

Analysis Qualifying Exam Solutions

Sarah Mantell

October 20, 2022

Overview

1

Results and Definitions to Know

2

2.1 Uncategorized

Theorem 2.1.1

Cauchy Riemann Equations

Theorem 2.1.2

Cauchy Integral Formula

In Progress Problems

3

Problem 3.0.1

Spring 2020.C5

Suppose that f is analytic in a domain containing $|z| \leq 1$. If $|f(z)| \leq 1$ for each $|z| \leq 1$, show that f has at least one fixed point in $|z| \leq 1$. That is, prove there exists a point p with $|p| \leq 1$ and $f(p) = p$.

Davit's suggestions: Maximum Principle, Schwarz Lemma