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(03) Recursive and Recursive enumerable properties \* Recursive · ) Concatanation 4 Suppose that L1 & L2 are secresive languages. Then There is a tonachine m2 which accepts any input which is part of 12 and a machine are sejects others, same for L2, a machine m2 exists. Input for new language is w. 4 Concatenation: To we first non deterministically guess where to divide our input winto two parts, wiwz. Then we run Mi on wi and Mz on wiz We accept and reject is both accept or reject otherwise. : Close under Concetenation La Kleene's Closure : If we want to determine if wELi. If w is empty, we accept, otherwise we guess in how many parts we need to break our input. Then we guess where to put all our input breaks in air input, and our M, on each part. We accept if M. accepts all parts - Close under Kleene's Closure 1. Homomorphism: Pecursive languages are not under homomorphism. Posof: - we will show &l I and homomorphism h such that h(L) is undescideable -) let L= { xy | x € {0,13\*, y € {a,b3\* x = < H, w 7}} and y encodes an integer of slich that the TM M will hat on input w will halt in n steps ] -) L is decideable: can simulate Mon input w for n steps ·) Consider homomorphism h: h(0)=0, h(1)=1, h(a)=h(b)=e ·) h(L) = Halt which is undecidable

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Froof: - Given TM M. that decides L., a TM to decide hi'(L) is on input x, compute h(1) and run M, on h(x) accepts if and only if M. accepts

\* Récursively enumerable:-Suppose M. & M2 accept L. & L2 respectively w is our new language

Union both Mi & M2 will accept. RE is absoluted Concatenation.

many parts we need to break our input and where to put our breaks. Then we own on each part. If w is the language then each of these will accept. Thus he is closed under kkenes Closure

both union of Intersection. HE language are closed under

Proof:-given TMs M, & M2 that recognize L. &L2

-) A TM that recognizes L, UL2: on ignore 25 run

M, & M2 on x in parallel, and accept if and only if

either accepts. (Similarly for intersection but no need

for parallel simulation.)