# Assignment 6: GLMs (Linear Regressios, ANOVA, & t-tests)

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#### **OVERVIEW**

This exercise accompanies the lessons in Environmental Data Analytics on generalized linear models.

#### **Directions**

- 1. Change "Student Name" on line 3 (above) with your name.
- 2. Work through the steps, **creating code and output** that fulfill each instruction.
- 3. Be sure to **answer the questions** in this assignment document.
- 4. When you have completed the assignment, **Knit** the text and code into a single PDF file.
- 5. After Knitting, submit the completed exercise (PDF file) to the dropbox in Sakai. Add your last name into the file name (e.g., "Fay\_A06\_GLMs.Rmd") prior to submission.

The completed exercise is due on Monday, February 28 at 7:00 pm.

#### Set up your session

- Load the tidyverse, agricolae and 1. Set up your session. Check your working directory. Import the raw NTL-LTER raw data file for chemistry/physics other needed packages. (NTL-LTER\_Lake\_ChemistryPhysics\_Raw.csv). Set date columns to date objects.
- 2. Build a ggplot theme and set it as your default theme.

```
getwd()
## [1] "/Users/saradiamond/Documents/Environmental_Data_Analytics_2022/Assignments"
setwd("/Users/saradiamond/Documents/Environmental_Data_Analytics_2022")
#install.packages("agricolae")
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5
                    v purrr
                              0.3.4
## v tibble 3.1.4
                     v dplyr
                              1.0.7
## v tidyr
           1.1.4
                    v stringr 1.4.0
## v readr
           2.0.2
                    v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
library(agricolae)
NTL.LTER.ChemPhys <- read.csv("./Data/Raw/NTL-LTER_Lake_ChemistryPhysics_Raw.csv",
                        stringsAsFactors = TRUE) #reading in the data
```

### Simple regression

Our first research question is: Does mean lake temperature recorded during July change with depth across all lakes?

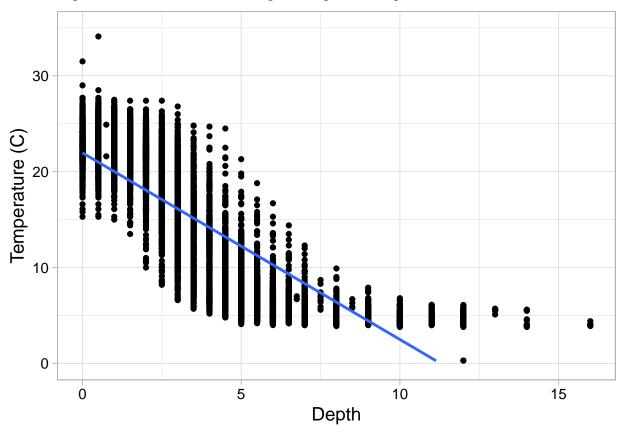
- 3. State the null and alternative hypotheses for this question: > Answer: H0: There is no change in mean lake temperature during July with depth across all lakes. Ha: There is a change in mean lake temperature during July with depth across all lakes.
- 4. Wrangle your NTL-LTER dataset with a pipe function so that the records meet the following criteria:
- Only dates in July.
- Only the columns: lakename, year4, daynum, depth, temperature\_C
- Only complete cases (i.e., remove NAs)
- 5. Visualize the relationship among the two continuous variables with a scatter plot of temperature by depth. Add a smoothed line showing the linear model, and limit temperature values from 0 to 35 °C. Make this plot look pretty and easy to read.

```
class(NTL.LTER.ChemPhys$sampledate) #checking the class of the date column
## [1] "factor"
NTL.LTER.ChemPhys$sampledate <- as.Date(NTL.LTER.ChemPhys$sampledate,
                                        format = "%m/%d/%y") #changing to date format
class(NTL.LTER.ChemPhys$sampledate)
## [1] "Date"
#adding month column
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
NTL.LTER.ChemPhys.Mutate <- NTL.LTER.ChemPhys
  mutate(Month = month(sampledate))
#wrangling data
library(dplyr)
NTL.LTER.ChemPhys.Filter <-
  NTL.LTER.ChemPhys.Mutate %>%
  filter(Month == 7) %>% # #
  select(lakename, year4, daynum, depth, temperature_C) %>% # %>%
  drop_na(temperature_C)
#5
```

```
#plotting the relationship with a line of best fit
tempbydepth <-
    ggplot(NTL.LTER.ChemPhys.Filter, aes(x = depth, y = temperature_C)) +
    ylim(0, 35) +
    geom_point() +
    geom_smooth(method = "lm") +
    ylab("Temperature (C)") +
    xlab("Depth")
print(tempbydepth)</pre>
```

## `geom\_smooth()` using formula 'y ~ x'

## Warning: Removed 24 rows containing missing values (geom\_smooth).



6. Interpret the figure. What does it suggest with regards to the response of temperature to depth? Do the distribution of points suggest about anything about the linearity of this trend?

Answer: By looking at the plot, it is obvious that as depth increased so does the temperature. The points of temperature greatly vary with each unit of depth some are quite warm and some much colder so it is hard to make an assumption based on this plot.

7. Perform a linear regression to test the relationship and display the results

```
#7 building the linear regression model
Temp.regression <- lm(data = NTL.LTER.ChemPhys.Filter, temperature_C ~ depth)
summary(Temp.regression)</pre>
```

## ## Call:

```
lm(formula = temperature_C ~ depth, data = NTL.LTER.ChemPhys.Filter)
##
   Residuals:
##
##
       Min
                                    3Q
                  1Q
                      Median
                                            Max
##
   -9.5173 -3.0192
                      0.0633
                                2.9365 13.5834
##
##
   Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
##
   (Intercept) 21.95597
                              0.06792
                                          323.3
                                                    <2e-16 ***
                                         -165.8
##
   depth
                 -1.94621
                               0.01174
                                                    <2e-16 ***
##
                              0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Signif. codes:
##
## Residual standard error: 3.835 on 9726 degrees of freedom
## Multiple R-squared: 0.7387, Adjusted R-squared: 0.7387
## F-statistic: 2.75e+04 on 1 and 9726 DF, p-value: < 2.2e-16
#looking at the plots
par(mfrow = c(2,2), mar=c(4,4,4,4))
plot(Temp.regression)
                                                   Standardized residuals
                                                                     Normal Q-Q
              Residuals vs Fitted
Residuals
                                                         \alpha
     0
                                                         0
     -19
                                                                            0
                                                                                   2
         -10
                   0
                       5
                           10
                                15
                                    20
                                                                    -2
                                                                                          4
                   Fitted values
                                                                  Theoretical Quantiles
Standardized residuals
                                                   Standardized residuals
                                                                Residuals vs Leverage
                Scale-Location
           0804
     1.0
                                                         0
                                                                       ook's distance
     0.0
                                                         ကု
         -10
                   0
                       5
                               15
                                                                            0.0008
                                                                                    0.0012
                           10
                                    20
                                                           0.0000
                                                                   0.0004
```

8. Interpret your model results in words. Include how much of the variability in temperature is explained by changes in depth, the degrees of freedom on which this finding is based, and the statistical significance of the result. Also mention how much temperature is predicted to change for every 1m change in depth.

Leverage

Fitted values

Answer: The results of the linear regression show that there is a significant relationships in temperature and in depth with p values less than 0.05. Additionally, the results are saying that for every 1 m in depth, the temperature decreased by 1.95 degrees Celsius This is based on 9726 degrees of freedom and the R squared explains 73.9% of the variability in the temperature.

## Multiple regression

Let's tackle a similar question from a different approach. Here, we want to explore what might the best set of predictors for lake temperature in July across the monitoring period at the North Temperate Lakes LTER.

- 9. Run an AIC to determine what set of explanatory variables (year4, daynum, depth) is best suited to predict temperature.
- 10. Run a multiple regression on the recommended set of variables.

```
#9 running the AIC
AIC.mod <- lm(data = NTL.LTER.ChemPhys.Filter, temperature_C ~ year4 + daynum +
              depth)
step(AIC.mod)
## Start: AIC=26065.53
## temperature_C ~ year4 + daynum + depth
##
            Df Sum of Sq
##
                            RSS
                                  AIC
## <none>
                         141687 26066
## - year4
             1
                     101 141788 26070
## - daynum 1
                    1237 142924 26148
## - depth
             1
                  404475 546161 39189
##
## Call:
## lm(formula = temperature_C ~ year4 + daynum + depth, data = NTL.LTER.ChemPhys.Filter)
## Coefficients:
## (Intercept)
                      year4
                                  daynum
                                                depth
      -8.57556
                    0.01134
                                 0.03978
                                             -1.94644
##
#10
Mult.Regress.Mod <- lm(data = NTL.LTER.ChemPhys.Filter, temperature_C ~ year4 +
                         daynum + depth)
summary(Mult.Regress.Mod)
##
## lm(formula = temperature_C ~ year4 + daynum + depth, data = NTL.LTER.ChemPhys.Filter)
##
## Residuals:
##
                1Q Median
                                3Q
       Min
                                       Max
## -9.6536 -3.0000 0.0902 2.9658 13.6123
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.575564 8.630715
                                     -0.994 0.32044
                                       2.639 0.00833 **
## year4
               0.011345
                           0.004299
## daynum
                           0.004317
                                       9.215 < 2e-16 ***
                0.039780
## depth
               -1.946437
                           0.011683 -166.611 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 3.817 on 9724 degrees of freedom
## Multiple R-squared: 0.7412, Adjusted R-squared: 0.7411
## F-statistic: 9283 on 3 and 9724 DF, p-value: < 2.2e-16</pre>
```

11. What is the final set of explanatory variables that the AIC method suggests we use to predict temperature in our multiple regression? How much of the observed variance does this model explain? Is this an improvement over the model using only depth as the explanatory variable?

Answer: The final variables used are year4, daynum, and depth. When you include all these in the linear regression it makes the new r squared value go up and explains 74.1% of the variability in temperature. This is an improvement, however, it is not a drastic improvement from the previous model.

### Analysis of Variance

12. Now we want to see whether the different lakes have, on average, different temperatures in the month of July. Run an ANOVA test to complete this analysis. (No need to test assumptions of normality or similar variances.) Create two sets of models: one expressed as an ANOVA models and another expressed as a linear model (as done in our lessons).

```
#12
Lake.anova <- aov(data = NTL.LTER.ChemPhys.Filter, temperature C ~ lakename)
summary(Lake.anova) #creating the anova
##
                 Df Sum Sq Mean Sq F value Pr(>F)
                            2705.2
## lakename
                  8 21642
                                        50 <2e-16 ***
               9719 525813
## Residuals
                              54.1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Lake.lm <- lm(data = NTL.LTER.ChemPhys.Filter, temperature_C ~ lakename)
summary(Lake.lm) #creating the linear model
##
## lm(formula = temperature_C ~ lakename, data = NTL.LTER.ChemPhys.Filter)
##
## Residuals:
      Min
                10
                   Median
                                30
                                       Max
## -10.769 -6.614
                   -2.679
                             7.684
                                    23.832
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             17.6664
                                         0.6501 27.174 < 2e-16 ***
## lakenameCrampton Lake
                             -2.3145
                                         0.7699
                                                 -3.006 0.002653 **
## lakenameEast Long Lake
                             -7.3987
                                         0.6918 -10.695 < 2e-16 ***
## lakenameHummingbird Lake
                             -6.8931
                                         0.9429
                                                 -7.311 2.87e-13 ***
## lakenamePaul Lake
                             -3.8522
                                         0.6656
                                                 -5.788 7.36e-09 ***
## lakenamePeter Lake
                             -4.3501
                                         0.6645
                                                 -6.547 6.17e-11 ***
## lakenameTuesday Lake
                             -6.5972
                                         0.6769
                                                 -9.746
                                                         < 2e-16 ***
## lakenameWard Lake
                             -3.2078
                                         0.9429
                                                 -3.402 0.000672 ***
## lakenameWest Long Lake
                             -6.0878
                                         0.6895
                                                 -8.829
                                                         < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 7.355 on 9719 degrees of freedom
## Multiple R-squared: 0.03953,
                                   Adjusted R-squared: 0.03874
## F-statistic:
                  50 on 8 and 9719 DF, p-value: < 2.2e-16
```

13. Is there a significant difference in mean temperature among the lakes? Report your findings.

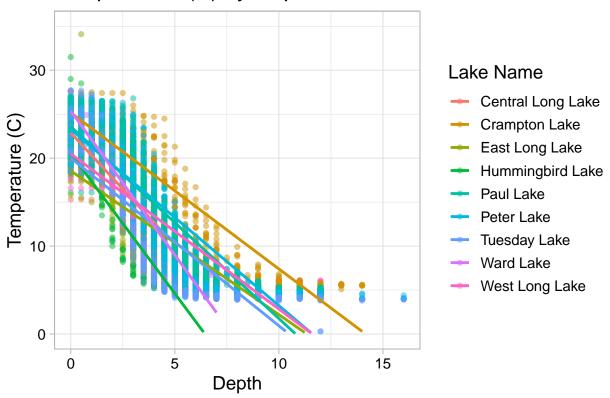
Answer: Yes, there is a significant difference in mean temperature among the lakes. All of the p values of the lakes are statistically significant meaning you would reject the null hypothesis that there is no difference in the means.

14. Create a graph that depicts temperature by depth, with a separate color for each lake. Add a geom smooth (method = "lm", se = FALSE) for each lake. Make your points 50 % transparent. Adjust your y axis limits to go from 0 to 35 degrees. Clean up your graph to make it pretty.

```
#14.
Temp.Depth.Plot<-</pre>
  ggplot(NTL.LTER.ChemPhys.Filter, aes(x = depth, y = temperature_C,
                                        color = lakename)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "lm", se = FALSE) +
 vlim(0,35) +
  ylab("Temperature (C)") +
  xlab("Depth") +
  labs(color = "Lake Name", title = "Temperature (C) by Depth")
print(Temp.Depth.Plot)
## `geom_smooth()` using formula 'y ~ x'
```

## Warning: Removed 73 rows containing missing values (geom\_smooth).

# Temperature (C) by Depth



15. Use the Tukey's HSD test to determine which lakes have different means.

```
#15
TukeyHSD(Lake.anova) #running the Tukey HSD
```

```
Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
##
## Fit: aov(formula = temperature_C ~ lakename, data = NTL.LTER.ChemPhys.Filter)
##
## $lakename
##
                                            diff
                                                         lwr
                                                                    upr
                                                                            p adj
## Crampton Lake-Central Long Lake
                                      -2.3145195 -4.7031913 0.0741524 0.0661566
## East Long Lake-Central Long Lake
                                      -7.3987410 -9.5449411 -5.2525408 0.0000000
## Hummingbird Lake-Central Long Lake -6.8931304 -9.8184178 -3.9678430 0.0000000
## Paul Lake-Central Long Lake
                                      -3.8521506 -5.9170942 -1.7872070 0.0000003
## Peter Lake-Central Long Lake
                                      -4.3501458 -6.4115874 -2.2887042 0.0000000
## Tuesday Lake-Central Long Lake
                                      -6.5971805 -8.6971605 -4.4972005 0.0000000
## Ward Lake-Central Long Lake
                                      -3.2077856 -6.1330730 -0.2824982 0.0193405
## West Long Lake-Central Long Lake
                                      -6.0877513 -8.2268550 -3.9486475 0.0000000
## East Long Lake-Crampton Lake
                                      -5.0842215 -6.5591700 -3.6092730 0.0000000
## Hummingbird Lake-Crampton Lake
                                      -4.5786109 -7.0538088 -2.1034131 0.0000004
## Paul Lake-Crampton Lake
                                      -1.5376312 -2.8916215 -0.1836408 0.0127491
## Peter Lake-Crampton Lake
                                      -2.0356263 -3.3842699 -0.6869828 0.0000999
## Tuesday Lake-Crampton Lake
                                      -4.2826611 -5.6895065 -2.8758157 0.0000000
## Ward Lake-Crampton Lake
                                      -0.8932661 -3.3684639 1.5819317 0.9714459
## West Long Lake-Crampton Lake
                                      -3.7732318 -5.2378351 -2.3086285 0.0000000
## Hummingbird Lake-East Long Lake
                                       0.5056106 -1.7364925 2.7477137 0.9988050
```

```
## Paul Lake-East Long Lake
                                       3.5465903 2.6900206 4.4031601 0.0000000
                                       3.0485952 2.2005025
                                                             3.8966879 0.0000000
## Peter Lake-East Long Lake
## Tuesday Lake-East Long Lake
                                       0.8015604 -0.1363286
                                                            1.7394495 0.1657485
## Ward Lake-East Long Lake
                                       4.1909554 1.9488523
                                                             6.4330585 0.0000002
## West Long Lake-East Long Lake
                                       1.3109897 0.2885003
                                                             2.3334791 0.0022805
## Paul Lake-Hummingbird Lake
                                       3.0409798 0.8765299 5.2054296 0.0004495
## Peter Lake-Hummingbird Lake
                                       2.5429846 0.3818755
                                                             4.7040937 0.0080666
## Tuesday Lake-Hummingbird Lake
                                       0.2959499 -1.9019508
                                                             2.4938505 0.9999752
## Ward Lake-Hummingbird Lake
                                       3.6853448 0.6889874
                                                             6.6817022 0.0043297
## West Long Lake-Hummingbird Lake
                                       0.8053791 -1.4299320
                                                             3.0406903 0.9717297
## Peter Lake-Paul Lake
                                      -0.4979952 -1.1120620
                                                             0.1160717 0.2241586
## Tuesday Lake-Paul Lake
                                      -2.7450299 -3.4781416 -2.0119182 0.0000000
## Ward Lake-Paul Lake
                                      0.6443651 -1.5200848 2.8088149 0.9916978
                                     -2.2356007 -3.0742314 -1.3969699 0.0000000
## West Long Lake-Paul Lake
## Tuesday Lake-Peter Lake
                                     -2.2470347 -2.9702236 -1.5238458 0.0000000
## Ward Lake-Peter Lake
                                      1.1423602 -1.0187489 3.3034693 0.7827037
## West Long Lake-Peter Lake
                                     -1.7376055 -2.5675759 -0.9076350 0.0000000
## Ward Lake-Tuesday Lake
                                      3.3893950 1.1914943 5.5872956 0.0000609
## West Long Lake-Tuesday Lake
                                      0.5094292 -0.4121051 1.4309636 0.7374387
## West Long Lake-Ward Lake
                                      -2.8799657 -5.1152769 -0.6446546 0.0021080
Lake.Test <- HSD.test(Lake.anova, "lakename", group = TRUE)</pre>
Lake. Test #another test to determine differences in means
## $statistics
##
    MSerror Df
                     Mean
##
     54.1016 9719 12.72087 57.82135
##
## $parameters
##
            name.t ntr StudentizedRange alpha
##
     Tukey lakename
                                4.387504 0.05
                      9
##
## $means
                                                             Q25
                                                                   Q50
                     temperature_C
                                        std
                                               r Min Max
## Central Long Lake
                         17.66641 4.196292 128 8.9 26.8 14.400 18.40 21.000
## Crampton Lake
                          15.35189 7.244773
                                             318 5.0 27.5 7.525 16.90 22.300
## East Long Lake
                          10.26767 6.766804
                                             968 4.2 34.1
                                                          4.975 6.50 15.925
## Hummingbird Lake
                         10.77328 7.017845 116 4.0 31.5
                                                           5.200 7.00 15.625
## Paul Lake
                         13.81426 7.296928 2660 4.7 27.7
                                                          6.500 12.40 21.400
## Peter Lake
                         13.31626 7.669758 2872 4.0 27.0 5.600 11.40 21.500
## Tuesday Lake
                         11.06923 7.698687 1524 0.3 27.7
                                                          4.400 6.80 19.400
## Ward Lake
                         14.45862 7.409079 116 5.7 27.6 7.200 12.55 23.200
                         11.57865 6.980789 1026 4.0 25.7 5.400 8.00 18.800
## West Long Lake
##
## $comparison
## NULL
##
## $groups
                     temperature_C groups
## Central Long Lake
                         17.66641
                                        a
## Crampton Lake
                          15.35189
                                       ab
## Ward Lake
                          14.45862
                                       bc
## Paul Lake
                         13.81426
                                        С
## Peter Lake
                          13.31626
                                        С
## West Long Lake
                         11.57865
                                        d
```

```
## Tuesday Lake 11.06923 de
## Hummingbird Lake 10.77328 de
## East Long Lake 10.26767 e
##
## attr(,"class")
## [1] "group"
```

16. From the findings above, which lakes have the same mean temperature, statistically speaking, as Peter Lake? Does any lake have a mean temperature that is statistically distinct from all the other lakes?

Answer: From the adhoc tests, it seems that Paul Lake is the only lake that is similar in mean temperature as Peter Lake. Central Long Lake seems to be the one lake to have the highest differences out of all the other lakes.

17. If we were just looking at Peter Lake and Paul Lake. What's another test we might explore to see whether they have distinct mean temperatures?

Answer: You could also run the HSD.test to see which lakes are distinct from one another because it provides a categorical grouping instead of the numerical differences.