

1. Find the equation of a tangent plane to  $e^y + x + x^2 - z = -6$  at the point  $(1, 0, 9)$ .
  
  
  
  
  
  
  
  
  
  
2. (a) Compute the directional derivative of  $f(x, y) = 3xy + y^2$  at  $(2, 3)$  in the direction of  $\underline{u} = \langle 3, -1 \rangle$ .
  
  
  
  
  
  
  
  
  
  
- (b) Find the maximum possible directional derivative at  $(2, 3)$  (choosing from any direction).
  
  
  
  
  
  
  
  
  
  
3. Let  $z = f(x, y) = xy^2$  with  $x = u \cos v$  and  $y = u \sin v$ . Let  $\underline{x} = \begin{pmatrix} x \\ y \end{pmatrix}$  and  $\underline{u} = \begin{pmatrix} u \\ v \end{pmatrix}$ . Find  $\frac{\partial z}{\partial \underline{x}}$  and  $\frac{\partial \underline{x}}{\partial \underline{u}}$ . Use the chain rule to find  $\frac{\partial z}{\partial \underline{u}}$ . Evaluate it at  $u = 2, v = \pi/2$ .