## Two Sample t-test

```
data: c(y1, y3) and y2
t = 0.19396, df = 18, p-value = 0.8484
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -1.357702 1.633892
sample estimates:
mean of x mean of y
 17.67143 17.53333
> 0.19396^2
[1] 0.03762048
> library(ISwR)
> data(red.cell.folate)
> attach(red.cell.folate)
> red.cell.folate
   folate ventilation
1
      243 N20+02,24h
2
      251
           N20+02,24h
3
           N20+02,24h
      275
4
      291
           N20+02,24h
5
      347
           N20+02,24h
6
           N20+02,24h
      354
7
      380
           N20+02,24h
8
           N20+02,24h
      392
9
      206
            N20+02, op
10
      210
            N20+02, op
11
      226
            N20+02, op
12
      249
            N20+02,op
13
      255
            N20+02, op
14
      273
            N20+02, op
15
      285
            N20+02,op
      295
16
            N20+02,op
17
      309
            N20+02, op
18
      241
                02,24h
19
      258
                02,24h
20
                02,24h
      270
21
      293
                02,24h
22
      328
                02,24h
> summary(red.cell.folate)
     folate
                      ventilation
        :206.0
 Min.
                  N20+02,24h:8
 1st Qu.:249.5
                  N20+02, op : 9
 Median :274.0
                  02,24h
        :283.2
 Mean
 3rd Qu.:305.5
 Max.
        :392.0
> anova(lm(folate~ventilation))
```

```
Response: folate
            Df Sum Sq Mean Sq F value
                      7757.9 3.7113
ventilation
            2
               15516
            19 39716
                       2090.3
Residuals
             Pr(>F)
ventilation 0.04359 *
Residuals
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1
> mean(red.cell.folate[1:8,1])
[1] 316.625
> mean(red.cell.folate[9:17,1])
[1] 256.4444
> mean(red.cell.folate[18:22,1])
[1] 278
> tapply(folate, ventilation, mean)
N20+02,24h N20+02,op
                          02,24h
  316.6250
             256.4444
                        278.0000
> data(juul)
> attach(juul)
> head(juul)
   age menarche sex igf1 tanner testvol
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    NA
             NA NA
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2
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                      88
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5
    NA
             NA
                NA
                     131
                             NA
                                     NA
6 0.17
             NA
                  1
                     101
                              1
                                     NA
> dim(juul)
[1] 1339
            6
> anova(lm(igf1~tanner))
Analysis of Variance Table
Response: igf1
           Df
                Sum Sq Mean Sq F value
            1 10985605 10985605 686.07
tanner
Residuals 790 12649728
                          16012
             Pr(>F)
          < 2.2e-16 ***
tanner
Residuals
Signif. codes:
  0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1
  · 1
> tanner
   [1] NA NA NA NA NA 1 1 1 1 1 1 1 1 1 1
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Analysis of Variance Table

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[1291] NA NA NA NA NA NA NA
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[1306] NA NA NA NA NA NA NA
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[1321] NA NA NA NA 5
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[1336] NA NA NA NA
> juul<-transform(juul,tanner=factor(tanner,</pre>
+ labels=c("one","two","three","four","five")))
> anova(lm(juul$iqf1~juul$tanner))
Analysis of Variance Table
Response: juul$iqf1
               Df
                     Sum Sq Mean Sq F value
                                                    Pr(>F)
                4 12696217 3174054
iuul$tanner
                                       228.35 < 2.2e-16
Residuals
              787 10939116
                                13900
```

```
juul$tanner ***
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> data(juul)
> anova(lm(juul$iqf1~juul$tanner))
Analysis of Variance Table
Response: juul$igf1
                  Sum Sq Mean Sq F value
             Df
              1 10985605 10985605 686.07 < 2.2e-16
juul$tanner
           790 12649728
Residuals
                            16012
iuul$tanner ***
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> iuul$tanner<-
+ factor(juul$tanner,labels=c("one","two","three","four","five"))
> anova(lm(juul$igf1~juul$tanner))
Analysis of Variance Table
Response: juul$igf1
             Df
                  Sum Sq Mean Sq F value
                                             Pr(>F)
              4 12696217 3174054 228.35 < 2.2e-16
            787 10939116
Residuals
                           13900
iuul$tanner ***
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> red.cell.folate
   folate ventilation
1
      243 N20+02,24h
2
      251 N20+02,24h
3
      275 N20+02,24h
4
      291 N20+02,24h
5
      347
          N20+02,24h
6
      354
          N20+02,24h
7
           N20+02,24h
      380
8
      392
           N20+02,24h
9
      206
            N20+02,op
10
      210
            N20+02, op
11
      226
            N20+02,op
12
      249
            N20+02, op
13
      255
            N20+02.0p
14
      273
            N20+02, op
```

```
15
      285
            N20+02,op
      295
            N20+02,op
16
            N20+02, op
17
      309
               02,24h
18
      241
19
      258
               02,24h
      270
               02,24h
20
21
      293
               02,24h
      328
               02,24h
22
> anova(lm(folate~ventilation))
Analysis of Variance Table
Response: folate
            Df Sum Sq Mean Sq F value Pr(>F)
ventilation 2 15516 7757.9 3.7113 0.04359 *
Residuals
            19 39716 2090.3
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> summary(lm(folate~ventilation))
Call:
lm(formula = folate ~ ventilation)
Residuals:
             10 Median
    Min
                             30
                                    Max
-73.625 -35.361 -4.444 35.625 75.375
Coefficients:
                     Estimate Std. Error t value
(Intercept)
                       316.62
                                   16.16 19.588
ventilationN20+02,op
                       -60.18
                                   22.22 - 2.709
ventilation02,24h
                       -38,62
                                   26.06 -1.482
                     Pr(>|t|)
(Intercept)
                     4.65e-14 ***
ventilationN20+02,op
                       0.0139 *
ventilation02,24h
                       0.1548
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 45.72 on 19 degrees of freedom
Multiple R-squared: 0.2809,
                                Adjusted R-squared:
F-statistic: 3.711 on 2 and 19 DF, p-value: 0.04359
> summary(lm(folate~ventilation))
Call:
lm(formula = folate ~ ventilation)
Residuals:
```

```
10 Median
                             30
                                    Max
    Min
-73.625 -35.361 -4.444 35.625 75.375
Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
                                   16.16 19.588 4.65e-14
(Intercept)
                       316.62
ventilationN20+02,op
                      -60.18
                                   22.22 -2.709
                                                   0.0139
ventilation02,24h
                      -38.62
                                  26.06 -1.482
                                                   0.1548
(Intercept)
ventilationN20+02,op *
ventilation02,24h
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 45.72 on 19 degrees of freedom
Multiple R-squared: 0.2809, Adjusted R-squared:
F-statistic: 3.711 on 2 and 19 DF, p-value: 0.04359
> pairwise.t.test(folate,ventilation,p.adj="bonferroni")
        Pairwise comparisons using t tests with pooled SD
data:
     folate and ventilation
          N20+02,24h N20+02,op
N20+02, op 0.042
          0.464
                     1.000
02,24h
P value adjustment method: bonferroni
> pairwise.t.test(folate,ventilation)
        Pairwise comparisons using t tests with pooled SD
data:
     folate and ventilation
          N20+02,24h N20+02,op
N20+02,op 0.042
02,24h
          0.310
                     0.408
P value adjustment method: holm
> anova(lm(juul$igf1~juul$tanner))
Analysis of Variance Table
Response: juul$igf1
             Df
                  Sum Sq Mean Sq F value
                                            Pr(>F)
             4 12696217 3174054 228.35 < 2.2e-16 ***
juul$tanner
           787 10939116
Residuals
                           13900
```

```
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> pairwise.t.test(juul$igf1,juul$tanner,p.adj="bonferroni")
        Pairwise comparisons using t tests with pooled SD
       juul$iqf1 and juul$tanner
data:
      one
              two
                      three four
two
      < 2e-16 -
three < 2e-16 9.9e-08 -
four < 2e-16 5.5e-13 1.000 -
five < 2e-16 1.3e-11 1.000 0.048
P value adjustment method: bonferroni
> summary(lm(juul$igf1,juul$tanner))
Error in formula.default(object, env = baseenv()) : invalid formula
> summary(lm(juul$igf1~juul$tanner))
Call:
lm(formula = juul$igf1 \sim juul$tanner)
Residuals:
    Min
             10 Median
                             30
                                    Max
-365.33 -71.37 -10.24
                          61.53 448.67
Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
(Intercept)
                  207.473
                               6.685
                                      31.034
                                               <2e-16 ***
                  145.199
                              15.597
                                       9.309
                                               <2e-16 ***
juul$tannertwo
iuul$tannerthree 275.750
                              18.804
                                      14.665
                                               <2e-16 ***
juul$tannerfour
                  305.545
                              16.863
                                      18.120
                                               <2e-16 ***
                                      27.208
                  257.862
                               9.477
                                               <2e-16 ***
juul$tannerfive
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 117.9 on 787 degrees of freedom
  (547 observations deleted due to missingness)
                     0.5372,
Multiple R-squared:
                                  Adjusted R-squared: 0.5348
F-statistic: 228.4 on 4 and 787 DF, p-value: < 2.2e-16
> pairwise.t.test(juul$igf1,juul$tanner)
        Pairwise comparisons using t tests with pooled SD
data:
       juul$igf1 and juul$tanner
                      three four
      one
              two
      < 2e-16 -
two
```

```
three < 2e-16 \ 3.9e-08 -
four < 2e-16 3.3e-13 0.407 -
five < 2e-16 6.3e-12 0.407 0.015
P value adjustment method: holm
> oneway.test(folate~ventilation)
         One-way analysis of means (not assuming equal
         variances)
       folate and ventilation
data:
F = 2.9704, num df = 2.000, denom df = 11.065,
p-value = 0.09277
> red.cell.folate
   folate ventilation
1
      243 N20+02,24h
      251 N20+02,24h
2
3
      275
           N20+02,24h
4
      291
           N20+02,24h
5
           N20+02,24h
      347
6
      354
           N20+02,24h
7
      380
           N20+02,24h
8
      392
           N20+02,24h
9
      206
            N20+02, op
10
      210
            N20+02, op
11
      226
            N20+02,op
12
      249
            N20+02.0p
13
      255
            N20+02, op
14
      273
            N20+02,op
15
      285
            N20+02, op
16
      295
            N20+02, op
17
      309
            N20+02,op
18
      241
               02,24h
19
      258
               02,24h
20
      270
               02,24h
21
      293
               02,24h
               02,24h
22
      328
> pairwise.t.test(folate,ventilation,pool.sd=F)
         Pairwise comparisons using t tests with non-pooled SD
       folate and ventilation
data:
          N20+02,24h N20+02,op
N20+02, op 0.087
02,24h
          0.321
                      0.321
P value adjustment method: holm
> bartlett.test(folate~ventilation)
```

## Bartlett test of homogeneity of variances

```
folate by ventilation
Bartlett's K-squared = 2.0951, df = 2, p-value =
0.3508
> xbar<-tapply(folate,ventilation,mean) s<-</pre>
tapply(folate, ventilation, sd) n<-tapply(folate, ventilation, length)</pre>
Error: unexpected symbol in "xbar<-tapply(folate,ventilation,mean) s"</pre>
> sem<-s/sqrt(n)</pre>
Error: object 's' not found
> xbar<-tapply(folate,ventilation,mean) ;s<-</pre>
tapply(folate, ventilation, sd) ;n<-tapply(folate, ventilation, length)</pre>
> sem<-s/sqrt(n)</pre>
stripchart(folate~ventilation,vert=T,pch=16 ,method="jitter") ;arrows(
1:3,xbar+sem,1:3,xbar-
sem,angle=90,code=3,length=0.1) ;lines(1:3,xbar,pch=4,type="b",cex=2)
> pain = c(4, 5, 4, 3, 2, 4, 3, 4, 4, 6, 8, 4, 5, 4, 6, 5, 8, 6, 6, 7,
6, 6, 7, 5, 6, 5, 5)
> drug = c(rep("A",9), rep("B",9), rep("C",9))
> migraine = data.frame(pain,drug);migraine
   pain drug
1
      4
            Α
2
      5
            Α
3
      4
            Α
4
      3
            Α
5
      2
            Α
6
      4
            Α
7
      3
            Α
8
      4
            Α
9
      4
            Α
10
      6
            В
11
      8
            В
      4
12
            В
      5
13
            В
      4
            В
14
15
      6
            В
16
      5
            В
17
      8
            В
18
      6
            В
19
      6
            C
20
      7
            C
21
      6
            C
            C
22
      6
23
      7
            C
      5
24
            C
25
      6
            C
```

```
5
           C
27
> plot(pain ~ drug, data=migraine)
> anova(lm(pain~drug, data=migraine))
Analysis of Variance Table
Response: pain
          Df Sum Sq Mean Sq F value
drug
           2 28.222 14.1111 11.906
Residuals 24 28.444 1.1852
             Pr(>F)
          0.0002559 ***
drug
Residuals
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
  0.1 ' ' 1
> summary(aov(pain~drug, data=migraine))
            Df Sum Sq Mean Sq F value
                      14.111
drug
             2 28.22
                                11.91
            24 28.44
Residuals
                       1.185
              Pr(>F)
            0.000256 ***
drug
Residuals
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
  0.1 ' ' 1
> pairwise.t.test(pain, drug, p.adjust="bonferroni")
        Pairwise comparisons using t tests with pooled SD
data: pain and drug
  Α
          В
B 0.00119 -
C 0.00068 1.00000
P value adjustment method: bonferroni
> pairwise.t.test(pain, drug)
        Pairwise comparisons using t tests with pooled SD
data:
       pain and drug
          В
B 0.00079 -
C 0.00068 0.83042
P value adjustment method: holm
```

26

```
> results = aov(pain ~ drug, data=migraine)
> TukeyHSD(results, conf.level = 0.95)
  Tukey multiple comparisons of means
    95% family—wise confidence level
Fit: aov(formula = pain ~ drug, data = migraine)
$drug
         diff
                      lwr
                               upr
                                        p adj
B-A 2.1111111
               0.8295028 3.392719 0.0011107
               0.9406139 3.503831 0.0006453
C-A 2.222222
C-B 0.1111111 -1.1704972 1.392719 0.9745173
> TukeyHSD(results, conf.level = 0.9)
  Tukey multiple comparisons of means
    90% family—wise confidence level
Fit: aov(formula = pain ~ drug, data = migraine)
$drug
         diff
                      lwr
                               upr
                                        p adi
B-A 2.1111111
              1.0053515 3.216871 0.0011107
               1.1164627 3.327982 0.0006453
C-A 2.222222
C-B 0.1111111 -0.9946485 1.216871 0.9745173
> plot(TukeyHSD(results, conf.level = 0.95))
> plot(TukeyHSD(results, conf.level = 0.9))
> plot(TukeyHSD(results, conf.level = 0.999))
> plot(TukeyHSD(results, conf.level = 0.999999))
> heart.rate <- data.frame(hr = c(96,110,89,95,128,100,72,79,100,
92, 106, 86, 78, 124, 98, 68, 75, 106, 86, 108, 85, 78, 118, 100, 67, 74, 104,
92,114,83,83,118,94,71,74,102),
+ subj=gl(9,1,36), time=gl(4,9,36,labels=c(0,30,60,120)))
> heart.rate
    hr subj time
1
    96
          1
               0
2
   110
          2
                0
3
          3
    89
                0
4
    95
          4
               0
5
   128
          5
               0
6
          6
   100
               0
7
          7
    72
               0
          8
8
    79
               0
9
          9
               0
   100
10
   92
          1
              30
          2
11 106
              30
12
   86
          3
              30
          4
13
   78
              30
          5
14 124
              30
15 98
          6
              30
```

```
16
   68
              30
          7
17
   75
              30
          8
18 106
          9
              30
          1
19
  86
              60
20 108
          2
              60
21
   85
              60
          3
22 78
          4
              60
23 118
          5
              60
24 100
          6
              60
          7
25
              60
   67
26 74
          8
              60
27 104
          9
              60
28
          1
   92
             120
          2
29 114
             120
30 83
          3
             120
31 83
          4
             120
32 118
          5
             120
33 94
          6
             120
34
   71
          7
             120
35 74
          8
             120
36 102
          9
             120
> c(1:9,1:9,1:9,1:9)
 [1] 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2
[21] 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9
> gl(9,1,36)
 [1] 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2
[21] 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9
Levels: 1 2 3 4 5 6 7 8 9
> gl(9,1,37)
 [1] 1 2 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1 2
[21] 3 4 5 6 7 8 9 1 2 3 4 5 6 7 8 9 1
Levels: 1 2 3 4 5 6 7 8 9
> c(rep(0,9),rep(30,9),rep(60,9),rep(120,9))
                     0
 [1]
       0
         0
               0
                  0
                           0
                              0
                                  0
                                       0 30
[11]
      30 30
              30
                 30 30 30 30 30 60 60
[21] 60 60 60 60 60 60 60 120 120 120
[31] 120 120 120 120 120 120
> gl(4,9,36,labels=c(0,30,60,120))
 [1] 0
        0
             0
                 0
                     0
                         0
                             0
                                     0
                                         30
[11] 30
        30
            30
                30
                         30
                             30
                                 30 60
                     30
                                         60
[21] 60 60
            60
                60
                     60 60
                             60
                                 120 120 120
[31] 120 120 120 120 120 120
Levels: 0 30 60 120
> ql(4,9,36)
 [1] 1 1 1 1 1 1 1 1 1 2 2 2 2 2 2 2 2 2 3 3
[21] 3 3 3 3 3 3 3 4 4 4 4 4 4 4 4 4
Levels: 1 2 3 4
> gl(4,9,36,labels=c(0,30,60,120))
 [1] 0
         0
             0
                 0
                                         30
[11] 30 30
            30
                30
                     30
                         30
                             30
                                 30
                                     60
                                         60
```

```
[21] 60 60 60 60 60 60 60 120 120 120
[31] 120 120 120 120 120 120
Levels: 0 30 60 120
> anova(lm(hr~subj+time))
Error in eval(predvars, data, env) : object 'hr' not found
> attach(heart.rate)
> anova(lm(hr~subj+time))
Analysis of Variance Table
Response: hr
          Df Sum Sq Mean Sq F value
           8 8966.6 1120.82 90.6391
subi
                      50.32 4.0696
time
           3 151.0
Residuals 24 296.8
                      12.37
             Pr(>F)
          4.863e-16 ***
subi
time
            0.01802 *
Residuals
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.'
  0.1 ' ' 1
> anova(lm(hr~subj+time))
Analysis of Variance Table
Response: hr
          Df Sum Sq Mean Sq F value
                                       Pr(>F)
           8 8966.6 1120.82 90.6391 4.863e-16 ***
subi
time
           3 151.0
                      50.32 4.0696
                                       0.01802 *
Residuals 24 296.8
                      12.37
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
> interaction.plot(time,subj,hr)
> data(thuesen)
> attach(thuesen)
> thuesen
   blood.glucose short.velocity
                           1.76
1
            15.3
2
                           1.34
            10.8
3
             8.1
                           1.27
4
            19.5
                           1.47
5
             7.2
                           1.27
6
             5.3
                           1.49
7
                           1.31
             9.3
8
            11.1
                           1.09
9
            7.5
                           1.18
                           1.22
10
            12.2
                           1.25
11
             6.7
12
             5.2
                           1.19
13
            19.0
                           1.95
```

```
14
            15.1
                           1.28
15
             6.7
                           1.52
16
             8.6
                             NA
17
             4.2
                           1.12
18
                           1.37
            10.3
                           1.19
19
            12.5
20
            16.1
                           1.05
21
            13.3
                           1.32
22
             4.9
                           1.03
23
             8.8
                           1.12
24
             9.5
                           1.70
> lm.velo<-lm(short.velocity~blood.glucose); summary(lm.velo)</pre>
Call:
lm(formula = short.velocity ~ blood.glucose)
Residuals:
               10
                    Median
     Min
                                 30
                                         Max
-0.40141 -0.14760 -0.02202 0.03001 0.43490
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.11748
                                    9.345 6.26e-09 ***
(Intercept)
               1.09781
blood.glucose 0.02196
                          0.01045
                                    2.101
                                            0.0479 *
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.2167 on 21 degrees of freedom
  (1 observation deleted due to missingness)
Multiple R-squared: 0.1737, Adjusted R-squared: 0.1343
F-statistic: 4.414 on 1 and 21 DF, p-value: 0.0479
> anova(lm.velo)
Analysis of Variance Table
Response: short.velocity
              Df Sum Sq Mean Sq F value Pr(>F)
blood.glucose 1 0.20727 0.207269
                                    4.414 0.0479 *
Residuals
              21 0.98610 0.046957
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
> 2.101^2
[1] 4.414201
> 0.20727/(0.20727+0.98610)
[1] 0.1736846
> sqrt(0.046957)
[1] 0.2166956
> Drug = c(rep("Placebo",6), rep("5mg",6),rep("10mg",6))
> Drug
```

```
[1] "Placebo" "Placebo" "Placebo"
 [5] "Placebo" "Placebo" "5mg"
                                    "5ma"
                          "5mg"
                                    "5ma"
 [9] "5mg"
               "5ma"
[13] "10mg"
               "10ma"
                          "10mg"
                                    "10mg"
[17] "10ma"
               "10ma"
> Age = c(rep(c(rep("young",3), rep("old",3)),3))
> Age
 [1] "young" "young" "young" "old"
             "young" "young" "old"
 [6] "old"
             "old"
                     "young" "young" "young"
[11] "old"
                     "old"
[16] "old"
             "old"
> Value = c(4, 3, -1, 2, 1, -2, 4, 5, 7, 3, 3, 4, 9, 12, 10, 7, 8, 7)
> data<-data.frame(Drug,Age,Value);data</pre>
      Drug
             Age Value
   Placebo young
                     4
  Placebo young
2
                     3
3 Placebo young
                     -1
                     2
4 Placebo
             old
5
             old
   Placebo
                     1
6
                     -2
   Placebo
             old
7
                     4
       5mg young
8
       5mg young
                     5
9
                     7
       5mg young
                     3
10
       5mg
             old
                     3
11
       5mg
             old
12
       5mg
             old
                     4
13
                     9
      10mg young
14
                     12
      10mg young
15
      10mg young
                     10
16
                     7
      10mg
             old
17
      10ma
             old
                     8
18
      10mg
             old
                     7
> par(mfrow=c(1,2))
> plot(Value ~ Drug + Age, data=data)
Hit <Return> to see next plot:
> interaction.plot(data$Age, data$Drug, data$Value)
> interaction.plot(data$Drug, data$Age, data$Value)
> anova(lm(Value ~ Drug + Age +Drug*Age, data=data)
Analysis of Variance Table
Response: Value
          Df Sum Sq Mean Sq F value
                                         Pr(>F)
Drug
           2 178.111 89.056
                                32.06 1.535e-05
              22.222
                      22.222
                                 8.00
                                        0.01522
Age
           1
Drug:Age
           2
               1.444
                        0.722
                                 0.26
                                        0.77529
Residuals 12
              33.333
                        2.778
Drug
          ***
Age
          *
```

```
Drug:Age
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> anova(lm(Value ~ Drug + Age, data=data))
Analysis of Variance Table
Response: Value
          Df Sum Sq Mean Sq F value
                                        Pr(>F)
           2 178.111 89.056 35.8498 3.105e-06
Drua
           1
             22.222 22.222 8.9457 0.009725
Age
Residuals 14 34.778 2.484
Drug
          ***
Age
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> anova(lm(Value ~ Drug + Age +Drug*Age, data=data))
Analysis of Variance Table
Response: Value
          Df Sum Sq Mean Sq F value
                                        Pr(>F)
           2 178.111 89.056
                               32.06 1.535e-05
Drug
             22,222 22,222
                                8.00
                                       0.01522
Age
           1
Drug:Age
           2
               1.444
                     0.722
                                0.26
                                       0.77529
Residuals 12 33.333
                      2.778
Drua
          ***
Age
Drua:Aae
Residuals
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> prop.test(39, 215, 0.15)
        1-sample proportions test with continuity
        correction
data: 39 out of 215, null probability 0.15
X-squared = 1.425, df = 1, p-value = 0.2326
alternative hypothesis: true p is not equal to 0.15
95 percent confidence interval:
 0.1335937 0.2408799
sample estimates:
0.1813953
```

```
> (39-215*0.15)/sqrt(215*0.15*0.85)
[1] 1.289227
> ((39-215*0.15)/sqrt(215*0.15*0.85))^2
[1] 1.662107
> ((38.5-215*0.15)/sqrt(215*0.15*0.85))^2
[1] 1.424989
> 39/215
[1] 0.1813953
> binom.test(39, 215, 0.15)
        Exact binomial test
       39 and 215
data:
number of successes = 39, number of trials =
215, p-value = 0.2135
alternative hypothesis: true probability of success is not equal to
0.15
95 percent confidence interval:
 0.1322842 0.2395223
sample estimates:
probability of success
             0.1813953
> caff.marital <-matrix(c(652,1537,598,242,36,46,38,21,218,327,
106,67), nrow=3,byrow=T)
> colnames(caff.marital) <- c("0","1-150","151-300",">300")
rownames(caff.marital) <- c("Married","Prev.married","Single")</pre>
Error: unexpected symbol in "colnames(caff.marital) <-</pre>
c("0","1-150","151-300",">300") rownames"
> caff.marital
     [,1] [,2] [,3] [,4]
[1.] 652 1537 598 242
[2,]
      36
            46
                38
                      21
[3,] 218 327 106
                      67
> caff.marital < -matrix(c(652,1537,598,242,36,46,38,21,218,327,
106,67), nrow=3,byrow=T)
> ;colnames(caff.marital) <-</pre>
c("0","1-150","151-300",">300"); rownames(caff.marital) <-
c("Married","Prev.married","Single")
Error: unexpected ';' in ";"
> caff.marital
     [,1] [,2] [,3] [,4]
[1,] 652 1537 598 242
[2,]
            46
                 38
                      21
       36
      218 327 106
                      67
[3,]
> caff.marital < -matrix(c(652,1537,598,242,36,46,38,21,218,327,
106,67), nrow=3,byrow=T);colnames(caff.marital) <-
c("0","1-150","151-300",">300") ;rownames(caff.marital) <-
c("Married","Prev.married","Single")
```

```
> ;caff.marital
Error: unexpected ';' in ";"
> caff.marital<-matrix(c(652,1537,598,242,36,46,38,21,218,327,</pre>
106,67), nrow=3,byrow=T);colnames(caff.marital)<-
c("0","1-150","151-300",">300");rownames(caff.marital) <-
c("Married","Prev.married","Single");caff.marital
                0 1-150 151-300 >300
             652
                   1537
                            598
Married
                                 242
Prev<sub>•</sub>married
             36
                     46
                             38
                                  21
                    327
                            106
                                  67
Single
             218
> chisq.test(caff.marital)
         Pearson's Chi-squared test
       caff.marital
X-squared = 51.656, df = 6, p-value =
2.187e-09
> chisq.test(caff.marital)$expected
                             1-150
                                      151-300
Married
             705.83179 1488.01183 578.06533
Prev.married 32.85648
                          69.26698 26.90895
                         352.72119 137.02572
Single
             167.31173
                   >300
Married
             257.09105
Prev.married 11.96759
Single
              60.94136
> chisq.test(caff.marital)$observed
                0 1-150 151-300 >300
Married
             652
                   1537
                            598
                                242
Prev<sub>married</sub> 36
                     46
                             38
                                  21
Sinale
             218
                    327
                            106
                                  67
> caf.marital[.1]
Error: object 'caf.marital' not found
> caff.marital[,1]
     Married Prev.married
                                 Single
         652
                                    218
> sum(caff.marital[,1])
[1] 906
> sum(caff.marital[1,])
[1] 3029
> sum(caff.marital)
[1] 3888
> sum(caff.marital[1,])*sum(caff.marital[1,])/ sum(caff.marital)
[1] 2359.784
> sum(caff.marital[1,])*sum(caff.marital[,1])/ sum(caff.marital)
[1] 705.8318
> sum(caff.marital[3,])*sum(caff.marital[,2])/ sum(caff.marital)
[1] 352.7212
> E <- chisq.test(caff.marital)$expected
```

```
> 0 <- chisq.test(caff.marital)$observed</pre>
> (0-E)^2/E
                            1-150
                                    151-300
Married
              4.1055981 1.612783 0.6874502
Prev.married 0.3007537 7.815444 4.5713926
             15.3563704 1.875645 7.0249243
Single
                   >300
Married
             0.8858331
Prev.married 6.8171090
Single
             0.6023355
> sum((0-E)^2/E)
[1] 51.65564
> dim(caff.marital)
[1] 3 4
> data(juul)
> head(juul)
   age menarche sex igf1 tanner testvol
1
    NA
             NA NA
                       90
                              NA
                                       NA
2
    NA
             NA NA
                       88
                              NA
                                      NA
3
    NA
             NA NA
                      164
                              NA
                                       NA
4
    NA
             NA NA
                      166
                              NA
                                       NA
5
    NA
             NA
                NA
                      131
                              NA
                                       NA
                               1
                                      NA
6 0.17
             NA
                   1
                      101
> chisq.test(tanner,sex)
```

## Pearson's Chi-squared test

```
data: tanner and sex
X-squared = 28.867, df = 4, p-value =
8.318e-06
```

objc[600]: Class FIFinderSyncExtensionHost is implemented in both / System/Library/PrivateFrameworks/FinderKit.framework/Versions/A/FinderKit (0x7fff949aec90) and /System/Library/PrivateFrameworks/FileProvider.framework/OverrideBundles/FinderSyncCollaborationFileProviderOverride.bundle/Contents/MacOS/FinderSyncCollaborationFileProviderOverride (0x110e2ccd8). One of the two will be used. Which one is undefined.