$

$$\text{BCD of } 54 = 0101 \quad 0100$$

$$\begin{array}{r} \text{BCD of } 65 \\ 119 \end{array} \quad \begin{array}{r} 0110 \\ \hline 1011 \end{array} \quad \begin{array}{r} 0101 \\ \hline 1001 \end{array}$$

$$1010$$

$$00010001 \quad 1001$$

$$0110 \quad 1010 \quad 0110$$

$$1110 \quad 0010 \quad 1110$$

-  $33 + 79$

$$\text{BCD value of } 33 \quad 0011 \quad 0010\ 0$$

$$79 \quad 0111 \quad 1001$$

$$112 \quad 1010 \quad 1100$$

$$0110 \quad 0110$$

$$00010001 \quad 0010$$

### Exclusive OR

$$0 \cdot 0 = 0$$

$$1 \cdot 1 = 0$$

$$0 \cdot 1 = 1$$

$$1 \cdot 0 = 1$$

$$1 \cdot 1 \cdot 0 \quad 110 \quad 11$$

↓

$$10110110$$

$$\begin{array}{r} 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \end{array}$$

Digital	Binary	Gray	BCD
1	0001	0001	0001
2	0010	0011	0010
3	0011	0010	0011
4	0100	0110	0100
5	0101	0111	0101
6	0110	0101	0110
7	0111	0100	0111
8	1000	1100	1000
9	1001	1101	1001
10	1010	1111	00010000
11	1011	1110	00010001
12	1100	1010	00010010
13	1101	1011	00010011
14	1110	1001	00010100
15	1111	1000	00010101

Binary coded decimal: BCD is a type of binary representation for decimal value where each digit is represented by a fixed number of bits usually between four and eight.

Q. Write difference between Analog signal & digital signal.

Analog signal

Digital signal

i. Analog signal are difficult to get analysed at first. Digital signal are easy to analyses.

ii It is more accurate than digital

It is less accurate

iii It produce too much noise

It do not produce noise

iv It take time to stored. It can be easily stored.  
It has infinite memory

v. There is a continuous representation of signal. There is a discontinuous representation of signal.

Q. Subtract as indicate

~~1011.101 from 101.1010~~

soln:

1's complement of 1011.101 = 0100.0101

2's complement of 0100.0101 0100.0101  

$$\begin{array}{r} 0 \cdot 0 + 0 \\ \hline 0100 \cdot 0110 \end{array}$$

Adding it with 0101.1010 = ~~0101.1010~~

$$\begin{array}{r} 0100 \cdot 0110 \\ 0101 \cdot 1010 \\ \hline 1010 \cdot 0000 \end{array}$$

Hence, there is no extra bit  
 1's complement of net  $0101 \cdot 1111$   
 2's complement  $0101 \cdot 1111$ .

$$0110 \cdot 0000$$

ii  $1100 \cdot 110$  from  $11100 \cdot 1011$

SOLY

1's complement  $01100 \cdot 1100 = 10011 \cdot 0011$

2's complement Add it with  $11100 \cdot 1011$

$$\begin{array}{r} 10011 \cdot 0011 \\ + 11100 \cdot 1011 \\ \hline 101111 \cdot 1110 \end{array}$$

So removing extra bit and edit add it with remaining.

$$\begin{array}{r} 01111 \cdot 1110 \\ + 1 \\ \hline 01111 \cdot 1111 \end{array}$$

Difference -  $(01111 \cdot 1111)_2$

- Gray Code:

A Gray code is an encoding of numbers so that adjacent numbers have a single digit differing by 1.

Binary to Gray code

10110

$$\begin{array}{cccccc} 1 & \xrightarrow{-1} & 0 & \xrightarrow{-1} & 1 & \xrightarrow{-1} 0 \\ \downarrow & & \downarrow & & \downarrow & \downarrow \\ 1 & 1 & 1 & 0 & 1 & \rightarrow \text{Gray} \end{array}$$

Gray to binary

10101111

$$\begin{array}{cccccccc} 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\ \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow \\ 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \end{array}$$

- Excess - 3 Code :

The excess-3 code is a non-weighted code used to express decimal numbers. It is self-complementary BCD code and numerical system which has biased representation.

### - EBCDIC

Extended Binary coded Decimal Interchange code is an 8 bit character - coding scheme used primarily on IBM computer.

- American standard code for information interchange. ASCII is a 7-bit code, which means that only 128 characters i.e.  $2^7$  can be represented. It is a very well known fact that computer can manage internally only 0s and 1s. In ASCII "A" is represented by 65.

for example

$$65 = 1000001 = A$$

$$B = 65 + 1 =$$

$$D = 65 + 25 + 4 = 94$$

EBCDIC

$$65 + 4 = 69$$

$$65 + 1 = 66$$

$$65 + 5 = 70$$

### # Error Detection Code

Even parity  $\rightarrow$  If message have 1 even then add 0 in front of MSB

If message have  $\neq$  odd then add 1 in front of Ms.

$$\text{e.g.: } 10110 \rightarrow \text{add 1} \\ \text{parity} = 110110$$

$$101101 \rightarrow \text{even 1} \\ \text{parity 0} = 0101101$$

Odd parity: If you have odd no of 1, you need to add 0 as parity.

If you have even no of 1 you need to add 1 as parity.

## 1. Perform binary into decimal

$$\text{a. } 101_2 = N_{10}$$

soln

$$1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ 4 + 1 = 5$$

$$\text{b. } 11001_2 = N_{10}$$

soln

$$1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ 16 + 8 + 1 = 25$$

$$\text{c. } 1111_2 = N_{10}$$

soln

$$= 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 \\ = 8 + 4 + 2 + 1 = 15$$

$$\text{d. } 10011110_2 = N_{10}$$

soln

$$1 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\ 128 + 16 + 8 + 2 + 1 = 155$$

$$\text{e. } 10101_2 = N_{10}$$

$$1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\ 16 + 4 + 1 = 21$$

$$\text{f. } 101101_2 = N_{10}$$

$$1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 \\ 32 + 8 + 4 + 1 = 45$$

g.  $1111110_2 = N_{10}$

sol/5

$$= 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$= 128 + 64 + 32 + 16 + 8 + 4 + 2 = 222$$

q. Convert the following binary into decimal equivalent

a.  $100001$

sol/5

$$1 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$$

$$32 + 1 = 33$$

b.  $10110110_1$

sol/5

1	0	1	1	0	1	1	0	1
256	128	64	32	16	8	4	2	1

$$= 256 + 64 + 32 + 8 + 4 + 1 = 365$$

c.  $111111$

sol/5

1	1	1	1	1	1	1
32	16	8	4	2	1	

$$= 32 + 16 + 8 + 4 + 2 + 1 = 63$$

d.  $11110000$

solt

$$\begin{array}{r} 1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \\ \times 128 \ 64 \ 32 \ 16 \ 8 \ 4 \ 2 \end{array}$$

$$= 128 + 64 + 32 + 16 = 240$$

### 3. Converting decimal into binary

a.  $225_{10} = N_2$

solt

2	225	- 1 ↑
2	112	- 0
2	56	- 0
2	28	0
2	14	0
2	7	1
2	3	1
		1

$$225_{10} = (11100001)_2$$

b.  $129_{10} = N_2$

solt

2	129	1 ↑
2	64	0
2	32	0
2	16	0
2	8	0
2	4	0
2	2	0
		1

$$129_{10} = (10000101)_2$$

C.  $670_{10} = N_2$

sol/5

2	670	0	↑
2	335	1	
2	167	1	
2	83	1	
2	41	1	
2	20	0	
2	10	0	
2	5	1	
2	2	0	
			↓

$$(670)_{10} = (101001110)_2$$

d.  $(5634)_{10} = N_2$

sol/11

2	5634	0	↑
2	2817	1	
2	1408	0.	
2	704	0.	
2	352	0.	
2	176	0.	
2	88	0	
2	44	0.	
2	22	0	
2	11	1	
2	5	1	
2	2	0	
			↓

$$(5634)_{10} = (101000000010)_2$$

4. Convert octal into hexadecimal

a. 6.

sol:

Converting octal into binary

$$\begin{array}{r} 6 = 421 \\ \quad 1 \oplus 0 \end{array}$$

now, representing value in binary

$$(6)_8 = (1\oplus 0)_2$$

again,

Converting binary into hexadecimal

$$\begin{array}{r} 0110 \\ 8^4 2^3 1 \\ 6 \end{array}$$

Here, representing value into hexa

$$(6)_8 = (6)_{16}$$

b. 12

sol:

Converting octal into binary

$$\begin{array}{r} 12 = 0 \\ 2 | 6 - 0 \\ 2 | 3 - 1 \\ \quad \quad \quad \downarrow \end{array}$$

now, representing value in binary

$$(12)_8 = (1100)_2$$

Converting into binary into hexa.

$$\begin{array}{r} \cancel{1100} \quad 1100 \\ 84 \rightarrow 8421 = 12 = C \end{array}$$

c. 555

sol/

Converting octal into binary

$$\begin{array}{r} 2 | \underline{\underline{5 \quad 55}} - 1 \quad \uparrow \\ 2 | \underline{\underline{2 \quad 77}} - 1 \\ 2 | \underline{\underline{1 \quad 38}} - 0 \\ 2 | \underline{\underline{69}} - 1 \\ 2 | \underline{\underline{34}} - 1 \\ 2 | \underline{\underline{17}} - 1 \\ 2 | \underline{\underline{8}} - 0 \\ 2 | \underline{\underline{4}} - 0 \\ 2 | \underline{\underline{2}} - 0 \\ \quad \quad \quad \downarrow \end{array}$$

$$(555)_8 = (1000111011)_2$$

Converting binary into hexa

$$\begin{array}{ccccccc} 0 & 0 & 1 & 0 & 0 & 0 & 1 \\ 8421 & 8421 & 8421 & & & & \end{array}$$

23B

Now representing value in hexa

$$(555)_8 = (23B)_{16}$$

d. 123456

sol:

Converting octal into binary

2	123456	0 ↑
2	61728	0 ↑
2	30864	0
2	15432	0
2	7716	0
2	3858	0
2	1929	1
2	964	0
2	482	0
2	241	1
2	120	0
2	60	0
2	30	0
2	15	1.
2	7	1.
2	3	1.
		1.

$(123456)_8 = (111000100100000)_2$

Converting binary into hexa

0001	1110	0010	0100	0000
8421	8421	8421	8421	8421
· 1	14=E	2	4	· 0

Now, representing value in hexa

$(123456)_8 = (1E240)_{16}$

5. Convert hexadecimal into decimal

a. AA

sol's

$$A = 10$$

$$A = 10$$

$$= 1 \times 16^0 + 0 \times 16^1 + 1 \times 16^1 + 0 \times 16^0$$

$$= 4096 + 16 + 1$$

$$= 4113$$

b. FBDCBA

sol's

$$F = 15$$

$$E = 14$$

$$D = 13$$

$$C = 12$$

$$B = 11$$

$$A = 10$$

now,

$$\begin{aligned} & F \times 16^5 + E \times 16^4 + D \times 16^3 + C \times 16^2 + B \times 16^1 + A \times 16^0 \\ & = 15 \times 16^5 + 14 \times 16^4 + 13 \times 16^3 + 12 \times 16^2 + 11 \times 16^1 + 10 \times 16^0 \end{aligned}$$

$$= 15 \times 16702650$$

c. BABE

~~5015~~

$$B = 17$$

$$A = 10$$

$$B = 17$$

$$E = 14$$

nolo,

$$= B \times 16^3 + A \times 16^2 + B \times 16^1 + E \times 16^0$$

$$= 17 \times 16^3 + 10 \times 16^2 + 11 \times 16^1 + 14 \times 16^0$$

$$= 47806$$

d. FFFFFFFFA

~~5015~~

$$F = 15$$

$$A = 10$$

$$15 \times 16^7 + 15 \times 16^6 + 15 \times 16^5 + 15 \times 16^4 + 15 \times 16^3 + 15 \times 16^2 + 15 \times 16^1 + 10 \times 16^0$$

$$= 4294967295$$

6. Convert the following octal into decimal:

a. 5

b.

g

$$5 \times 8^0 \\ = 5$$

$$9 \times 8^0 \\ = 9$$

c. 777

Soln

$$7 \times 8^2 + 7 \times 8^1 + 7 \times 8^0$$

$$= 511$$

d. 05726

$$0 \times 8^4 + 5 \times 8^3 + 7 \times 8^2 + 2 \times 8^1 + 6 \times 8^0$$

$$= 3030$$

7. Convert decimal into octal

a. 4

Soln

$$\begin{array}{r} 8 | 4 - 4 \\ 0 - 0 \end{array}$$

$$(4)_{10} = (04)_8$$

b. 10

Soln

$$\begin{array}{r} 8 | 10 - 2 \\ 1 - 1 \end{array}$$

$$(10)_{10} = (12)_8$$

c. 625

$$\begin{array}{r} 8 | 625 - 1 \\ 8 | 78 - 6 \\ 8 | 9 - 1 \end{array}$$

$$625 = (1161)_8$$

d. 1024

$$\begin{array}{r} 8 | 1024 - 0 \\ 8 | 128 - 0 \\ 8 | 16 - 0 \\ 2 \end{array}$$

$$(1024)_{10} = (2000)_8$$

8. Convert the following octal number to binary

a. 107

Soln

Converting octal into decimal  
 $1 \times 8^2 + 0 \times 8^1 + 7 \times 8^0$

Converting decimal to octal binary  
71

2	71	-1↑
2	35	1
2	17	1
2	8	0
2	4	0
2	2	0
		1

$$(71)_8 = (1000111)_2$$

b. 2746

SOL)

Converting octal into decimal

$$2 \times 8^3 + 7 \times 8^2 + 4 \times 8^1 + 6 \times 8^0$$

$$= 1510$$

Converting decimal into binary

2	1510	0	↑
2	755	1	
2	377	1	
2	188	0	
2	94	0	
2	47	1	
2	23	1	
2	11	1	
2	5	1	
2	2	0	

$$(2746)_8 = (10.11100110)_2$$

C. 66542

SOLY

Converting octal into decimal

$$\begin{aligned} 66542 &= 6 \times 8^4 + 6 \times 8^3 + 5 \times 8^2 + 4 \times 8^1 + 2 \times 8^0 \\ &= 28002 \end{aligned}$$

Converting decimal into binary

2	28002	0	↑
2	10041	1	
2	5020	0	
2	2510	0	
2	1255	1	
2	627	1	
2	313	0	
2	156	0	
2	78	0	
2	39	1	
2	19	1	
2	9	1	
2	4	0	
2	2	0	
			1

$$(66542)_8 = (10011100011010)_2$$

d.  $76543210$ Sol:

$$76543210 = 7 \times 8^7 + 6 \times 8^6 + 5 \times 8^5 + 4 \times 8^4 + 3 \times 8^3 + 2 \times 8^2 + 1 \times 8^1 + 0 \times 8^0$$

$$= 16434824$$

Converting decimal into binary

$$\begin{array}{r}
 1 \rightarrow 001 \\
 6 - 110 \\
 4 \quad 100 \\
 3 \quad 011 \\
 4 \quad 100 \\
 8 \quad \text{---} \\
 4
 \end{array}$$

$$(16434824)_{10} =$$

g. Convert binary to octal

a.  $110$

Sol:

$$110 \rightarrow 6$$

$4 \times 1$

b.  $011101$

Sol:

$$011 \quad 101 \rightarrow 35$$

$4 \times 1 \quad 4 \times 1$

k.  $010101011$

Sol:

$$010 \quad 101 \quad 011 \rightarrow 253$$

$4 \times 1 \quad 4 \times 1 \quad 4 \times 1$

d.  $101110011$

Sol:

$$101 \quad 110 \quad 011 \rightarrow 563$$

$4 \times 1 \quad 4 \times 1 \quad 4 \times 1$

10. Convert the hexadecimal number into octal:

a. 10

Q13

Converting hexa into decimal

$$10 = 1 \times 16^1 + 0 \times 16^0$$

$$= 16$$

Converting decimal into binary

$$\begin{array}{r} 2 | 16 \rightarrow 0 \\ 2 | 8 \rightarrow 0 \\ 2 | 4 \rightarrow 0 \\ 2 | 2 \rightarrow 0 \\ \hline \end{array}$$

$$16 = (10000)_2$$

Converting binary into octal

$$(10000)_2$$

$$\begin{array}{r} 010 \quad 000 \rightarrow 2 \\ 4 \quad 2 \end{array}$$

b. 8

Q13:

Converting hexa into binary

$$\begin{array}{r} 2 | 8 \rightarrow 0 \\ 2 | 4 \rightarrow 0 \\ 2 | 2 \rightarrow 0 \\ \hline \end{array}$$

$$(1000)_2$$

Convert binary into octal

$$\begin{array}{r} 001 \quad 000 \\ \hline u_2 \quad u_1 \end{array} \rightarrow 1$$

d.  $2A4F28$

sol<sup>b</sup>

$$A = 10$$

$$F = 15$$

$$D = 13$$

$$\begin{array}{r} 2 \ 10 \ 4 \ 15 \ 2 \ 13 \\ \hline -8421 \end{array}$$

$$\begin{array}{ccccccccc} 2 & 10 & 4 & 15 & 2 & 13 \\ 8421 & 8421 & 8421 & 8421 & 8421 & 8421 \\ 0010 & 1010 & 0100 & 1111 & 0010 & +101 \\ & & & & & & 1101 \end{array}$$

(0.0101010010011110010.110),  
Converting binary into octal.

$$\begin{array}{ccccccccc} 001 & 010 & 100 & 111 & 100 & 101 & 101 \\ \hline u_2 & u_1 & u_2 & u_1 & u_2 & u_1 & u_1 \\ 1 & 2 & 4 & 7 & 4_{14} & 5 & 5 \end{array}$$

12442455

11. Convert decimal into hexadecimal

a. 32

sol<sup>b</sup>

$$\begin{array}{r} 16 \underline{|} 32 - 0 \\ 2 \end{array} \quad 16 = (20)_{16}$$

b. 73

~~Q8(b)~~

$$\begin{array}{r} 16 \mid 73 \rightarrow 9 \\ \quad\quad\quad 4 \end{array}$$

$$16 = (49)_{16}$$

c. 65536

~~Q8(c)~~

$$\begin{array}{r} 16 \mid 65536 - 0 \\ \quad\quad\quad 4096 - 0 \\ \quad\quad\quad 256 - 0 \\ \quad\quad\quad 16 - 0 \\ \hline \quad\quad\quad 1 \end{array}$$

$$(65536)_{16} = 1$$

d.

d. 3020

~~Q8(d)~~:

$$\begin{array}{r} 16 \mid 3020 - 12 - C \\ \quad\quad\quad 118 - 12 - C \\ \quad\quad\quad 14 \end{array}$$

$$3020 - (CC)_{16}$$

e. 7848

~~Q8(e)~~

$$\begin{array}{r} 16 \mid 7848 - 8 \\ \quad\quad\quad 490 \rightarrow 10 - A \\ \quad\quad\quad 30 \rightarrow 14 - E \\ \hline \quad\quad\quad 1 \end{array}$$

$$7848 = (\text{8AE})_{16}$$

12. Perform arithmetic operation

a.  $A = (+42)$

$B = (-13)$

b.  $A(+42) +$

$B = (-13)$

~~a. Q8(b)~~

$A+B$

$A = (+42)$

$B = (-13)$

Binary value of  $42 = 00101010$

Making it 8 bit =  $00101010$

Binary value of  $-13 = 1101$

1's complement =  $0010$

2's complement =

$$\begin{array}{r} 0010 \\ +1 \\ \hline 0011 \end{array}$$

Making it 8bit = 11110011

$$\begin{array}{r} A (+42) = 0^1 0^1 1.0.1\ 0\ 1.0 \\ B (-13) = \underline{1\ 1\ 1\ 1.0\ 0\ 1\ 1} \\ \hline 29 \qquad \qquad \qquad 1\ 0\ 0\ 0\ 1\ 1\ 1\ 0\ 1 \end{array}$$

now,

neglect the extra bit then  $A+B=00011101$

b. ~~A (+42)~~  
~~B (-13)~~