

# IMPORTANT POINTS

- Focus on work on skill and build networks those work in companies and can talk to HR for you
- Internship- do if you want to learn or convert it as PPO
- Rough sols. and dry run are very important
- Do documentation to promote and mail everything you discuss with HR or team
- Think twice, Code once
- To clarify any code you are confused, use cout statements every where to know what is going on in the code
- Code all approaches you can think of and can find & understand from google
- Revise all incorrect & skipped questions in quizzes regularly
- Watch sol. only after attempting the question
- Interviewer will ask Time & Space complexity after every sol. you give

→ 2 websites

- cppreference
- cplusplus.com

→ Think on paper → with 5 testcases atleast

→ Write readable codes

→ In interviews, tell approaches of questions using example

→ Signs of beginner → no logic build

can't solve new ques

forget the approach

memorizing the ans

↓  
Improve → with more no. of questions

with time

with dry run on mind logic, not on  
code

with your new approach

(even brute force)

with a lot of practice on syntax

with consistency

→ Focus on placement, not on feeling

You are not studing to get fun

You are studing to get placed

First placement, then fun and interest.

Also focus on health of you and your parents

Bhaad me gya interest yaar, placement ke baad karna

Jo duniya sunna chahati hai, use sunado

Growth is important

Week 4 [Connect] Class 1:45 - 2:01

→ 20-30 interview experience

↳ to break Google pattern

→ Web Dev and DSA → both are important

CP → do if you enjoy it.

→ At least learn one more approach if you are doing questions with map

Many times if you tell map approach, interviewer asks another approach

→ Tag all khatarnak questions

↳ Otherwise you will forget them after some time

→ Revise and code all, every after 2 weeks

→ For 6<sup>th</sup> sem student (like me),

↳ At least do ptd on leetcode everyday along with course

→ Make notes

→ In dev, you should have at least 2 major projects

1 → in dot batch  
2 → group project  
if you want

→ Focus on Networking,  
After 5 months, you should have atleast 2 friends in every company

→ All questions doing in batch, should be on your tips

- Focus on accuracy more than speed
- Resume is made company specific
- Make sure others don't take your credits
- Higher position  $\propto \frac{\text{Development}}{\text{DSA Complexity}}$   
in career
- Interview experience before interview
- Flex se kuch nhi hota  
Comparision se kuch nhi hota
- Don't forcefully try to increase the speed of DSA learning,  
Try to increase the number of hours spent everyday in DSA learning
- if ques seems tough in another datatype but easy in another datatype, then first do that in later datatype and after solving the sol. change datatypes

→ In interview, you must have clarity and strong concepts and strong argument behind the things you say, whether the ans comes right or wrong is another thing

# IMPORTANT C++ NOTES

→ -1 in binary 1.....1  
-2<sup>31</sup> in binary 10...0

→ In left shift, vacant bit will be filled by 0  
In right shift, vacant bit will be filled by MSB  
1 → in -ve no.  
0 → in +ve no.

$(-1) \gg n$  → (-1) no change  
any no. of times

→ int a = 5;  
cout <<  $(++a) * (++a)$ ;  
a \* (++a), a = 6  
a \* a, a = 7  
7 \* 7 = 49

cout <<  $(a++) * (a++)$ ;  
5 \* (++a), a = 6  
5 \* a, a = 7  
5 \* 7 = 35

cout <<  $(++a) * (a++)$ ;  
a \* (a++), a = 6  
a \* 6, a = 7  
7 \* 6 = 42

cout <<  $(a++) * (a++)$ ;  
5 \* (a++), a = 6  
5 \* 6, a = 30

→ Continue cannot be used in switch case  
can only used in loops

→ int main () {

return 0; —————> returns to OS

} 0 is used to represent successful execution

→ A cpp file can't have more than 1 main function

→ main() can't have return type other than int  
in offline compiler

→ % is heavy operator, so try to use it less

→ array name returns address of first index

## Integer Array -

`cout << arr ;`  $\longrightarrow$  `A1`  $\longrightarrow$  address of first index of array  
address of integer  $\underline{\hspace{100px}}$

cout << &arr ;  $\longrightarrow$  A<sub>1</sub>  $\longrightarrow$  base address of array arr

address of array

from symbol table

diff. things

→ To find max., initialize ans with INT\_MIN

To find min., initialize ans with INT\_MAX

→ xor → cancels out same element

→  $0 \wedge \text{ans} = \text{ans}$

$$\begin{array}{l} 0 \wedge 1 = 1 \\ 0 \wedge 0 = 0 \end{array}$$

→ Mapping of 2D array with memory 1D array

$$\text{linear\_index} = c * i + j$$

no. of cols ←  
row index ←  
col index ←

$i = \text{linear\_index} / c$   
 $j = \text{linear\_index} \% c$

→ Arrays and 2D arrays of any datatype

→ pass by reference

→ Search space

→ range of ans (start and end) in  
binary search questions

→ store mid in ans if needed in binary search ques

## → In binary search questions

while ( $s \leq e$ ) {  
    ans = mid;  
     $s = mid + 1$ ;  
    left search  $\leftarrow e = mid - 1$ ;  
}  
right search

ans = mid  
 $s = mid + 1$   
convert

while ( $s < e$ ) {  
     $s = mid$ ; → right search  
     $e = mid - 1$ ;  
}  
OR  
 $s = mid + 1$  → right search  
 $e = mid$ ;

ans = mid,  $e = mid - 1$   
convert

left search  
} ←  $e = mid$ ;

→ cout << (int)(-3.74);

→ - [ int (3.74) ]

→ - (3) → - 3

cout << (-22)/7; → - 3

cout << 22/(-7); → - 3

→ In ASCII → '0' → 48  
      'A' → 65  
      'a' → 97

→ In sorted array, try to apply binary search or  
2 pointer / 3pointer approach

→ To maximize or minimize  
try to use binary search using concept of search space

- find search space of answer
- find mid
- if isPossibleAns(mid) → go to left / right acc.  
to the ques.

You can use above approach also in other  
ques like find the duplicate number in an array  
having elements range 1 to n

## → Week 6 Lecture 2

### → Magical line for recursion

↳ Ek case solve krdo baaki recursion smbhali lega

↳ Just believe on it, dont doubt on recursion

## → Week 7 Lecture 2

## → Week 7 Lecture 3

→ If the recursion ques seems tough,  
use void function and pass ans by reference  
in function

→ If in ques. array elements are in range  $[1, n]$  or  $[0, n)$ , try to treat elements as indices of an array  
(Week 3 Assignment)

→ Try to make cnts [max element present in array] instead of making cnts [max limit given in question.]

→ int digit = 7;  
string s;  
s.push\_back ( digit + '0' );  
cout << s; → 7  
s.push\_back( digit );  
cout << s; → contains  
char with  
ascii value = digit

'7' to 7  $\longrightarrow$  '7' - '0'

7 to '7'  $\longrightarrow$  7 + '0'

# ERROR / BAD PRACTICE

If let's go page

→ 13

31, 33, 43, 70, 71, 72, 73, 75, 76, 79, 86, 87, 89, 90, 93, 95

→ 14

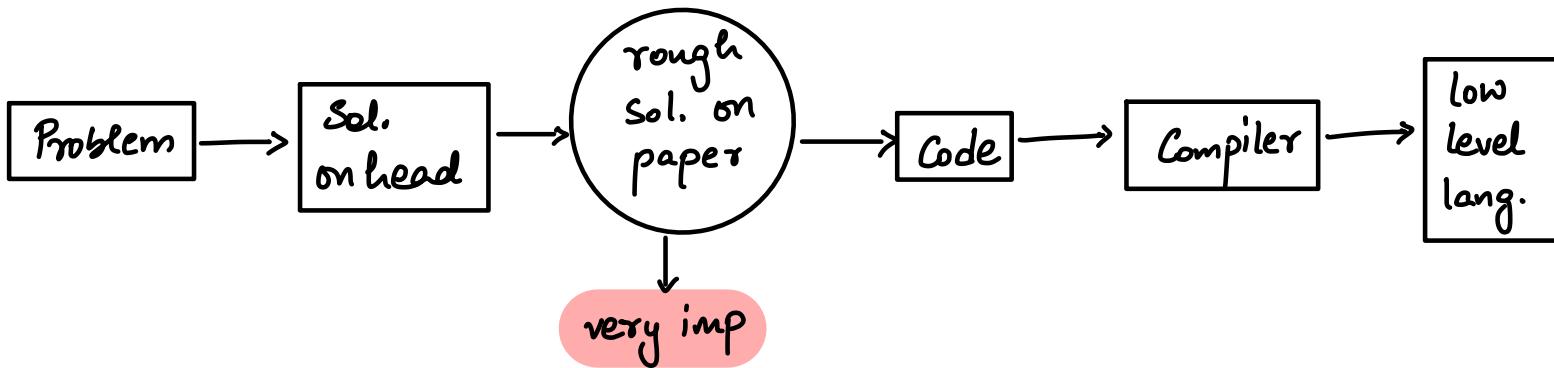
104

**LET'S GO**

Thought process to solve a problem-

W1-L1

- Understand a problem
- input values
- find approach



Algorithm - Sequence of steps

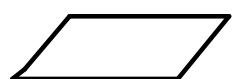
Flowchart - Graphical representation of algo

Components -

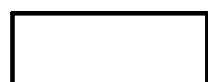


terminator

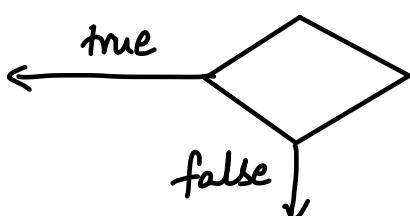
for start / end



for input /output read /write



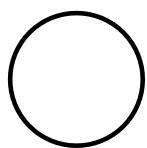
computation / process / declaration



decision making block  
takes condition



flow



Connector  
takes function

Pseudo Code - Generic way of writing algo

Dry Run → Very important to understand any topic

W1-L2

IDE - Replit, VS-Code

```
# include <iostream>           → preheader file contains implementation of keyword
using namespace std;
int main () {
    cout << "Namaste Bharat";
}
region where scope of keyword is defined
used to print on console / standard display
```

→ using standard namespace implementation of cout choosing from multiple types of namespace

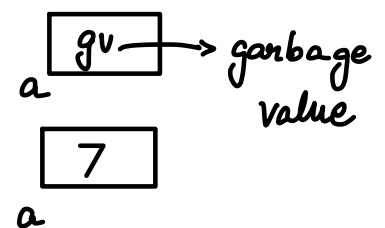
→ to end any statement

→ string

cout << endl; → for next line

cout << '\n';

int a;  $\longrightarrow$  a is an integer  
 cin >> a;  $\longrightarrow$  input a from user  
 ex- 7



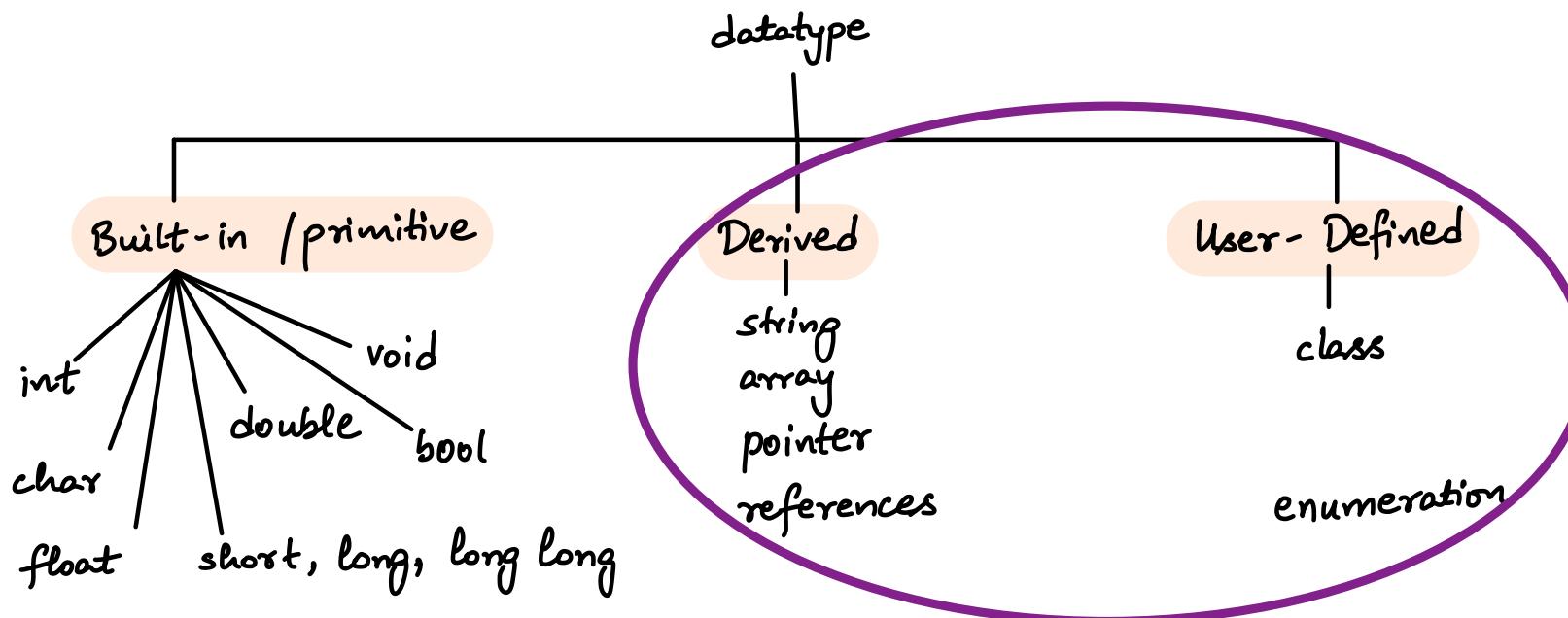
## Variables

named memory location

int  $\downarrow$   
 datatype  
 a = 5;  
 variable  
 name  $\longrightarrow$  value

## Datatypes

type of data



int - 4 byte - 32 bits in memory  
 $\longrightarrow$   $-2^{31}$  to  $2^{31}-1$  in signed int  
 $\longrightarrow$  0 to  $2^{32}-1$  in unsigned int

char - 1 byte - 8 bits in memory  
 $\longrightarrow 2^8$  different chars.

## ASCII

↳ char maps with numerical ASCII value

char  $\leftrightarrow$  ASCII value  $\rightarrow$  store in memory

bool  $\rightarrow$  1 byte  $\rightarrow$  8 bits

true - 1  
false - 0

↳ because minimum addressable memory is 1 byte  
we cannot address 1 bit in memory

float  $\rightarrow$  4 byte  $\rightarrow$  32 bits

double  $\rightarrow$  8 byte  $\rightarrow$  64 bits

long long  $\rightarrow$  8 byte  $\rightarrow$  64 bits

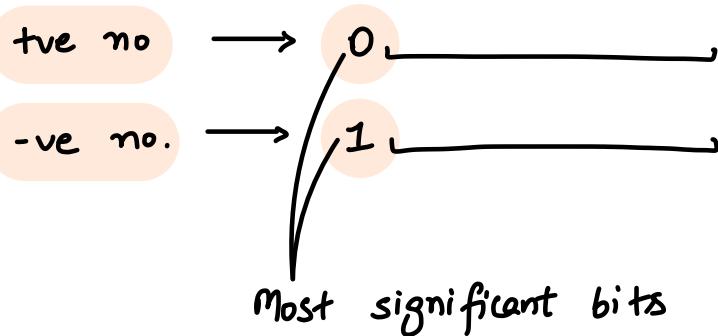
short  $\rightarrow$  2 byte  $\rightarrow$  16 bits

long  $\rightarrow$  4 byte  $\rightarrow$  32 bits

## How data is stored

int a=5;

↳ 32 bits  $\underbrace{0 \dots 00}_{29 \text{ bits}} 101$



### How -ve number is stored in memory

In 2's complement form

→ 1's complement + 1

→ reverse all bits

int a = -7;

7 → 0.....00111 } 32 bits

ignore -ve sign  
find binary equivalent

1's (7) → 1.....11000

find 2's complement

2's (7) → 1.....11001

→ this is how -7 will be stored in memory

### How to read -ve no. present in memory

→ take 2's complement

1....11001

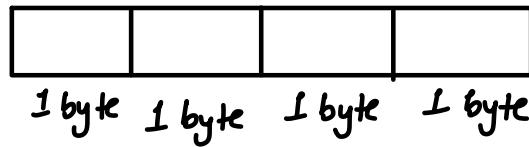
→ 1's complement → 0...00110

2's complement → 0...00111

→ + 7

-7

## Interesting problem



how computer know these are 4 chars or a single integer

↳ Using datatype

↳ tell 2 things

- type of data used
- space used in memory

## Signed vs Unsigned

↓  
↳ 0, +ve

↳ +ve, -ve, 0

↳ by default

int - 4 byte - 32 bits in memory

↳ total no. of combinations -  $2^{32}$

↳ signed int

$-2^{31}$  to  $2^{31}-1$

↳ unsigned int

0 to  $2^{32}-1$

} range

① 0...0

011...1

0.....0

1....1

} in memory

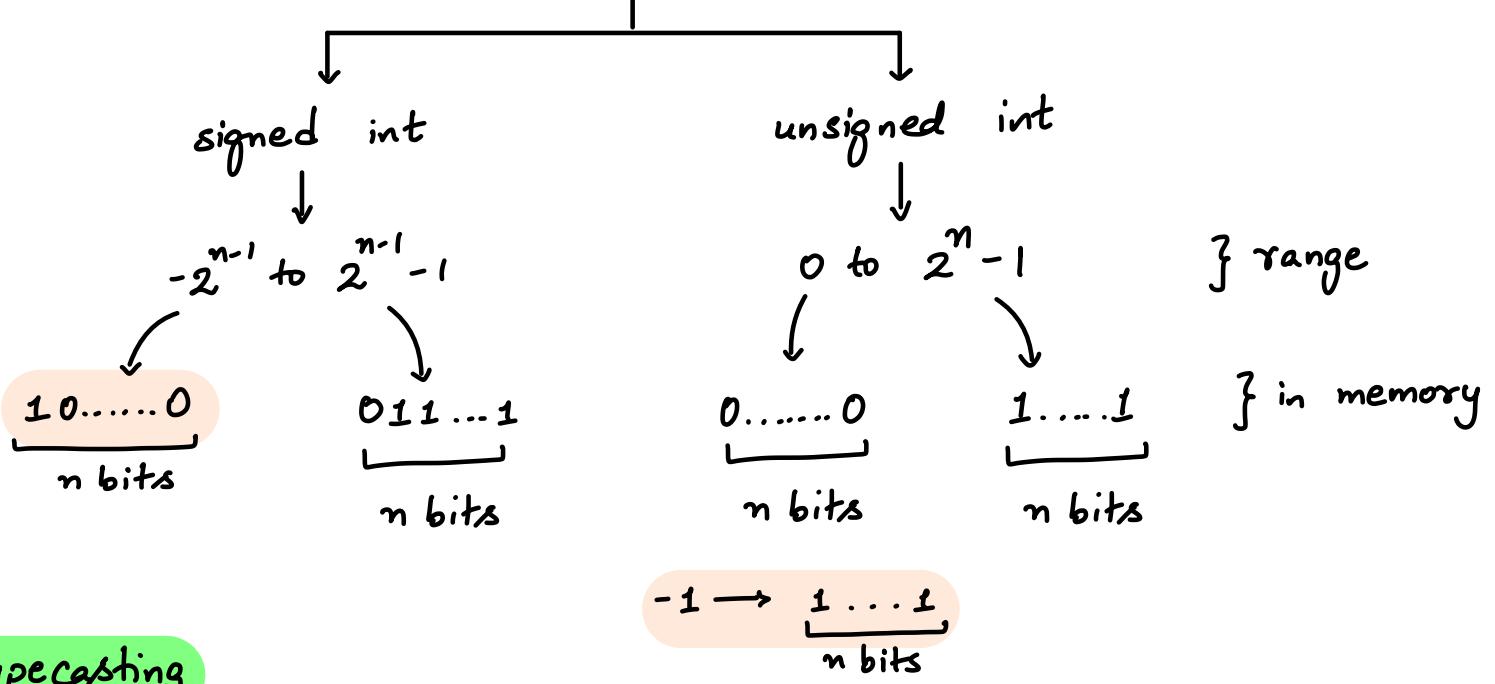
2's → 10...0

→ -2<sup>31</sup>

## General Formula

$n$  bits in memory

↳ total no. of combinations -  $2^n$



## Typecasting

↳ convert one type of data to another

## implicit typecasting

ex- `char ch = 97;`  
`cout << ch;` → (a)

## explicit typecasting

ex- `char ch = (char) 97;`  
`cout << ch;` → (a)

overflow ex- `char ch = 9999;`  
`cout << ch;`

$9999 \xrightarrow{\text{binary conversion}} 10011100001111$   
stores only last 8 bits

so  $ch$  stores 00001111 in memory  
 ↓  
 7  
 ↓  
 acc. to ASCII table

## Operators -

### Arithmetic Operator

→ +, -, \*, /, %,  
 int op int → int  
 float op int  
 int op float } float  
 float op float  
 double op int  
 int op double } double  
 double op double  
 float op double  
 double op float  
 3 → int  
 3.0 → float / double by default → cout << sizeof(3.0);  
 not int ↓  
 ⑧

### Relational Operator

(a op b)

>, <, >=, <=, !=, ==

Output - 0 or 1

false

true

These are different things

## Assignment Operators

=

## Logical Operators

↳ when you have multiple conditions

$(a \& \& b)$  → and → true if both are true

$(a || b)$  → or → true if any one is true

$(!a)$  → not → negate the result

Output - 0 or 1  
false      true

$(\text{cond1} \& \& \text{cond2} \& \& \text{cond3})$

if cond1 is false

compiler will not check further  
as ans will already false

$(\text{cond1} || \text{cond2} || \text{cond3})$

if cond1 is true

compiler will not check further  
as ans will already true

## Conditions

if (cond.){  
    execute  
}

if

if (cond.){  
    execute 1  
}

else {  
    execute 2  
}

if - else

W1-L3

if (cond1)  
    execute 1

else if (cond2)  
    execute 2

if - else if

```

if (cond 1)
  execute 1
else if (cond 2)
  execute 2
else if (... )
else
  execute n

```

if - else if - else

```

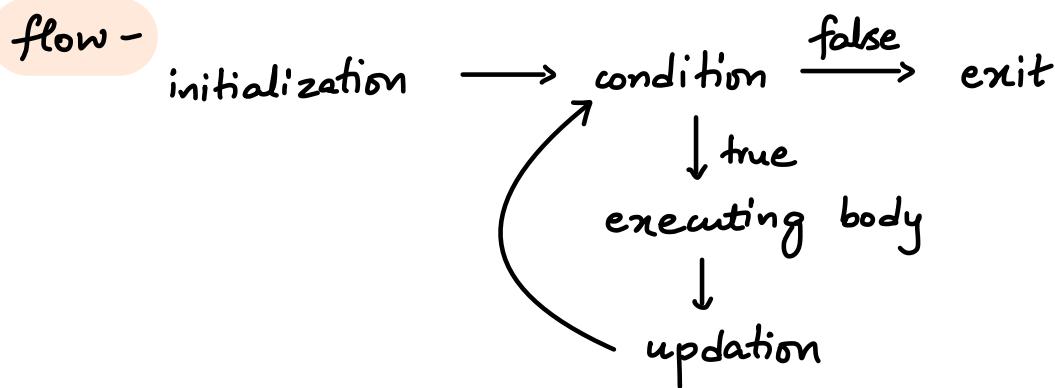
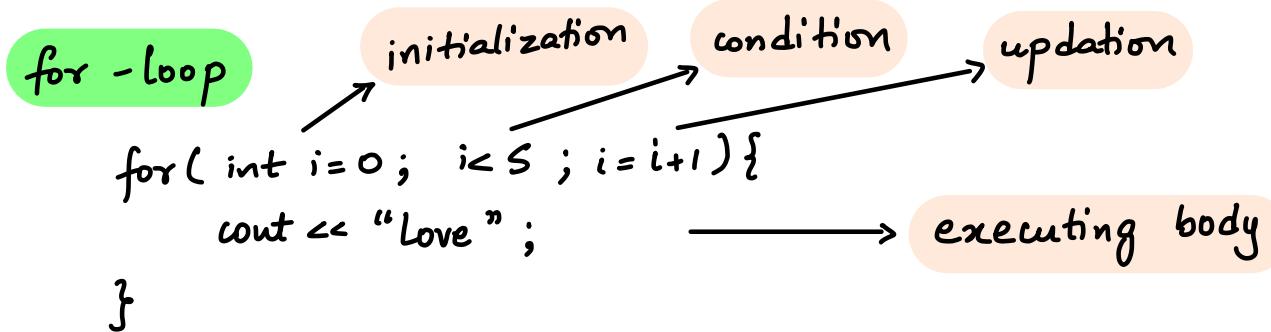
if (cond 1)
  execute 1
else {
  if () { }
  else () { }
}

```

nesting if - else

## Loops

↳ to do something repeatedly



initialization  
 condition  
 updation }      none is mandatory  
                   one or multiple i, c, u can be added

multiple c → i > 5, i < 10; → i > 5 & & i < 10

## patterns -

generally 2 loops  $\longrightarrow$  outer loop() { for rows  
inner loop() { for cols  
}  
}  
cout << endl;

$\rightarrow a \ op = b \longrightarrow a = a \ op \ b$

op  $\rightarrow +, -, *, /, \%, \ll, \gg$

## cin in if()

```
int num;  
if(cin >> num){  
    cout << "hello";  
}  
else {  
    cout << "hi";  
}
```

it will not give error

output -  
hello

for all input values of num

↓  
0, true, -ve

## cout in if()

```
int num = 0;  
if(cout << num << endl){  
    cout << "hello";  
}  
else {  
    cout << "hi";  
}
```

it will not give error

output -  
0  
hello

for all values of num

↓  
0, true, -ve

HLL - High level language

↳ human readable and user friendly

W1-L4

C++, C - Middle Level language

namespace → to avoid collision



multiple definitions of a single keyword

hierarchy

↳ various namespaces



std namespace



iostream preheader file



keyword definition

various namespaces

std



iostream



cout



definition

other



iostream



cout



definition

float f = 2.0 + 100;

cout << f; → output -

102 or 102.0  
compiler dependent

float f = 2.7;

int n = 157;

int diff = n - f;

cout << diff;

output -

154

explanation -

$$n - f = 157 - 2.7 = 154.3$$

$$\text{int diff} = n - f$$

$$\text{diff} = 154$$

## ternary operator -

W1-HW

↳ syntax

variable = (condition) ? expression2 : expression3

(condition)? variable = expression2 : variable = expression3

2 and 3 cant be statements, they must be exp.

ex- `return (a > b) ? a : b;` → CORRECT

`(a > b) ? return a : return b;` → WRONG  
ERROR

these are statements, not expression

## by default -

`cout << sizeof(2.3);` → 8

↳ float

`cout << sizeof(a);` → 4 → int

↳  $-(2^{31}-1)$  to  $2^{31}-1$

`cout << sizeof(-2^{31});` → 8

↳ long long

↳ how to think

→ finding formula for rows and cols

$n=5$

row	stars
0	0
1	0
2	1
3	2
4	3

→ formula -

0 to  $< n-1$

$n-1$

-1

0

1

2

3

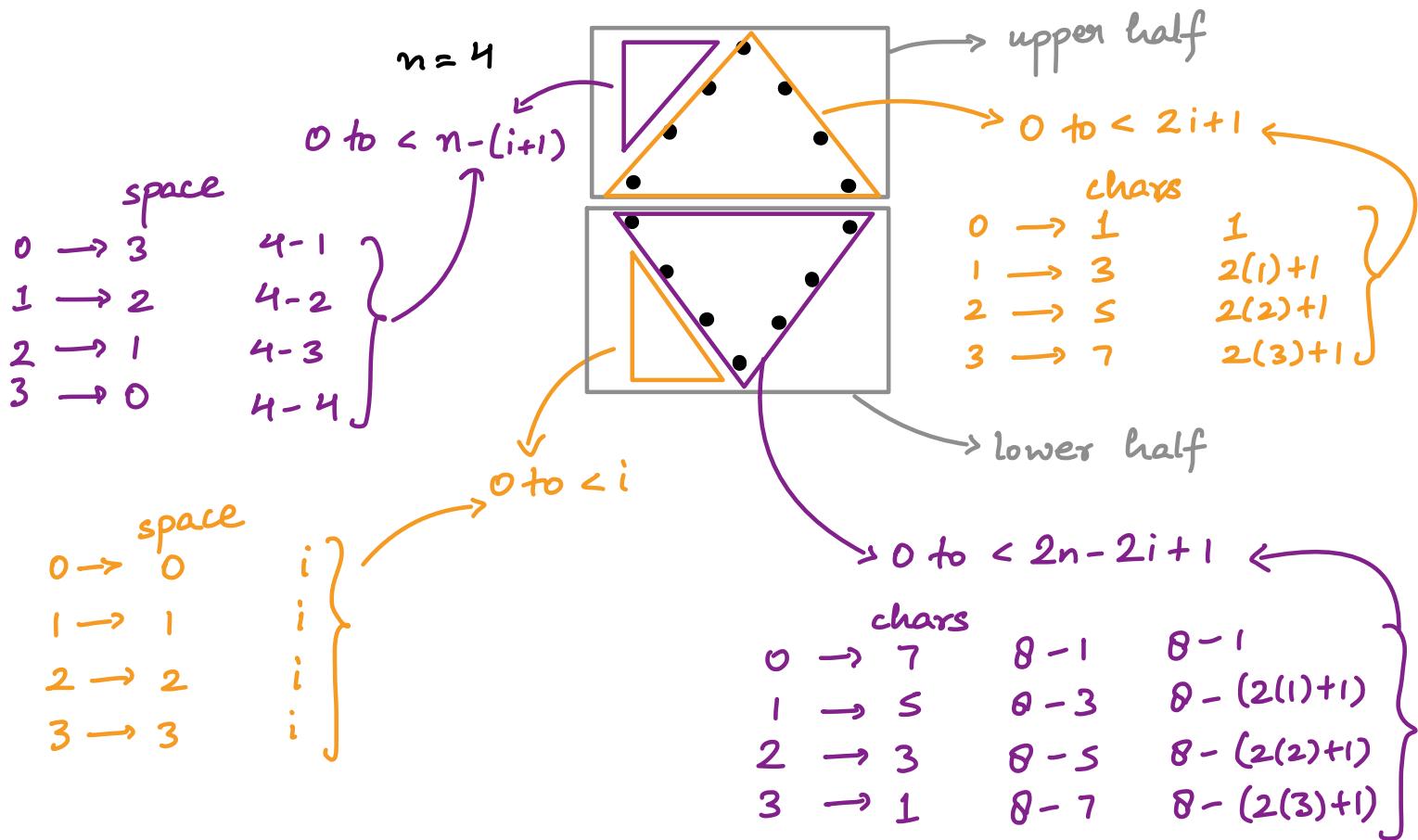
no. of times loop runs
0
1
2
3

as condition fails ( $0 < -1$ )

→ to do anything  $n$  times

→ `for(i=0; i<n; i++) {}`

→ break the complex patterns



## Bitwise Operators

W2-L2

↳ use on bit level

And  $(a \& b)$  1 if both bits are 1

Or  $(a | b)$  1 if any or both bits are 1

not  $(\sim a)$  negate the result

nor  $(a \wedge b)$  same values  $\rightarrow 0$   
diff. values  $\rightarrow 1$

$\sim 5$

$\sim 5 \rightarrow 5 \rightarrow 0 \dots 0101$

$\sim 5 \rightarrow 1 \dots 1010$

↳ how compiler read this

↳ 2's complement

$0 \dots 0101 \rightarrow 1$ 's complement

$0 \dots 0110 \rightarrow 2$ 's complement

-6

So  $\sim 5 = -6$

## Left and right shift operators

<<

shift all bits to left

\* by 2 (not in every case)

↳ if MSB is 1 and

2nd MSB is 0

>>

shift all bits to right

/ by 2 (not in every case)

↳ in -1

$a = a \ll b$  a left shifts, b times  $\rightarrow$  result  $\rightarrow a \times 2^b$

$a = a \gg b$  a right shifts, b times  $\rightarrow$  result  $\rightarrow \frac{a}{2^b}$

b cant be -ve

$\hookrightarrow$  in case of -ve

$a = 5;$

$\hookrightarrow$  gives 8<sup>v</sup>

$a = a \ll 1;$   $a = 10$

$a = 5;$

in left shift  $\rightarrow$  filled with 0

$a = a \ll 2;$   $a = 20$

in right shift  $\rightarrow$  filled with

0 or 1

in +ve no.

in -ve no.

right shift in -ve number

-ve no. in memory  $\rightarrow 1 \dots$

$\downarrow$  right shift

1 1 ...

$\hookrightarrow$  signed bit is used to fill the vacant bit

ex-

$s \rightarrow 0 \dots 0 101$

$-s \rightarrow 1 \dots 1 011$

$-s \gg 1 \rightarrow 1 \dots 1 01 \rightarrow -3$

$-1 \gg 1 \rightarrow -1$

left shift in number where MSB is 1

and 2nd MSB is 0

no.  $\rightarrow 1 0 \dots \rightarrow$  -ve no.

left shift

$\rightarrow 0 \dots$

$\rightarrow$  +ve no.

## Pre- Post $\rightarrow$ Increment / Decrement Operator

### pre- increment

$\hookrightarrow ++a$

$\hookrightarrow$  first increment by 1, then use

### post- increment

$\hookrightarrow a++$

$\hookrightarrow$  first use then increment by 1

### pre- decrement

$\hookrightarrow --a$

$\hookrightarrow$  first decrement by 1, then use

### post- decrement

$\hookrightarrow a--$

$\hookrightarrow$  first use then decrement by 1

int a = 5;

cout  $\ll$  (++a) \* (++a);

output -

49

$\hookrightarrow$  due to operator precedence

$\rightarrow$  links.txt in repo

## break and continue

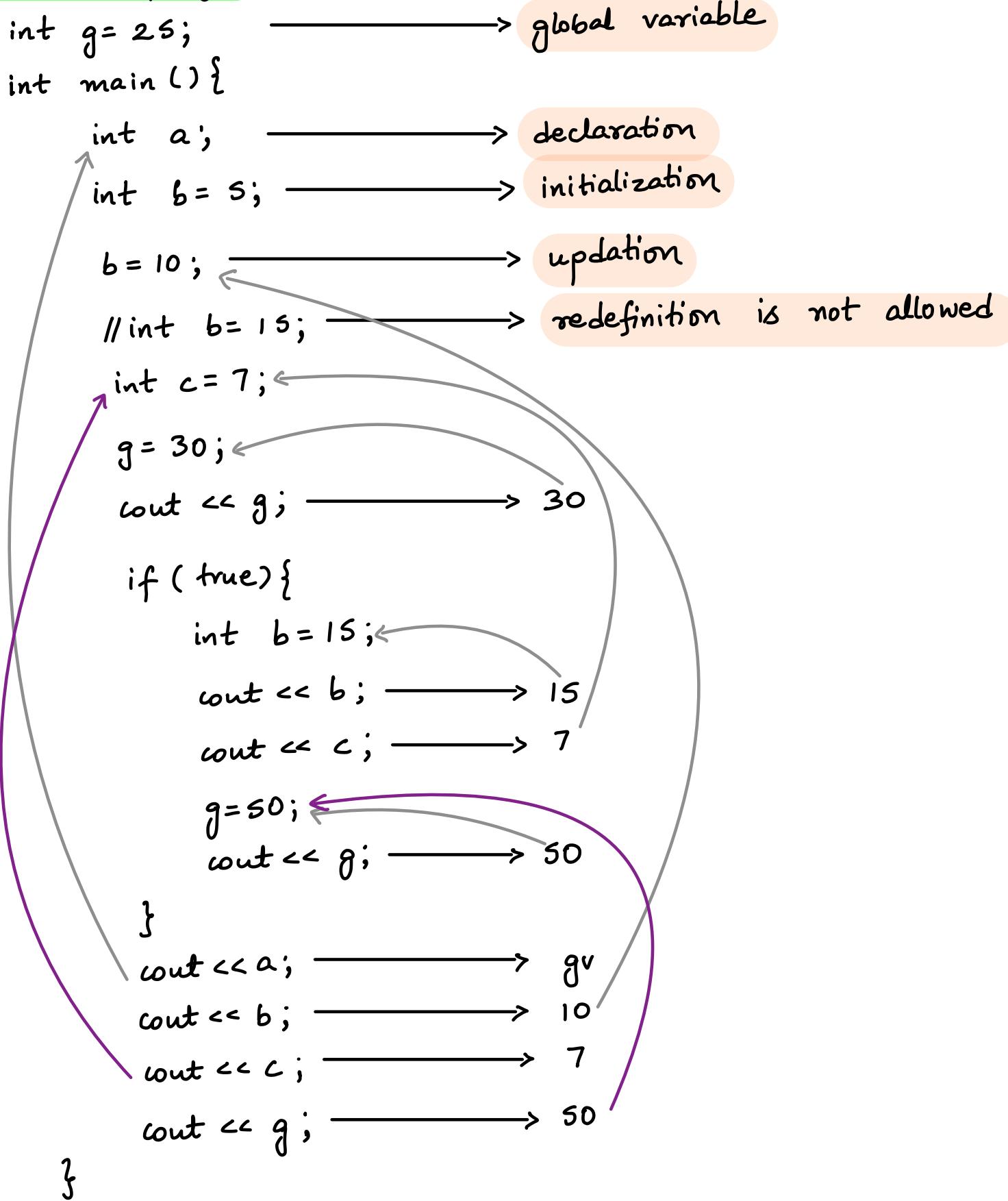
### break

$\hookrightarrow$  exit from that loop

### continue

$\hookrightarrow$  skip that iteration

## Variable Scoping -



Making global variable is very **BAD PRACTICE**

## Operator Precedence

- order of priority of operator
- no need to remember  
use brackets properly

## Switch Case

```
switch (expression) {
```

```
    case value1 :
```

executing body 1

break;

```
    case value2 :
```

executing body 2

break;

:

```
    case value n :
```

executing body n

break;

```
    default :
```

executing body

}

without break

→ all below executing body will also execute

→ continue cannot be used in switch case

→ can only use in loops

can also have  
nested switch

case

not  
mandatory

## Function -

## W2-L3

- program linked with well defined task
- why
  - reusable
  - readable
- without
  - bulky
  - lengthy
  - buggy if mistake in any place

### Syntax -

```
return type function name (input parameters){  
    executing body
```

```
}
```

void → empty / no value      void x; → ERROR  
cout << sizeof(int) → 4  
cout << sizeof(void) → ERROR

```
int main(){  
    return 0;}
```

→ returns 0 to Operating System  
→ 0 is used as means of successful execution

- a cpp file can't have more than 1 main functions
- main can't have return type other than int in offline compiler

# Function Call Stack

function call  $\leftrightarrow$  function invoke

Stack

↳ Last In First Out

- ↳ tells what functions are active
- ↳ which function calls which
- ↳ local variables of function
- ↳ return type of function

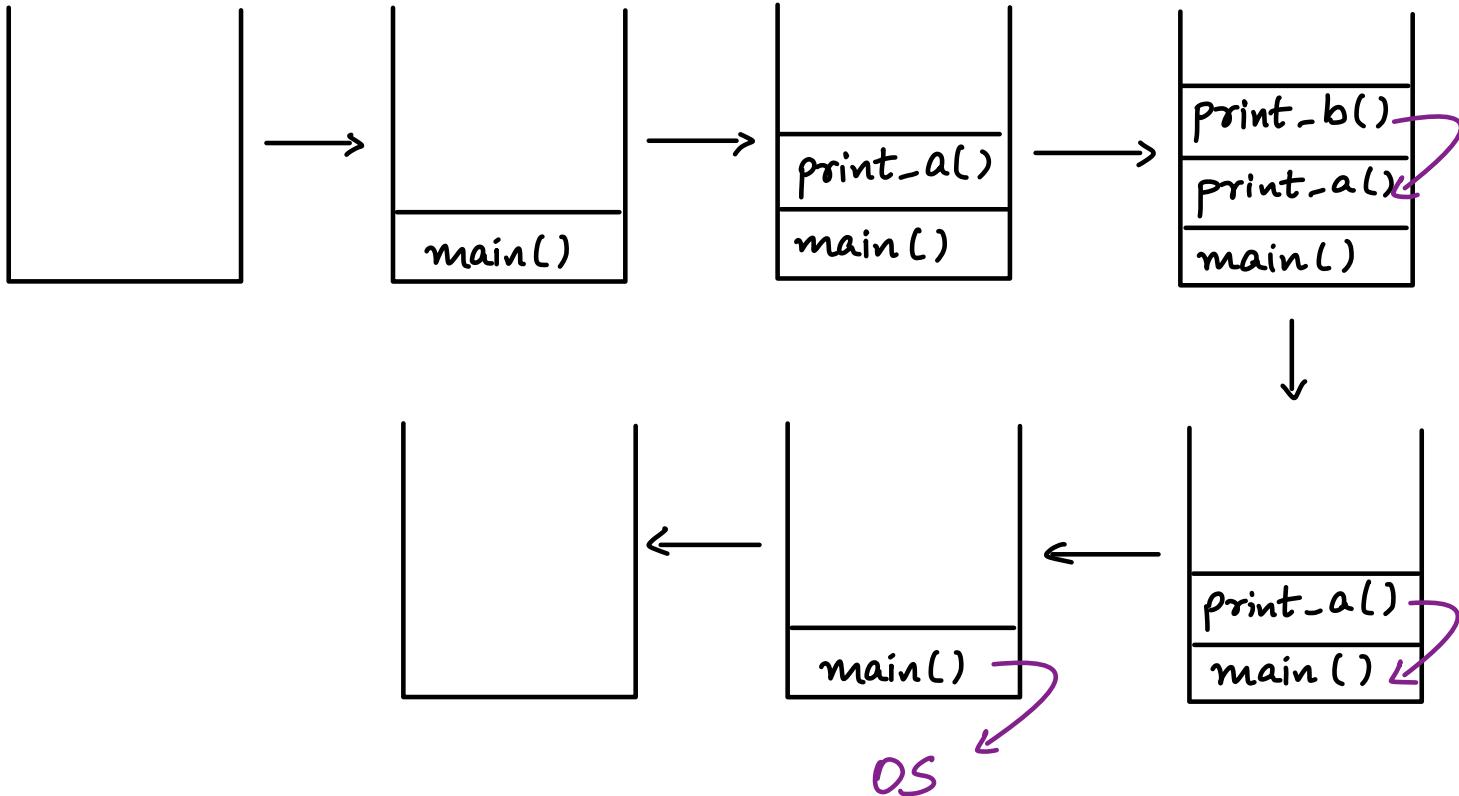
ex -

```
int main() {
    int a=5;
    print_a(a);
    return 0;
} return to OS
```

```
void print_a(int a) {
    cout << a;
    int b=3;
    print_b(b);
}
```

```
void print_b(int b) {
    cout << b;
}
```

Output - 5 3



Pass by value  $\rightarrow$  value is passed to another variable

$\hookrightarrow$  a copy will be created of variables

```
int main() {  
    int a=5;  
    printNumber(a);  
    cout << a;  
}
```

$A_1$   
a  
5

argument

diff. memory  
locations

parameter  
void printNumber(int a){  
 cout << a;  $\rightarrow 5$   
 a++;  
 cout << a;  $\rightarrow 6$   
}

$A_2$   
a  
5

$A_2$   
a  
6

new copy

## Address Of Operator &

```
int n=5;  
cout << &n;  $\rightarrow$  output -  
address of n
```

$\hookrightarrow$

```
int main() {  
    int a=3;  
    int b=4;  
    int sum = add(a, b);  
    cout << sum;  
    return 0;  
}
```

$A_1$   
sum  
7

$\hookrightarrow$

```
int add(int a, int b) {  
    int result = a+b;  
    return result;  
}
```

$A_2$   
result  
7

copying the  
returning value in sum

returning a value

# Function Order

## Order 1

```
int add (int a, int b) {  
    return a+b;  
}  
  
int main () {  
    int a=3;  
    int b=5;  
    int sum= add (a,b);  
    cout << sum;  
    return 0;  
}
```

function  
declaration  
and  
definition

## Order 2

```
function declaration  
int add (int a, int b);  
  
int main () {  
    int a=3;  
    int b=5;  
    int sum= add (a,b);  
    cout << sum;  
    return 0;  
}  
  
int add (int a, int b) {  
    return a+b;  
}
```

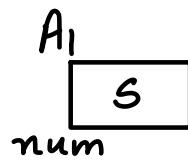
function  
definition

% operator → heavy operator

↳ so try to use it less

int num=5;

### Symbol table



int num  $\longleftrightarrow$  A<sub>1</sub>  
 ↓  
 datatype      variable name

memory location of variable

variable address mapping is stored

cout << num;

go to symbol table  $\longrightarrow$  A<sub>1</sub>  
 (address)  $\xrightarrow{\text{print}}$  5  
 (value)

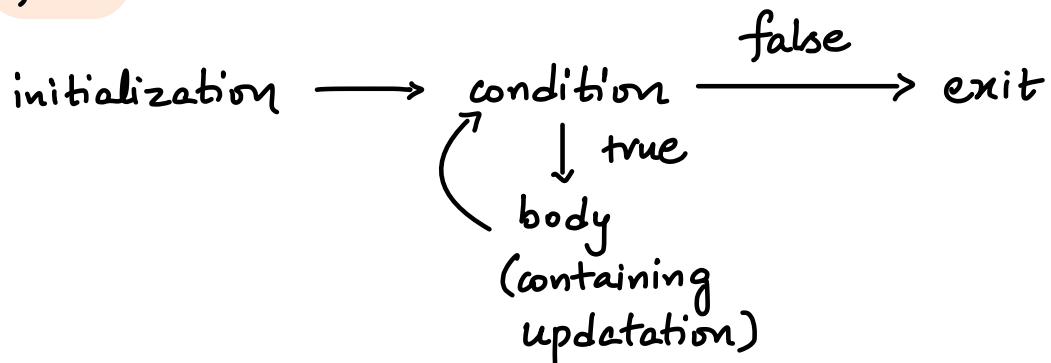
cout << sizeof(num);

go to symbol table  $\longrightarrow$  int  
 datatype  $\xrightarrow{\text{print}}$  4

### while loop

int i=0;  $\longrightarrow$  initialization  
 while (i < 5) {  $\longrightarrow$  condition  
 cout << i << endl;      }  $\longrightarrow$  body  
 i++;  $\longrightarrow$  updatation  
 }

### flow



## left and right shift operators

int a = 2;

$a \ll 1;$   $\longrightarrow$  no change

$\text{cout} \ll a;$   $\longrightarrow$  2

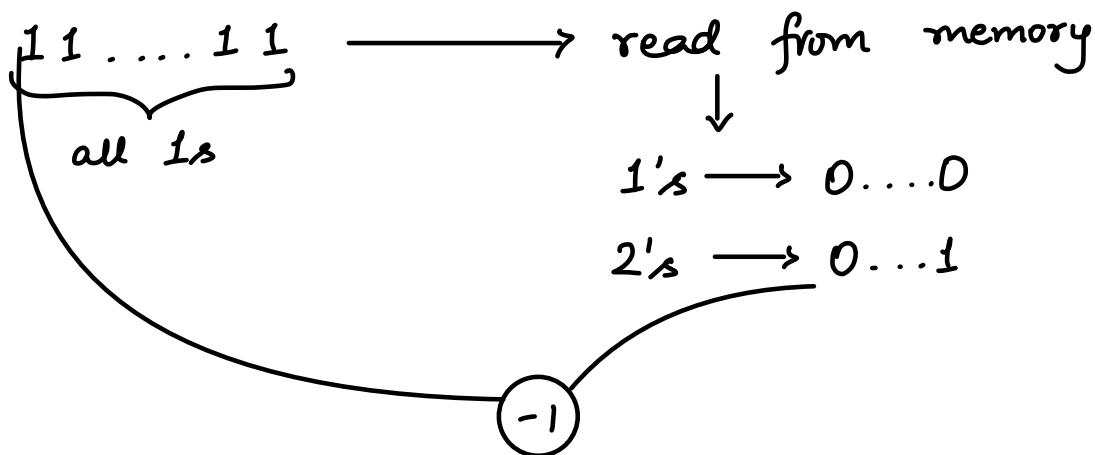
$a = a \ll 1;$   $\longrightarrow$  change  $\longrightarrow$  left shift by 1

$\text{cout} \ll a;$   $\longrightarrow$  4

right shift in -ve no.

$\hookrightarrow$  link in links.txt in repo

## How -1 is stored in memory -



$$\sim a = -(a+1) \quad \text{and} \quad \sim(\sim a) = a$$

ex -  $a = 5; \longrightarrow 0 \dots 0101$

$a = \sim a; \longrightarrow 1 \dots 1010 \longrightarrow -6 \longrightarrow -(5+1)$

$a = -6;$

$\hookrightarrow 1 \dots 1010$

$\xrightarrow{\text{read}}$

-6

$a = \sim a; \longrightarrow 0 \dots 0101$

$\hookrightarrow 5 \longrightarrow -(-6+1)$

## Number System

W2-R

↳ method to represent numeric values using digits

### Decimal Number System

↳ base 10

↳ digits → 0 to 9

### Binary Number System

↳ base 2

↳ digits → 0, 1

↳ used in CPU, memory, computer

↳ 0 → power off

↳ 1 → power on

↳ number, images, all files & folder are in binary

### Decimal to Binary

↳ divide no. by 2

↳ store remainder

↳ repeat above steps until no. is 0 or 1

↳ reverse the bits so obtained

## Binary to Decimal

- multiply each bit with its place value
  - base  $i$
- add all products
  - $2^i$

## Time & Space Complexity

W3-R

### Time Complexity

- amount of time taken by an algo as a function of length of input
- not actual time
- it defines CPU operations
- use case -
  - to make efficient programs
  - ask by interviewer after every sol. you give

### Space Complexity

- amount of space taken by an algo as a function of length of input

## Units to represent Complexity

Big O  $\longrightarrow$  upper bound  $\longrightarrow$  worst case

Theta  $\Theta$   $\longrightarrow$  average case

Omega  $\Omega$   $\longrightarrow$  lower bound  $\longrightarrow$  best case

## Big O Complexities

$O(1)$   $\longrightarrow$  Constant time

$O(n)$   $\longrightarrow$  Linear time

$O(\log_2 n)$   $\longrightarrow$  Logarithmic time

$O(n^2)$   $\longrightarrow$  Quadratic time

$O(n^3)$   $\longrightarrow$  Cubic time

nesting  $\longrightarrow$  multiply  $\longrightarrow$  { } { } { }

in sequence  $\longrightarrow$  add

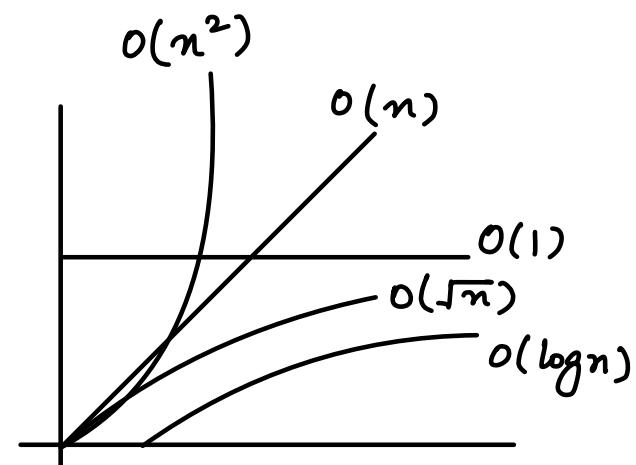
→ { } { }

$$f(n) = 4n^4 + \frac{n^3}{5} + \log n + n \log n \longrightarrow O(n^4)$$

## Complexity Order

$$O(1) < O(\log_2 n) < O(\sqrt{n}) < O(n) < O(n \log_2 n) < O(n^2)$$

$$< O(n^3) < O(2^n) < O(n!) < O(n^n)$$



# ARRAY

W3-L1

- Data Structure to store similar items
  - ↳ same datatype
- Continuous memory location
- use case
  - ↳ for multiple same kind of data

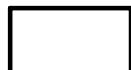
int a[30000]; → 30000 variables are ready

## continuous memory allocation

- ↳ memory wastage
  - if needable memory is present but not in continuous way

int a = 5;

A



a

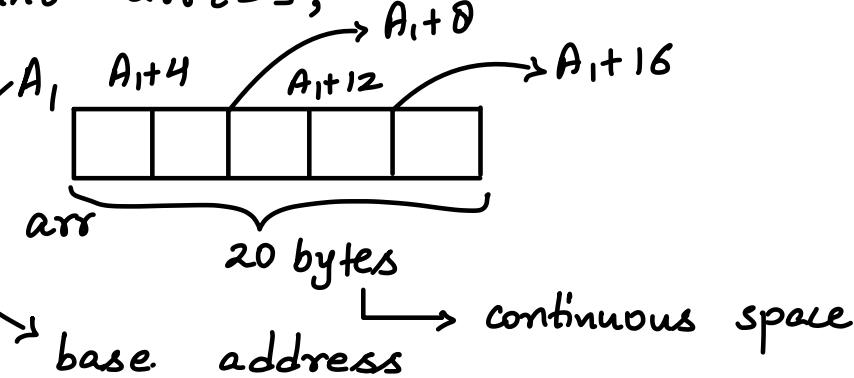
## symbol table

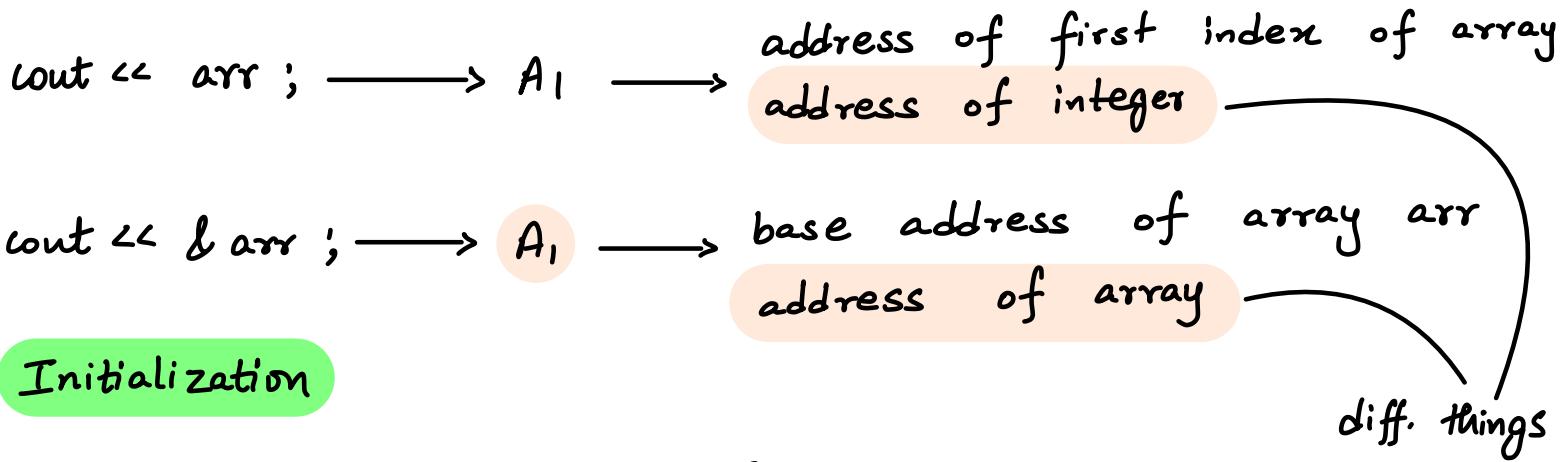
int a ↔ A

int arr ↔ A<sub>1</sub>

## Declaration

int arr[5];





int arr [] = { 2, 4, 6, 8, 10 };

int arr2 [5] = { 2, 4, 6, 8, 10 };

int arr3 [10] = { 2, 4, 6, 8, 10 } ;  $\longrightarrow$  remaining 5 will be 0

//int arr4 [4] = { 2, 4, 6, 8, 10 } ;  $\longrightarrow$  ERROR

int arr5 [10] = { 0 } ;  $\longrightarrow$  initializing all values with 0

### Making array at runtime

int n;

cin >> n;

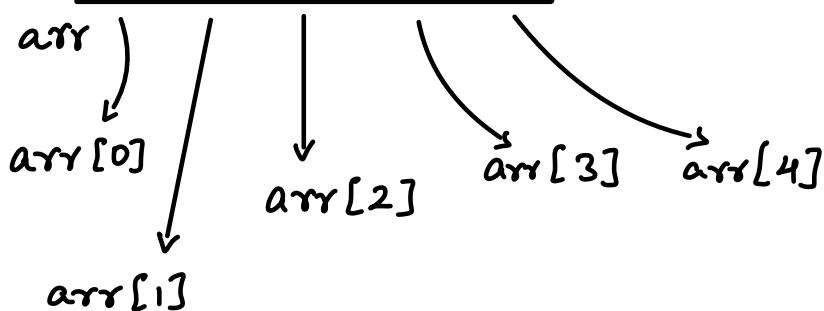
int arr [n];  $\longrightarrow$  BAD PRACTICE

### Index and Access in memory

int arr [5] = { 10, 20, 30 } ;  $\longrightarrow$  0<sup>th</sup> based indexing

$\downarrow$  0 to n-1

A <sub>1</sub>	0	1	2	3	4
10	20	30	0	0	



$\text{arr}[i] \rightarrow \text{value at address } [A_1 + (i * 4)]$

that's why 0 based indexing

BA index due to int (datatype size)

taking input in array

$\text{cin} >> \text{arr}[i];$

due to internal working

## Arrays and Function

$\text{func ( int arr[], int size) \{ }$

}

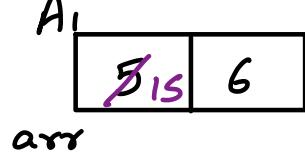
arr here is not an array, it is pointer pointing to first index of array (will learn ahead)

array is passed by reference because pointer is passed by value

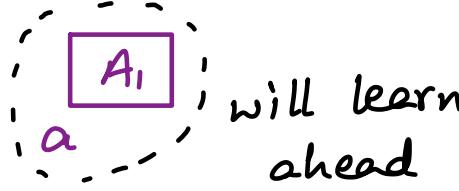
updation in actual array

always pass size alongwith arr

```
int main() {
    int arr[] = {5, 6};
    int size = 2;
    func (arr, size);
    return 0;
}
```



```
void func ( int a[], int size) {
    a[0] = a[0] + 10;
}
```



`sizeof( int );`  $\rightarrow 4$   $\rightarrow$  in bytes

`int arr [5];`

`sizeof( arr );`  $\rightarrow 20$   $\rightarrow$  in bytes

not  $\varnothing$  ( size of pointer )

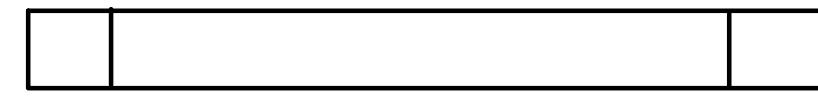
linear search in array

INT-MIN and INT-MAX

→ to find max. , start ans with INT-MIN

→ to find min. , start ans with INT-MAX

2 pointer approach



start  $\qquad$  end

use of 2 variables as extreme points

To find size of array

`int arr [ ] = { 1, 2, 3, 4 };`

`int size = sizeof( arr ) / sizeof( int );`

datatype

## Vector

## W3-L2

- Data structure
- Same as array but dynamic
  - size not fixed
- default size → 0
- if gets full and new items are inserted
  - size gets doubled
- pass by value in functions

## Initialization

- vector <int> arr {10, 20, 30}; → 

10	20	30
----	----	----
- vector <int> arr (5); → 

0	0	0	0	0
---	---	---	---	---
- vector <int> arr (5, -2);
  - size
  - value → 

-2	-2	-2	-2	-2
----	----	----	----	----
- int n; → let n = 5
- vector <int> arr(n); → 

0	0	0	0	0
---	---	---	---	---
- vector <int> arr (n, 10); → 

10	10	10	10	10
----	----	----	----	----

## Insertion -

arr.push\_back (5);

## Remove

arr.pop\_back();

## Size -

arr.size();

→ no. of elements it stores

## declaration

vector <int> arr;

→ arr.size() → 0

→ arr.capacity() → 0

## Empty or Not

arr. empty();  $\longrightarrow$  true if empty

## Capacity -

arr. capacity();  $\longrightarrow$  \* by 2 if arr gets fully filled  
and a new element is inserted

→ no. of elements it can store

→ in initialization, capacity = size in all methods of initialization

sizeof(arr);  $\longrightarrow$  compiler dependent

initially

cout << arr;  $\longrightarrow$  give ERROR

→ Xor  $\longrightarrow$  Cancels out same element

$$0 \wedge \text{ans} = \text{ans}$$

$0 \wedge 1 = 1$   
 $0 \wedge 0 = 0$

## for each loop

```
for (auto val: arr){  
    cout << val << ' ';  
}
```

## 2D Arrays

## W3-L3

→ array of arrays  
→ use case

→ to work on multiple rows and columns

### Declaration -

`int arr [m][n];` →  $m \times n$  elements  
    |      |  
    |      → cols → 0 to  $n-1$   
    |      → rows → 0 to  $m-1$

`int arr [2][3];`

### visualize -

↓  
rows

	0	1	2	cols
0	10	20	30	
1	40	50	60	

### in memory -

→ mapping → arr

0	1	2	3	4	5
10	20	30	40	50	60
			row 1	row 2	

### Access -

`arr [i][j];`  
    |      |  
    |      → col index       $0 \leq j < n$   
    |      |  
    |      → row index       $0 \leq i < m$

### Mapping -

$$\text{linear\_index} = c * i + j$$

no. of cols  
row index  
col index

$$i = \text{linear\_index} / c$$

$$j = \text{linear\_index \% c}$$

## Initialization -

int arr[3][3] = {{10, 20, 30}, {40, 50}}; same  
int arr[3][3] = {10, 20, 30, 40, 50};

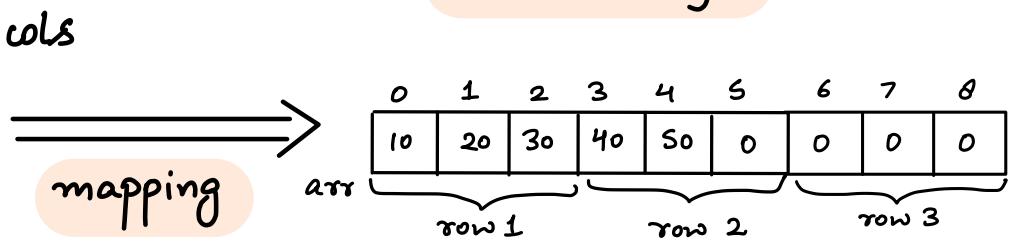
### visualize -

cols →

0	10	20	30
1	40	50	0
2	0	0	0

↓  
rows      0      1      2

### in memory -



## 2D Arrays and function -

→ pass by reference

func (arr[][500], int rows, int cols)

actually arr  
here is  
int (\*)[500]  
(array of pointers),  
not a 2D array

→ cannot leave blank  
why → if dont know, put large value

500 tells size of array of pointers

→ this value and no. of cols  
in array passed in function  
call should be same

## 2D Array -

→ not an array of pointers  
→ array of arrays

```

func( int a [ ][3], int rows, int cols) {
    cout << &a; ----- add. of a -----> A4
    cout << a ;
    cout << a[0];
    cout << &a[0];
    cout << &a[0][0];
    cout << a[0][0]; -----> 10
    cout << sizeof( a); -----> 4
    cout << sizeof( a[0]); -----> 12
}

```

```

int main () {

```

```

    int arr [2][3] = {10, 20, 30, 40, 50};

```

```

    func( arr, 2, 3);

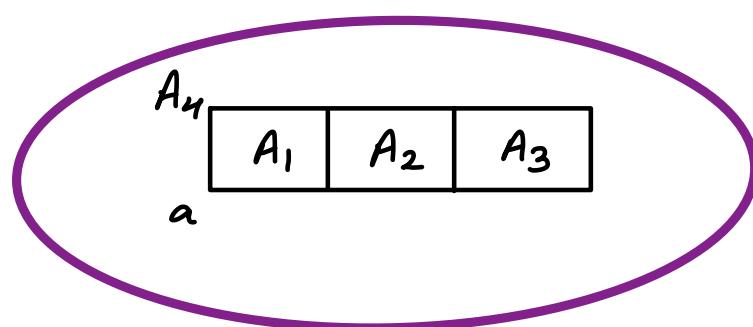
```

```

    return 0;
}

```

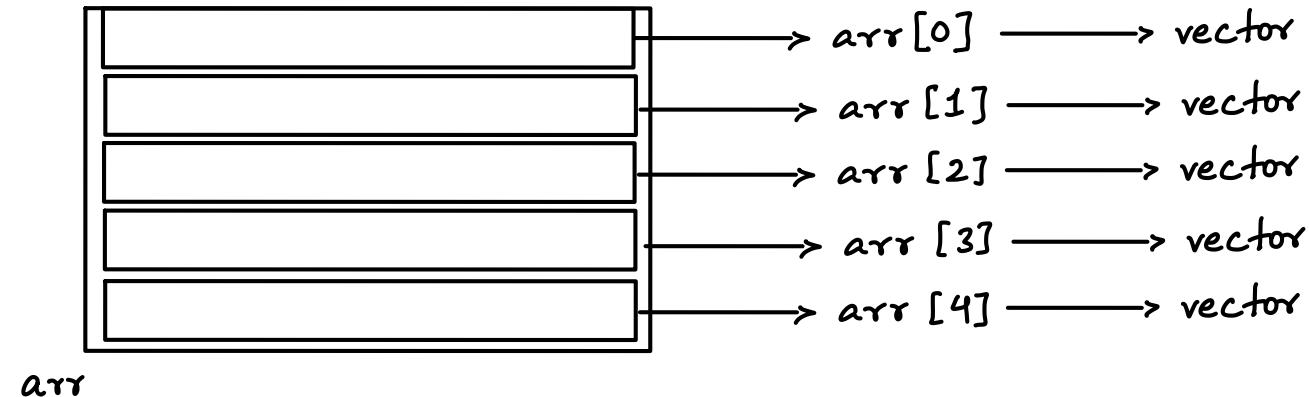
arr	A <sub>1</sub>	10	20	30
	A <sub>2</sub>	40	50	0
	A <sub>3</sub>	0	0	0



# 2D Vector

## Declaration -

```
vector <vector <int>> arr;
```



## Declaration -

```
vector <vector <int>> arr;
```

```
vector <vector <int>> arr (m);
```

## Number of rows

`arr.size()`

## Number of cols

`arr[i].size()`

→ in  $i^{\text{th}}$  row  
→ size of  $i^{\text{th}}$  row

## Initialization

```
vector <vector <int>> arr (rows, (vector <int> (cols, value)));
```

`rows` → no. of rows in arr

`cols` → no. of cols in arr

→ size of 1D vector

`size`      `initial value in 2D vector`  
↑              ↑

initialization of 1D vectors in arr

`value` → initial value in all elements

of all 1D vectors

```
vector<vector<int>> arr(2, vector<int>(4, 101));
```



101	101	101	101
101	101	101	101

arr

### auto keyword -

→ automatically replace with required data type

```
int arr [4]
```

```
for( auto i = 0; i < 4; i++ )  
    cout << arr [i];
```

### : Operator

→ belongs to operator

→ generally used for sequential access

→ map, set, array, vector

```
ex - vector<int> arr {1,2,3};
```

```
for( int i: arr)  
    cout << i;           → 1 2 3
```

```
for( auto i: mapping)  
    cout << i;
```

```
for( auto i: sett)  
    cout << i;
```

## Searching

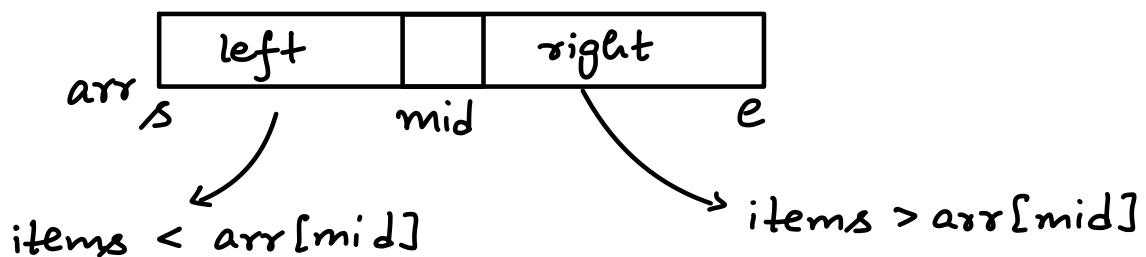
## Linear Search

```
int linearSearch ( vector <int> arr, int target) {
    int n = arr.size();
    for( int i=0; i<n ; i++) {
        if ( target == arr[i])
            return i;
    }
    return -1;
}
```

T.C -  $O(n)$ S.C. -  $O(1)$ 

## Binary Search -

→ condition → sorted order → monotonic function  
 → binary → 2 → left and right search



```

int binarySearch ( int arr[], int n, int target ){

    int s= 0, e=n-1;

    int mid = s+(e-s)/2;

    while ( s<=e ) {

        int element = arr[mid];

        if ( target == element )
            return mid;

        else if ( target < element )
            e=mid-1;  $\longrightarrow$  search in left subarray

        else
            s= mid +1;  $\longrightarrow$  search in right
                           subarray
            mid = s + (e-s)/2;
    }

    return -1;
}

```

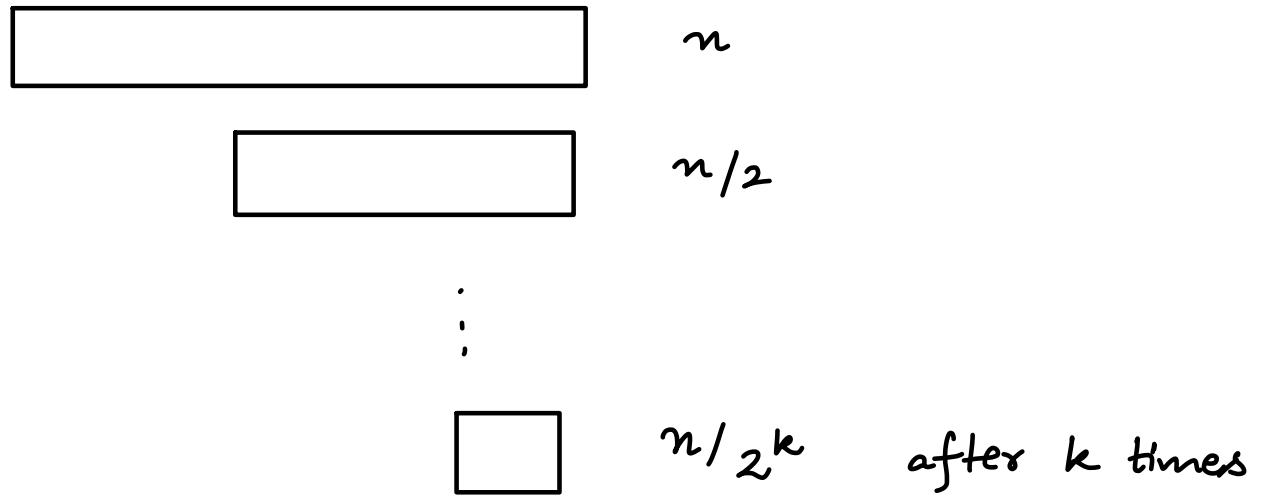
issue in  $mid = \frac{s+e}{2}$ ;  $\longrightarrow$  int overflow  
 if  $s+e > \text{INT\_MAX}$

$\longrightarrow$  So use  $mid = s + \frac{e-s}{2}$ ;

T.C -  $O(\log_2 n)$

S.C. -  $O(1)$

## T.C. of binary Search



at last  $\frac{n}{2^k} = 1$

$$k = \log_2 n$$

So loop runs  $\log_2 n$  times

$$\text{T.C.} = O(\log_2 n)$$

W4-L2

→ Search Space

↳ find range of search space (start & end) in ques of. Binary Search

→ store mid in ans if needed



## In binary search questions

```

while (s <= e) {
    ans = mid;
    s = mid + 1;
    e = mid - 1;
}
left search
right search
    
```

convert

ans = mid, e = mid - 1

left search

OR

s = mid + 1 → right search

s = mid; → right search

e = mid;

```
cout << (int)(-3.74);
```

**W4-L3**

→ - [ int (3.74) ]

→ - (3) → - 3

```
cout << (-22)/7; → -3
```

```
cout << 22/(-7); → -3
```

**Types of ques in binary search**

→ 1<sup>st</sup> type → classic questions

→ lower bound

upper bound

peak in mountain array

can also find array is sorted or not

→ pivot in sorted rotated array

→ pivot index = n-1

search in sorted rotated array

→ 2<sup>nd</sup> type → find in search space (range)

→ predicate function → logic to decide either left or right

→ sqrt of a no.

divide 2 numbers

Advance Binary Search Problems

→ Book allocation

Painters Partition

Aggressive Cows

Roti / Paratha Spoj

Eko Spoj

→ 3<sup>rd</sup> type → observation in index

→ missing element in sorted array

add appearing element in array

Sorting

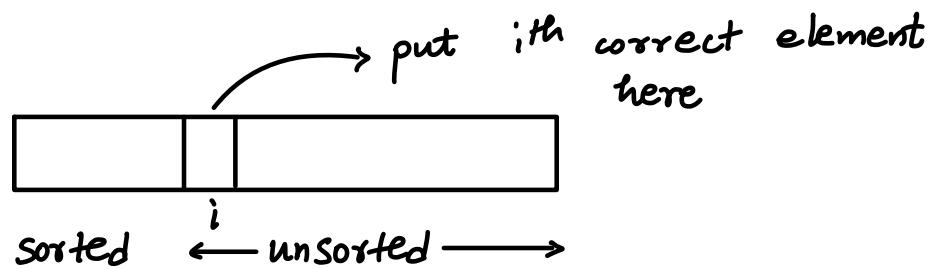
W4-L5

→ putting all elements either in increasing order or decreasing order

## Selection Sort -

- select minimum element and put it in its right position
- select correct element for  $i^{\text{th}}$  index
  - $i^{\text{th}}$  minimum element

```
void selectionSort ( int arr[], int n) {  
    for ( int i=0; i<n-1; i++) {  
        mini = i;  
        for ( int j=i+1; j<n; j++) {  
            if ( arr[mini] > arr[j])  
                mini = j;  
        }  
        swap (arr[i], arr[mini]);  
    }  
}
```



T.C.  $O(n^2)$

S.C.  $O(1)$

Use Case - for small size array

- put  $i^{\text{th}}$  lowest element to its correct position

## Bubble Sort -

→ in  $i^{\text{th}}$  round put  $i^{\text{th}}$  largest element to its correct position using adjacent comparisions

```
void bubbleSort ( int arr[], int n){  
    for( int i=0 ; i<n-1 ; i++) {  
        bool swapping = false;  
        for( int j= 0 ; j<n-i-1 ; j++) {  
            if (arr[j] > arr[j+1]) {  
                swap ( arr [j], arr [j+1]);  
                swapping = true;  
            }  
        }  
        if ( swapping == false)  
            break;  
    }  
}
```

T. C. -  $O(n^2)$  → Worst and average case  
→ reverse sorted

$O(n)$  → best case → already sorted

S.C. -  $O(1)$

Use Case - To put  $i^{\text{th}}$  largest element to its correct position

## Insertion Sort -

→ take an element and insert it on its correct position by shifting

```
void insertionSort( int arr[], int n){  
    for( int i= 1; i<n; i++) {  
        int curr = arr[i];  
        int j= i-1;  
        for( ; j>=0; j--) {  
            if( arr[j] > curr)  
                arr[j+1] = arr[j]; // shifting  
            else  
                break;  
        }  
        arr[j+1] = curr; // inserting  
    }  
}
```

T.C. -  $O(n^2)$  → worst & average case

$O(n)$  → best case

S.C. -  $O(1)$

Use Case - when array is small or when array is partially sorted

## Inbuilt sort function

- sort (arr. begin(), arr. end());
- algo used is Intro sort
  - hybrid of quick sort, heap sort, insertion sort
- min. time than any of other sort

T. C. -  $O(n \log n)$

S. C. - Not Defined

## Stable and Unstable Algorithm

Stable → order preserve after sorting

                  → of same values

### Stable Sorting Algo

2 1 2 2 3

↓  
after sorting

if  $A[i] = A[j]$  ,  $i < j$

then  $A[i]$  comes first before  
 $A[j]$  after sorting too

1 2 2 3

Stable - Bubble Sort, Insertion Sort, Merge Sort,  
Count Sort

Other (unstable) sorting algorithms can be made stable  
by some changes

# T.C. and S.C Sorting Algorithm Table

Algo	S. C.	Worst T.C.	Avg. T. C.	Best T.C.
Selection	$O(1)$	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble	$O(1)$	$O(n^2)$	$O(n^2)$	$O(n)$
Insertion	$O(1)$	$O(n^2)$	$O(n^2)$	$O(n)$
sort func. (intro sort)	not defined	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
merge	$O(n)$	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
quick	$O(n)$	$O(n \log n)$	$O(n \log n)$	$O(n^2)$

# CHAR ARRAYS & STRING

W5-L1

## Char Arrays -

→ Data structure → used to store data

Not Datatype → tells type of data

char ch[5];

g	v	g	v	g
ch				

char ch[] = {'U', 'j', 'j', 'w', 'a', 'l'};

U	j	j	w	a	l	\0
---	---	---	---	---	---	----

char ch[] = "Ujjwal";

U	j	j	w	a	l	\0
---	---	---	---	---	---	----

## Taking input in char array

char ch[7];

cin >> ch[i];

cin >> ch; → by default NULL char will

insert at end

→ '\0'



NULL char refers string termination

→ cin reads until it gets any white space

→ space ''

tab '\t'

endl '\n'

cout << ch; → cout print until it gets delimiter

```
char ch [10];
```

cin >> ch ;  $\longrightarrow$  Ujjwal

store in buffer memory

'U'	'j'	'j'	'w'	'a'	'l'	'\0'
-----	-----	-----	-----	-----	-----	------

buffer

copy in memory of ch

'U'	'j'	'j'	'w'	'a'	'l'	'\0'	gv	gv	gv
-----	-----	-----	-----	-----	-----	------	----	----	----

ch 0 1 2 3 4 5 6 7 8 9

cout << ch ;  $\longrightarrow$  Ujjwal  $\longrightarrow$  stops after 'l'

because of '\0' char

### Overflow -

```
char ch [4];
```

cin >> ch ;  $\longrightarrow$  Ujjwal

cout << ch ;  $\longrightarrow$  Compiler Dependent

### sizeof (char array)

```
char ch [] = "Ujjwal";
```

cout << sizeof(ch) ;  $\longrightarrow$  7

$\longrightarrow$  6 + 1

$\longrightarrow$  NULL char

## get line

`cin.getline (char array, max char to write, delimiter);`

char where taking input stops ←  
↓  
by default 'n' → enter

ex- `cin.getline (ch, 50);`

`cin.getline (ch, 50, '');`

## Char arrays and function

→ pass by reference

`func (char ch []){`

}

Size of char array →  $\frac{\text{size of (ch)}}{\text{size of (char)}}$   
→ 1

## Some inbuilt functions of char array

`strlen(ch);`

`strcmp(ch1, ch2);`

`strcpy(ch1, ch2);`

## Strings

- Datatype
- Not Data Structure
- Dynamic char array
- NULL char at last of string

string str; → empty string created

cin >> str; → Ujjwal

'U'	'j'	'j'	'w'	'a'	'l'	'l'	'\0'
-----	-----	-----	-----	-----	-----	-----	------

cout << str; → Ujjwal str

cout << str.length(); → 6, not 7

## getline -

string str;

getline (cin, str);

## char array

char ch[] = "B\_abba-r";  
cout << ch; → B\_abba-r  
cout << arr.size() → 9

ch[1] = '\0';

ch[6] = '\0';

cout ch; → B

stops just as it gets NULL char

## string

string str = "B\_abba-r";  
cout << str; → B\_abba-r  
cout << str.length() → 8  
cout << str.size() → 8

str[1] = '\0';

str[6] = '\0';

cout << str; → Babbar

Runs till the length of string

```
string str = "babbar";
```

```
sort(str.begin(), str.end()); -----> aabbbr
```

```
sort(str.begin(), str.end(), greater<char>());
```

-----> rbbbbaa

### Custom Comparator -

```
bool cmp (char a, char b) {
```

```
    return a < b; -----> can be any function  
}                                         according to need
```

```
bool cmp2 (char a, char b) {
```

```
    return a > b;
```

```
}
```

```
int main () {
```

```
    string str = "babbar";
```

```
    sort(str.begin(), str.end(), cmp);
```

```
    cout << str; -----> aabbbr
```

```
    string str2 = "babbar";
```

```
    sort(str.begin(), str.end(), cmp2);
```

```
    cout << str2; -----> rbbbbaa
```

```
    return 0;
```

```
}
```

Hash Map

WILL LEARN  
LATER

→ Data structure

→ data stored in key-value pair

### Initialization

`map<key datatype, value datatype> map-name;`

`map<int, char> m;` → ordered map

`m[0] = 'a';`

`m[1] = 'b';`

`m[25] = 'z';`

`cout << m[0];` → 'a'

`cout << m[25];` → 'z'

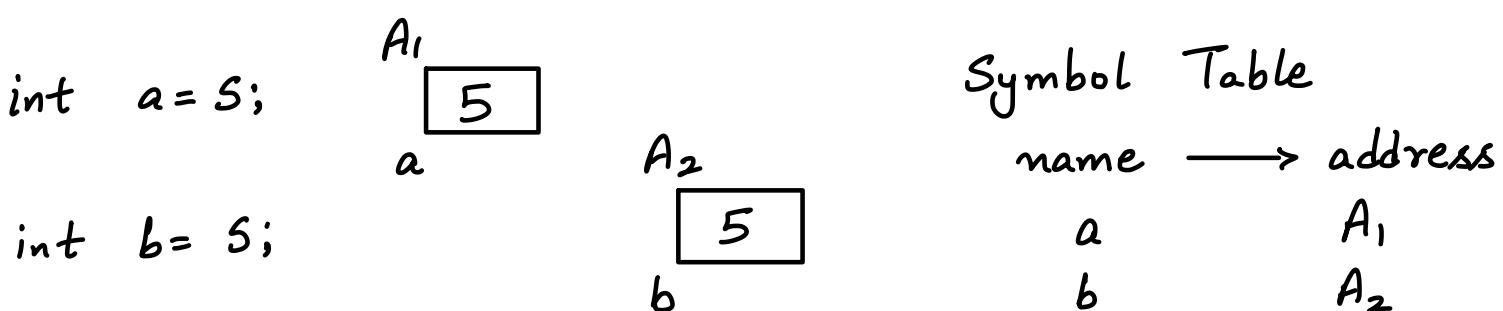
`cout << m[20];` → " → NULL char

`cout << (int) m[20];` → 0

# SYMBOL TABLE

W6-L1

- Data Structure
- Stores mapping of variable name, datatype & memory location address → Done by OS
- entries in symbol table can't be changed



entry of a in symbol table  
is made

cout << a; → 5

## & Address Of Operator

cout << &a; → A<sub>1</sub> → address of  
variable a in  
memory

Not 100%  
Sure

$A_2 = A_1 \pm 4$  → because of consecutive  
variables in memory

int datatype  
of a and b

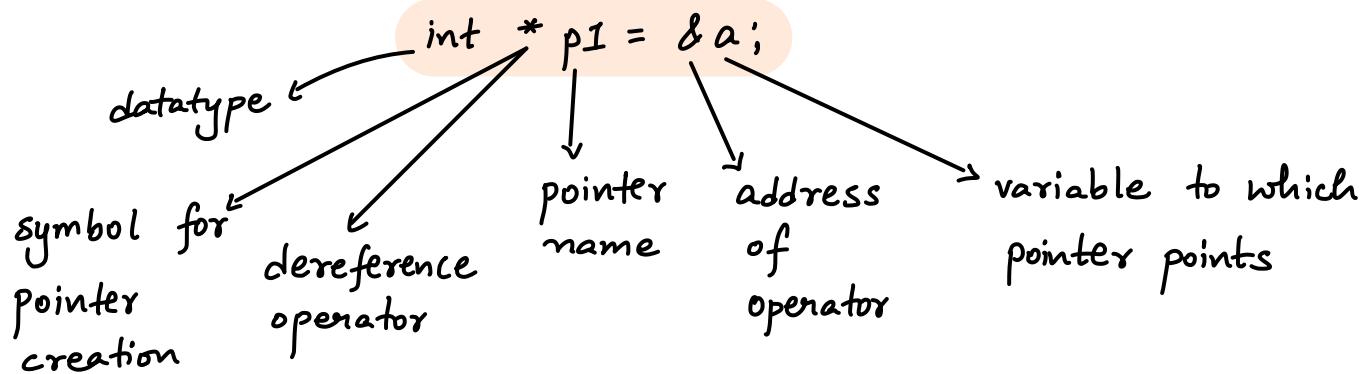
# POINTERS

→ stores address

→ NOT a datatype, just a variable storing address of another variable

int a = 5;

int \* pI = &a; pI is a pointer to integer datatype



string s = "Ujjwal 2327";

string \* ptr = &s → ptr is a pointer to string datatype

int a = 5;

int \* ptr = &a;

cout << a; → 5

cout << \* a; → ERROR

cout << &a; → A<sub>1</sub>

cout << ptr; → A<sub>1</sub>

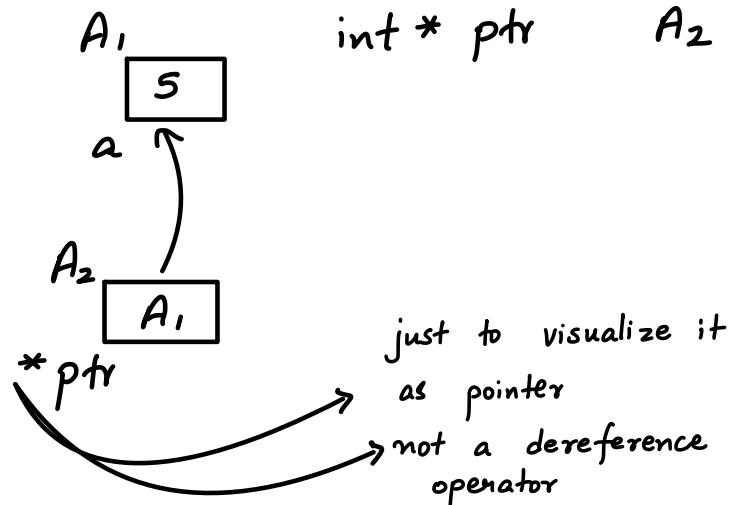
cout << \* ptr; → 5

cout << &ptr; → A<sub>2</sub>

symbol table

int a A<sub>1</sub>

int \* ptr A<sub>2</sub>



`*ptr` → value at (address stored in `ptr`)  
→ dereference operator

`&ptr` → address of `ptr`

size of pointer

`sizeof(ptr);` → 8 → Always  
64 bit architecture  
depends on  
architecture  
compiler implementation  
memory organization  
it stores address,  
datatype does not matter

Use case of pointer

- dynamic memory allocation
- memory management
- pointer arithmetic
  - ↳ go from one location to other
- pass by reference in array
- to create pointer to function
  - ↳ passing a function inside another function as an argument

`int *ptr;` → **VERY BAD PRACTICE**  
`cout << ptr;` → `gv` → Segmentation fault

`*ptr` gv  
A1

ptr points to a memory location that may not be of its program

## Segmentation fault -

→ using other's memory

## NULL Pointer

int \* ptr = 0;

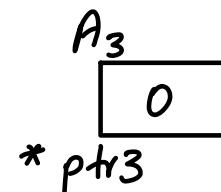
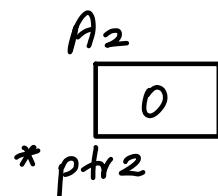
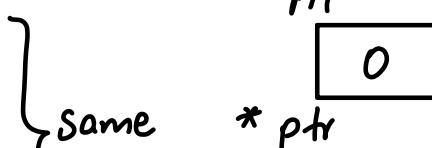
int \* ptr2 = NULL;

int \* ptr3 = nullptr;

cout << ptr ; → 0

cout << \*ptr ; → ERROR

cout << &ptr ; → A<sub>1</sub>



Segmentation fault

## Arithmetic Operations In Pointers

int a = 5;

a++;

int \* ptr = &a;

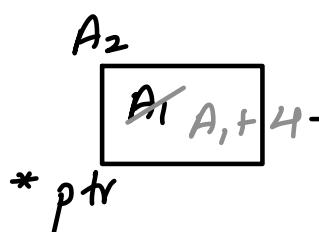
\*ptr++;

ptr++;



a

A<sub>2</sub>



A<sub>1</sub> to A<sub>1</sub> + 3 has already be taken by integer a, so next address will be A<sub>1</sub> + 4

```
int a = 10;
```

```
int *ptr = &a;
```

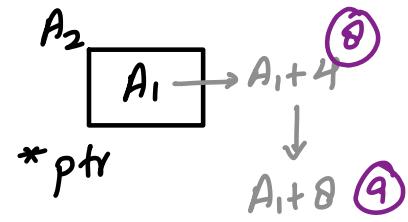
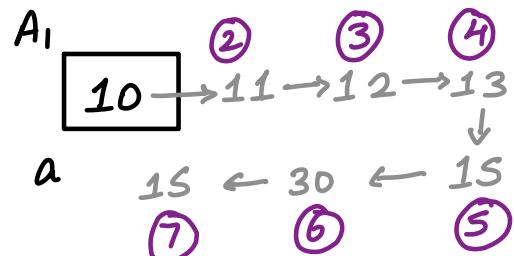
a 10

&a A<sub>1</sub>

ptr A<sub>1</sub>

\*ptr 10

&ptr A<sub>2</sub>



① \*ptr \* 2

20

② (\*ptr) ++

10

③ ++(\*ptr)

12

④ a = a + 1

13

⑤ \*ptr = \*ptr + 2

15

⑥ \*ptr = \*ptr \* 2

30

⑦ \*ptr =  $\frac{*ptr}{2}$

15

⑧ \*(ptr++)

15

⑨ \*(++ptr)

9v

```
int a = 5;
```

```
int *ptr = a; → ERROR
```

### Copying a pointer

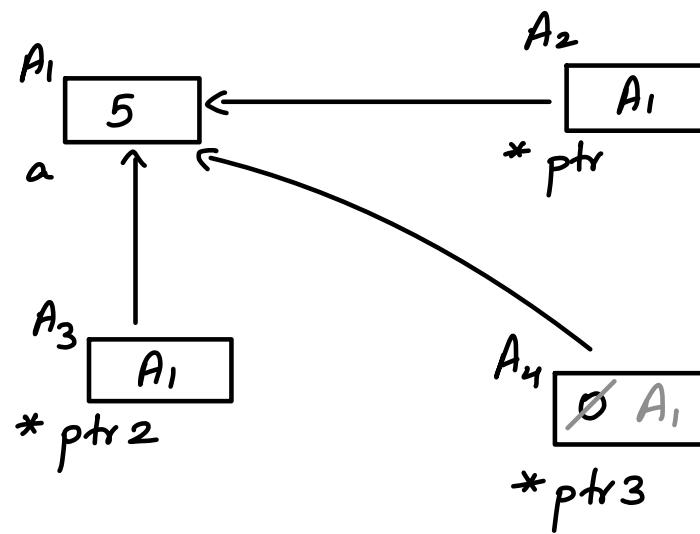
```
int a = 5;
```

```
int *ptr = &a;
```

```
{ int *ptr2 = ptr;
```

```
{ int *ptr3 = 0;
```

```
{ ptr3 = ptr;
```



# ARRAYS & POINTERS

W6-L2

int arr[ ] = { 10, 20, 30, 40, 50 };

→ CONSTANT pointer to the first element of array

cannot change

also does not have separate memory

arr[i] → element at index i

& arr[i] → address of arr[i]

cout << arr[0]; → 10

cout << &arr[0]; → A<sub>1</sub>

{ cout << arr ; → A<sub>1</sub>

array name returns add. of 1<sup>st</sup> index of array

cout << &arr ; → A<sub>1</sub>

→ from symbol table (add. of array)

same address unlike pointers

int \*ptr = arr ;

cout << \*ptr ; → 10

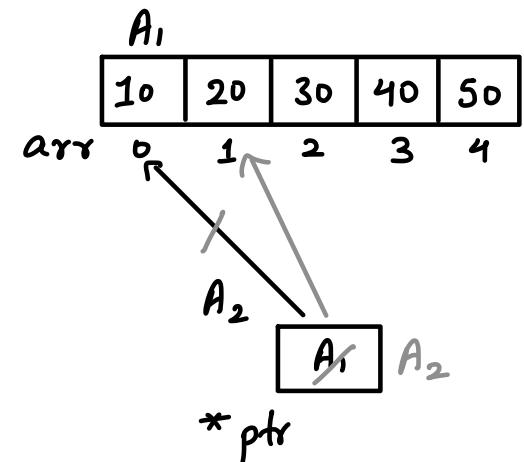
cout << ptr ; → A<sub>1</sub>

cout << &ptr ; → A<sub>2</sub>

cout << \*arr ; → 10

cout << \*(&arr) ; → 10

cout << \*(&arr[0]) ; → 10



Symbol table

type	name	address
int(*)[5]	arr	A <sub>1</sub>
int *	ptr	A <sub>2</sub>

cout << \*arr + 1;  $\longrightarrow$  11

cout << \*(arr + 1);  $\longrightarrow$  20

cout << \*(arr + 2);  $\longrightarrow$  30

cout << arr[2];  $\longrightarrow$  30

cout << 2[arr];  $\longrightarrow$  30

arr[i]  $\longleftrightarrow$  \*(arr + i)  $\longleftrightarrow$  i[arr]

arr++;  $\longrightarrow$  ERROR  $\longrightarrow$  Entry in symbol table

ptr++;  $\longrightarrow$  A<sub>1</sub> + 4  $\longrightarrow$  can't be change

→ You can access subpart of an array using pointers

int \*ptr = arr;

cout << \*(ptr + 2);  $\longrightarrow$  40

cout << \*(ptr + 100);  $\longrightarrow$  gv / segmentation fault /  
out of bound error

### Arrays / Array pointers

int arr[] = {10, 20, 30};

① cout << arr;  $\longrightarrow$  A<sub>1</sub> }  
cout << &arr;  $\longrightarrow$  A<sub>1</sub> }  
Same

### Pointers / Normal pointers

int \*ptr = arr;

① cout << ptr;  $\longrightarrow$  A<sub>1</sub> }  
cout << &ptr  $\longrightarrow$  A<sub>4</sub> }  
diff.

② arr++;  $\longrightarrow$  ERROR

② ptr++;  $\longrightarrow$  VALID

③ sizeof(arr);  $\longrightarrow$  3 \* 4 = 12

③ sizeof(ptr)  $\longrightarrow$  8  
↓  
size of address

```
int * p1 = arr;
```

```
int * p2 = &arr; -----> ERROR
```

```
int * p3 = &arr[0];
```

## CHAR ARRAYS & POINTERS

```
char ch[] = "Babbar";
```

```
char * ptr = ch;
```

```
char * p = &ch; -----> ERROR
```

```
char * p2 = &ch[0]; -----> valid
```

```
cout << ch; -----> Babbar
```

not an address

```
cout << ptr; -----> Babbar
```

not an address

whole string from that  
location until NULL char

cout implementation

is diff. in char

pointers and char arrays

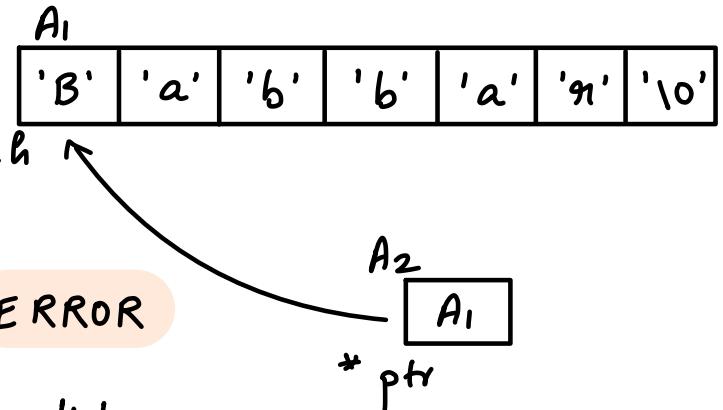
```
cout << &ch; -----> A1
```

```
cout << ch[0]; -----> B
```

```
cout << &ch[0]; -----> Babbar
```

```
cout << *ptr; -----> B
```

```
cout << &ptr; -----> A2
```



$$ch[i] \longleftrightarrow * (ch + i) \longleftrightarrow i[ch]$$

→  $ch$ ,  $\&ch[0]$ , and  $ptr$  values are addresses  
but due to diff. cout implementation in char pointers  
and char arrays,  
 $cout \ll ch$ ,  $cout \ll \&ch[0]$  and  $cout \ll ptr$   
will give Babbar

`char ch[] = "Sherbano";`

`char *ptr = ch;`

`cout \ll ch ;` → Sherbano

`cout \ll *ch ;` → S

`cout \ll \&ch ;` → A<sub>1</sub>

`cout \ll *(ch + 3);` → 91

`cout \ll ptr ;` → Sherbano

`cout \ll \&ptr ;` → A<sub>2</sub>

`cout \ll *(ptr + 3);` → 91

`cout \ll ptr + 2;` → erbano

`cout \ll *ptr ;` → S

`cout \ll ptr + 8;` → " → NULL char

`cout \ll ptr + 9;` → gv

cout << ch[0];  $\longrightarrow$  S

cout << &ch[0];  $\longrightarrow$  Sherban

cout << &(\*ch);  $\longrightarrow$  Sherban

## CHAR AND POINTER

char ch = 'k';

char \* ptr = &ch;

cout << ch;  $\longrightarrow$  k

cout << &ch;  $\longrightarrow$  k.....

$\rightarrow$  gv  
 $\rightarrow$  print until it gets '\0'

cout << ptr;  $\longrightarrow$  k.....

cout << &ptr;  $\longrightarrow$  A<sub>2</sub>  $\rightarrow$  gv  
 $\rightarrow$  print until it gets '\0'

cout << \*ptr;  $\longrightarrow$  k

## Behind The Scenes

char ch[10] = "Babber";

$\longrightarrow$  2 step process

① 

'B'	'a'	'b'	'b'	'a'	'r'	'\0'
-----	-----	-----	-----	-----	-----	------

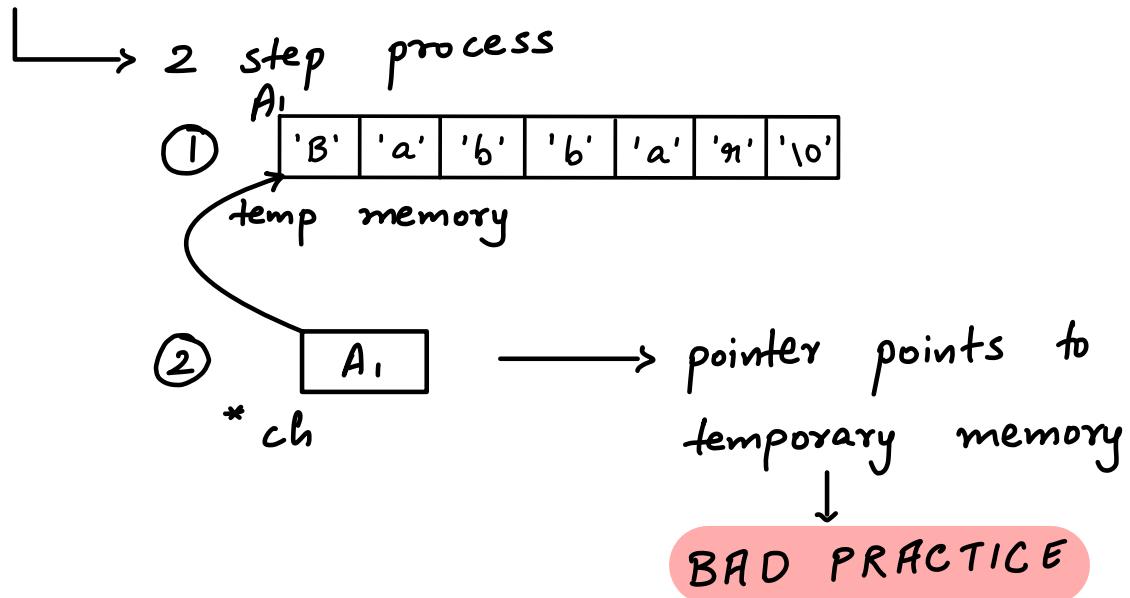
temp memory  $\downarrow$  copy

② 

'B'	'a'	'b'	'b'	'a'	'r'	'\0'	gv	gv	gv
-----	-----	-----	-----	-----	-----	------	----	----	----

ch

```
char * ch = "Babbar"
```



## POINTERS WITH FUNCTIONS

→ pass by value

a copy of pointer is made

→ but simulates pass by reference

→ as in case of arrays & functions

→ pointer is passed

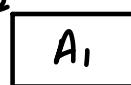
```
int func ( int arr[]){
```

cout << arr; → A1

cout << \*arr; → 10

cout << &arr; → A2

cout << sizeof(arr); → 8

A2  
  
copy of pointer  
is created

```

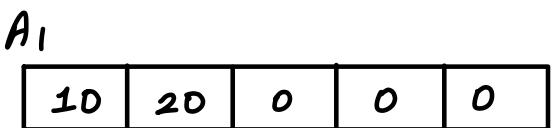
int func2 ( int * arr ) {
    cout << arr;           → A1
    cout << * arr;         → 10
    cout << &arr;           → A3
    cout << sizeof(arr);   → 8
}

```

pointer is passed  
 $A_3$   
 $A_1$   
 $*arr$   
copy of pointer  
is created

```
int main() {
```

```
    int arr [5] = {10, 20};      arr
```



```
    cout << arr;           → A1
```

```
    cout << * arr;         → 10
```

```
    cout << &arr;           → A1
```

```
    cout << sizeof(arr);   → 5*4 = 20
```

```
    func (arr);
```

```
    func (arr 2);
```

```
    return 0;
```

```
}
```



→ whole array will not pass

→ only array pointer / base address will pass

→ pass by reference for array

→ copy of pointer pointing to base address will be created

```

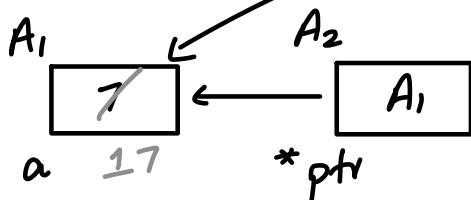
int main() {
    int a = 7;
    int * ptr = &a;
    update(ptr);
    return 0;
}

```

```

void update( int * p) {
    ① *p = *p + 10;
    ② p++;
}

```



$$\begin{aligned}
 *p &= A_1 + 4 \\
 *A_1 &= *A_1 + 10 \\
 *A_1 &= 7 + 10 = 17 \\
 a &= 17
 \end{aligned}$$

## Function to Pointers in HW

### Basic Mathematics for DSA

### Sieve of Eratosthenes Theorem

### W6-L3 R

→ to find no. of prime numbers between 1 & n

Steps-

- make an array of size n and mark them all as primes from 2 to n
- Start from 2 till end, mark all no.  $> 2$  comes in the table of 2 as non prime
- Do above step for numbers 2 to  $< n$  if they are marked prime
- Count all remaining marked prime numbers

```
int countPrimes ( int n) {
```

```
if (n <= 1)
```

```
    return 0;
```

```
vector <int> isPrime (n, true);
```

```
isPrime [0] = isPrime [1] = 0; // making both 0
```

```
int ans = 0;
```

```
for ( int i=2 ; i<n ; i++) {
```

```
    if ( isPrime [i]) {
```

```
        ans ++;
```

```
        for ( int j= 2*i ; j<n ; j+= i)
```

```
            isPrime [j] = false;
```

```
}
```

```
}
```

```
return ans;
```

```
}
```

$i * i < n$

↳ to optimize T.C.  
as  $2i$  to  $(i-1)*i$  are  
already marked when  
 $i = 2$  to  $(i-1)$

TC -  $O(n * \log(\log n))$

SC -  $O(n)$

$$n \left[ \frac{n}{2} + \frac{n}{3} + \frac{n}{5} + \frac{n}{7} + \frac{n}{11} + \dots \right]$$

$$n^2 \left[ \frac{1}{2} + \frac{1}{3} + \frac{1}{5} + \frac{1}{7} + \frac{1}{11} + \dots \right]$$

$$n \log(\log n)$$

Same with **segmented sieve**  $\longrightarrow$  having high & low

## GCD/HCF and LCM

→ Greatest Common Divisor

$$\rightarrow \text{gcd}(a, b) = \text{gcd}(a - b, b) \quad a > b$$

$$\text{gcd}(a, b) = \text{gcd}(b - a, a) \quad b > a$$

$$\text{gcd}(a, b) = \text{gcd}(a \% b, b) \quad a > b$$

$$\text{gcd}(a, b) = \text{gcd}(b \% a, a) \quad b > a$$

takes more time bcz of \% op.

Use first method as \% is heavy operator and computer takes more time

→ Euclid Algorithm

Apply above formula till one of the parameters becomes 0

And other one will be GCD

```
int gcd( int a, int b) {
```

```
    if (a == 0)
```

```
        return b;
```

```
    else if (b == 0)
```

```
        return a;
```

```
    while (a > 0 && b > 0) {
```

```
        if (a > b)
```

```
            a = a - b;
```

```
        else
```

```
            b = b - a;
```

```
}
```

```

}
    return (a == 0) ? b : a;
}

```

TC -  $O(\min(a, b))$

## LCM

$$\text{lcm} * \text{gcd} = a * b$$

$$\text{lcm} = \frac{a * b}{\text{gcd}}$$

## Modulo Arithmetic

$$\rightarrow a \% n \rightarrow [0, n)$$

$$\rightarrow (a + b) \% n = (a \% n) + (b \% n)$$

$$(a - b) \% n = (a \% n) - (b \% n)$$

$$(a * b) \% n = (a \% n) * (b \% n)$$

$$(\dots((a \% n) \% n) \dots \% n) = a \% n$$

## Fast Exponentiation

$$\rightarrow a^b = a^{b/2} * a^{b/2} \quad , \quad b \text{ is even}$$

$$a^b = [a^{b/2} * a^{b/2}] * a \quad , \quad b \text{ is odd}$$

```
int fastExponentiation ( int a, int b){  
    int ans = 1;  
    while (b){  
        if (b & 1)  
            ans = ans * a;  
        a = a * a;  
        b >>= 1; // b = b >> 1 or b = b / 2  
    }  
    return ans  
}
```

dry run code on  $2^5$ , if confusion

T.C. -  $O(\log n)$

Learn wild, void and dangling pointers from dashboard

after learning dynamic allocation

# MULTI LEVEL POINTER

W6-L4

int a = 5;

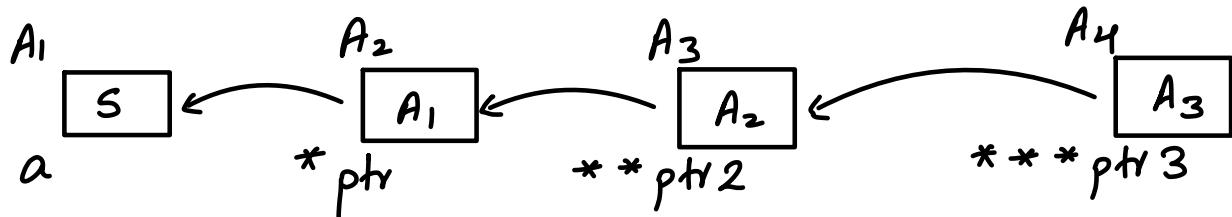
int \*ptr = &a;

int \*\*ptr2 = &ptr  $\longrightarrow$  double pointer

$\longrightarrow$  ptr2 is a pointer to int \* data

int \*\*\*ptr3 = &ptr2;

$\longrightarrow$  ptr3 is a pointer to int \*\* data



a  $\longrightarrow$  5

&a  $\longrightarrow$  A1

&&a  $\longrightarrow$  ERROR

ptr  $\longrightarrow$  A1

&ptr  $\longrightarrow$  A2

\*ptr  $\longrightarrow$  5

ptr2  $\longrightarrow$  A2

&ptr2  $\longrightarrow$  A3

\*ptr2  $\longrightarrow$  A1

\*\*\*ptr2  $\longrightarrow$  5

apply dereference operator 2 times

ptr3  $\longrightarrow$  A3

&ptr3  $\longrightarrow$  A4

\*ptr3  $\longrightarrow$  A2

\*\*\*ptr3  $\longrightarrow$  A1

\*\*\*\*ptr3  $\longrightarrow$  5

```

int main(){
    int a = 5;
    int *ptr = &a;
    int **ptr2 = &ptr;
    func (ptr2);
    return 0;
}

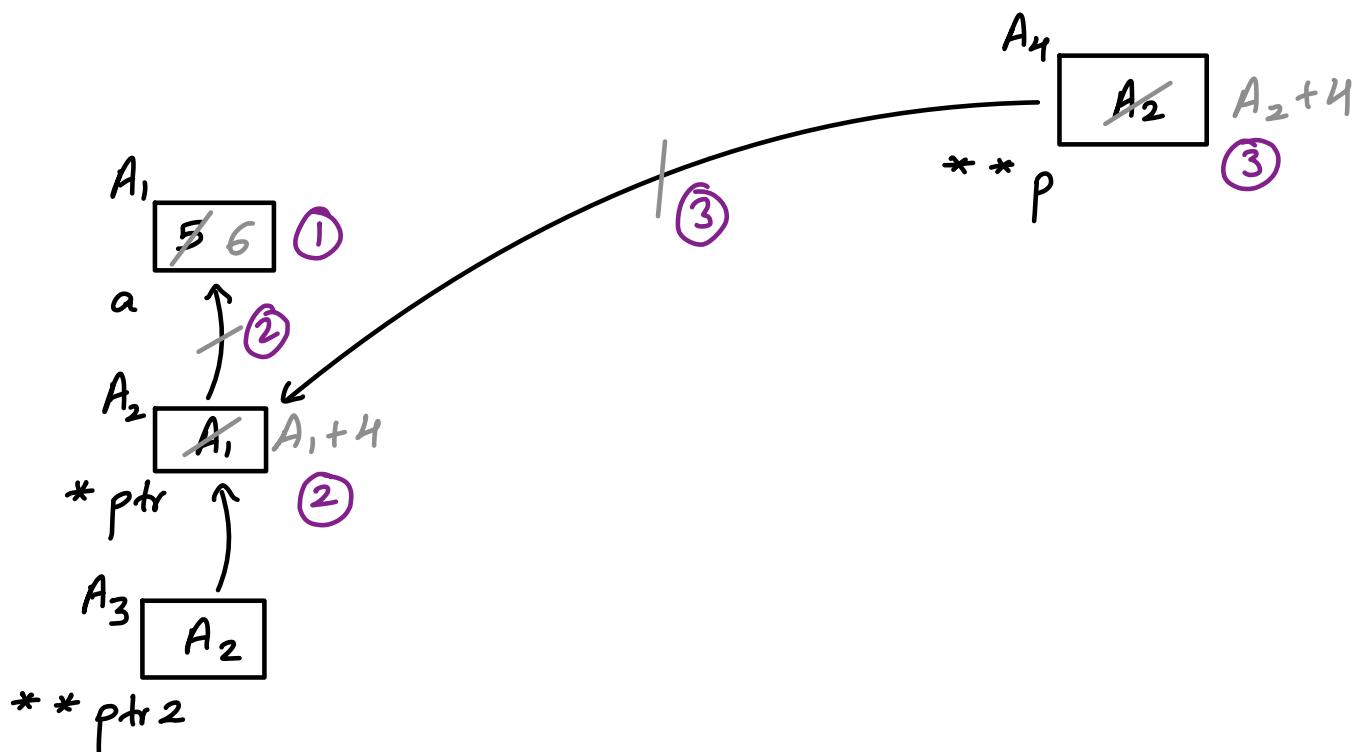
```

```

void func( int ** p){
    ① (** p) ++ ;
    ② (* p) ++ ;
    ③ p ++ ;
}

```

both are same



```

int a = 5;
int *p = &a;
int **q = p; -----> ERROR

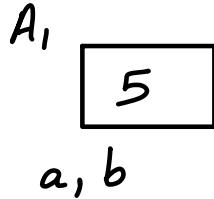
```

## REFERENCE VARIABLE

- alternate of pointers
- diff. names of same variable
  - same memory location
- only new entry in symbol table,  
no other memory will allocate
- can access a variable by diff. names

int a = 5;

int &b = a;



Symbol Table

a	A <sub>1</sub>
b	A <sub>1</sub>

## Use Case

- reference variable can't be set to NULL  
pointers can be set to NULL  
So more safety in reference variable  
Always points to valid object / variable
- pointers are difficult to understand,  
more readability in reference variable
- generally used to implement **PASS BY  
REFERENCE** concept

# PASS BY REFERENCE

- reference variable passes in function
- does not create copy

```
int main () {
    int a = 5;
    update (a);
    update2 (&a);
    int *ptr = &a;
    //update3 (&a); → ERROR
    update3 (ptr);
    return 0;
}
```

constant  
add. in  
pass by  
reference

```
void update ( int &x ) {
```

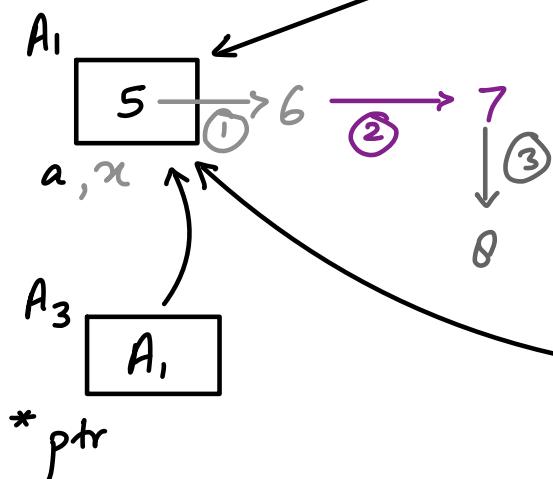
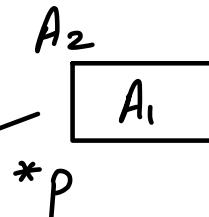
① x++;  
}

PASS BY  
REFERENCE

```
void update2 ( int * p ) {
```

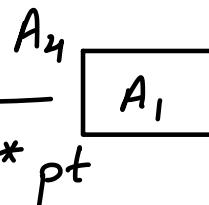
② (\* p)++;  
}

PASS BY  
VALUE



```
void update3 ( int * &pt ) {
```

③ (\* pt)++;  
}



```

vector<int> func( vector<int> &arr) {
    for (int i=0; i< arr.size(); i++)
        arr[i]++;
    return arr;
}

```

```

int solve( int &arr ) {
    cout << arr;
}

```

this is reference variable  
of type int

```

int solve( int &arr[] )

```

```

int main() {

```

```

vector<int> arr { 1, 2, 3, 4 };

```

```

vector<int> ans = func(arr);

```

```

for (auto i: ans)

```

```

    cout << i;           -----> 2 3 4 5

```

array of reference  
is not allowed

```

solve( arr );           -----> ERROR

```

vector != int

```

int arr2[] = { 1, 2, 3 };

```

```

solve( arr2 );           -----> ERROR

```

int[3] != int

```

return 0;
}

```

# RETURN BY REFERENCE

→ return a variable, not a value

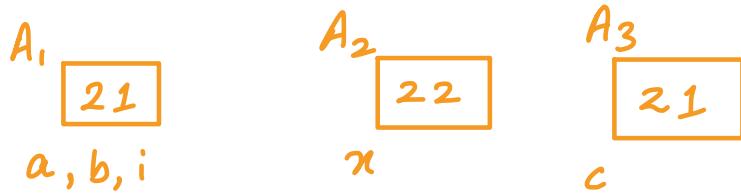
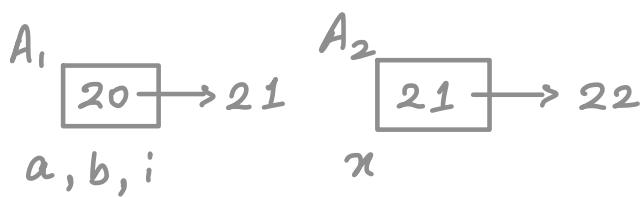
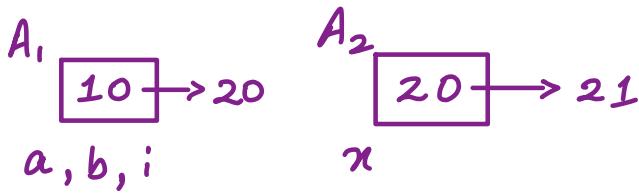
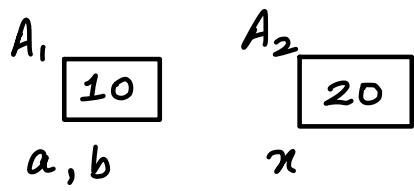
→ To implement atleast 1 of 2 conditions must be true.

1. passing a reference variable
2. passing a global variable

## passing a reference variable

```
int main () {  
    int a = 10;  
    int & b = a;  
  
    int x = 20;  
  
    ref(a) = x;  
  
    x++;  
  
    ref(b) = x;  
  
    x++;  
  
    int c = ref(a);  
  
    int &d = ref(a);  
  
    return 0;  
}
```

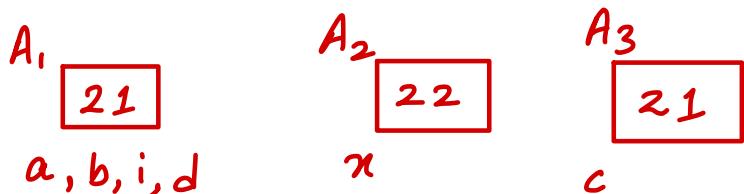
```
int & ref( int &i) {  
    return i;  
}
```



```

int c = ref(a) = i;
int c = 21;

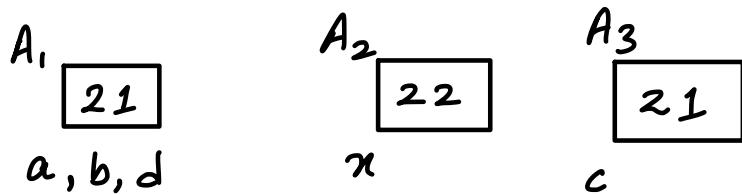
```



```

int &d = ref(a) = i;
int &d = i;

```



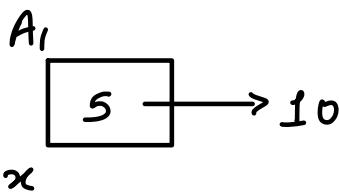
## passing a global variable

```
int x = 5;
```

```
int main () {  
    ref () = 10;
```

```
    ref2 () = 20; → ERROR  
    return 0;
```

```
}
```



```
int & ref () {  
    return x;  
}
```

```
int ref2 () {  
    return x;  
}
```

returning a value, not variable

10 = 20;

→ that's why ERROR

## pass by value but return by reference

```
int main () {  
    int a = 10;  
    int & b = a;  
    int x = 20;  
    ref (a) = x;
```

$x++;$

$ref (b) = x;$

$x++;$

BAD PRACTICE

ERROR

```
int & ref ( int temp ) {  
    return temp;  
}
```

returning a variable stored  
in temporary memory

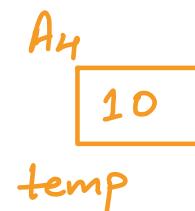
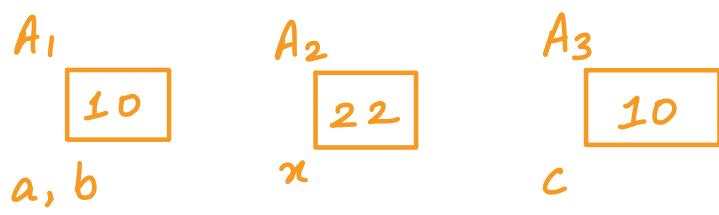
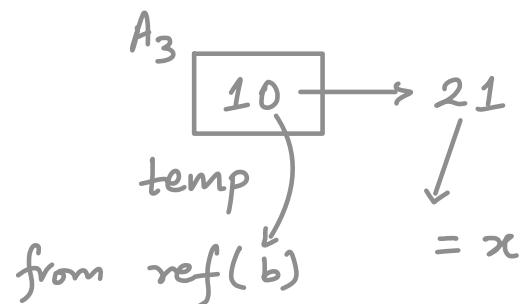
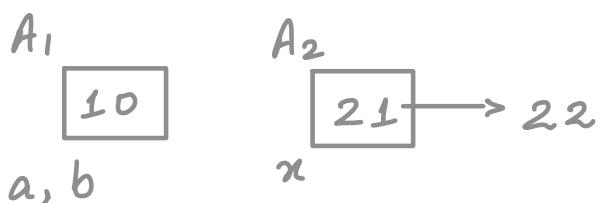
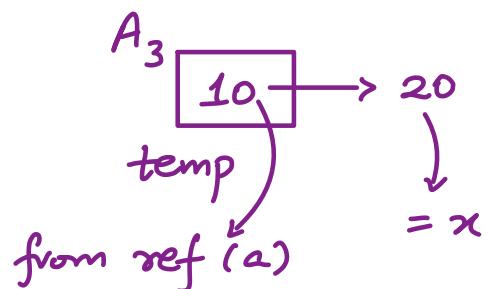
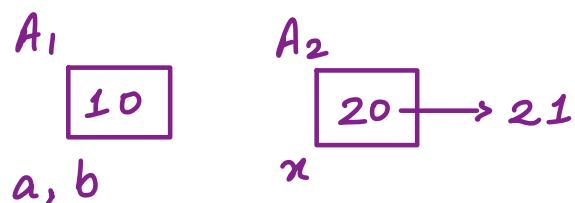
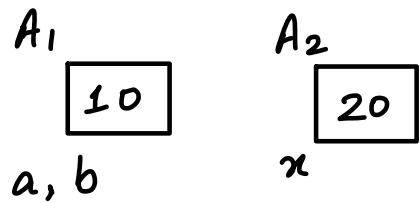
```
int c = ref(a);
```

```
int &d = ref(a);
```

```
return 0;
```

```
}
```

lets assume it will run, then this would happen



```
int c = ref(a) = temp;  
int c = temp;  
int c = 10
```

$A_1$   
10  
 $a, b$

$A_2$   
22  
 $x$

$A_3$   
10  
 $c$

$A_4$   
10  
 $temp, d$

$d$  (variable of main function refers to  
a temporary memory

 BAD PRACTICE

DON'T DO THIS  
AT HOME

Have similarity  
IMP QUESTION

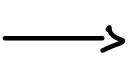
```
int main () {  
    int * ptr = solve ();  
    return 0;  
}
```

```
int * solve () {  
    int a = 5;  
    int * p = &a;  
    return p;  
}
```

$A_2$   
\*  
ptr  
 $A_1$

$A_1$   
a  
5  
 $A_3$   
 $*p$   
 $A_1$

pointing to a temp  
memory, 'a' variable  
will finished outside  
solve function so value  
of 'a' can be change with time

 BAD PRACTICE

## Some Important Questions

W6-A

→ `int *ptr = 0;`  
`int a = 10;`  
`*ptr = a; → runtime ERROR`  
`cout << *ptr;`

→ `char *ch = 'a';`  
`char *ptr = &a;`  
`ch++;`  
`cout << *ptr; → 'b'`

→ `int a[] = {1, 2, 3, 4, 5};`

`int *p = a++; → ERROR`

`cout << *p;`

→ pointer of static variables  
are constant pointers

→ pointer of dynamic  
memory allocation variables  
can be change

→ `char ch = "hello";`  
`cout << ch; → hello`  
`ch++; → ERROR`  
`cout << ch;`

name of array refers  
to base address

→ `double arr [] = {2.5, 7.9, 50.25};`

`double * ptr = arr;`

`ptr = ptr + 0.25;` → **ERROR**

`cout << ptr;`

→ pointer arithmetic op-  
can only be done  
using integers

→ `int arr [] = {1, 2, 3, 4, 5};`

`int * ptr1 = arr;`

`int * ptr2 = arr + 3;`

`cout << ptr2 - ptr1;` → **3, NOT 12**

→ `int a = 5;`

`int * ptr = &a;`

`int ** ptr2 = &ptr;`

`ptr2 = &a;` → **ERROR** → `int **` can't convert  
to `int *`

`cout << *ptr2;`

→ `int a = 5;`

`int * p = &a;`

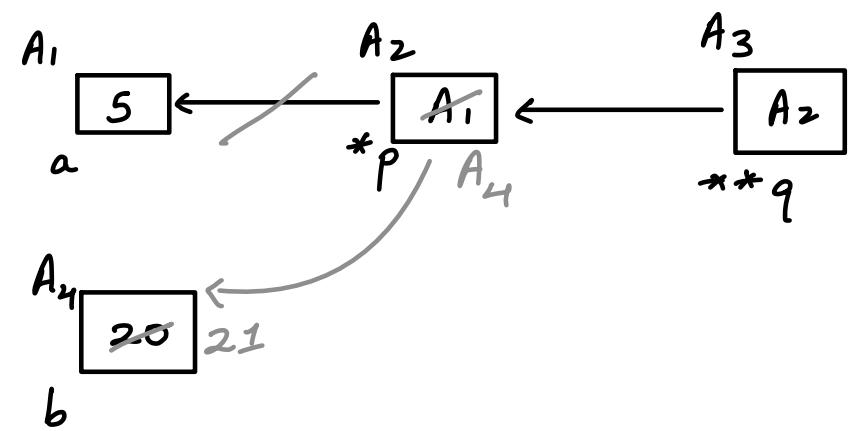
`int ** q = &p;`

`int b = 20;`

`* q = &b;`

`(*p) ++;`

`cout << a << ' ' << b;` → **5 21**





int a = 5;

int \* ptr = &a;

int \*\* ptr2 = &ptr;

int \*\* ptr3 = &(&a); → ERROR

cout << \*\* ptr3;

address of (address in  
memory location)

(doesn't make any sense)

W6-L5

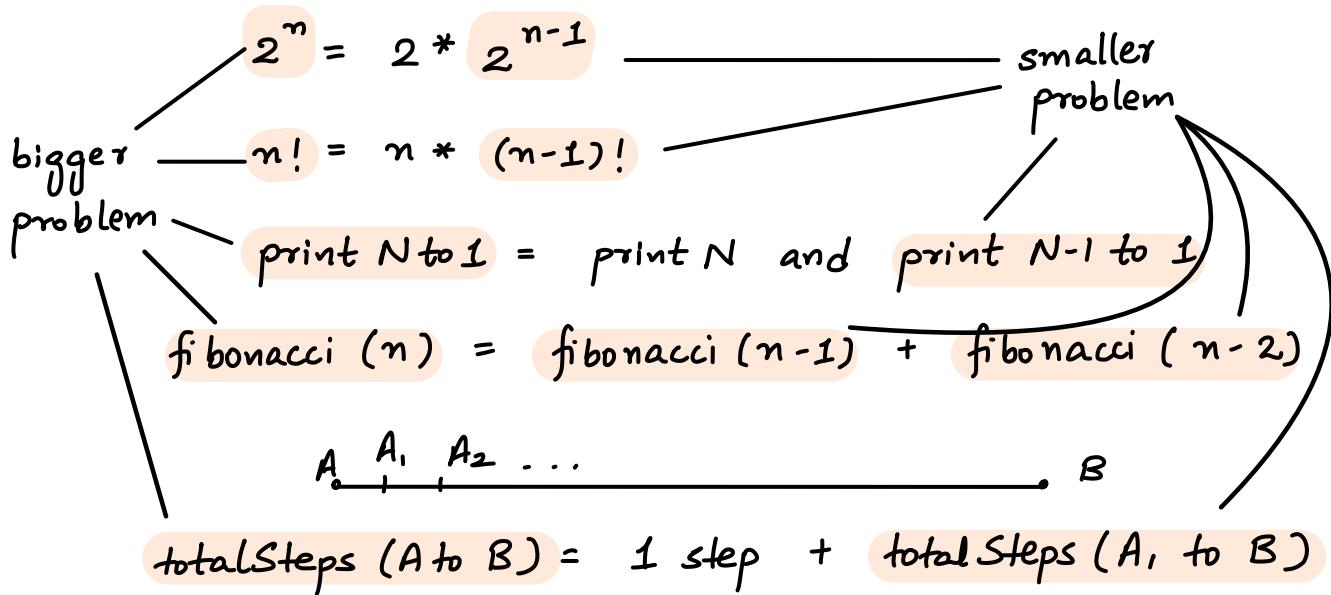
POINTER IMP DOUBT

(IN DASH BOARD)

# RECURSION

W7-L1

- When a function calls itself
- When sol. of bigger problem depends on similar smaller problem(s)



## Components of Recursion

- Base Case / Stopping cond. → return statement
- Recurrence Relation (recursive call)
- Processing → optional

## Head Recursion

- recurrence relation before processing

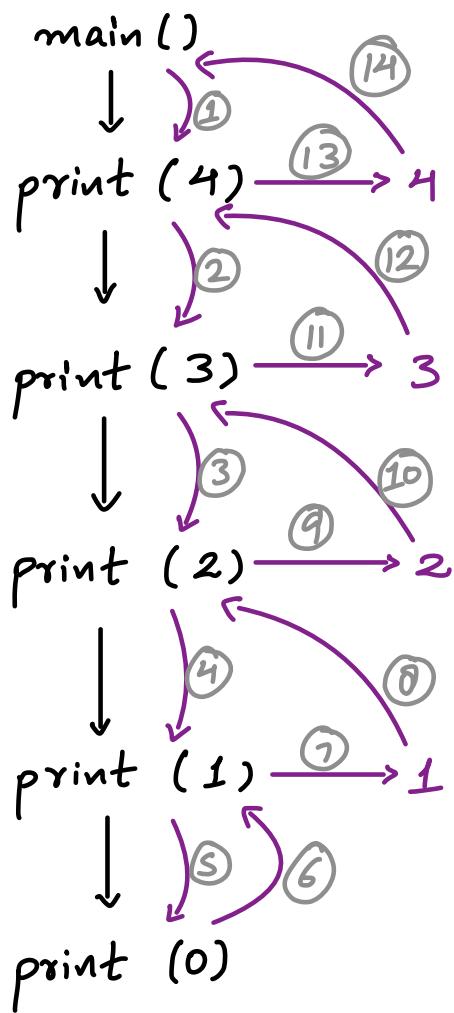
## Tail Recursion

- recurrence relation after processing

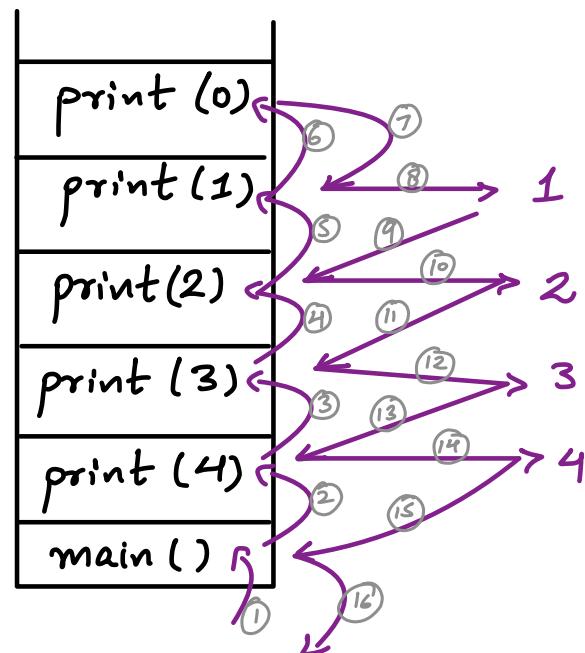
```
int main () {
    int n = 4;
    print (n);
    return 0;
}
```

```
void print ( int n) {
    // base condition
    if ( n==0)
        return;
    // recurrence relation
    print (n-1);
    // processing
    cout << n;
}
```

### Recursion Tree



### Call Stack



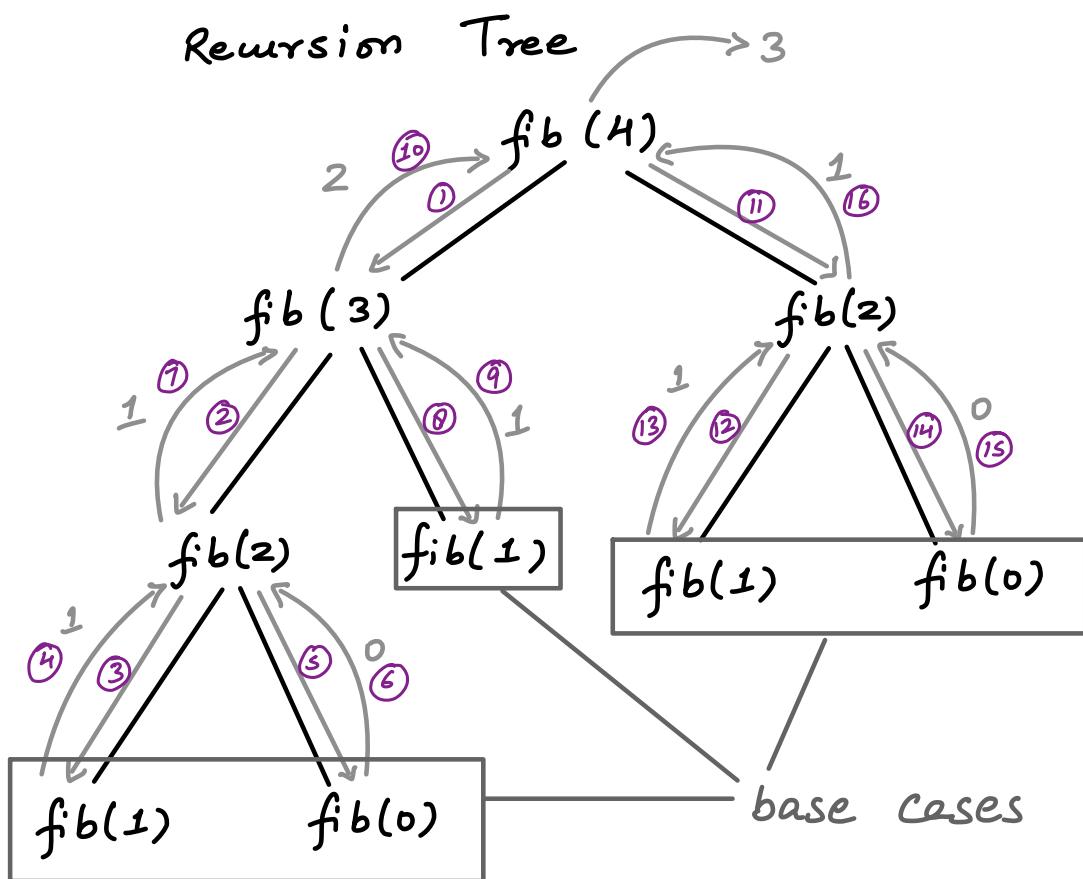
Output - 1 2 3 4

```
int main(){
    int n = 4;
    int ans = fib(n);
    cout << ans;
    return 0;
}
```

```
int fib( int n){
    if( n == 0 || n == 1)
        return n;
    return fib(n-1) + fib(n-2);
}
```

$n \rightarrow 0 \ 1 \ 2 \ 3 \ 4$

$\text{fib}(n) \rightarrow 0 \ 1 \ 1 \ 2 \ 3$



Magical line for Recursion

Ek case solve krdo, baaki recursion sambhal lega

→ Just believe on it, dont doubt on recursion

→ func ( vector <int> arr, int i, int &ans)

W7-L2

pass by reference

if we want to retain value of ans after function call

→ Try to pass everything by reference IF POSSIBLE

↳ SC ↓es

TC ↓es (no copying of variables again & again)

→ to reverse answer, you can use recursion

Integer literal with a leading 0

n = 0100; → interpreted as an octal number

cout << n; → 64 → convert 0100 octal to decimal

cin >> n; → (0100)

cout << n; → 100 → no conversion as  
cin reads 0100 as 100

Entry in function call stack

W7-L3

↳ Computer has track of variables of that function about their memory location and all in symbol table

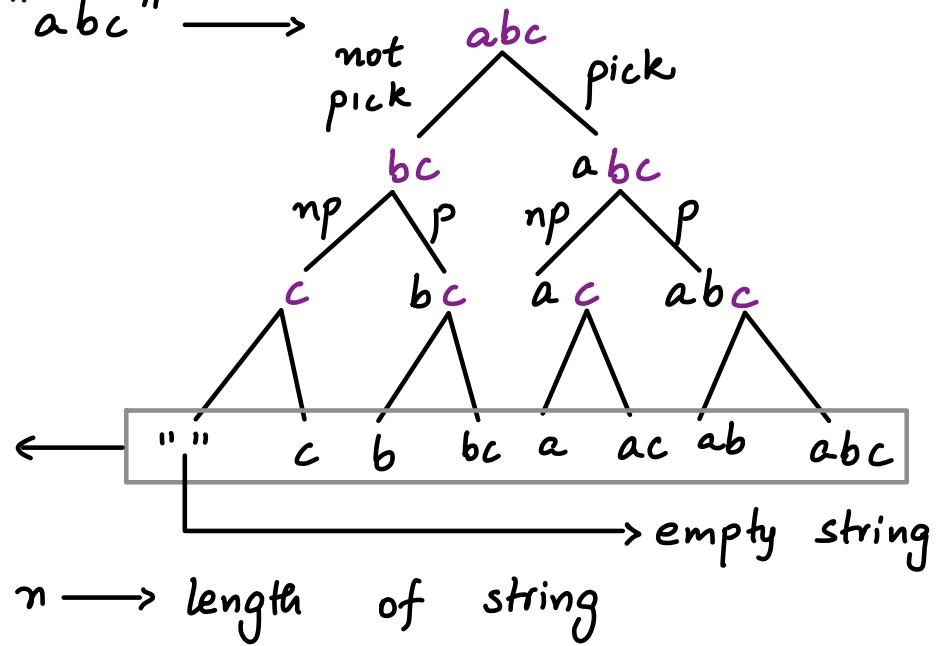
→ Expression can't be pass by reference

## Subsequences

→ Made by either including or excluding every element, but order remains same

→ ex- "abc" →

subsequences of string "abc"



→  $2^n$ ,  $n \rightarrow$  length of string

## Arithmetic Operations on Strings

$s1 = "Ujjwal";$

$s2 = "2327";$

$cout \ll "Ujjwal" + "2327";$  → ERROR

$s1 = s1 + s2;$

$cout \ll s1;$  → "Ujjwal2327" → Concatenate

- , \* , / , % → NOT VALID in strings

## Coin change problem

W7-L4

→ find min. coins equivalent to given amount

```
int coinChange( vector<int> arr, int amount) {  
    if (amount == 0)  
        return 0;  
    if (amount < 0)  
        return INT_MAX; // means INVALID or  
                           cant be changed  
    int mini = INT_MAX;  
    for (int i=0; i < arr.size(); i++) {  
        mini = min (mini, coinChange (arr, target - arr[i]));  
    }  
    // now min. coins req. has been found  
    if (mini == INT_MAX)  
        return INT_MAX; // means INVALID or  
                           cant be changed  
    else  
        return mini + 1;  
}
```

Type 1 - inclusion exclusion pattern → for using  
either this or that subsequence questions

Type 2 - for loop in recursion

→ If the recursion ques seems tough, use void function and pass ans by reference in function

## TC & SC of Recursive Solutions

## W7-R

T.C. → Can be found by recursive relation or recursive tree

S.C. → found using max depth of function call stack  
└→ max space used in any particular time instant in function call stack

### Linear Search

$$f(n) = k + f(n-1) \quad \text{Base case} \rightarrow \text{for } n=0$$

### Recursive Relation Method -

$$T(n) = k + T(n-1)$$

$$T(n-1) = k + T(n-2)$$

:

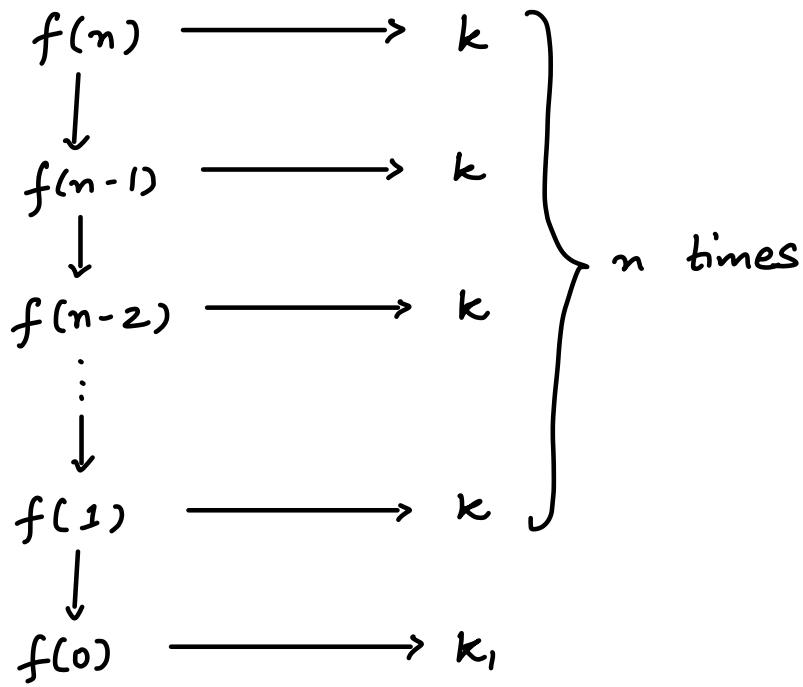
$$T(0) = k_1$$

$$T(n) = nk + k_1$$

$$T(n) = O(n)$$

T.C -  $O(n)$

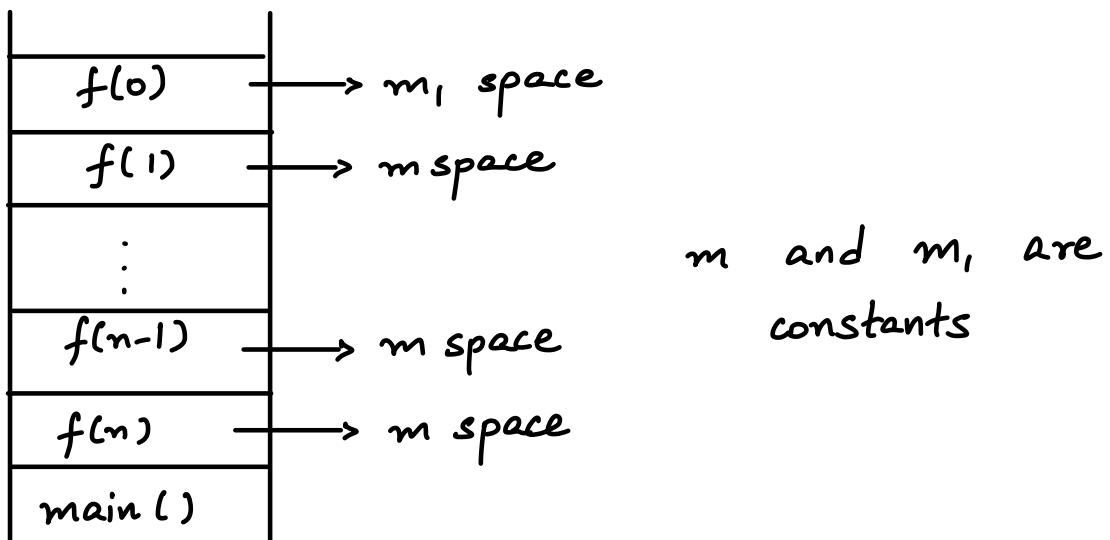
## Recursive Tree Method - Best method



$$T(n) = nk + k_1$$

$$T(n) = O(n)$$

## Space Complexity -



$$SC = mn + m_1$$

$$SC = O(n)$$

→ max depth

## Binary Search

$$f(n) = k + f(n/2); \quad \text{base case} \rightarrow \text{for } n=0$$

## Recursive Relation Method

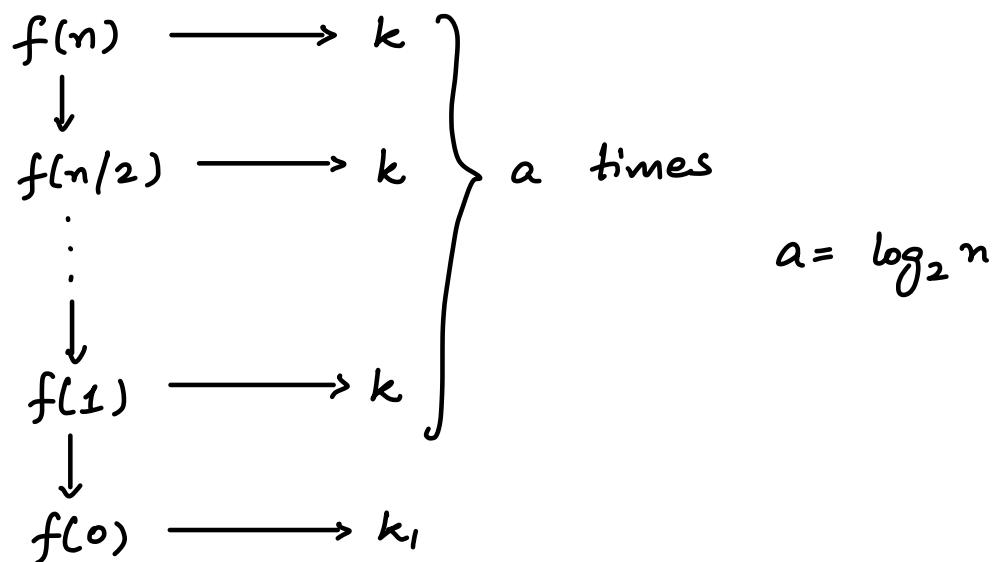
$$\begin{aligned} T(n) &= k + T(n/2) \\ T(n/2) &= k + T(n/4) \\ &\vdots \\ T(1) &= k + T(0) \\ T(0) &= k_1 \end{aligned} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} a \text{ times} \quad a = \log_2 n$$

$$T(n) = ak + k_1$$

$$T(n) = k \log_2 n + k_1$$

$$T(n) = O(\log_2 n)$$

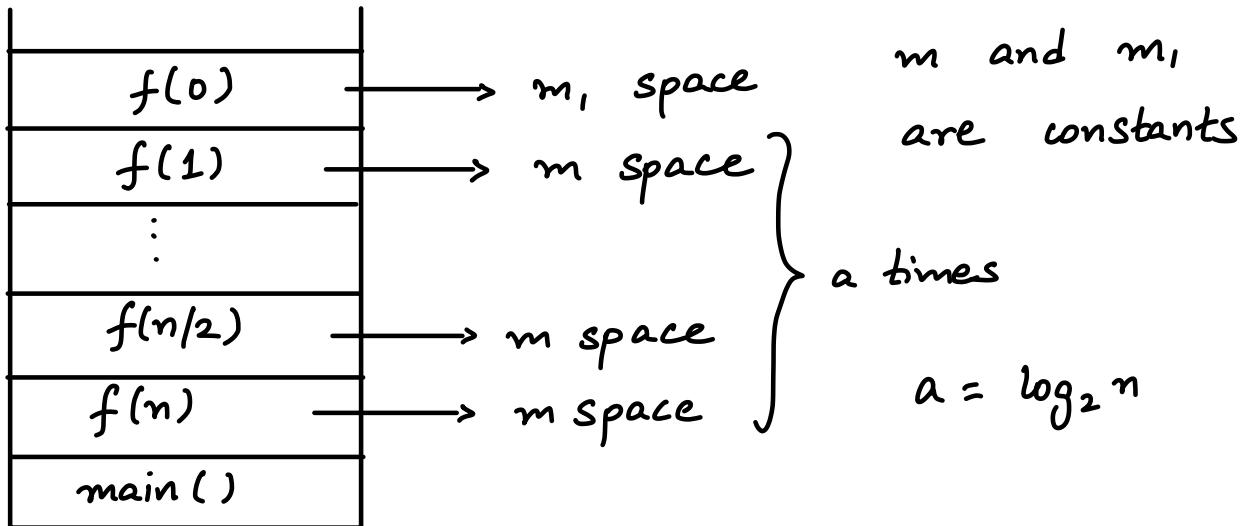
## Recursive Tree Method



$$TC = k \log_2 n + k_1$$

$$TC = O(\log_2 n)$$

## Space Complexity -



$$SC = m \log_2 n + m_1$$

$$SC = O(\log_2 n)$$

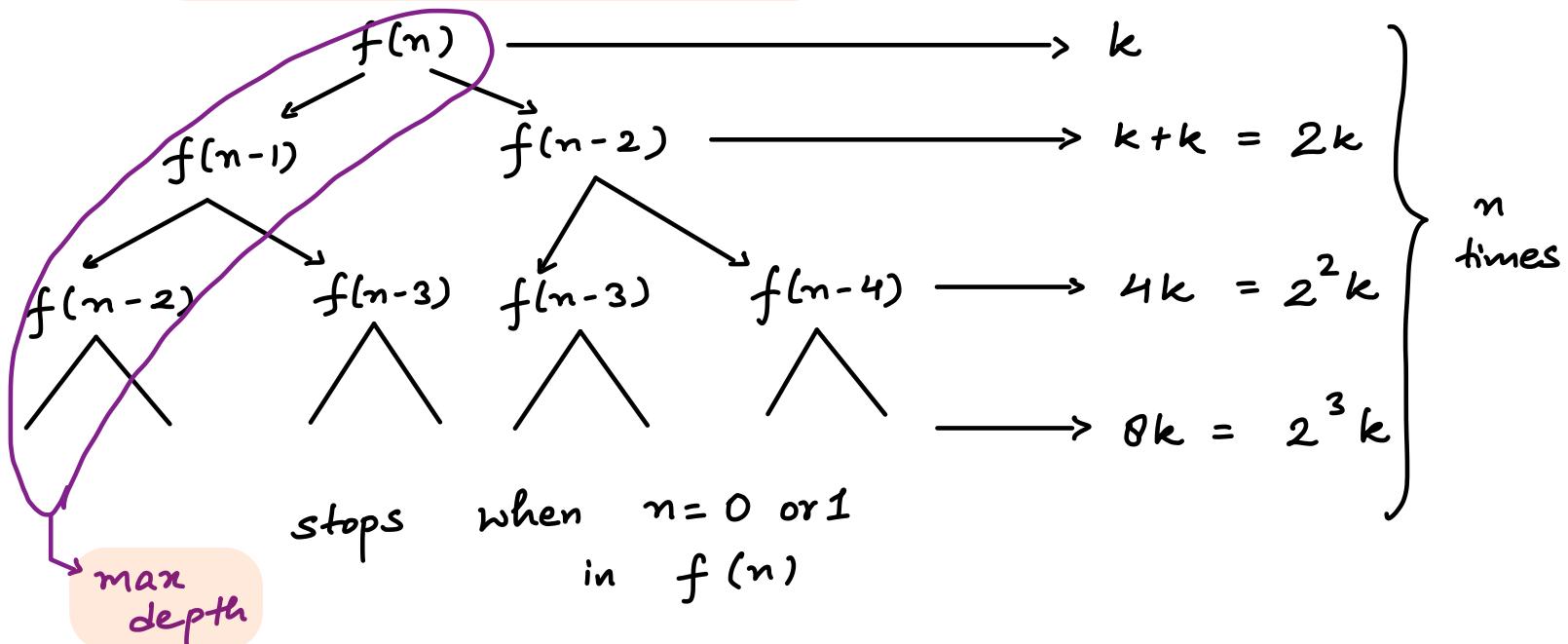
→ max depth

## Fibonacci Series

$$f(n) = k + f(n-1) + f(n-2)$$

base case → for  $n = 0$  or  $1$

## Recursive Tree Method



$$T.C \leq [k + 2k + 2^2k + \dots + 2^{n-1}k]$$

$$T.C. \leq k * [1 + 2 + 2^2 + \dots + 2^{n-1}]$$

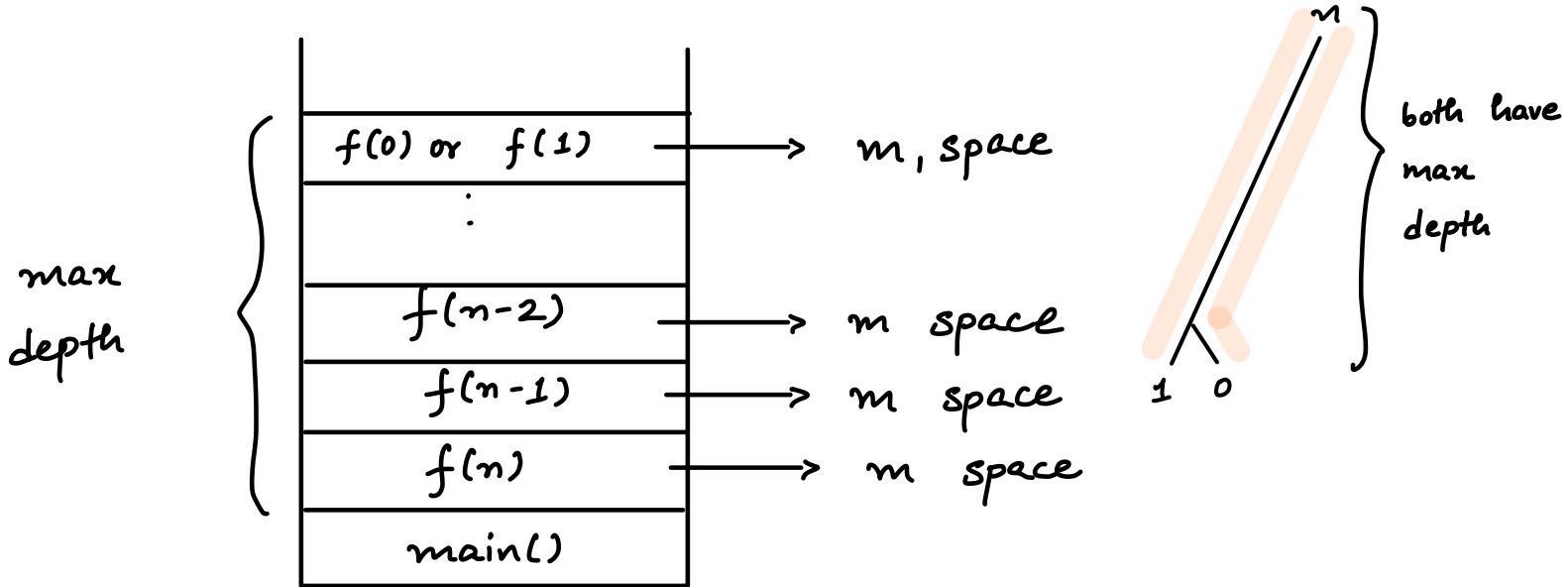
assume  
for simplicity  
and for large  
numbers

$$T.C = O(2^n)$$

→ exponential TC

→ very bad

## Space Complexity

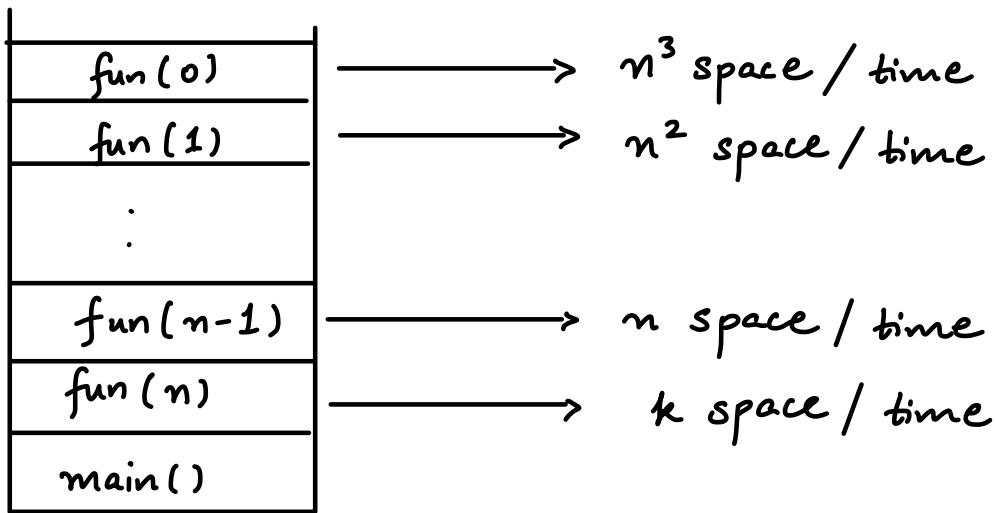


$$SC = m(n-1) + m,$$

$$SC = O(n)$$

→ max depth

if this is such a case



$$S.C. - n * n^3$$

↳ max SC in any call

$$T.C. - n * n^3$$

↳ max T.C. in any call

## Divide & Conquer

↳ using recursion

W8-L1

## Merge Sort

- Divide the array in 2 halves
- Sort them
- Merge those 2 sorted subarrays

## Standard Merge Sort

```
void merge( vector <int> &arr, int s, int e) {  
    int mid = e - (s + e)/2;  
    int len1 = s - mid + 1;  
    int len2 = e - mid;  
    vector <int> left (len1);  
    vector <int> right (len2);  
    int i=0, j=0, k=s;  
    while ( i < len1)  
        left [i++] = arr [k++];  
    while ( j < len2)  
        right [j++] = arr [k++];  
    i=0, j=0, k=s;
```

```

while ( i < len1 & & j < len2 ) {
    if ( left [i] <= right [j] )
        arr [k++] = left [i++];
    else
        arr [k++] = right [j++];
}

while ( i < len1 )
    arr [k++] = left [i++];

while ( j < len2 )
    arr [k++] = right [j++];

}

void mergeSort ( vector <int> &arr, int s, int e ) {
    if ( s >= e )
        return;

    int mid = s + (e-s)/2;

    mergeSort ( arr, s, mid );
    mergeSort ( arr, mid+1, e );

    merge ( arr, s, e );
}

```

due to copy in every level

in best case too

T.C. -  $O(n \log n)$   $\rightarrow$  number of levels

S.C. -  $O(n)$   $\rightarrow$   $(n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \dots \text{ till } 1)$

IMPLEMENT MERGE SORT - GFG

## Quick Sort

W8-L2

→ Partition

Choose one element named pivot and put it on its correct position

Put elements less than pivot in left subarray and otherwise in right subarray

→ Sort left & right subarrays recursively

```
int partition( vector<int> &arr, int s, int e){  
    int pivotIndex = s; —————> This is one way  
    int pivot = arr[s]; Other ways - choose last  
- choose random  
    int cnt = 0; ↓  
randomised  
quick sort  
    for( int i=s+1; i<=e ; i++ ){  
        if( arr[i] > pivot )  
            cnt++;  
    }  
    int correctPosition = s + cnt;  
    swap( arr[pivotIndex], arr[correctPosition]);  
    pivotIndex = correctPosition
```

```

int i=s, j=e;
while( i < correctPosition && j > correctPosition) {
    while( arr[i] < pivot)
        i++;
    while( arr[j] >= pivot)
        j--;
    if( i < correctIndex && j > correctIndex)
        swap( arr[i++], arr[j--]);
}
return correctPosition;
}

void quickSort( vector <int> &arr, int s, int e) {
if( s >= e)
    return;
int p = partition( arr, s, e);
quickSort( arr, s, p-1);
quickSort( arr, p+1, e);
}

```

T.C. -  $O(n \log n)$   $\rightarrow$  logn number of function calls

$O(n^2)$   $\rightarrow$  for both ascending & descending sort

S.C. -  $O(n)$   $\rightarrow$  n number of function calls

## Backtracking

- specific form of recursion
- explore all possible solutions and
- don't check the solution you have already discard
- brute force
- used for reference variables passed in functions

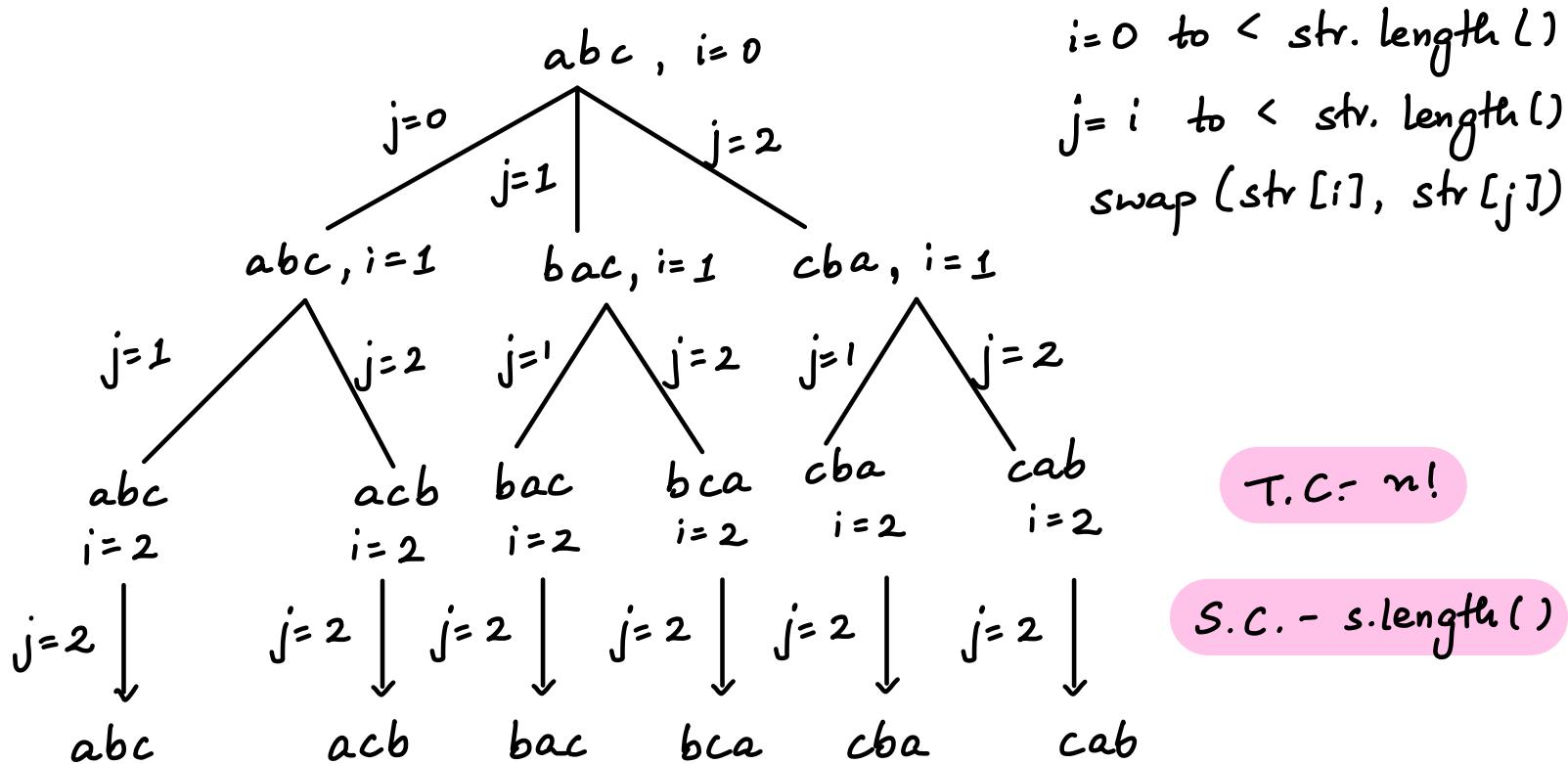
## Permutation in a string

$s = "abc"$

permutations - abc, acb, bac, bca,

cab, cba

→ total -  $n!$



## Time Complexity

W8-L7

- max time required by an algorithm as a function of input
- for worst case
- number of calls \* T.C. - time in 1 call
- T.C. - total time in 1 level \* number of levels

## Space Complexity -

- max space taken by an algorithm at any particular instant
- S.C. - space in 1 call \* max depth

→ Remember min space and time can be  $O(1)$  not  $O(0)$

## Type 1 Linear Tree

fun (n){

    Base Case

    Processing

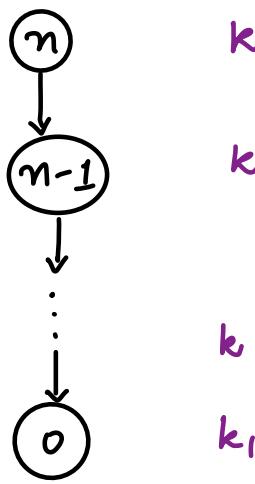
    fun (n-1)

}

$k_1$  }  $k$   
 $k_2$  }

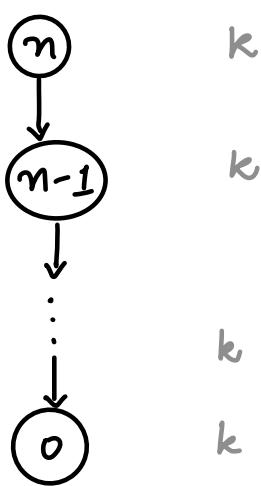
→ pass by value  
1 variable  $n$  is created

→ pass by reference  
min space is constant



$$T.C. - nk + k_1$$

$T.C. - O(n)$

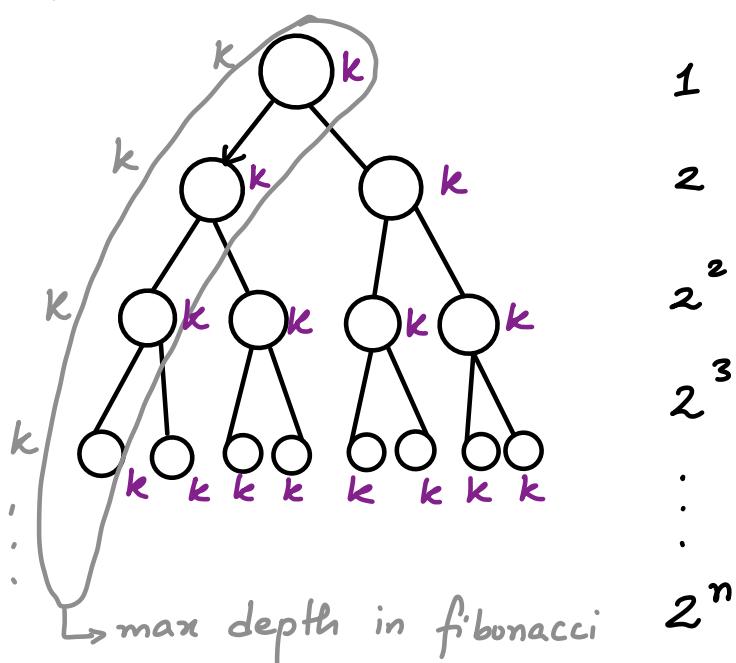


$$S.C. - (n+1)k$$

$S.C. - O(n)$

Counting  
factorial  
power of 2  
check sorted  
max in array  
min in array

## Type 2 Non Linear Tree



$$T.C. = k + 2k + 4k + \dots + 2^n k$$

T.C. =  $O(2^n)$

S.C. =  $nk$

S.C. =  $O(n)$

fibonacci

jump stairs

subsequences

### Type 3 Logarithmic



T.C. =  $\log n * k$

S.C. =  $\log n * k$

S.C. =  $\log n * n$

T.C. =  $O(\log n)$

S.C. =  $O(\log n)$

S.C. =  $n \log n$

binary search

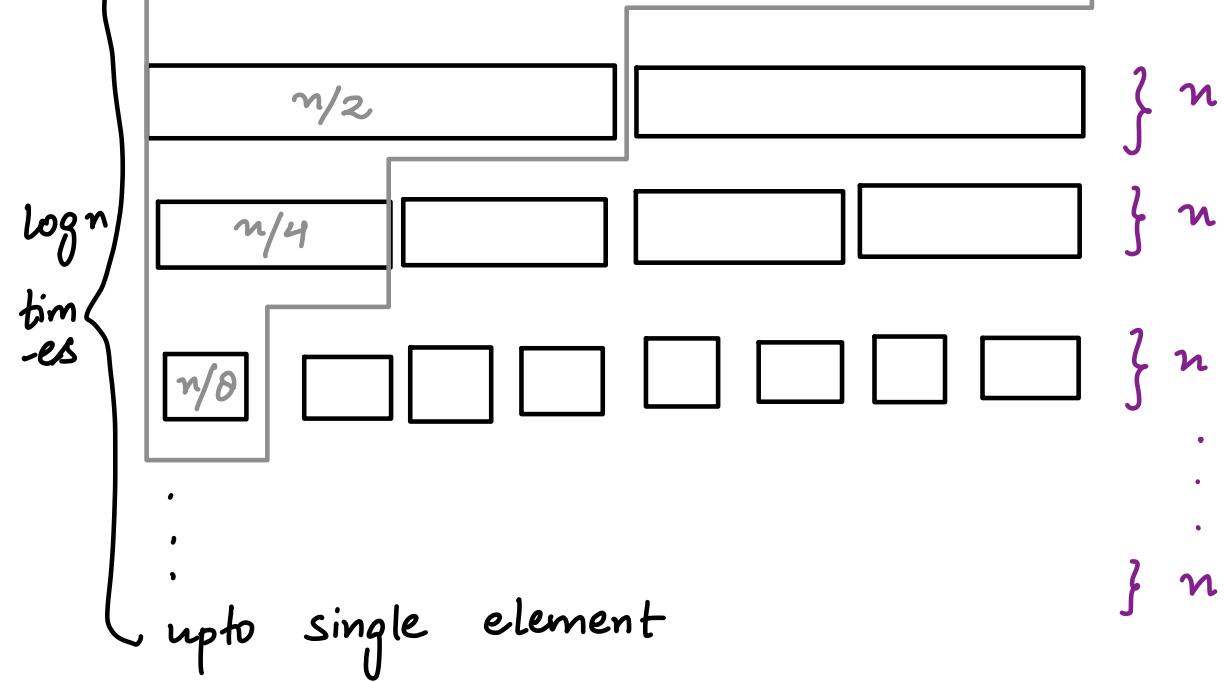
array / vector  
pass by reference

vector pass  
by value

## Merge Sort

in merge func. (in copying in left & right arrays)

in merge func.  
(by copying in left & right arrays)



T.C. - time in 1 level \* number of levels

T.C. -  $n * \log n$

T.C. -  $O(n \log n)$

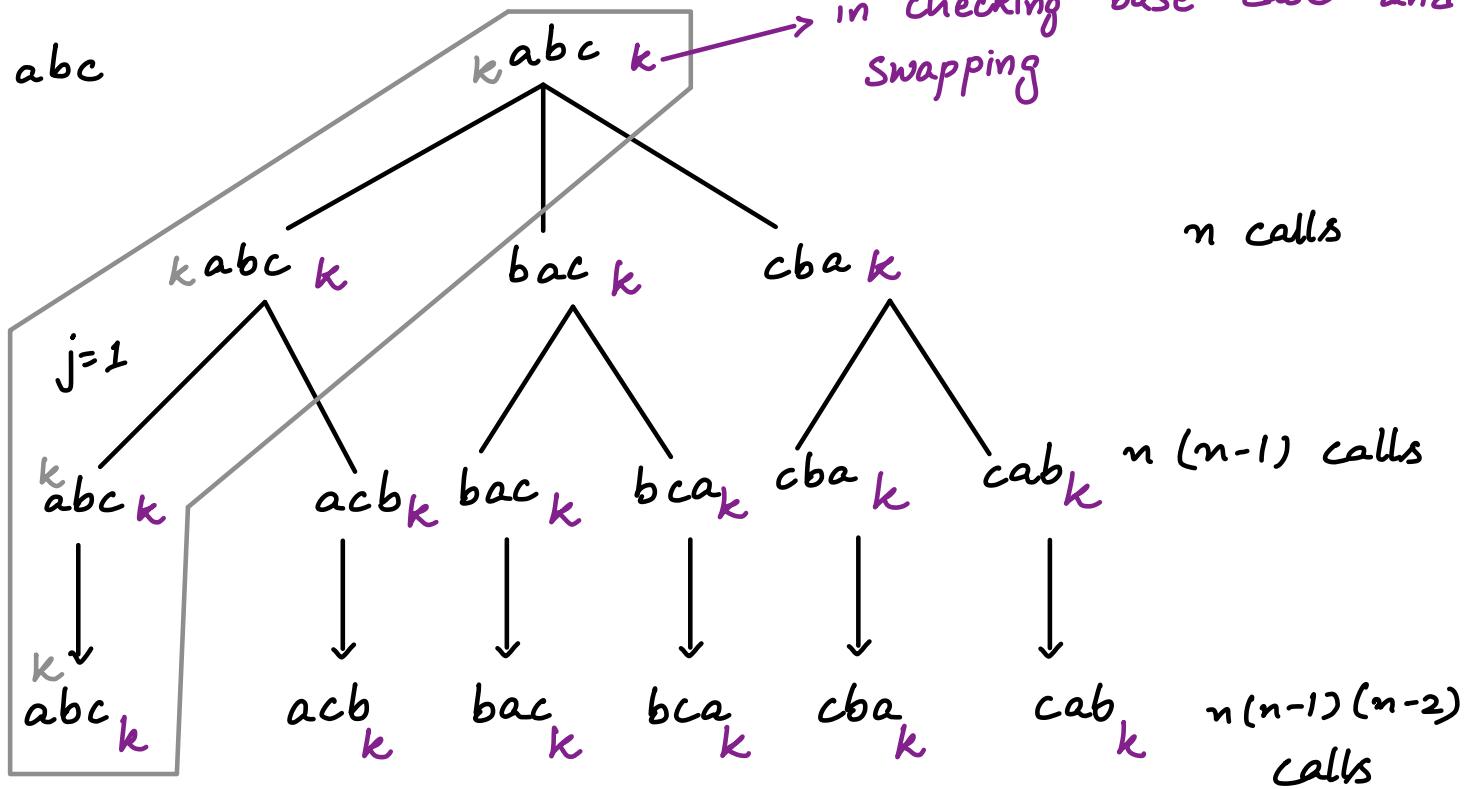
S.C. -  $n + \frac{n}{2} + \frac{n}{4} + \dots + 2$

S.C. -  $O(n)$

# Backtracking Questions

## Permutations of a string

$s = abc$



$$T.C. = k + nk + n(n-1)k + n(n-1)(n-2)k + \dots + \textcircled{n! k}$$

$$T.C. = O(n!)$$

$$S.C. = n^* k$$

$$S.C. = O(n)$$

## Rat in a maze

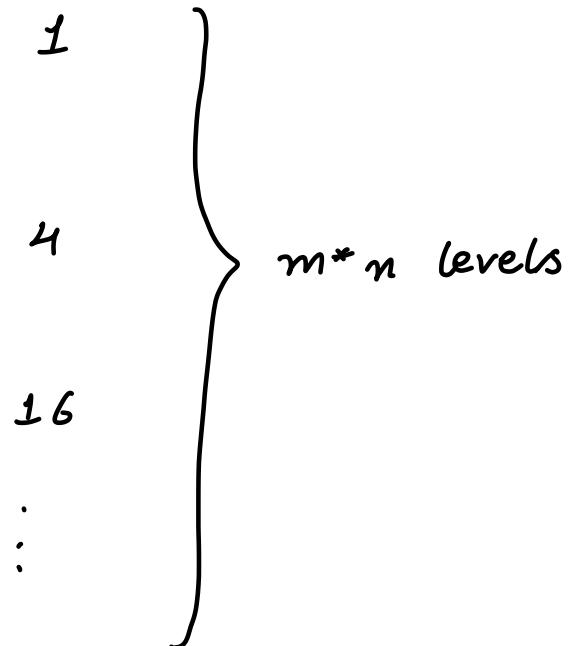
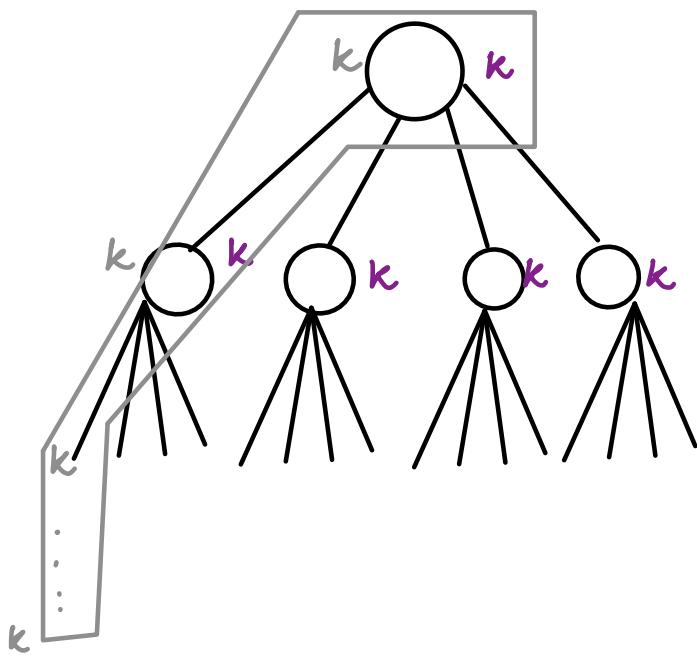
$m$  rows  
 $n$  cols

func ( )  
base case

4 recursive calls

↳ down, left, right, up

}



$$T.C. - k + 4k + 4^2k + \dots + 4^n k$$

$$T.C. - O(4^m)$$

S.C. -  $k * mn$   $\xrightarrow{\text{depth}}$  of visited 2D array &  $mn$  pass by reference

$$S.C. - O(m * n)$$

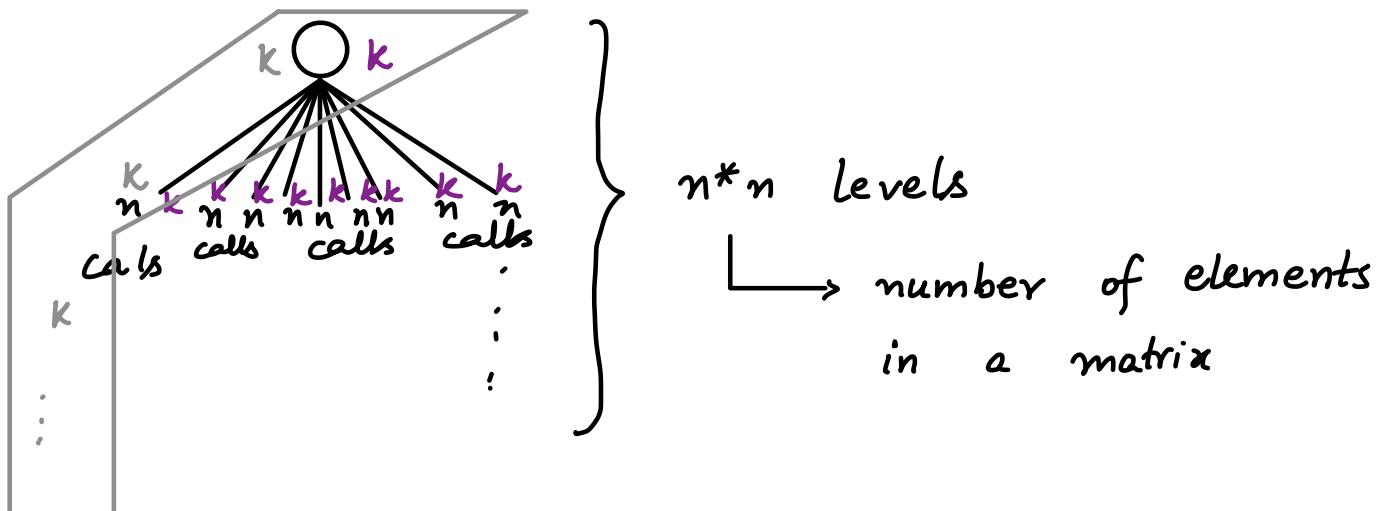
# Sudoku Solve

$n \times n$  matrix

standard

$$\hookrightarrow n = 9$$

```
func() {
    base case
    n recursive calls + isSafe func.
}
```



$$T.C. - k + kn + kn^2 + \dots k n^{n \times n}$$

$$T.C. - O(n^{n^2})$$

$$S.C. - k^* (n^{n \times n}) \xrightarrow{\text{depth}}$$

$$S.C. - O(n^2)$$

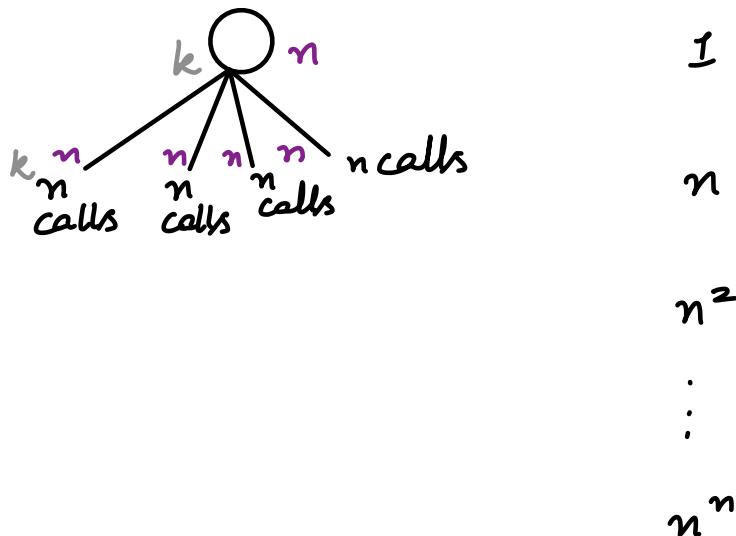
if  $n$  is already given 9,  $T.C - O(1)$  &  $S.C - O(1)$

## N Queens

func ( )

$\left\{ \begin{array}{l} k_1 \text{ base case} \longrightarrow k \\ k_2 \text{ n isSafe function} \longrightarrow O(n) \\ n \text{ recursive calls} \end{array} \right\} O(n)$

}



$$T.C. = n(1) + n(n) + n(n^2) + \dots + n(n^n)$$

T.C. -  $O(n^n)$  → worst case

T.C. -  $O(n!)$  → average case

S.C. -  $k^* n$

S.C. -  $O(n)$

S.C. -  $k^* n + n \xrightarrow{\text{in optimized sol for creating 3 maps}} O(n)$

→  $n^* n!$  can be written as  $n!$

→  $n^* 2^n$  can be written as  $2^n$

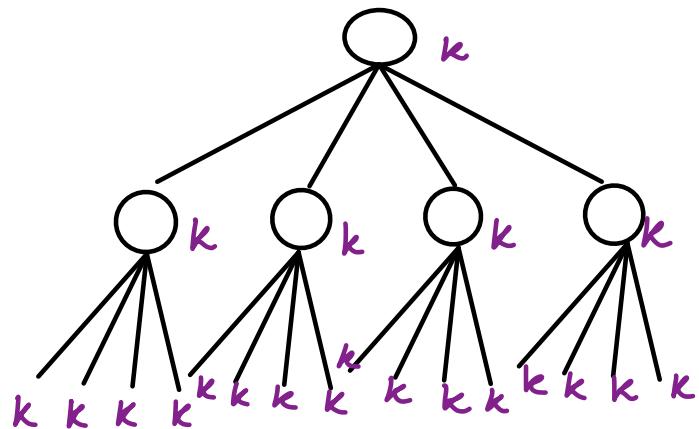
# Phone Keypad Problem

1	2	3
	abc	def
4	5	6
ghi	jkl	mno
7	8	9
pqrs	tuv	wxyz

```

fun ( ) {
    base case k
    ↳ store output in ans array
    at max 4 recursive calls
}

```



1  
4  
 $4^2$   
.  
.  
 $4^n$

$$T.C. = k + 4k + 4^2k + \dots + 4^n k$$

$$T.C. = O(4^n)$$

$S.C. = (k + 2k + \dots + nk) + (4^n * n)$

in max depth  $\uparrow$  length of 1 output string  $\uparrow$   
 store output in base case  $\downarrow$  no. of strings stored in ans array

$$S.C. = O(4^n)$$

- Object Oriented Programming
- programming technique in which everything revolves around objects
  - creation
  - interaction
  - access
  - changes
- 2 things
  - property / state → variables
  - behaviour / method → functions
- why ?
  - readable
  - reusable
  - easily maintain
  - easily to understand

### Class

- to make user defined / custom datatype
- has structure definition

class - design / blueprint / idea

object - actual entity

↳ instance of class

→ has existence

→ Class and Object both take memory

### Creating a class

```
class className {  
    // states  
    string name;  
  
    // method  
    void sleep(){  
    }  
};
```

### size of (class) -

```
class animal {
```

```
};
```

cout << sizeof (animal); → 1 to give existence  
for identifying this  
class, so min.  
possible memory is  
allocated

```
};
```

cout << sizeof (animal); → 4

```
class animal {  
    string name;  
};
```

```
cout << sizeof (animal);
```

24

Why ?

```
class animal {  
    int age;  
    char ch;  
};
```

```
cout << sizeof (animal);
```

→ due to padding  
and greedy alignment

```
class animal {
```

```
    string name;  
    string age;
```

} states / properties / data members

```
    void sleep () {
```

```
        cout << name << " is sleeping " ;  
    }
```

```
};
```

} method /  
behaviour /  
member  
function

## Static Object Creation

animal ramesh ;

Accessing state and method of object

not class

object Name. state ;

object Name. method( parameters );

ex- ramesh. age ;

ramesh. sleep();

## Access Modifiers

→ defines access scope of state / method

3 types

↓  
public

can access that  
state / behaviour  
inside as well as  
outside the class

↓  
private ( by default )  
can access that  
state / behaviour  
only inside the  
class, not outside  
the class

↓  
protected  
same as  
private but  
can be  
access  
inside class  
child

```
class animal {  
    public : —————> after marking,  
    string name; all below state /  
    string age; behaviour will be of  
    void sleep () { that type  
        cout << name;  
    }  
    private :  
        void eat () {  
    }  
};
```

To access private member outside class

↳ use public methods getter and setter

```
class animal {  
    string name;  
    public :  
        string getName () { getter  
            return name;  
    }  
};
```

```

void setName ( string newName) {   setter
    name = newName;
}

int main () {
    animal ramesh;

    cout << ramesh. name; -----> ERROR

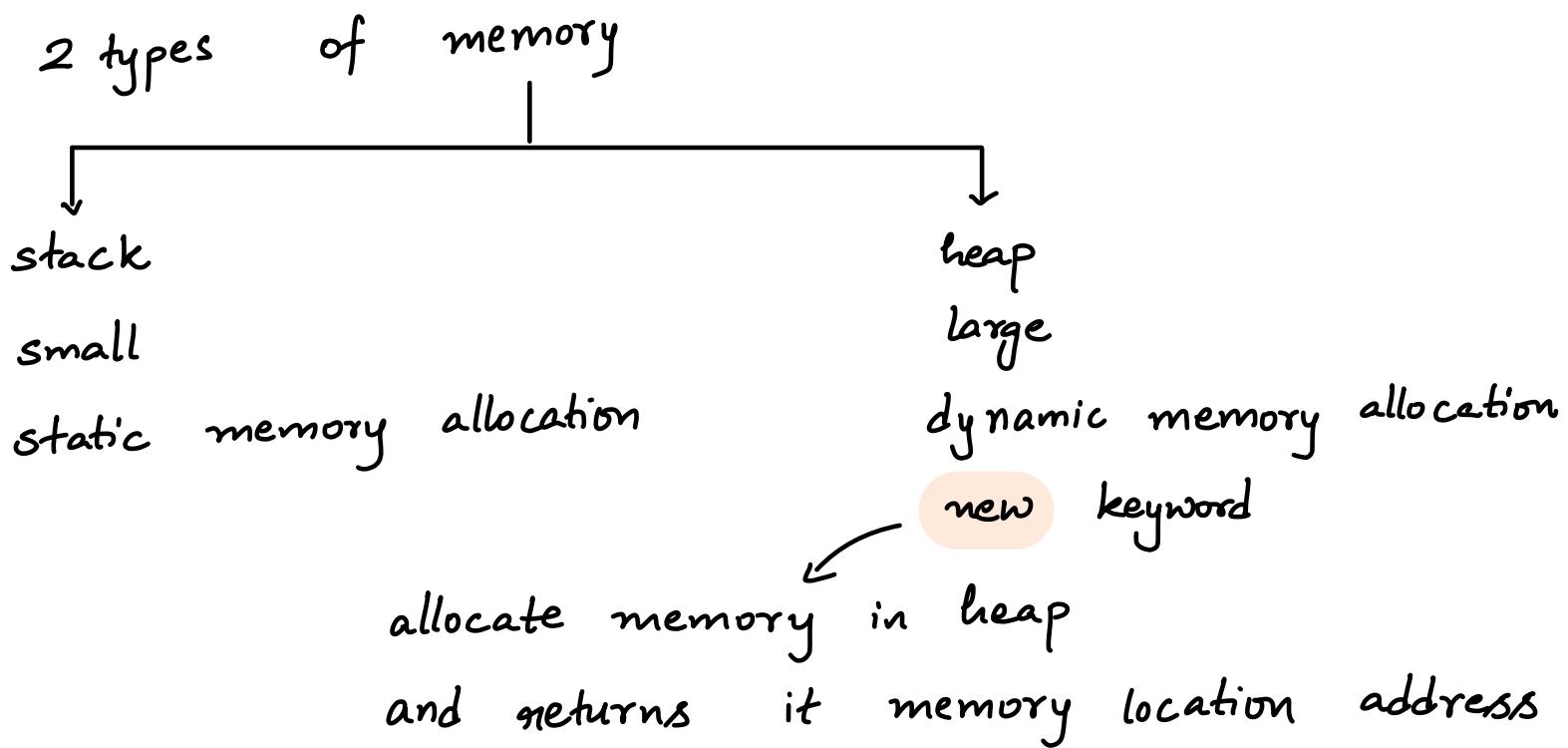
    cout << ramesh. getName(); -----> gu

    ramesh. setName ("Lion");

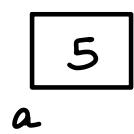
    cout << ramesh. getName(); -----> Lion

```

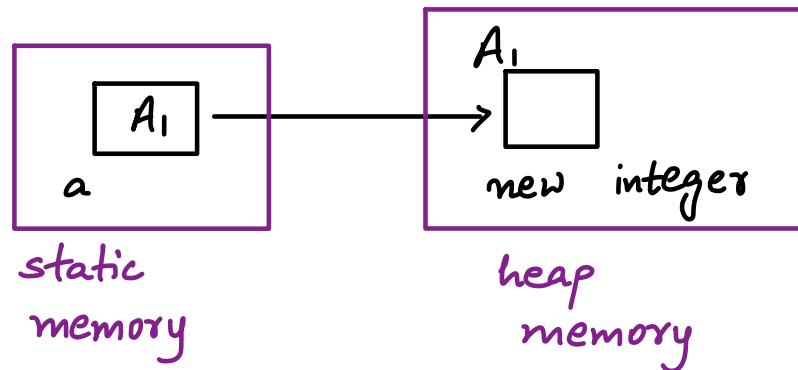
## Dynamic Memory Allocation



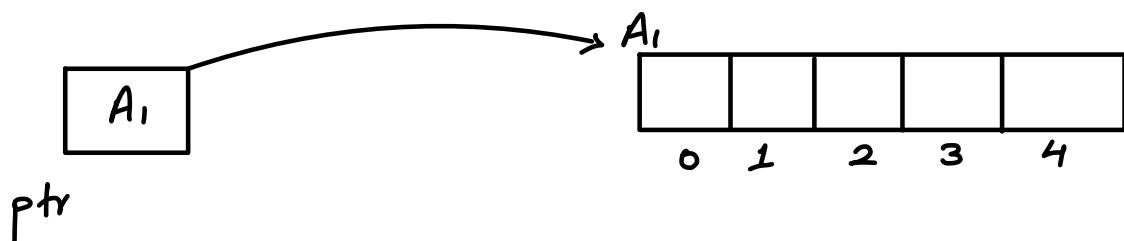
```
int a = 5;
```



```
int * a = new int
```



```
int * ptr = new int [5];
```



- space allocated in heap memory, cannot be cleaned automatically even after finishing of func.
- there is no garbage collector in C++

Allocation

```
int * a = new int;
```

```
int * arr = new int [5];
```

De allocation

```
delete a;
```

```
delete arr [ ];
```

# Object Creation using dynamic memory allocation

```
animal * suresh = new animal;
```

suresh.name;  $\longrightarrow$  ERROR as suresh is a pointer, \*suresh is object

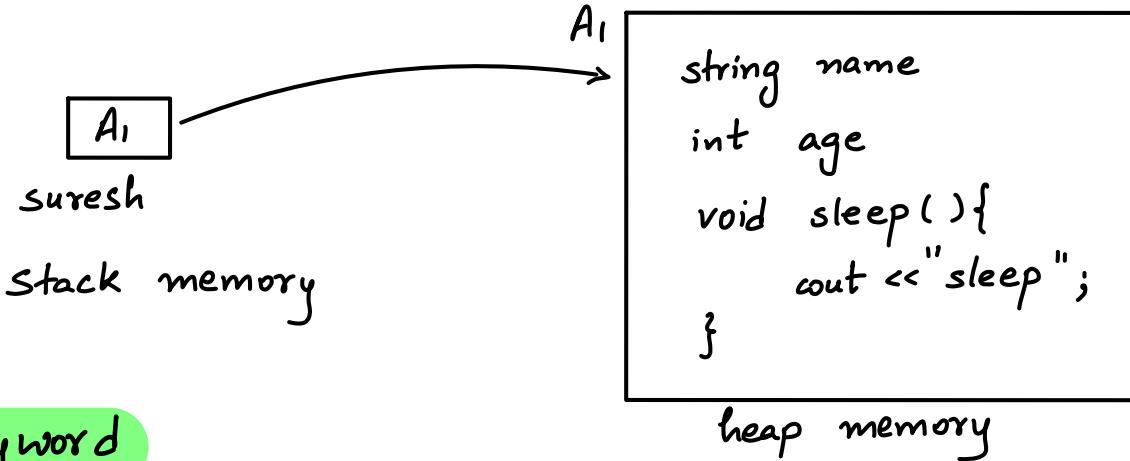
(\*suresh).name; } 1<sup>st</sup> way of access

(\*suresh).sleep();

suresh  $\rightarrow$  name;

} 2<sup>nd</sup> way of access

suresh  $\rightarrow$  sleep();



this keyword

$\hookrightarrow$  pointer to current object

```
class animal {
```

```
    int age;
```

```
public:
```

```
    void setAge ( int age){
```

```
        this  $\rightarrow$  age = age;
```

```
        // (*this).age = age;
```

```
}
```

```
};
```

} both are correct

## Object Creation

→ Constructor Call (in both static and dynamic allocation)

- initialize the object
- function with no return type
- its name is same as class
- created by default

```
class animal {
```

```
    int age;
```

```
    int weight;
```

// default constructor

```
animal () {
```

```
    cout << "Constructor Called";
```

```
    this->age = 10;
```

```
    this->weight = 20;
```

```
}
```

now built-in  
constructor does not  
called, it will be  
called

→ accessing members and methods

using this keyword is **GOOD PRACTICE**

// parameterised constructor

```
animal ( int age) {
```

```
    this->age = age;
```

```
    cout << "Parameterised constructor called";
```

```
}
```

// parameterised constructor 2

```
animal ( int age, int weight){  
    this->age = age;  
    this->weight = weight;  
    cout << "Parameterised constructor 2 called";  
}
```

// copy constructor (wrong way)

```
animal (animal obj) {  
    this->age = obj.age;  
    this->weight = obj.weight;  
    cout << "Copy Constructor Called";  
}
```

animal a;

animal b = new animal;

```
animal c = a;  
animal d (a);  
animal e = * b;  
animal f (* b);
```

// copy constructor (right way)

```
animal (animal & obj) {  
    this->age = obj.age;  
    this->weight = obj.weight;  
    cout << "Copy Constructor Called";  
}
```

copy constructor call  
pass by value  
infinite loop

}

## Destructor

- free memory
- for static object creation,  
destructor gets called automatically  
where object's scope ends
- for dynamic object creation,  
you have to do it manually using  
`delete objName;`
- no return type
- no input parameter

```
class animal {  
    int age;  
    int weight;  
  
    // destructor  
    ~animal () {  
        cout << "destructor called";  
    }  
}
```

- Encapsulation
- Inheritance
- Polymorphism
- Abstraction (Pitaji of all OOPs pillars)

### Encapsulation

- Wrap data members and member functions in one parent entity (class)
- Objective → Data Hiding
  - security
  - privacy
  - can make readonly
  - can decide what to hide and what to show
  - work with parent entity is simple

Objective of class → Encapsulation

### Perfect / Full / 100% Encapsulation

- When all data members are marked private and access them using getter and setter

## Inheritance

- inherit some properties (data members and data functions) from parent / super / base class to sub / child / derived class
- Objective → Reusability
- is a relationship
- syntax
  - class childName : mode1 parentName1, ... , modeN parentNameN {  
  //additional states and methods  
}

```
class Animal {  
    int age;  
    public:  
    int weight;  
    protected:  
    void eat() {  
        cout << "eating";  
    }  
};
```

```
class Dog : public Animal {  
};  
↓  
Dog is a Animal  
class cat : public Animal,  
protected Dog {  
};
```

Access Modifier of Base class	Mode of inheritance		
	Public	Protected	Private
Public	Public	Protected	Private
Protected	Protected	Protected	Private
Private	NA	NA	NA

NA → Not Accessible

↳ can't be inherited

Protected

↳ Same as private access modifier

but can be inherited



can be accessed inside child class

Private

↳ can access inside class but not outside

cannot be inherited

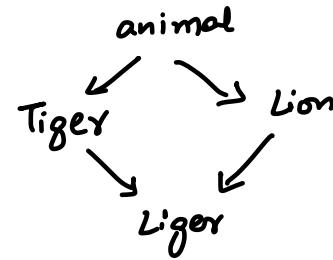


cannot be accessed inside child class

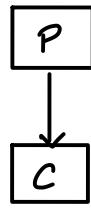
## Type of Inheritance

P- Parent      C- Child

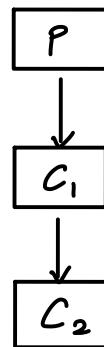
- Single
- Multilevel
- Multiple
- Heirarchical
- Hybrid → mixture of all above 4



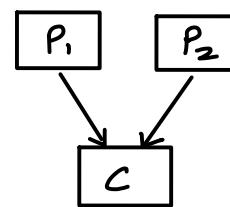
Single



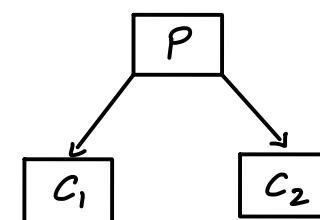
Multilevel



Multiple



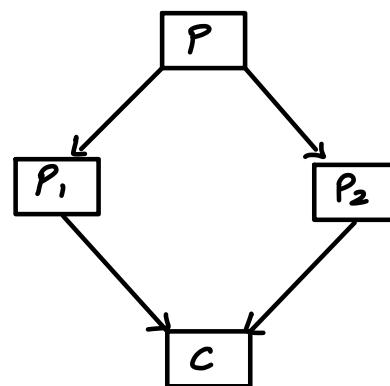
Heirarchical



## Diamond Problem / Inheritance Ambiguity Problem

- If multiple parents have same property then how to access them

→ `objectName . Parent Class Name :: property ;`

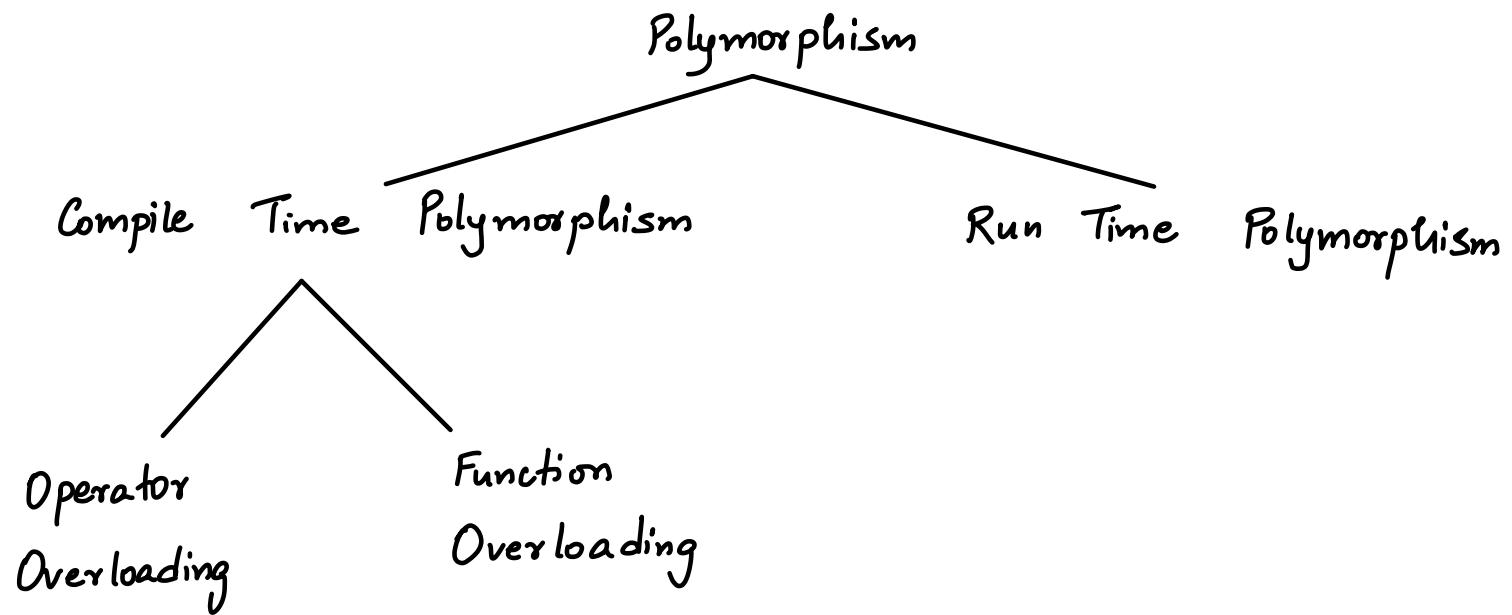


scope resolution operator

→ If parent and child have same property, then parent property inside child class will get overwrite by child property

→ Multiple inheritance is possible in C++, not in Java

Polymorphism  
→ form  
→ existed in many forms



## Function Overloading

→ one function existing in multiple forms / signatures

→ Multiple Signatures

→ diff. in either no. of parameters or type of parameters, not diff. in return type

→ 5.12 → double

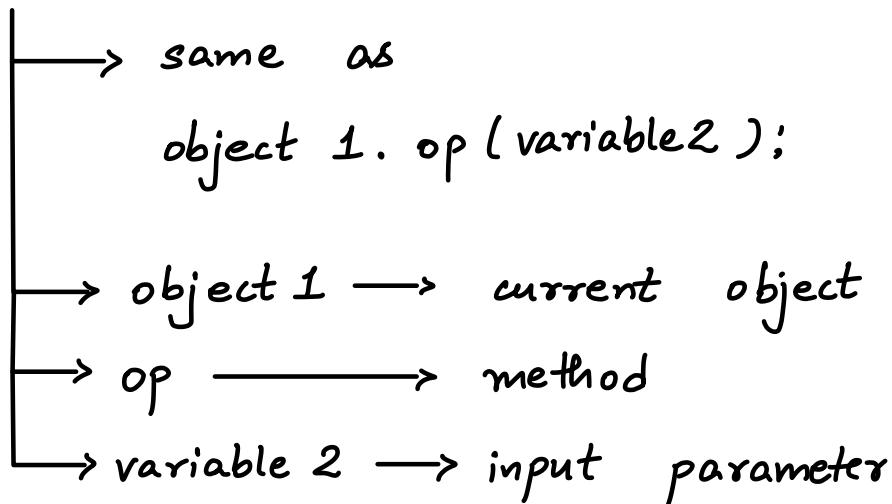
5.12f → float

```
class Maths {  
public:  
    int sum (int a, int b){  
        return a+b;  
    }  
  
    float sum ( int a, double b){  
        return a+b;  
    }  
  
    int sum( int a, int b, int c){  
        return a+b+c;  
    }  
};  
  
int main () {  
    Maths m;  
  
    cout << m.sum(5, 2); -----> 7  
  
    cout << m.sum(5, 2.5); -----> 7.5  
  
    cout << m.sum(5, 2, 7); -----> 14  
  
    return 0;  
}
```

## Operator Overloading -

→ to make new implementation of an operator

object1 op variable2



```
class Para {  
public:  
int val;  
  
Para ( int val ) {  
    this → val = val;  
}  
  
int operator + ( Para obj2 ) {  
    return this → val - obj2. val;  
}  
  
int operator + ( char ch ) {  
    cout << this → val + 10;  
}  
};
```

```

int main (){
    Para a(5);
    Para b(2);
    cout << a + b; -----> same as a.+ (b)
                                         ↳ 3
    a + 'c'; -----> 15
    a + '7' ; -----> 15
    return 0;
}

```

→ "operator + " function must have exactly 1 parameter as + is binary operator

↓  
 2 operands  
 current object      input parameter

Run Time Polymorphism -

↳ polymorphism after execution

Function Overriding -

## Function / Method Over-riding

- when function of parent class is defined separately inside child class
- reusable + custom behaviour wherever you want

```
class Animal {
```

```
public:
```

```
void speak () {
```

```
    cout << "speak";
```

```
}
```

```
};
```

```
class Dog : public Animal {
```

```
public:
```

```
void speak () {
```

```
    cout << "bark";
```

```
}
```

```
};
```

```
int main () {
```

```
    Animal a;
```

```
    cout << a.speak();
```

```
    Dog d;
```

```
    cout << d.speak();
```

```
class Animal {
```

```
public:
```

// upcasting

Animal \* b = new Dog ;

cout << b. speak(); —————> speak —> function of parent class called

Animal \* b = new Dog;

cout << b. speak(); —————> bark

// down casting

Dog \* c = new Animal ; —————> Compiler dependent (ERROR or not)

cout << c. speak(); —————> bark

Dog \* c = new Animal ;

OOPS Week is not completed

from my side

will complete in future

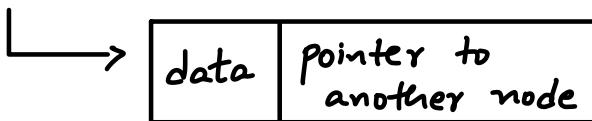
## Abstraction

- Objective → Implementation Hiding
- Talk about in a larger scale  
not focus on detail

# LINKED LIST

W10-L1

- Dynamic linear data structure to store similar data
- non-continuous memory allocation
- insertion and deletion is easy  
 $O(1)$  if you are standing on that node / pointer
- no concept of indexing,  
it has concept of addresses
- collection of nodes

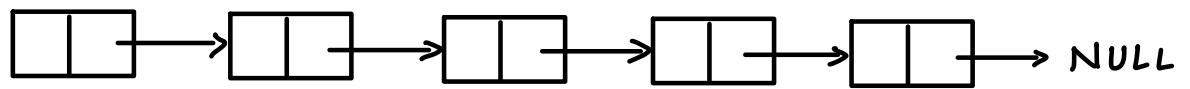


## node creation (simplest)

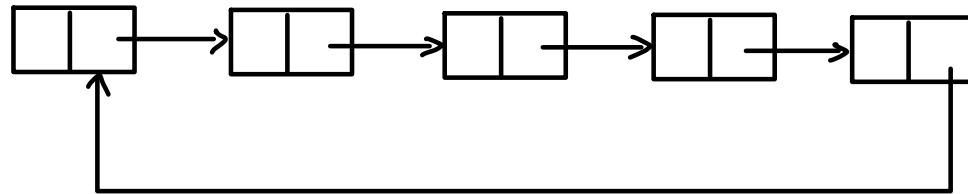
```
class node {  
public:  
    int data;  
    node * next;  
}
```

# Types of linked list

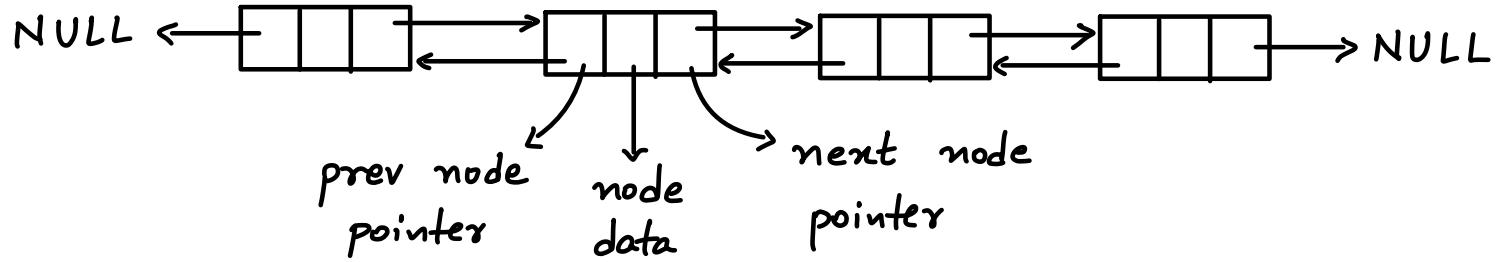
→ Singly LL



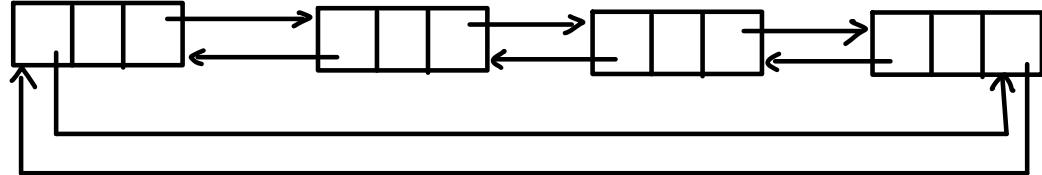
→ Circular LL



→ Doubly LL



→ Circular Doubly LL



→ LL is nothing but Hindi (any other language)

→ Linear Data Structure

└→ single descendent

→ In LL ques, there are high chances of error,

so check edge cases (head, tail, size=1, not found, and more) before submit.

## W10-L2

### Doubly Linked list

→ node creation

```
class node {  
public:  
    int data;  
    node * next;  
    node * prev;  
}
```

### Circular Linked List

→ no Head and Tail

→ insertion & deletion is only on the basis of value

→ Converting loop code to recursion code

→ Add parameters that are changing in loop

→ Stopping condition in loop acts as base case

