## Error Calculations

February 13, 2024

# 1 Error Calculations for Peruvian Bluberry Data: Price, Volume and Value

### 1.1 Introduction

We are interested in calculating standard errors for quantities such as price, value and volume. A parametric approach in our case would be assuming that the data for a specific week follows (let's say) a normal distribution. Normal distribution is the most widely used distribution in statistics. However, we must check our data's distribution before we make such a claim.

A widely used test in Statistics to check for normality is called the Shapiro Wilk test, We can carry out this test on some rows of our data to see if pricing for any given week is normally distributed. Below, we carry out the test on row 47 of our data.

```
[887]: #Import the necessary libraries
import pandas as pd
from scipy.stats import shapiro
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
```

```
[888]: file_path = 'Price.xlsx'

# Read the Excel file into a Pandas DataFrame
df = pd.read_excel(file_path)

first_row = df.iloc[47,:] #Select the 47th row

# Perform the Shapiro-Wilk test
statistic, p_value = shapiro(first_row)

# Display the test result
print("Shapiro-Wilk Test Statistic:", statistic)
print("P-value:", p_value)

# Interpret the result
alpha = 0.05
if p_value > alpha:
```

```
print("The sample looks normally distributed (fail to reject H0)")
else:
    print("The sample does not look normally distributed (reject H0)")
```

Shapiro-Wilk Test Statistic: 0.7900190949440002

P-value: 0.0052005513571202755

The sample does not look normally distributed (reject HO)

According to our results, the data is not normally distributed. Therefore we follow a non-parametric approach for the calculation of the standard errors. A non parametric approach is one that does not assume an underlying distribution for the given data.

## 1.2 Non-Parametric Approach - Bootstrapping

Bootstrapping is a resampling technique that can be used to estimate the sampling distribution of a statistic, such as the standard error, even when the underlying data is not normally distributed. This makes bootstrapping a versatile and robust method for estimating parameters.

Bootstrapping is a non-parametric method, meaning it does not rely on assumptions about the underlying distribution of the data. Instead, it directly uses the observed data to estimate the sampling distribution of a statistic. This makes it more robust and flexible, especially when the underlying distribution is unknown or not easily characterized. Bootstrapping involves randomly sampling from the observed data with replacement to create multiple bootstrap samples. This process effectively captures the variability and structure of the original data, allowing for more accurate estimation of parameters and uncertainty measures.

Overall, bootstrapping is a powerful and widely used technique for statistical inference and estimation, providing valuable insights even in cases where the data is not normally distributed.

### 1.3 Moving Block Bootstrapping for Time Series Data

Moving block bootstrapping is particularly useful for time series data because it takes into account the temporal structure and dependencies present in the data. Time series data often exhibits temporal dependence, where the value of a data point is related to the values of previous data points. Moving block bootstrapping preserves this temporal dependence by sampling contiguous blocks of data, allowing the bootstrap samples to capture the autocorrelation structure of the original time series. It maintains the sequential ordering of observations in the time series. This is crucial for time series analysis, as the order of observations often carries important information about the underlying process.

#### 1.4 Moving Block Bootstrapping With Overlap

In bootstrapping with time series data, using an overlap can be beneficial for several reasons:

Preserving Temporal Dependence: Overlapping blocks allow for the preservation of temporal dependence in the resampled data. By including overlapping segments from adjacent blocks, the resampled data maintains some level of continuity and autocorrelation structure, which is essential for capturing the characteristics of the original time series.

Reduced Variance: Overlapping blocks can help reduce the variance of estimates derived from bootstrapping. By incorporating information from neighboring blocks, the resampled data may

exhibit less variability, leading to more stable estimates of parameters and statistics.

#### 1.5 Error Calculations

I have used a modified formula for the calculation of the standard deviation. In place of mean, I have used the target value ( which is the last value in the respective row and the value that we are comparing each value in the past to)

Standard Deviation 
$$(\sigma) = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \text{target value})^2}{n}}$$

Once we have the standard deviation, we can calculate the standard error for each week by dividing the standard deviation with the square root of the block size.

Standard Error 
$$= \left(\frac{\sigma}{\sqrt{n}}\right)$$

## 1.6 Code Summary

First, we Initialize variables **block\_size** and **overlap** to specify the size of blocks and the overlap between consecutive blocks for moving block bootstrapping.

Then we set the number of bootstrap samples to generate (num\_bootstrap\_samples) to 1000. This helps us ensure that our results will be precise. This step could be thought of as replicating an experiment several times to get the best results.

We then define a function **calculate\_standard\_error** to calculate the standard error for each row using moving block bootstrapping with overlap.

This function iterates over each row of the DataFrame and performs the following steps: 1.Divides the row into blocks and generates bootstrap samples with overlap. 2.Calculates errors by subtracting the value of interest (from the "LastColumn" of the row) from the bootstrap samples. 3.Separates positive and negative errors. 4.Computes standard errors for positive and negative errors using the formula for standard deviation. 5.Returns the positive and negative standard errors as a Pandas Series. 6.Applies the calculate\_standard\_error function to each row of the DataFrame to compute the standard errors Both, the positive standard errors (positive\_std\_error) and negative standard errors (negative\_std\_error) are then printed and then the results are plotted. In the plot, positive standard errors are plotted above the original line while the negative standard errors are plotted below the original line.

## 1.7 Standard Error Calculations for Price (Using Moving Block Bootstrapping With Overlap)

```
[901]: file_path = 'Price.xlsx'  # Read the Excel file containing the data

# Read the Excel file into a Pandas DataFrame

df = pd.read_excel(file_path)

# Set option to display all rows of a DataFrame if it is printed
```

```
pd.set_option('display.max_rows', None)
      df['LastColumn'] = df.iloc[:, -1] # Extract the last column of the DataFrame_
       ⇔as a new column named 'LastColumn'
      block_size = 4  # Size of the blocks used in moving block bootstrapping
      overlap = 3 # Size of the overlap between consecutive blocks
      num_bootstrap_samples = 1000 # Number of bootstrap samples to generate
      custom_labels = ['42', '43', '44', '45', '46', '47', '48', '49', '50', '51', _
       _{9}'26', '27', '28', '29', '30', '31', '32', '33', '34', '35', '36', '37', _{\square}
       _{9}'38', '39', '40', '41', '42', '43', '44', '45', '46', '47', '48', '49']
[902]: # Function to calculate standard error for each row using moving block,
       ⇔bootstrapping with overlap
      def calculate_standard_error(row):
          # Extract the value of interest from the row
          value_of_interest = row['LastColumn']
          \# Calculate the number of blocks and initialize array to store bootstrap.
       ⇔samples
          num_blocks = (len(row[:-1]) - block_size) // overlap + 1
          bootstrap_samples = np.zeros((num_bootstrap_samples, block_size))
          last_index = 0 # Track the last used index
          # Generate bootstrap samples using moving block bootstrapping with overlap
          for j in range(num_bootstrap_samples):
              start_index = last_index
              last_index += overlap # Increment by the overlap size for the next_
       ⇔block
              if last_index + block_size > len(row[:-1]):
                 last_index = 0 # Wrap around if the next block goes beyond the
       \hookrightarrow array
              bootstrap_samples[j] = row[start_index:start_index + block_size].values
          # Flatten the bootstrap samples array
          bootstrap_samples = bootstrap_samples.reshape((num_bootstrap_samples, -1))
          # Calculate errors (deviation from value of interest)
          errors = value_of_interest - bootstrap_samples
          # Separate positive and negative errors
          positive_errors = errors[errors >= 0]
          negative_errors = errors[errors < 0]</pre>
```

```
# Calculate standard error for positive and negative errors
   positive_std_error = np.sqrt((sum((positive_errors)**2) /__
 →len(positive_errors))) / np.sqrt(block_size) if len(positive_errors) > 0⊔
   negative_std_error = np.sqrt((sum((negative_errors)**2) /__
 →len(negative errors))) / np.sqrt(block size) if len(negative errors) > 0,,
 ⊶else 0
    # Return standard errors as a Pandas Series
   return pd.Series({'Positive_Standard_Error': positive_std_error,__
 →'Negative_Standard_Error': negative_std_error})
# Calculate standard error for each row using moving block bootstrapping with
 ⇔overlap
standard_errors = df.apply(calculate_standard_error, axis=1)
# Create DataFrame for standard errors
df_se = pd.DataFrame(standard_errors)
# Create DataFrame for custom labels
df_cl = pd.DataFrame(custom_labels, columns=['Week'])
# Merge custom labels DataFrame with standard errors DataFrame
merged_df = pd.merge(df_cl, df_se, left_index=True, right_index=True)
merged_df.index.name = None # Remove index name
(merged_df.head(62))
```

```
[902]:
          Week Positive_Standard_Error Negative_Standard_Error
       0
            42
                                0.000000
                                                           0.000000
       1
            43
                                0.000000
                                                           0.000000
       2
            44
                                0.000000
                                                           0.000000
       3
            45
                                0.000000
                                                           0.000000
       4
            46
                                0.000000
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       5
            47
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       6
            48
                                0.000000
                                                           0.000000
       7
            49
                                0.000000
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       8
            50
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       9
            51
                                0.000000
                                                           0.000000
       10
            52
                                0.039191
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             1
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       12
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             3
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             4
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       17
             7
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       18
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```

```
19
             9
                                 0.000000
                                                            0.030000
       20
            10
                                 0.000000
                                                            0.023884
       21
            11
                                 0.000000
                                                            0.210000
       22
            12
                                 0.000000
                                                            0.370000
       23
            13
                                 0.000000
                                                            0.100000
       24
            14
                                 0.000000
                                                            0.185000
       25
            15
                                 0.000000
                                                            0.00000
       26
            16
                                 0.000000
                                                            0.005000
       27
                                 0.000000
            17
                                                            0.005000
       28
            18
                                 0.000000
                                                            0.045000
       29
            19
                                 0.043714
                                                            0.000000
       30
            20
                                 0.060947
                                                            0.015000
       31
            21
                                 0.006250
                                                            0.00000
       32
            22
                                 0.017912
                                                            0.030000
       33
            23
                                 0.022256
                                                            0.000000
       34
            24
                                 0.105933
                                                            0.000000
       35
            25
                                 0.185018
                                                            0.005000
       36
            26
                                 0.215433
                                                            0.010000
       37
            27
                                 0.249321
                                                            0.00000
       38
            28
                                 0.263391
                                                            0.005000
       39
            29
                                 0.311839
                                                            0.00000
       40
            30
                                 0.442761
                                                            0.00000
       41
            31
                                 0.526259
                                                            0.00000
       42
            32
                                 0.514027
                                                            0.000000
       43
            33
                                 0.502078
                                                            0.00000
       44
            34
                                 0.505547
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       45
            35
                                 0.547613
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       46
            36
                                 0.675783
                                                            0.00000
       47
            37
                                 0.744653
                                                            0.00000
       48
            38
                                 0.683418
                                                            0.00000
       49
            39
                                 0.807181
                                                            0.000000
       50
            40
                                 0.821675
                                                            0.00000
       51
            41
                                 0.725644
                                                            0.000000
       52
            42
                                 0.891458
                                                            0.00000
       53
            43
                                 1.071726
                                                            0.000000
       54
            44
                                 0.961428
                                                            0.00000
       55
            45
                                 1.106961
                                                            0.00000
       56
            46
                                 1.224763
                                                            0.00000
       57
            47
                                 0.590099
                                                            0.00000
       58
            48
                                 0.084853
                                                            0.00000
       59
            49
                                 0.000000
                                                            0.000000
[903]: from matplotlib.lines import Line2D
       # Scatterplot with area chart and markers
       fig, ax = plt.subplots(figsize=(18, 9))
       # Plot the original line
```

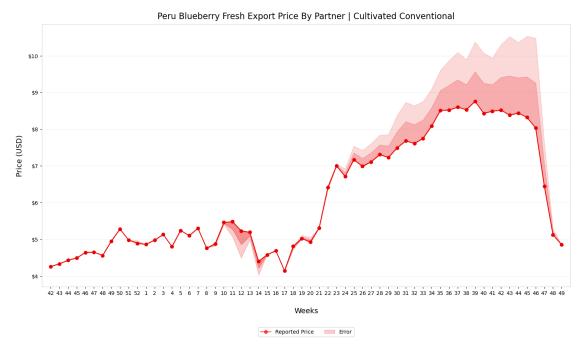
```
ax.plot(range(len(df)), df['LastColumn'], color='#EA0000')
# Separate positive and negative standard errors
positive_errors = standard_errors['Positive_Standard_Error']
negative_errors = standard_errors['Negative_Standard_Error']
# Fill the area above the curve for positive errors
if not positive_errors.empty:
   fill=ax.fill between(range(len(df)), df['LastColumn'], df['LastColumn'] +11
 →positive_errors, color='#EA0000', alpha=0.2, label='Positive Errors')
   fill=ax.fill between(range(len(df)), df['LastColumn'], df['LastColumn'] + |
 # Fill the area below the curve for negative errors
if not negative_errors.empty:
   fill=ax.fill_between(range(len(df)), df['LastColumn'] - negative_errors.
 →abs(), df['LastColumn'], color='#EA0000', alpha=0.3, label='Positive Errors')
   fill=ax.fill_between(range(len(df)), df['LastColumn'] - 2*negative_errors.
abs(), df['LastColumn'], color='#EA0000', alpha=0.2, label='Positive Errors')
# Scatterplot with opaque circular markers
ax.scatter(range(len(df)), df['LastColumn'], color='#EA0000', s=38)
# Customize the plot
ax.set_xlabel('Weeks', fontsize=14, labelpad=22) # Set x-axis label and adjust_
\hookrightarrow padding
ax.set_ylabel('Price (USD)', fontsize=14, labelpad=10) # Set y-axis label and_
⇔adjust padding
ax.yaxis.set_major_formatter('${:,.0f}'.format) # Add a dollar sign to y-axis_
 \rightarrow ticks
# Customize x-axis ticks
plt.xticks(range(len(custom_labels)), custom_labels)
# Set plot title
ax.set title('Peru Blueberry Fresh Export Price By Partner | Cultivated
 →Conventional', fontsize=16, pad=10)
# Add gridlines
ax.grid(axis='y', color='grey', linestyle='-', linewidth=0.5, alpha=0.2)
# Set x-axis limit
ax.set_xlim(-1, len(df))
# Add legend
circle_line = Line2D([0], [0], color='red', marker='o', markersize=6,_
 →markerfacecolor='red', alpha=0.7)
legend_handles = [ circle_line,fill]
```

```
legend_labels = [ 'Reported Price', 'Error']
ax.legend(handles=legend_handles, labels=legend_labels, loc='lower center', use bbox_to_anchor=(0.5, -0.2), ncol=3)

# Customize spine color
for spine in plt.gca().spines.values():
    spine.set_edgecolor('#d3d3d3')

# Save the figure
fig.savefig('Price_errors.png')

# Show the plot
plt.show()
```



# 1.8 Standard Error Calculations for Value (Using Moving Block Bootstrapping With Overlap)

```
[910]: file_path = 'Value.xlsx'  # Read the excel file

# Read the Excel file into a Pandas DataFrame

df = pd.read_excel(file_path)  # Read data into DataFrame
```

```
[911]: # Function to calculate standard error for each row using moving block
       ⇒bootstrapping with overlap
       def calculate standard error(row):
           value_of_interest = row['LastColumn']
           # Perform moving block bootstrapping with overlap
           num blocks = (len(row[:-1]) - block size) // overlap + 1
           bootstrap_samples = np.zeros((num_bootstrap_samples, block_size))
           last index = 0 # Track the last used index
           for j in range(num_bootstrap_samples):
               start index = last index
               last_index += overlap # Increment by the overlap size for the nextu
        \hookrightarrowblock
               if last_index + block_size > len(row[:-1]):
                   last_index = 0 # Wrap around if the next block goes beyond the
        \hookrightarrow array
               bootstrap_samples[j] = row[start_index:start_index + block_size].values
           # Flatten the bootstrap samples array
           bootstrap_samples = bootstrap_samples.reshape((num_bootstrap_samples, -1))
           # Calculate standard error
           errors = value_of_interest-bootstrap_samples
           positive_errors = errors[errors >= 0] # Filter positive errors
           print(positive_errors)
```

```
negative_errors = errors[errors < 0] # Filter negative errors</pre>
   positive_std_error = np.sqrt((sum((positive_errors)**2)/
 -len(positive_errors))) / np.sqrt(block_size) if len(positive_errors) > 0 __
 ⇔else 0
   negative_std_error = np.sqrt((sum((negative_errors)**2)/
 →len(negative_errors))) / np.sqrt(block_size) if len(negative_errors) > 0⊔
 ⇔else 0
   return pd.Series({'Positive Standard Error': positive std error, __
 →'Negative_Standard_Error': negative_std_error})
# Calculate standard error for each row using moving block bootstrapping with
 \hookrightarrow overlap
standard_errors = df.apply(calculate_standard_error, axis=1)
# Create DataFrame for standard errors
df se = pd.DataFrame(standard errors)
# Create DataFrame for custom labels with column name 'Week'
df_cl = pd.DataFrame(custom_labels, columns=['Week'])
# Print a message indicating the purpose of the displayed results
print("Standard Error for each row using moving block bootstrapping with⊔
 ⇔overlap:\n")
# Merge the custom labels DataFrame and standard errors DataFrame on their
merged_df = pd.merge(df_cl, df_se, left_index=True, right_index=True)
# Remove the index name
merged_df.index.name = None
# Display the merged DataFrame
(merged df.head(62))
```

```
[5497187.24 5497187.24 5497187.24 5497187.24 5497187.24 5497187.24
5497187.24 5497187.24 5497187.24 5497187.24 5497187.24 4122890.43
4122890.43 2748593.62 1374296.81
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[46391.03 14563.34 14563.34 14563.34 14563.34 14563.34 14563.34
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[26114.08 18024.83 18024.83 18024.83 18024.83 18024.83 11968.33 27953.88
27953.88 22579.54
               0.
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[219360.11 224756.87 213561.77 213561.77 213561.77 213561.77 207558.85
 65226.93 65226.93 52434.35
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[426599.87 473376.01 469924.01 378519.28 378519.28 378519.28 193973.86
217080.47 217080.47 200298.29
                         0.
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[766146.19 689006.82 624798.24 402125.01 402125.01 402125.01 305798.82
227996.22 227996.22 89814.63
                         0.
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[1373709.37 1289505.83 1096950.03 784130.39 784130.39 784130.39
 523791.56 336219.59 336219.59 326089.62
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    0.
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                            0. ]
[1586212.46 1478694.11 1254114.03 817985.22 817985.22 817985.22
 367093.79 245459.83 245459.83 211852.35
                                   0.
[2632202.55 2486193.84 1929341.01 1187741.67 1187741.67 1190908.37
```

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591965.32 244027.56 244027.56 192774.42
                                               85177. 87429.51
  87429.51
             27599.81
                            0.
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[4030457.07 3997503.02 3945873.85 2533620.35 2533620.35 2591394.24
1310564.59 929059.82 929059.82 622840.63 117037.64
                 0.
                            0. 1
  32456.38
[7082954.33 7053884.69 6827801.44 5319060.06 5319060.06 5065653.75
2639363.74 1871539.62 1871539.62 1217803.46 224788.94 137883.48
 137883.48 143733.82
                            0.
                                        0. 1
[7598351.32 7556358.35 7352144.75 6605770.17 6605770.17 6178594.43
3454567.75 2354127.1 2354127.1 1339455.24 417010.4
                                        0. ]
 292184.6
            399568.12
                        72092.02
[8106309.97]
                 8056796.77
                                   8056796.77
                                                    6916182.29
6916182.29
                 6488801.68
                                   4723055.27
                                                    3329025.18
3329025.18
                 2166394.77
                                   1114379.73999999
                                                    452760.13
 452760.13
                   246845.72
                                    24197.66
                                                          0.
[8281261.44000001 8138180.44000001 8096948.54
                                                    7639435.65000001
7639435.65000001 7601558.27
                                   5798152.88
                                                    4661396.28
4661396.28
                 3038444.29
                                   1435920.54
                                                    1116527.13
1116527.13
                                     56500.17
                                                          0.
                   360987.72
[11186610.24 9026435.86 8269298.15 8256579.78 8256579.78 7940027.74
 7138836.93 6460720.55 6460720.55 5665002.19
                                                 3139010.23 2227878.01
 2227878.01 1131275.99
                            97699.68
                                           0. ]
[24618072.62]
                  13525203.75
                                      9286553.25
                                                        8763806.97000001
 8763806.97000001 8608117.72000001 8249646.68
                                                        7847556.23
 7847556.23
                   6715231.12
                                      4118270.42
                                                        3634993.46
 3634993.46
                   2191123.42
                                      396543.07
                                                              0.
                                                                        ]
                                                        7615169.98999999
[27001926.93
                  24171004.88999999 10660220.79
 7615169.98999999 7401178.05999999 7338372.87
                                                        7232591.83
                                                        3743284.88999999
 7232591.83
                   7077326.08
                                      4773665.2
 3743284.88999999 2298096.45
                                      581246.38
                                                              0.
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                                                       12582662.
[33518404.25
                   25489967.33
                                     12582662.
 6527446.08
                   5789874.08
                                      5982052.15000001 5982052.15000001
 5855774.28999999 5051887.86
                                      4712073.81999999 4712073.81999999
                                                      1
 3794048.06
                   1021776.86
                                           0.
[37449550.53
                   28786377.74
                                     28786377.74
                                                        8738793.61
 5040047.91
                   4395674.17
                                      4395674.17
                                                        4485559.91
 3979760.86
                   3693384.52
                                      3693384.52
                                                        2795843.2
 1421619.65000001
                         0.
                   33702610.49
                                     27892974.46000001 9909926.42
[33702610.49
 2179863.08
                   2179863.08
                                      1681472.69000001 1633667.82000001
 1635093.84
                   1635093.84
                                      1092170.16000001
                                                         838551.28
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       0.
[39644498.30999999 31708516.68999999 5172073.83
                                                        5172073.83
 3628878.22999999
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  285627.72
                     272883.38999999
                                            0.
[39679021.13
                  29397145.28999999 29397145.28999999 16630458.69
 2781951.52
                     759219.33
                                       759219.33
                                                         268984.63
  223209.44
                         0.
                                   ]
```

```
[41730237.74999999 41730237.74999999 38784496.41999999 13833902.25
 3238000.27999999 3238000.27999999 775720.97999999 101935.64
              ]
       0.
[39094963.93
                34001902.03 13812401.86
                                             13812401.86
 3066980.81
                 674741.84999999
                                      0.
                                               ]
[32449827.16
                28698163.42999999 28698163.42999999 12377000.88
 2916196.88
                     0.
[28914909.36 28914909.36 24070520.62 8562518.4 0. ]
[15517731.52 10858795.75 0. ]
[2044647.90000001 0.
                             1
[0.]
Standard Error for each row using moving block bootstrapping with overlap:
```

[911]:	Week	Positive_Standard_Error	Negative_Standard_Error
0	42	0.00000e+00	0.00000
1	43	0.00000e+00	0.00000
2	44	0.00000e+00	0.00000
3	45	0.00000e+00	0.00000
4	46	0.00000e+00	0.00000
5	47	0.00000e+00	0.00000
6	48	0.00000e+00	0.00000
7	49	0.00000e+00	0.00000
8	50	0.00000e+00	0.00000
9	51	0.00000e+00	0.00000
10	52	2.423355e+06	0.00000
11	. 1	0.00000e+00	0.00000
12	2	0.00000e+00	0.00000
13	3	0.00000e+00	0.00000
14	4	7.510717e+02	0.00000
15	5 5	0.00000e+00	0.00000
16	6	0.00000e+00	0.00000
17	7	0.00000e+00	0.00000
18	8	0.00000e+00	0.00000
19	9	0.00000e+00	46990.475000
20	10	0.00000e+00	24831.012831
21	. 11	0.00000e+00	178421.605000
22	2 12	0.00000e+00	161095.430000
23	13	0.00000e+00	34555.325000
24	14	0.00000e+00	57149.505000
25	15	0.00000e+00	0.00000
26	16	0.00000e+00	1020.000000
27	17	4.989500e+01	813.540000
28	18	0.00000e+00	14095.805000
29	19	1.703446e+04	0.00000
30	20	2.092183e+04	5745.640000
31	. 21	2.093574e+03	828.480000

```
33
            23
                            9.706455e+03
                                                          49.950000
       34
            24
                            7.476721e+04
                                                          38.350000
       35
            25
                            1.431040e+05
                                                       4068.430000
       36
            26
                            2.029940e+05
                                                      12906.624589
       37
            27
                            3.355165e+05
                                                           0.00000
       38
            28
                            4.228585e+05
                                                       4216.059066
       39
            29
                            5.809706e+05
                                                           0.000000
       40
                            1.089311e+06
                                                       2330.155000
            30
       41
                            1.953978e+06
            31
                                                           0.000000
       42
            32
                            2.234867e+06
                                                           0.000000
       43
            33
                            2.450085e+06
                                                           0.00000
       44
            34
                            2.698009e+06
                                                           0.000000
       45
            35
                            3.216148e+06
                                                           0.000000
       46
            36
                            4.656301e+06
                                                           0.000000
       47
            37
                            5.394924e+06
                                                           0.000000
       48
            38
                            6.267943e+06
                                                           0.000000
       49
            39
                            7.645343e+06
                                                           0.000000
       50
            40
                            7.808033e+06
                                                           0.000000
       51
            41
                            7.752921e+06
                                                           0.000000
       52
            42
                            9.471530e+06
                                                           0.000000
       53
            43
                            1.201853e+07
                                                           0.000000
       54
            44
                            1.048123e+07
                                                           0.00000
       55
            45
                            1.091989e+07
                                                           0.000000
       56
                            1.078158e+07
            46
                                                           0.000000
       57
            47
                            5.467430e+06
                                                           0.000000
                            7.228922e+05
                                                           0.00000
       58
            48
       59
            49
                            0.000000e+00
                                                           0.00000
[912]: # Scatterplot with area chart and markers
       fig, ax = plt.subplots(figsize=(18, 9))
       # Plot the original line
       ax.plot(range(len(df)), df['LastColumn'], color='#EA0000')
       # Separate positive and negative standard errors
       positive_errors = standard_errors['Positive_Standard_Error']
       negative_errors = standard_errors['Negative_Standard_Error']
       # Fill the area above the curve for positive errors
       if not positive errors.empty:
           fill=ax.fill_between(range(len(df)), df['LastColumn'], df['LastColumn'] + __
        ⇔positive_errors, color='#EA0000', alpha=0.3)
           fill=ax.fill_between(range(len(df)), df['LastColumn'], df['LastColumn'] + |
        $\text{\text{\cut}} 2*positive_errors, color='#EA0000', alpha=0.15, label='Positive Errors')
       # Fill the area below the curve for negative errors
       if not negative_errors.empty:
```

12729.450000

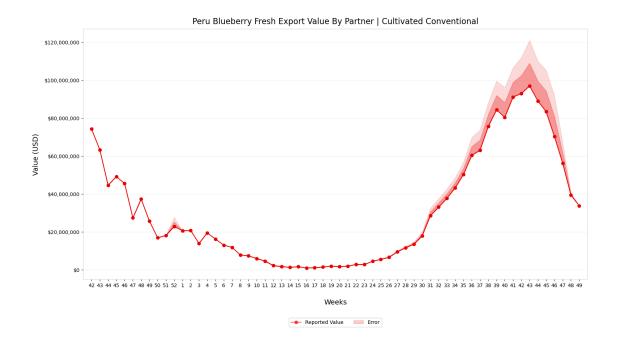
32

22

8.446736e+03

```
fill=ax.fill_between(range(len(df)), df['LastColumn'] - negative_errors.
 ⇔abs(), df['LastColumn'], color='red', alpha=0.3)
   fill=ax.fill_between(range(len(df)), df['LastColumn'] - 2*negative_errors.
 →abs(), df['LastColumn'], color='#EA0000', alpha=0.2, label='Positive Errors')
# Scatterplot with opaque circular markers
ax.scatter(range(len(df)), df['LastColumn'], color='#EA0000', s=38)
# Customize the plot
ax.set_xlabel('Weeks', fontsize=14, labelpad=22)
ax.set_ylabel('Value (USD)', fontsize=14, labelpad=10)
ax.yaxis.set_major_formatter('${:,.0f}'.format) # Add a dollar sign to y-axis_
 \hookrightarrow ticks
# Starting from 47 and ending at 49
plt.xticks(range(len(custom_labels)), custom_labels)
ax.set_title('Peru Blueberry Fresh Export Value By Partner | Cultivated_

→Conventional', fontsize=16, pad=10)
ax.grid(axis='y', color='grey', linestyle='-', linewidth=0.5, alpha=0.2)
ax.set xlim(-1, len(df))
# Add legend
circle_line = Line2D([0], [0], color='red', marker='o', markersize=6, __
legend_handles = [ circle_line,fill]
legend_labels = [ 'Reported Value', 'Error']
ax.legend(handles=legend_handles, labels=legend_labels, loc='lower center', u
 \rightarrowbbox_to_anchor=(0.5, -0.2), ncol=3)
for spine in plt.gca().spines.values(): #Adjust the color for spines
    spine.set_edgecolor('#d3d3d3')
# Save the figure
fig.savefig('Value_errors1.png')
# Show the plot
plt.show()
```



## 1.9 Standard Error Calculations for Volume (Using Moving Block Bootstrapping With Overlap)

```
[895]: import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt

# Replace 'your_file_path.xlsx' with the actual path to your Excel file
file_path = 'Volume.xlsx'

# Read the Excel file into a Pandas DataFrame
df = pd.read_excel(file_path)

df['LastColumn'] = df.iloc[:, -1]
```

```
last_index = 0 # Track the last used index
   for j in range(num_bootstrap_samples):
        start_index = last_index
       last_index += overlap # Increment by the overlap size for the next⊔
 ⇒block
        if last_index + block_size > len(row[:-1]):
            last index = 0 # Wrap around if the next block goes beyond the
 \rightarrow array
       bootstrap_samples[j] = row[start_index:start_index + block_size].values
    # Flatten the bootstrap samples array
   bootstrap_samples = bootstrap_samples.reshape((num_bootstrap_samples, -1))
   # Calculate standard error
   errors = value_of_interest-bootstrap_samples
   positive_errors = errors[errors >= 0] # Filter positive errors
   negative_errors = errors[errors < 0] # Filter negative errors</pre>
   #Standard error formula for Positive errors
   positive_std_error = np.sqrt((sum((positive_errors)**2)/
 -len(positive_errors))) / np.sqrt(block_size) if len(positive_errors) > 0 __
 ⇔else 0
    #Standard error formula for Negative errors
   negative_std_error = np.sqrt((sum((negative_errors)**2)/
 ulen(negative_errors))) / np.sqrt(block_size) if len(negative_errors) > 0∪
 ⇔else 0
    #Return positive and negative standard errors when the
 →calculate_standard_error function is called
   return pd.Series({'Positive Standard Error': positive_std_error,__

¬'Negative_Standard_Error': negative_std_error})
# Call the calculate_standard_error function
standard_errors = df.apply(calculate_standard_error, axis=1)
df se = pd.DataFrame(standard errors)
df_cl = pd.DataFrame(custom_labels,columns=['Week'])
# Display the results
print("Standard Error for each row using moving block bootstrapping with⊔
 ⇔overlap:\n")
```

```
merged_df = pd.merge(df_cl, df_se, left_index=True, right_index=True)
merged_df.index.name = None
# Display the merged DataFrame
(merged_df.head(62))
```

Standard Error for each row using moving block bootstrapping with overlap:

[896]:	Week	Positive_Standard_Error	Negative_Standard_Error
0	42	0.000000	0.00000
1	43	0.000000	0.000000
2	44	0.000000	0.00000
3	45	0.000000	0.000000
4	46	0.000000	0.000000
5	47	0.000000	0.000000
6	48	0.000000	0.000000
7	49	0.000000	0.000000
8	50	0.000000	0.000000
9	51	0.000000	0.000000
10	52	685.292315	0.000000
11		0.000000	0.000000
12		0.000000	0.000000
13	3	0.000000	0.000000
14	4	0.000000	0.000000
15	5 5	0.000000	0.000000
16	6	0.000000	0.000000
17		0.000000	0.000000
18	8	0.000000	0.000000
19	9	0.000000	0.000000
20		0.000000	0.000000
21		0.000000	0.000000
22	2 12	0.000000	0.000000
23	13	0.000000	0.000000
24	14	0.000000	0.000000
25		0.000000	0.000000
26		0.000000	0.000000
27		0.000000	0.000000
28		0.000000	0.000000
29		0.000000	0.000000
30		0.000000	0.000000
31		0.000000	0.000000
32		0.000000	0.000000
33		0.000000	0.000000
34	24	0.000000	0.000000

```
35
     25
                         0.000000
                                                    0.000000
36
     26
                         0.000000
                                                    0.000000
37
     27
                         0.000000
                                                    0.000000
38
     28
                         0.000000
                                                    0.000005
39
     29
                         0.000000
                                                    0.000000
40
     30
                         0.000000
                                                    0.00000
41
                         0.000000
     31
                                                    0.000000
42
     32
                         0.000000
                                                    0.00000
43
     33
                         0.000001
                                                    0.000000
44
                         0.983544
                                                    2.889250
     34
45
     35
                         0.991947
                                                    14.480490
46
     36
                         0.000000
                                                   43.624018
47
     37
                         0.000000
                                                   24.329138
48
     38
                        71.955293
                                                   40.584185
49
     39
                         3.250944
                                                   52.200923
50
     40
                         1.338108
                                                   14.166414
51
     41
                      2616.676053
                                                    8.507557
52
                         0.727256
     42
                                                   51.675162
53
     43
                        10.863382
                                                  123.822454
54
     44
                      1531.564448
                                                    0.000000
55
     45
                        23.955829
                                                   38.939642
56
     46
                        18.067917
                                                    0.000000
57
     47
                        80.419596
                                                    0.00000
58
     48
                        28.767713
                                                    0.000000
59
                         0.000000
                                                    5.664740
     49
```

```
[897]: # Scatterplot with area chart and markers
       fig, ax = plt.subplots(figsize=(18, 9))
       # Plot the original line
       ax.plot(range(len(df)), df['LastColumn'], color='#EA0000')
       # Separate positive and negative standard errors
       positive_errors = standard_errors['Positive_Standard_Error']
       negative_errors = standard_errors['Negative_Standard_Error']
       # Fill the area above the curve for positive errors
       if not positive_errors.empty:
           fill=ax.fill_between(range(len(df)), df['LastColumn'], df['LastColumn'] + |
        →positive_errors, color='#EA0000', alpha=0.3)
           fill=ax.fill_between(range(len(df)), df['LastColumn'], df['LastColumn'] + |
       42*positive_errors, color='#EA0000', alpha=0.15, label='Positive Errors')
       # Fill the area below the curve for negative errors
       if not negative_errors.empty:
           fill=ax.fill_between(range(len(df)), df['LastColumn'] - negative_errors.
        →abs(), df['LastColumn'], color='#EA0000', alpha=0.3)
```

```
fill=ax.fill_between(range(len(df)), df['LastColumn'] - 2*negative_errors.
 abs(), df['LastColumn'], color='#EA0000', alpha=0.2, label='Positive Errors')
# Scatterplot with opaque circular markers
ax.scatter(range(len(df)), df['LastColumn'], color='#EA0000', s=38)
# Customize the plot
ax.set_xlabel('Weeks', fontsize=14, labelpad=22)
ax.set_ylabel('Volume (KG)', fontsize=14, labelpad=10)
ax.yaxis.set_major_formatter('{:,.0f}M'.format) # Add a dollar sign to y-axis_
 \hookrightarrow ticks
# Add x axis ticks, starting from 47 and ending at 49
plt.xticks(range(len(custom_labels)), custom_labels)
ax.set_title('Peru Blueberry Fresh Export Volume By Partner | Cultivated
ax.grid(axis='y', color='grey', linestyle='-', linewidth=0.5, alpha=0.2)
ax.set_xlim(-1, len(df))
# Add legend
circle_line = Line2D([0], [0], color='red', marker='o', markersize=6,_
 →markerfacecolor='red', alpha=0.7)
legend handles = [ circle line,fill]
legend_labels = [ 'Reported Volume', 'Error']
#Adjust the location of the legend
ax.legend(handles=legend handles, labels=legend labels, loc='lower center', u
\rightarrowbbox_to_anchor=(0.5, -0.2), ncol=3)
for spine in plt.gca().spines.values(): #Set the color for spines
    spine.set_edgecolor('#d3d3d3')
# Save the figure
fig.savefig('Volume_errors.png')
# Show the plot
plt.show()
```

