

University of Wisconsin-Madison  
Department of Economics

Econ 703  
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**Homework #1**

1. Prove the following proposition : If  $x \in \phi$ , then  $x$  is a square orange.  
(Hint : Use a contrapositive proof).
2. Let  $A$  and  $B$  be sets of real numbers. Write the negation of each of the following statements:  
(a) For every  $a \in A$ , it is true that  $a^2 \in B$ .  
(b) For at least one  $a \in A$ , it is true that  $a^2 \in B$ .  
(c) For every  $a \in A$ , it is true that  $a^2 \notin B$ .  
(d) For at least one  $a \notin A$ , it is true that  $a^2 \in B$ .
3. Let  $f: \mathfrak{R} \rightarrow \mathfrak{R}$  be given by the rule  $f(x) = x^3 - x$ . By restricting the domain and range of  $f$  appropriately, obtain from  $f$  a bijective function  $g$ . Draw the graphs of  $g$  and  $g^{-1}$  (there are several possible choices for  $g$ ).
4. Define two points  $(x_0, y_0)$  and  $(x_1, y_1)$  of the plane to be equivalent if  $y_0 - x_0^2 = y_1 - x_1^2$ . Verify that this is an equivalence relation, and describe the equivalence classes.
5. Prove by induction that given  $n \in \mathbb{Z}_+$ , every nonempty subset of  $\{1, \dots, n\}$  has a largest element.