Exam Study Guide

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General Setup:

MAXE = Bt U(c(st)) IT(st)

S.t. = T q(st) c(st) = E q(st) e(st)

1) Take FOC

2) Divide types of agents FOCA | FOCB

-Show constant ratio over states | times

3) Divide times FOC+++| FOC+

- Shows progression of prices

4) Divide over states

- Shows ratio of prices by state
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Examples:

- Lectures 1 & 2
- HWI, Question 8.3

Sequential markets - solve using Bellman See PSI

Limited Commitment (Autarky):

- - This usually won't hold if types labor, capital, hidden. For w.r.t c1, C2 etc.
- ② Find value of punishment (Such as autavFy)
 for deviating at t=sVit = max $\sum_{t=s}^{\infty} g^{t-s} u(ci)$ See 2020 Exam Q2
 - s.t. HHBC: c; = e;
- Resolve planners publem w| IC cons.

 max $\Xi_1 \beta^+ [u(c_1) + u(c_2)]$ S.t. $c_1 + c_2 \leq e_1 + e_2$ No distortion
- see lecture 3 for spot market supporting ECZ, whas
 - This generally holds in CE with a borrowing constraint in HHBC bonds between HHs

Ramsey Problem:

O Solve HH problem to find policy wedge:

max $\geq \beta^{+}$ u(C4) + v(L +)

- v(n+)

st (1+TG)C++ K++++ b+++ \leq w(1-Th+) n++ R+ b++ R+ K+ diff.

where $R_{+}^{k} = 1 + (1-Te+)(r_{+}+8)$ wedges

Solve for labor supply & Euler to find wedges. See Lecture 7! FOC w.v.+ c, k, b, l,n

For the CE:

alloc: C+, K++1, b++1, L+, n+

prices: W, r

policy: Ti, Rt

 $\begin{array}{lll}
\text{Find} & \text{Implementability Constraint:} \\
\text{Sp}^+ \left[u_{\varsigma_1} \cdot c_{\varsigma_1} + u_{\varrho_1} \cdot l \right] = \underbrace{u_{\varsigma_0}}_{1+T_{\varsigma_0}} \left[R_{l_0} b_{-1} + R_{l_0} K_{-1} \right] \\
&+ u_{l_0} \cdot n & \text{I+T_{\varsigma_0}}
\end{array}$

3 Solve planners publish: $\max \sum_{k} g^{+} u(c) + v(l)$ S.t. C+ g+ + K++1 = F(K+1N+) + (1-8) k+ No Londs!

and 10 above

1) Take FOCS W.V.+ C, K, l, b, n

2) Compare Euler/15 fir egh with specified wedge to determine Tivalue

cash | Credit Good:

① Solve HH problem: c1-cash

max ≥ p+u(c1, c2, n2) c2-credit

Pt C1, t ≤ M+

FOCs w.r.+ C1, C2, n, M, B See PS4

@ Find IC:

$$pon-distorted$$
 $p^{\dagger} \left[u_{1} \cdot c_{1+} + u_{2} \cdot c_{2+} + u_{3} \cdot n_{+} \right] = \underbrace{u_{z_{0}}}_{p_{0}} \cdot \left[M_{-1} + R_{b_{0}} B_{-1} \right]$
 e^{-c}

3 Solve Planner problem: Fiscal monetary pol notes

max & B+ u(c1, C2, n)

s.t. M. - M. 1 + B+ = R+1 S+-1 + P+1 g+-1 - P+-1 m+1

s.t. $M_1 - M_{t-1} + B_t = R_{t-1} + P_{t-1} + P_{t-1}$

FOC W.V.+ C1 C2, N1 M18

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Friedman rule: return on bonds = 1

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Mirleesian: Discrete types
① Types θ are known, solve willtarian planner problem:

max ≥ β*[π(θ)[u(c(θ+))-v(y(θ+)/θ+)]

+π(θ)[u(c(θ+))-v(y(θ+)/θ+)]]
             5.4 T(OH) C(OH) + T(OL) C(OL) &
                       \pi(\theta_H)y(\theta_H) + \pi(\theta_U)y(\theta_U)
       FOC W.Y.+ CIN
       Usually get that everyone consumes equally.
            u(c(OH)) - v(y(OH) (OH) > u(c(OL)) - v(y(OL) / OH) Binds!
            u(c(02))-v(y(02)/02)> u(c(04))-v(y(04)/02)
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2 (c constraint:

u(c(θμ)) - v(y(θμ)|θμ) ≥ u(c(θμ)) - v(y(θμ)|θμ) Binds

u(c(θμ)) - v(y(θμ)|θμ) ≥ u(c(θμ)) - v(y(θμ)|θμ)

3 Planner's Problem with unknown types:

max ≥ β⁺[π(θμ)[u(c(θμ)) - v(y(θμ)|θμ)]

+π(θμ)[u(c(θμ)) - v(y(θμ)|θμ)]

3.+ π(θμ) c(θμ) + π(θμ) c(θμ) = Rc

π(θμ) y(θμ) + π(θμ) y(θμ)

and u(c(θμ)) - v(y(θμ)|θμ) = u(c(θμ)) - v(y(θμ)|θμ) (c

FOC w.v.+ c₁ y. No distortion for θμ.

Let these be c*, y*

Tax Structures:

T(y)=Sy-c if y 6 \(\) y otherwise

HH solves:

max u(c) - v(4/0)

s.t c= y-tly)

Mirleesian: continuum of types

1.
$$y(\theta)$$
 increasing in θ
2. $y(\theta) = y(\theta)$ $y'(y(\theta))$

$$N(\theta) = N\left(c(\theta) - N\left(\frac{\lambda(\theta)}{\theta}\right)\right)$$

$$\geq u\left(c(\hat{\theta}) - v\left(\underline{y(\hat{\theta})}\right)\right)$$
 whility of 0 pretending to be $\hat{\theta}$

$$\max_{c_1 y} \left\{ W(u(c(x) - v(\underbrace{y(\theta)}_{\theta})) dF(\theta) \right\}$$

and
$$u'(\theta) = \underbrace{y(\theta)}_{\theta^2} v'(\underbrace{y(\theta)}_{\theta})$$

and
$$y(\theta)$$
 increasing in θ