CPSC-354 Report

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Abstract

This report describes the concepts and techniques learned throughout the course, specifically Lean, proofs, and lambda calculus. Each week goes through a specific topic within the general concepts. The purpose of exploring all these topics is to get familiar with the core principles of programming languages.

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1 Introduction

The very fundementals of programming languages (syntax, interpretation, etc) are based on math and logic. The report goes over what was learned each week. The goal of exploring each topic is to understand what is takes to construct a programming language (e.g. recursion, AST). The report goes in order of what was learned first to the most recent. It first delves into mathmatical proofs/Lean and then slowly starts connecting to the concepts of programming languages.

2 Week by Week

2.1 Week 1

Notes

```
Learned about some tactics and theorems
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rfl: a tactic that proves theorems that take the form of X=X rw: a tactic that rewrites a proof one_eq_succ_zero: a theorem that proves 1=\mathrm{succ}\ 0 (there are also other similar existing theorems like two_eq_succ_one and so on) add_zero: a theorem that proves a+0=a. add_succ: a theorem that proves a+\mathrm{succ}\ b=\mathrm{succ}(a+b) succ_eq_add_one: a theorem that proves succ a=a+1
```

Homework

Problem 5:

a b c are in the set of natural numbers.

Prove that both sides are equal to each other.

$$a + (b + 0) + (c + 0) = a + b + c$$

rw [add_zero] - uses the add_zero theorem to prove that b + 0 = b

This is rewritten to:

$$a + b + (c + 0) = a + b + c$$

rw [add_zero] - this is done again to prove that c + 0 = c

This is rewritten to:

$$a + b + c = a + b + c$$

rfl - this proves that both sides that look the same are equal to each other

Problem 6:

```
This is the same problem as 5 but will be approached in a different manner.
```

$$a + (b + 0) + (c + 0) = a + b + c$$

rw [add_zero c] - specifically applies the add_zero theorem to c, making c + 0 into c

This is rewritten to:

$$a + (b + 0) + c = a + b + c$$

rw [add_zero b] - specifically applies the add_zero theorem to b, making b + 0 into b

This is rewritten to:

$$a + b + c = a + b + c$$

rfl - this proves that both sides that look the same are equal to each other

Problem 7:

n is in the set of natural numbers.

Prove that both sides are equal to each other.

succ n = n + 1 rw[one_eq_succ_zero] - rewrite 1 into successor 0 This is rewritten to:

succ n = n + succ 0

 $rw[add_succ]$ - uses the add_succ theorem to change $n + succ \ 0$ into succ(n + 0)

This is rewritten to:

$$succ n = succ (n + 0)$$

 $rw[add_zero]$ - uses the add_zero theorem to prove that n + 0 = n

This is rewritten to:

```
succ n = succ n
```

rfl - this proves that both sides that look the same are equal to each other

```
Problem 8:
Prove that both sides are equal to each other.
2 + 2 = 4
rw[two_eq_succ_one] - rewrites 2 into succ 1
This is rewritten to:
succ 1 + succ 1 = 4
rw[one_eq_succ_zero] - rewrites 1 into succ 0
This is rewritten to:
\operatorname{succ} (\operatorname{succ} 0) + \operatorname{succ} (\operatorname{succ} 0) = 4
rw[four_eq_succ_three] - rewrites 4 into succ 3
This is rewritten to:
succ (succ 0) + succ (succ 0) = succ 3
rw[three_eq_succ_two] - rewrites 3 into succ 2
This is rewritten to:
succ (succ 0) + succ (succ 0) = succ (succ 2)
rw[two_eq_succ_one] - rewrites 2 into succ 1
This is rewritten to:
succ (succ 0) + succ (succ 0) = succ (succ (succ 1))
rw[one_eq_succ_zero] - rewrites 1 into succ 0
This is rewritten to:
succ (succ 0) + succ (succ 0) = succ (succ (succ (succ 0)))
rw[add\_succ] - changes succ (succ 0) + succ (succ 0) into succ (succ (succ 0) + succ 0)
This is rewritten to:
succ (succ (succ 0) + succ 0) = succ (succ (succ (succ 0)))
rw[add\_succ] - changes succ (succ (succ 0) + succ 0) into succ (succ (succ (succ 0) + 0))
This is rewritten to:
\operatorname{succ} (\operatorname{succ} (\operatorname{succ} (\operatorname{succ} 0) + 0)) = \operatorname{succ} (\operatorname{succ} (\operatorname{succ} (\operatorname{succ} 0)))
rw[add\_zero] - changes succ (succ 0) + 0 into
This is rewritten to:
succ (succ (succ
rfl - this proves that both sides that look the same are equal to each other
```

For level 5: add_zero is a Lean proof that a+0=a (a representing any number). In mathematics, there are laws for arithemic. One of them is called the identity which applies to addition and multiplication. For addition, it states that m+0=m=0+m. This is the exact same as the Lean proof, a+0=a, which can also be written as a=0+a.

Comments and Questions

Learning the root of mathematics is very eye-opening, and I am confident it will be the same for programming languages. It provides another perspective for elementary functions like 2+2 equals 4, which is different from just knowing it through memorization. I feel as though this is why people have been able to expand mathematically. This makes me wonder: how can looking through the core of programming help us better current languages (e.g. python, rust)?

2.2 Week 2

Notes

Recursion as a concept using the Towers of Hanoi: It is broken down into: moving a tower of n disks from x to y moving a tower of n+1 disks when it is already known how to move a tower of n disks The algorithm is made up of a bunch of "pushs" and "pops" The logic overall is a bunch of back and forth movement of the disks

Lean: induction proof with: induction n with d hd succ_add: proves that succ a + b = succ (a + b) add_comm x y: proves that x + y = y + x add_assoc: proves that a + b + c = a + (b + c) add_right_comm a b c: proves that a + b + c = a + c + b

Homework

```
Problem 1:
n is in the natural number set
Prove 0 + n = n.
induction n with d hd - starting a proof by induction
Now our first goal is:
0 + 0 = 0
rw[add\_zero] - proves that 0 + 0 = 0
This is rewritten to:
rfl - this proves that both sides that look the same are equal to each other
Now, we prove our second goal
hd: 0 + d = d
0 + \operatorname{succ} d = \operatorname{succ} d
rw[add\_succ] - proves that 0 + succ d = succ (0 + d)
This is rewritten to:
\operatorname{succ} (0 + d) = \operatorname{succ} d
rw[hd] - this replaces 0 + d with d
This is rewritten to:
succ d = succ d
rfl - this proves that both sides that look the same are equal to each other
Problem 2:
a b is in the set of natural numbers
Prove succ a + b = succ (a + b)
inductin b with d hd - starting a proof by induction
Now our first goal is:
\operatorname{succ} a + 0 = \operatorname{succ} (a + 0)
rw[add\_zero] - proves that succ a + 0 = succ a
This is rewritten to:
succ a = succ(a + 0)
rw[add\_zero] - proves that succ (a + 0) = succ a
This is rewritten to:
succ a = succ a
rfl - this proves that both sides that look the same are equal to each other
Now, we prove our second goal
hd: succ a + d = succ (a + d)
succ a + succ d = succ (a + succ d)
rw[add\_succ] - proves that succ a + succ d = succ (succ a + d)
```

```
This is rewritten to:
succ (succ a + d) = succ (a + succ d)
rw[hd] - this replaces succ a + d with succ (a + d)
This is rewritten to:
succ (succ (a + d)) = succ (a + succ d)
rw[add\_succ] - proves that succ (a + succ d) = succ (succ (a + d))
This is rewritten to:
succ (succ (a + d)) = succ (succ (a + d))
rfl - this proves that both sides that look the same are equal to each other
Problem 3:
a b is in the set of natural numbers
Prove a + b = b + a
induction b with hd - starting a proof by induction
Now our first goal is:
a + 0 = 0 + a
rw[zero\_add] - proves that 0 + a = a
This is rewritten to:
a + 0 = a
rw[add\_zero] - proves that a + 0 = a
This is rewritten to:
rfl - this proves that both sides that look the same are equal to each other
Now, we prove our second goal
n_{i}: a + hd = hd + a
a + succ hd = succ hd + a
rw[add\_succ] - proves that a + succ hd = succ (a + hd)
This is rewritten to:
\operatorname{succ} (a + \operatorname{hd}) = \operatorname{succ} \operatorname{hd} + a
rw[succ\_add] - proves that succ hd + a = succ (hd + a)
This is rewritten to:
succ (a + hd) = succ (hd + a)
rw[n_ih] - replaces succ (a + hd) with succ (hd + a)
This is rewritten to:
\operatorname{succ} (\operatorname{hd} + \operatorname{a}) = \operatorname{succ} (\operatorname{hd} + \operatorname{a})
rfl - this proves that both sides that look the same are equal to each other
Problem 4:
a b c is in the set of natural numbers
Prove a + b + c = a + (b + c)
induction a with hd - starting a proof by induction
Now our first goal is:
0 + b + c = 0 + (b + c)
rw[zero\_add] - proves that 0 + b = b
This is rewritten to:
b + c = 0 + (b + c)
rw[zero\_add] - proves that 0 + (b + c) = b + c
This is rewritten to:
b + c = b + c
rfl - this proves that both sides that look the same are equal to each other
```

```
Now, we prove our second goal
n_i: hd + b + c = hd + (b + c)
\operatorname{succ} \operatorname{hd} + \operatorname{b} + \operatorname{c} = \operatorname{succ} \operatorname{hd} + (\operatorname{b} + \operatorname{c})
rw[succ\_add] - proves that succ\ hd + b + c = succ\ (hd + b) + c
This is rewritten to:
\operatorname{succ} (\operatorname{hd} + \operatorname{b}) + \operatorname{c} = \operatorname{succ} \operatorname{hd} + (\operatorname{b} + \operatorname{c})
rw[succ\_add] - proves that succ(hd + b) + c = succ(hd + b + c)
This is rewritten to:
succ (hd + b + c) = succ hd + (b + c)
rw[n_i] - replaces succ (hd + b + c) with succ (hd + (b + c))
This is rewritten to:
succ (hd + (b + c)) = succ hd + (b + c)
rw[succ\_add] - proves succ hd + (b + c) = succ (hd + (b + c))
This is rewritten to:
succ (hd + (b + c)) = succ (hd + (b + c))
rfl - this proves that both sides that look the same are equal to each other
Problem 5:
a b c is in the set of natural numbers
Prove a + b + c = a + c + b
induction c with hd - starting a proof by induction
Now our first goal is:
a + b + 0 = a + 0 + b
rw[add\_zero] - proves that b + 0 = b
This is rewritten to:
a + b = a + 0 + b
rw[add\_zero] 0 proves that a + 0 = a
This is rewritten to:
a + b = a + b
rfl - this proves that both sides that look the same are equal to each other
Now, we prove our second goal
n_ih: a + b + hd = a + hd + b
a + b + succ hd = a + succ hd + b
rw[add\_succ] - proves that a + b + succ hd = succ (a + b + hd)
This is rewritten to:
\operatorname{succ} (a + b + hd) = a + \operatorname{succ} hd + b
rw[add\_succ] - proves that a + succ hd + b = succ (a + hd) + b
This is rewritten to:
succ (a + b + hd) = succ (a + hd) + b
rw[succ\_add] - proves that succ(a + hd) + b = succ(a + hd + b)
This is rewritten to:
\operatorname{succ} (a + b + hd) = \operatorname{succ} (a + hd + b)
rw[n_i] - replaces a + b + hd with a + hd + b
This is rewritten to
succ (a + hd + b) = succ (a + hd + b)
rfl - this proves that both sides that look the same are equal to each other
Problem 5 Proof in Mathematics:
a + b + c = a + (b + c)
0 + b + c = 0 + (b + c) - Basis
```

```
b+c=0+(b+c) - Addition Identity b+c=b+c - Addition Identity Inductive Step: k+b+c=k+(b+c) The goal is to prove that Sk+b+c=Sk+(b+c) S(k+b+c)=Sk+(b+c)- Definition of Addition S(k+b+c)=S(k+(b+c)) - Definition of Addition S(k+b+c)=S(k+(b+c))- Inductive Hypothesis Therefore, by the Axiom of induction a+b+c=a+(b+c) for all a in the natural numbers set
```

Math to Lean

Basis: induction a with hd Addition Identity: zero_add Definition of Addition: succ_add Inductive Hypothesis: n_ih

Comments and Questions

The Towers of Hanoi reminded me of solving certain problems by simply using recursion. I also remember applying this method to the Fibonacci sequence. This makes me wonder how it transfers to math. How does recursion appear in mathematics or, specifically, in Lean?

2.3 Week 3

Homework

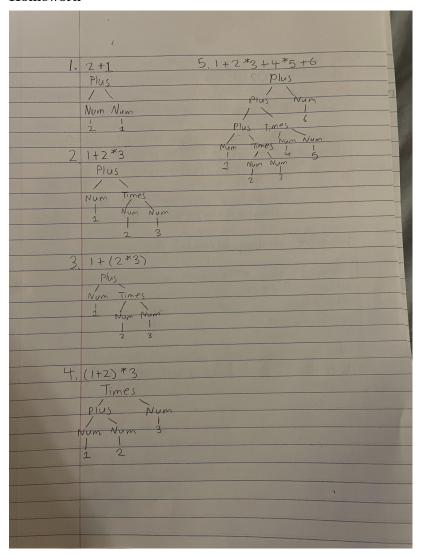
Week 3 Assignment

Comments and Questions

My literature review is about the cause for many different programming languages, the abstraction of them in the future, and what needs future ones would need to fulfill. I found that languages evolved depending on the different needs and users over time. For instance, Domain-specific languages were created to meet specific needs. SQL, being one of them, was created to interact with databases. Within the topic of abstraction, PLs are bound to become higher level to not worry about lower-level implementation. Examples of the current progress towards abstraction would be AI-assisted programming and declarative programming. However, abstraction will not change the usage of current languages like Java, Python, and C++ in the foreseeable future. These languages have made a huge impact and it is shown through their extensive ecosystems and sheer amount of existing codebases. On the other hand, some specific areas use newer languages like Rust and Kotlin. They fulfill more modern needs like memory safety and developer productivity. Future programming languages would need to deal with challenges like security, AI, and concurrency.

2.4 Week 4

Homework



Comments and Questions

Parsing seemed to work really great with expressions. In general, is parsing a good strategy when it comes to breaking things down?

2.5 Week 5

Notes

exact -conclusion of a proof Operator: \land -Logical And Example: $A \land B$ -A and B

and_into -takes two pieces of evidence and combines it into one

have -adds new assumptions to the proof

Homework

```
Problem 1:
exact todo_list
Problem 2:
exact and_intro p s
Problem 3:
exact \langle \langle a,i \rangle, \langle o,u \rangle \rangle
Problem 4:
have p := and_left \ vmS
exact p
Problem 5:
have q := and\_right h
exact q
Problem 6:
have a := and left h1
have u := and\_right h2
exact \langle a, u \rangle
Problem 7:
have h1 := h.left
have h2 := h1.right
have h3 := h2.left
have h4 := h3.left
have h5 := h4.right
exact h5
Problem 8:
have h1 := h.left
have a := h1.right
have h2 := h1.left
have p := h2.left
have s := h2.right
have h3 := h.right
have h4 := h3.right
have h5 := h4.left
have\ c:=h5.left
In mathmatical proof:
If ((P \wedge S) \wedge A) \wedge I \wedge (C \wedge O) \wedge U then A \wedge C \wedge P \wedge S.
Proof:
((P \land S) \land A) \land I \land (C \land O) \land U
```

assumption

(2)
$$(P \wedge S) \wedge A$$
 and left (1)
(3) A and right (2)
(4) $(P \wedge S)$ and left (2)
(5) P and left (4)
(6) S and right (4)
(7) $I \wedge (C \wedge O) \wedge U$ and right (1)
(8) $(C \wedge O) \wedge U$ and right (7)
(9) $C \wedge O$ and left (8)
(10) C and left (9)
(11) $A \wedge C \wedge P \wedge S$

Comments and Questions

and_intro (3)(10)(5)(6)

How does lean help with problem solving when it comes to programming?

2.6 Week 6

Homework

```
Problem 1:
have b := bakery_service p
exact b
Problem 2:
exact fun h : C => h
Problem 3:
exact fun h => and_intro h.right h.left
Problem 4:
exact fun h : C => have a : A := h1 h; h2 a
Problem 5:
have q : Q := h1 p
have t : T := h3 q
exact h5 t
Problem 6:
exact fun c : C =>
fun d : D =>
have cd : C \wedge D := \langle c, d \rangle;
h cd
```

Comments and Questions

Solving lean logic game is a simple view into proving theorems and the foundations of programming languages. When it comes to the lambda problems specifically, how do real-world challenges complicate the applications of lambda?

2.7 Week 7

Couldn't finish...

Homework

1.

$$((\lambda m.\lambda n.m n) (\lambda f.\lambda x.f (f x))) (\lambda f.\lambda x.f (f (f x)))$$
$$((\lambda m.\lambda n.m n) (\lambda f.\lambda x.f (f x))) \to \lambda n.(\lambda f.\lambda x.f (f x)) n$$
$$(\lambda f.\lambda x.f (f x)) n \to \lambda x.n (n x)$$

$$(\lambda n.\lambda x.n (n x)) (\lambda f.\lambda x.f (f (f x)))$$

$$(\lambda n.\lambda x.n (n x)) (\lambda f.\lambda x.f (f (f x))) \rightarrow \lambda x.(\lambda f.\lambda x.f (f (f x))) ((\lambda f.\lambda x.f (f (f x))) x)$$

$$(\lambda f.\lambda x.f (f (f x))) x \rightarrow \lambda x.x (x (x x))$$

$$\lambda x.(\lambda f.\lambda x.f (f (f x))) (\lambda x.x (x (x x)))$$

$$(\lambda f.\lambda x.f (f (f x))) (\lambda x.x (x (x x))) \rightarrow \lambda x.(\lambda x.x (x (x x))) ((\lambda x.x (x (x x))) x)$$

$$(\lambda x.x (x (x x))) x \rightarrow x (x (x x))$$

$$(\lambda x.x (x (x x))) (x (x (x x))) ((x (x (x x))) ((x (x (x x))) (x (x (x x))))$$

The lambda term implements addition on natural numbers. It is done by combing two Church numerals. It carries out addition by counting the the total number of times the function is being applied.

Comments and Questions

Can church numerals be used to represent recursive functions/processes?

2.8 Week 8

Homework

Answers on week 9

Comments and Questions

When it comes to evaluation strategies in lambda calculus, what are the trade-offs? How do these strategies affect performance and accuracy in a practical implementation?

2.9 Week 9

Homework

- 2. a is applied to b, which leads to (ab). Then, (ab) is applied to c, resulting in ((ab)c). Finally, ((ab)c) is applied to d, which leads to (((ab)c)d). (a) reduces to a it's already in its simplest form.
- 3. When substituting a variable, wall instances of that variable are replaced. However, if the variable being substituted for is also bound, the meaning of the expression is changed. This is implemented by traversing the AST of the expression, checking for bound variables, and renaming them.
- 4. No, not everything is the expected result.

5.

$$Y = \lambda f.(\lambda x. f(xx))(\lambda x. f(xx))$$

Comments and Questions

How could different evaluation strategies impact the trace output produced by an interpreter?

2.10 Week 10

Homework

- 1. The challenge of working through Homework 8/9 and Assignment 3 was figuring out why the interpreter wouldn't completely evaluate everything.
- 2. The key insight for Assignment 3 was just looking through the evaluation function and looking at where ecxactly it stopped evaluating the function and just returned whatever it found.
- 3. The most interesting take away was from the homework and assignment was using the debugger to see how far the program would evaluate a lambda function. I never really use the debugger, so it was interesting to break things apart.

Comments and Questions

How can the interpreter be expanded upon to handle more complex structures?

2.11 Week 11

Homework

Pictures for each of the ARSs:
A CONTRACTOR OF THE PROPERTY O
Homework II
normal normal
2 Empty (Terminating (confluent, has a unique form)
2. a (Terminating Confluent, has a unique normal form)
1. Empty (Termin ating, Confluent, has a unique form) 2. a (Terminating, Confluent, has a unique normal form) 3 as (Not terminating, Confluent, doesn't have unique normal form) 4 a (terminating, not antiluent, doesn't have unique normal form)
4 a (termination and confluent doesn't have well as
The state of the s
5 >a >b (1 > 100 + 01 + 1 > 100 + 10
5 to >b (terminating, confluent, has a unique normal form)
6. Or Inst francoching to Maril a + 1
6. a Last terminating, not confluent, doesn't have unique normal
form)
(b) (c) (d)
(LA) 20011:39 M
7. a (No-) terminating, not confluent, doesn't have
wrique normal form)
she are
A Company of the Comp
12-1/10 (1-10-10-10-10-10-10-10-10-10-10-10-10-10
Continue of the second

Example of ARS for each of the possible 8 combinations

 $\label{eq:confluent} \mbox{Confluent} = \mbox{True}, \mbox{Terminating: True}, \mbox{Has A Unique Normal Form: True}$

$$A = a, b, R = (a, b)$$

Confluent = True, Terminating: True, Has A Unique Normal Form: False

$$A = a, b, c, R = (a, b), (a, c)$$

Confluent = True, Terminating: False, Has A Unique Normal Form: True

$$A = a, R = (a, a)$$

Confluent = True, Terminating: False, Has A Unique Normal Form: False

$$A = a, b, R = (a, a), (a, b)$$

Confluent = False, Terminating: True, Has A Unique Normal Form: True

$$A = a, b, c, R = (a, b), (b, b)$$

Confluent = False, Terminating: True, Has A Unique Normal Form: True

$$A = a, b, c, R = (a, b), (a, c)$$

Confluent = False, Terminating: False, Has A Unique Normal Form: True

$$A = a, b, R = (a, b), (b, a)$$

Confluent = False, Terminating: False, Has A Unique Normal Form: False

$$A = a, b, c, R = (a, b), (b, b), (a, c), (c, c)$$

Comments and Questions

What characteristics of an ARS (confluency, termination, etc) is important when it comes to programming languages and why?

2.12 Week 12

Homework

1. ba - > ab

The number of substrings is finite. Therefore, the ARS must terminate.

The normal form is where b characters appear before a characters.

It is confluent because it only shifts the positions of the characters. It does not make a new substring.

The ARS sorts the string so that the b characters appear before the a characters.

2.

aa -> a

bb->a

ab - > b

ba - > b

The ARS terminates because the rules reduces the length of the string.

The normal forms are either a or b.

There is not string that reduces to both a and b.

It's confluent because each rewrite reduces the length of the string, and the choice of application does not affect the final result.

All the strings become become equal to their normal forms by switching from - >to =.

= is determined by whether the string has an even or odd number of a's and b's.

If the mod is 2, then the answer is a. if the mod is 1, then the answer is b.

The ARS computes the parity of the number of a's and b's.

3.

aa - > a

bb->b

ba - > ab

ab->ba

The ARS does not terminate because the rewrites alternate and end up looping.

There are no normal forms.

New Rules: ab -> b AND ba -> a

The ARS computes a simplified form.

4

ab - > ba

ba - > ab

The ARS does not terminate because it constantly switches between ab and ba.

There are no normal forms.

New Rules: ab - > a AND ba - > b

The ARS sorts the characters deterministically.

5.

ab - > ba

ba - > ab

aa - >

b->

Reduce Examples:

abba- > aabb- > ab- > ba (loops)

bababa-> infinite alternations

The ARS is not terminating because the ab->ba causes infinite alternations

There are two equivalence classes:

- string with a equal number of a's and b's are equal.
- strings with an unequal number of a's and b's can be reduced.

New Rules: ab - > a AND ba - > b

Question: Does a string reduce to an empty one?

Answer: The string will be empty depending on the number of a's and b's.

5b.

Rewrite: aa -> a AND b ->

The equivalence class is not changed.

Comments and Questions

How does modularity infuence the properties of an ARS?

2.13 Week 13

Homework

Compute fact 3:

```
let rec fact = \lambda n. if n = 0 then 1 else n * fact(n - 1) in fact 3
fact = fix F \text{ in fact } 3 \pmod{4}
(fix F) 3 (def of let)
(\lambda f.(\lambda x. f(x x))(\lambda x. f(x x)))F 3 (def of fix)
(\lambda x.F(x \ x))(\lambda x.F(x \ x)) 3 (beta rule)
F((\lambda x.F(x x))(\lambda x.F(x x))) 3 (beta rule)
(\lambda fact.\lambda n. \text{ if } n=0 \text{ then } 1 \text{ else } n*fact(n-1))((\lambda x.F(x x))(\lambda x.F(x x))) 3 (beta rule)
(\lambda n. \text{ if } n = 0 \text{ then } 1 \text{ else } n * ((\lambda x. F(x x))(\lambda x. F(x x)))(n-1)) 3 \text{ (beta rule)}
if 3 = 0 then 1 else 3 * ((\lambda x.F(x x))(\lambda x.F(x x)))(3 - 1) (beta rule)
3*((\lambda x.F(x x))(\lambda x.F(x x)))(3-1) (def of if)
3 * ((\lambda x.F(x x))(\lambda x.F(x x))) 2 (arithmetic)
3*(2*((\lambda x.F(x\ x))(\lambda x.F(x\ x)))(2-1)) (beta rule and arithmetic)
3*(2*((\lambda x.F(x x))(\lambda x.F(x x))) 1) (arithmetic)
3*(2*(1*((\lambda x.F(x x))(\lambda x.F(x x)))(1-1))) (beta rule and arithmetic)
3 * (2 * (1 * ((\lambda x.F(x x))(\lambda x.F(x x))) 0)) (arithmetic)
3*(2*(1*1)) (def of if)
3*(2*1)
3 * 2
6 (arithmetic)
fact 3 = 6
```

Comments and Questions

I noticed while computing fact 3, there was a repetition of substitution and expansion of the fixed point combinator. Is there a way to make this process more efficient?

3 Lessons from the Group Assignments and Projects

These group assignments have helped me to understand the hood behind a programming language. It was interesting making syntax or operations that I would normally take for granted in any programming language without even considering how they were implemented in the first place. The assignments helped me to see how the fundamentals come together.

Starting all the way from assignment 1 and 2, we were told to make a calculator in python with basic operations. At first, it just seemed like a very straightforward task, which was implementing addition, multiplication, etc. Although it was a simple, I realize looking back that the purpose of that assignment was to get us into to the concept of developing each syntax for a programming language. Implementing each operation was very similar to implementing different syntax like eq later on. It wasn't simply about the calculator, it was more so, the thought process behind building one.

As we were learning more throughout the lectures, the concept of ASTs were introduced. This was very new to me because I always viewed mathmatical expressions linearly like 1 + 3 * 6. Seeing the same equation as a tree entirely changed my perspective. The + would be the root node with 1 and * as its children with 3 and 6 as the *'s children. However, looking at them in this manner was helpful in creating the grammer for my programming language. I was able to break these equations into smaller pieces and solve them in a different way but with the same result. Assignment 4 brought the previous concepts together and challenged me with implementing more syntax to bring it closer to becoming an actual programming language. For

example adding the semi colons brought more structure to the language.

However, within these assignments, the debugger proved to be helpful in the implementation whether it was because of a running error or the wrong answer. For the expressions that we were evaluating, looking at it step by step would have been more tedious if not for the debugger. It helped me to see where exactly the evaluation went wrong.

4 Conclusion

Looking at the bigger picture of software engineering, this course is a reminder that most high-level programming languages are built on rules and abstractions that require implementation. The foundations of these languages are worth understanding for any software engineer to know as we deal with programming languages daily. When we look at recursion, evaluation strategies, etc we are engaged with constructing compilers, interpreters, and language runtime components, the very things that make the languages what they are. The course's concentration on formal proofs with Lean was very interesting. At first, I viewed these proofs as tedious and only applicable within discrete mathematics or our course and not within my life. But as the course went on, I saw them as important and reliable to keep in mind when developing anything. Proofs are kind of like debugging but with more explanations. One other thing that stood out to me was delving into lambda calculus and its connection to programming languages. Church numerals and fixed-point combinators gave me a new look at some of the simple concepts of programming languages like loops and conditionals. To conclusion, this course helped me to learn about what makes up a programming language.

References

[BLA] Author, Title, Publisher, Year.