Problem Set 2

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The minimum production occurs if only K=1 produces.

$$T(i) = \rho \left(\frac{p-1}{2}\right) - 1 - \left(\frac{p-1}{2}\right) - \left(\frac{p-1}{2}\right)^2 = 0$$

$$p^2 - p - 2 - p + 1 - \left(\frac{p^2 - 2p + 1}{2}\right) = 0$$

$$\rho^2 - 2\rho + 1 - 4 = 0$$

$$\rho^2 - 2\rho - 3 = 0$$

$$(p-3)(p+1)=0$$

We can't have a negative pince, so p = 3 is the minimum pince at which there is nonzero production.

2a) Given 7, a firm will choose q that maximizes profits and will enter the market if
$$TT \ge 0$$
.

$$T = (1-7) \cdot 20 \times - \times^2 - 1 \quad \text{choose } X \text{ to } \text{max} T$$

FOC:
$$2\theta(1-\gamma) = 2x$$

$$\rightarrow x = \theta(1-\gamma)$$

$$\Pi = 2 \theta^{2} (1-\tau)^{2} - \theta^{2} (1-\tau)^{2} - 1 \ge 0$$

$$\theta(1-t)=1$$

$$\theta(1-t)=1$$

$$\theta \geq 1$$

$$\theta(\iota-\gamma) \ge 1$$
 $\theta \ge 1$

$$\theta(\iota-\gamma) \ge \iota$$
 $\theta \ge \iota$

$$\theta \geq \frac{1}{1-\gamma}$$

). Then
$$f = -M^{1}(\theta) = \beta \theta^{-\beta-1}$$

Let
$$F=1-M(\theta)$$
. Then $F=-M^{1}(\theta)=\beta\theta^{-\beta-1}$

$$(0)_{i} = \int_{\frac{1}{1-T}}^{\infty} 2(1-T)\theta^{2} \cdot (\beta\theta^{-\beta-1}) d\theta$$

$$= \int_{\frac{1}{1-T}}^{\infty} 2\beta(1-T)\theta^{1-\beta} d\theta$$

$$\int_{1-\tau}^{\tau} 2\beta(1-\tau) \theta^{1-\beta} d\theta$$

$$= \int_{1-\tau}^{\infty} 2\beta(1-\tau) \theta^{1-\beta} d\theta$$

$$= 2\beta(1-\tau) \theta^{2-\beta} e^{\infty}$$

Note B>2

$$= 2\beta(1-T) \quad \theta^{2-\beta} \quad \infty$$

$$= 0 - 2\beta(1-T) \quad \left(\frac{1}{1-T}\right)^{2-\beta}$$

$$= 0 - \frac{2\beta(\nu-\gamma)}{\beta-2} \left(\frac{1}{2}\right)$$

$$= \frac{2B(1-\gamma)^{B-1}}{B-2}$$

The cutoff to produce is $\theta = 1/1-T$, so if T increases, fewer developers will produce. Further the production function is $q = 2\theta x$, where $x = \theta(1-T)$, so production developers that continue to produce when Y increases will produce a smaller quantity.

2c) $R = \Upsilon Q_3 = \Upsilon \frac{2B(1-\Upsilon)^{B-1}}{B-2}$ Foc: $\frac{2B(1-\Upsilon)^{B-1}}{B-2} = \frac{2(B-1)\Upsilon B(1-\Upsilon)^{B-2}}{B-2}$ $1-\Upsilon = \Upsilon (B-1)$

2d) When B rises, the distribution M(B) changes so that fewer firms produce, and firms are less productive. As a result Qs will decrease.

3)
$$P_1 = a_1 - b_1 Q$$
 Fruit Bowl
 $P_2 = a_2 - b_2 Q$ Triple chocolate chunk

$$a_1$$
 a_2 blc FB has higher pince intercept than TCC $p_1 = p_2$ at interior point then b_1 b_2

 $\Pi_1 = P_1 \cdot Q_1 - MCQ_1$ where MC is constant

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3)
$$\Pi_1 = P_1 \cdot Q_1 - MCQ_1$$
 where MC is constant $= (a_1 - b_1 \cdot Q_1)Q_1 - MCQ_1$

Foc:
$$a_1 - 2b_1 Q_1 - MC = 0$$

$$Q_1^* = \underbrace{a - MC}_{2b_1}$$

$$\frac{a_1-b_1}{2b_1}$$

Since a, 7 az, P, >Pz.

