

**Econ 703   Fall 2007**  
**Homework 2**

**Due Tuesday, October 2.**

1. Sundaram, #13, p.68
2. Sundaram, #17, p.68
3. Sundaram, #23, p.68
4. A point  $x$  is an interior point of set  $A$  if there exists a neighbourhood  $N$  of  $x$  such that  $N \subset A$ . Let  $\mathring{A}$  be the interior of the set  $A$ , i.e. the collection of all of its interior points. Prove the following :
  - (1)  $\mathring{A}$  is an open set;
  - (2)  $A$  is open iff  $A = \mathring{A}$
  - (3) If  $B \subset A$ , and  $B$  is open, then  $B \subset \mathring{A}$ .
5. Let  $K$  be the union of the set  $\{0\}$  and the set  $\{1/n, n \in \mathbb{Z}_{++}\}$ . Prove that  $K$  is compact directly from the definition (i.e., without using the Heine\_Borel Theorem).