

Method of Analysis of Multi-parent Mapping Populations Affects Detection of QTL

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ABSTRACT The search for quantitative trait loci (QTL) that explain complex traits such as yield and drought tolerance has been ongoing in all crops. Methods such as bi-parental QTL mapping and genome-wide association studies (GWAS) each have their own advantages and limitations. Multi-parent advanced generation inter-crossing (MAGIC) contain more recombination events and genetic diversity than bi-parental mapping populations and reduce the confounding effect of population structure that is an issue in association mapping populations. Here we discuss the results of using a MAGIC population of doubled haploid (DH) maize lines created from 16 diverse founders to perform QTL mapping, comparing QTL identified using a 600K SNP array to those found using founder probabilities and haplotype probabilities generated by determining the regions of the MAGIC DH lines that were derived from the 16 founders and by identifying regions of identity-by-descent (IBD) between the 16 founders, respectively. The three methods have differing power and resolution for detecting QTL for a variety of agronomic traits. This highlights the importance of considering different approaches to analyzing genotypic datasets, and shows the limitations of binary SNP data for identifying multi-allelic QTL.

KEYWORDS QTL, MAGIC

Introduction

The study of evolutionary quantitative genetics requires the ability to link differences in phenotype to genotypic variation. Natural and artificial selection acts on phenotypes, but only heritable phenotypic variation will result in changes in population means. Maize presents an excellent model organism to answer these questions due to the combination of extensive genetic and phenotypic resources, and the ability to create mapping populations. In addition, maize is one of the most widely produced crops in the world and is a major source of calories for millions of people. Decades of research into maize genetics have resulted in the identification of many quantitative trait loci (QTL) that explain variation in phenotypes such as yield, flowering time, and plant height ((Buckler *et al.* 2009);(Beavis *et al.* 1991);(Martinez *et al.* 2016)). Such traits are extremely agronomically important. They are also crucial plant phenotypes in terms of fitness and local adaptation. Researchers have been able to discover large-effect QTL for a number of agronomic traits through the use of different types of mapping populations (Wallace *et al.* 2014). The choice of any population comes with associated advantages and limitations. In particular, they tend to vary in two main characteristics: (1) their ability to capture genetic diversity and (2) their power to detect QTL of small effect. Multi-parent Advanced Generation Intercross (MAGIC) populations have been used in breeding to increase the genetic diversity and number of recombination events included in a mapping population compared to biparental populations (Huang *et al.* 2012);(Huang

et al. 2012);(Aylor *et al.* 2011);(Dell'Acqua *et al.* 2015);(Highfill *et al.* 2016). Compared to genome-wide association panels, MAGIC populations have more power to detect rare alleles (i.e. alleles that are only present in one of the parents) and can better estimate allelic effects because the crossing scheme increases the frequency of all parental alleles to be approximately equal. Simulations of an 8-parent MAGIC population showed that sample sizes of 300 could detect QTL accounting for 12% of variance with a power of 82% (Dell'Acqua *et al.* 2015). Lastly, a MAGIC population avoids confounding due to population structure that is encountered with GWAS because the pedigree of the lines is known. In this study, we utilized a MAGIC population of about 400 doubled-haploid lines derived from 16 inbred maize parents developed by Limagrain to understand how methods of representing genotypic data can impact the identification of QTL. Extensive genetic resources already exist for maize, but do not possess the same diversity and statistical power as the Biogemma MAGIC population. A maize nested association mapping (NAM) population exists, consisting of RIL populations derived from 25 inbred parents crossed to B73 (Yu *et al.* 2006). Only two inbred parents overlap between the NAM and Biogemma MAGIC populations (B73 and Oh43), and compared to the NAM, the MAGIC population can have similar power to the NAM using half the number of samples (Dell'Acqua *et al.* 2015). Likewise, another maize MAGIC population has previously been created, which overlaps by three parents (A632, B73, and B96) (Dell'Acqua *et al.* 2015). However, the previous MAGIC is derived from 8 inbred maize parents instead of 16, and consists of RILs, not doubled haploids, so some residual heterozygosity may exist. For these reasons, the Biogemma MAGIC population has great potential to reveal new insights into the

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genetic control of quantitative traits in maize. It also serves a reliable standard for QTL mapping method comparison because DH lines were used and the crossing scheme ensured that there is a reasonably even distribution of the 16 founders within the population (supplemental figure?)

vg1

Flowering time is a highly important trait. In addition to being a crucial agronomic trait, it is a large part of local adaptation for annual plants such as maize, ensuring that individuals can reproduce within the growing season of their environments [cite?]. Flowering time in maize has been shown to be a highly polygenic trait [cite] controlled by many, mostly small-effect loci. The relatively large effect of *vg1* compared to most other identified maize flowering time QTL has made it a target of a great deal of study. As a naturally-occurring variant, the frequency of the early-flowering allele of *vg1* has been shown to closely follow a latitudinal gradient, suggesting that there has been selection on *vg1* that allowed maize to spread to higher latitudes [cite Navarro?].

The flowering time QTL, *vg1* has been identified in multiple populations [cite]. Previous research by [cite] has shown that variation in flowering time at this site is strongly correlated with a MITE insertion within a conserved non-coding sequence about 70 kb upstream of a major flowering time regulatory gene, *ZmRAP2.7* [cite], with the presence of the MITE associated with an earlier flowering time. Within maize heterotic groups, Flint maize lines tend to possess the early-flowering allele of *vg1* (MITE+), while dents (such as B73) tend to carry the late-flowering allele (MITE-) [cite?]. It is hypothesized that the MITE represses expression of *ZmRAP2.7*, possibly due to change in methylation around the insertion [cite]. It has been shown that there are differentially-methylated regions between B73, landrace maize, and teosinte [cite]. However, the MITE has not been experimentally shown to cause a decrease in *ZmRap2.7* expression and results in earlier flowering. Further, there has been some evidence of epistatic interactions, potentially with another flowering time QTL, *vg3* which can impact the effect of the QTL (Alain Charcosset, personal communication). However, a recent study using multiple multi-parent populations suggested that variation in the effect of *vg1* in different genetic backgrounds was due to local genetic variation surrounding *vg1*, rather than epistasis with distant loci. This finding suggests two possibilities: either (1) that the causal variant underlying *vg1* is some as-yet unidentified variant that is in tight, but imperfect linkage disequilibrium with the MITE insertion, or (2) that the MITE insertion directly impacts flowering time, and that another variant nearby has a modifying effect on the MITE.

Using a well-characterized flowering time QTL with a strong candidate causal variant that is variable in the population, we demonstrate differences between the three methods and explore potential epistatic interactions between *vg1* and other genetic variation in the population.

Materials and Methods

Genotype Data

The MAGIC population was derived from 16 inbred maize parents representing the diversity of European flint and U.S. dent heterotic groups. The 16 founder lines were crossed in a funnel crossing scheme, and then the resulting synthetic population was intercrossed for 3 generations with around 2000 individuals per cycle (Figure 1A). Finally, 800 lines were selected from the

synthetic population to create doubled haploids (DH), resulting in 550 MAGIC DH lines at the end of the process. The 16 founder lines and the MAGIC DH lines were all genotyped with the Affymetrix 600K Axiom SNP array (Unterseer *et al.* 2014). Total of 503,892 SNPs from 600K after filtering out invariant sites and [num] sites with missing data...

Phenotype Data

The MAGIC DH lines were crossed to a tester MBS84 to produce 325 hybrids. Due to variation in flowering time, a subset of the lines could not be crossed to the tester. The hybrids were grown in five different field locations in four different years, resulting in six distinct environment-years. The environment-years included Blois, France in 2014 and 2017, Nerac, France in 2016, St. Paul, France in 2017, Szeged, Hungary in 2017, and Graneros, Chile in 2015. For each genotype, two blocks of around 80 plants were grown under well-watered conditions. Measured phenotypes included days to anthesis (DTA), days to silking (DTS), plant height, percent harvest grain moisture, grain yield, and thousand kernel weight (adjusted to 15% humidity), where values were averaged over blocks. Both flowering time phenotypes were measured as the sum of degree days since sowing with a base temperature of 6°C (48°F). Days to anthesis was considered as the growing degree days until 50% of plants in a block were flowering at 25% of the central tassel spike.

Calculation and Validation of Founder Probabilities

The package R/qrtl2 (Broman *et al.* 2019) was used to determine founder probabilities of the DH lines using the 600K genotype data and the cross type “riself16”. Due to the fact that the actual crossing scheme and the cross type input into R/qrtl2 differed, we wanted to assess the accuracy of the founder probabilities. This was done by simulating lines using the actual crossing scheme and assessing the performance of the `calc_genoprob` function of R/qrtl2 in correctly identifying the founder genotype (Figure 1). We developed an R package, `magicsim` (<https://github.com/sarahodell/magicsim>), to simulate the lines using the maize consensus genetic map from (Ogut *et al.* 2015) to generate approximate recombination rates across the chromosome. For 400 simulated lines, 99.6% of SNPs were correctly assigned to the founder genotype. Sites were dropped for individual founders if the sum of probabilities for a particular founder across all MAGIC lines was less than 1 or if there were fewer than 5 MAGIC lines that had a probability greater than 0.8 for one of the founders. This was to ensure that effect sizes for individual founders could be effectively estimated. In addition, the founder probabilities were filtered for LD using an iterative approach where a SNP was dropped if the R^2 value of probabilities between it and the kept SNP was greater than 0.95. After filtering, a total of 4,578 sites were kept to represent segments of chromosomes with little recombination in the MAGIC DH lines.

Calculation of Identity-by-Descent and Haplotype Probabilities

The use of founder probabilities makes the assumption that all 16 founders have distinct haplotypes. This assumption is not realistic, especially considering the known varying degrees of relatedness between the founders. The identification of regions of shared genetic sequence between founder pairs would allow for the collapsing of founder probabilities into haplotype probabilities. These haplotype probabilities have the potential to increase statistical power by reducing the number of tests performed in QTL mapping. Areas of uncertainty in founder

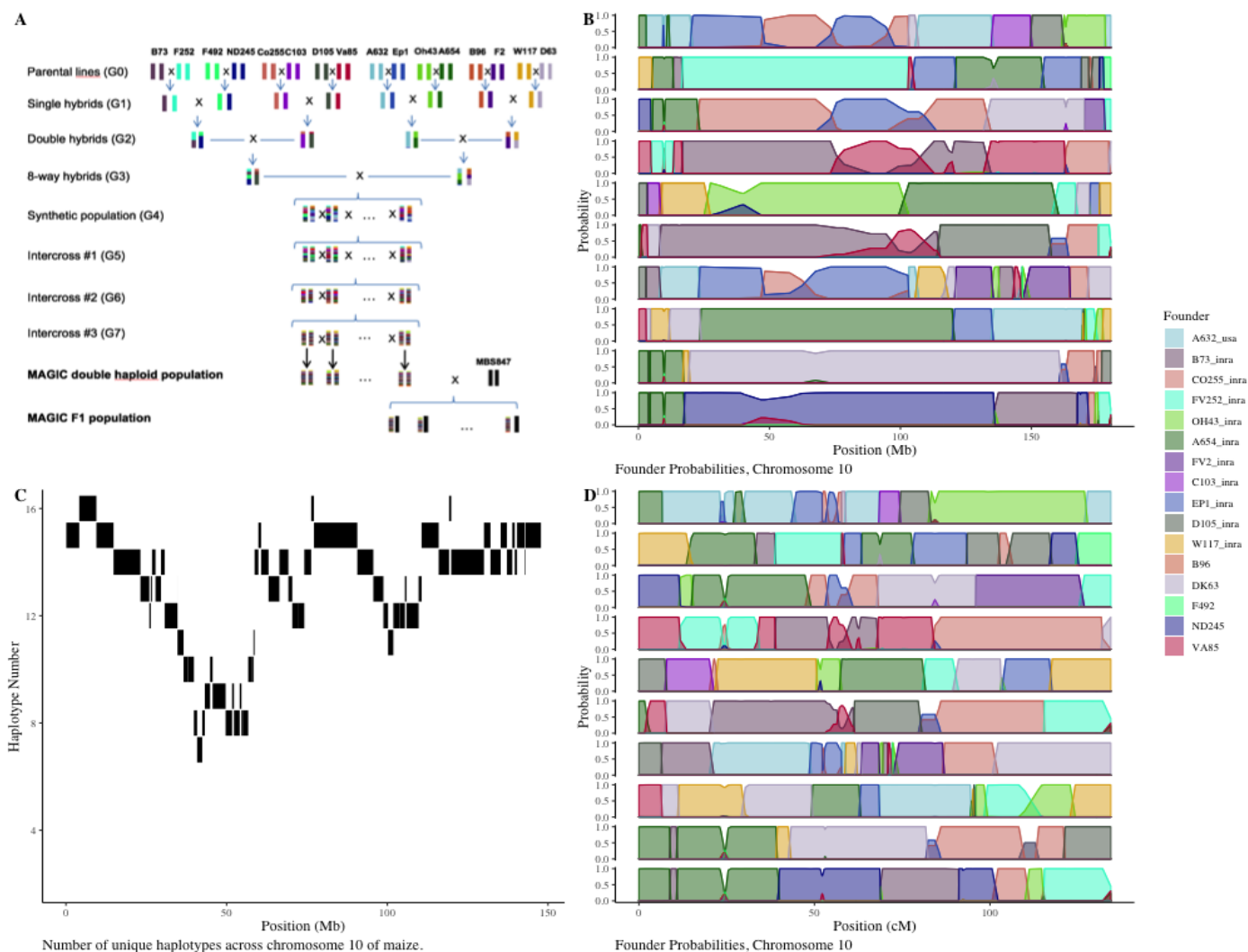


Figure 1 Structure, diversity, and founder representation of the MAGIC population. (A) The crossing scheme of the MAGIC population. (B) Founder probabilities for 10 MAGIC DH lines on chromosome 10 in physical distance. (C) The number of unique haplotype groups among the 16 founder lines across chromosome 10. (D) Founder probabilities for 10 MAGIC DH lines on chromosome 10 in genetic distance.

probabilities of the DH lines were associated with regions of identity-by-descent (IBD) between two or more founder lines in that region of the chromosome. IBD was measured from the 600K SNP data of the founders using the software Refined-IBD (Browning and Browning 2013). The resulting segments of pairwise IBD between each of the 16 founders were used to identify distinct haplotype blocks [elaborate, supplemental figure?]. Within blocks, the founder probabilities for founders that were in IBD were summed to obtain haplotype probabilities. This resulted in haplotype blocks with the number of unique haplotypes within blocks ranging from 6 at the lowest and 16 at the highest. Sites were dropped for individual haplotypes if the sum of probabilities for a particular haplotype across all MAGIC lines was less than 1 or if there were fewer than 5 MAGIC lines that had a probability greater than 0.8 for one of the haplotypes. This was to ensure that effect sizes for individual haplotypes could be effectively estimated. The haplotype probabilities were filtered for LD using an iterative approach where, for all haplotype blocks with the same number of distinct haplotypes, a

SNP was dropped if the correlation of probabilities between it and the kept SNP was greater than 0.95. After filtering, a total of 11,105 sites were kept to represent haplotype blocks in the MAGIC DH lines.

Association and QTL Mapping

The R package GridLMM was used to run association mapping using the three different methods of representing the genotype data (Runcie and Crawford 2019). The function GridLMM_ML was used with the "ML" option. The three methods differed in the X matrix used in the mixed linear model. The model that incorporated the raw 600K SNP genotype data (hereafter referred to as $GWAS_S$) was:

$$Y = X_S \beta_S + Zu + \epsilon \quad (1)$$

where Y is the response variable, X_S is the genotype matrix with reference and alternate alleles represented as 0 and 1, respectively, β_S is the effect size of the alternate allele, Z is the design matrix, u is the random effects, and ϵ is the error.

The model that incorporated the founder probabilities (hereafter referred to as $GWAS_F$) was:

$$Y = X_F \beta_F + Zu + \epsilon \quad (2)$$

where Y is the response variable, X_F is a $p \times n \times f$ matrix and x_{fnp} is the probability that at site p , individuals n was derived from founder f , β_F , is the effect size of each founder allele, Z is the design matrix, u is the random effects, and ϵ is the error.

The model that incorporated the haplotype probabilities (hereafter referred to as $GWAS_H$) was:

$$Y = X_H \beta_H + Zu + \epsilon \quad (3)$$

where Y is the response variable, X_H is a $p \times n \times h$ matrix and x_{hnp} is the probability that at site p , individuals n has haplotype h , β_H , is the effect size of each haplotype allele, Z is the design matrix, u is the random effects, and ϵ is the error.

Significance cutoffs for p-values were obtained using permutation testing, taking the 5% cutoff from 1000 randomized permutations for each method. Code for the analyses can be found [github link].

Method Comparison

The results of the three methods of identifying QTL were compared using two main criteria: (i) presence or absence of identified QTL peaks and (ii) the resolution of those QTL peaks. QTL bounds were determined by identifying the most significant SNP for a QTL peak and demarcating the left and right bounds of the QTL as the left-most and right-most SNPs within a 100Mb window centered on the highest SNP that have a \log_{10} p-value that is 2 \log_{10} p-values below that of the highest SNP.

The presence and absence of QTL was compared across the three methods for each phenotype. A QTL was said to be identified across methods if the QTL bound for that QTL overlapped between the three methods.

The effect of the method used on the size of QTL bounds was investigated using the QTL which were identified by all three methods ($n=40$). The model constructed was:

$$\text{BoundSize} = \text{EnvironmentQTL} + \text{Method} + \epsilon \quad (4)$$

The bound size response variable was represented both in terms of physical distance (Mb) and genetic distance (cM).

Results

MAGIC Population

Analysis of the MAGIC population showed that the representation of the 16 founders in the MAGIC DH lines was relatively even, with the highest percentage founder, A654, representing 6.741% and the lowest percentage founder, EP1, representing 5.237% (Supplemental Figure). Across all regions of the each chromosomes, for 99%(?) of markers in the 600K array, at least one DH line was derived from each of the 16 founders with high confidence (greater than 0.9 probability) (Supplemental Figure). A chi-squared test was performed to determine sites within the founder probabilities were over or under represented in the MAGIC lines, deviating from the expected 1/16th distribution. One notable exception was on chromosome 6, where a region [location] had no representation from [founders]. This may be due to these founders being in close IBD with another founder, resulting in uncertainty in the founder probabilities. Another possible explanation is that there was selection against

these founders during the breeding process. This region approximately corresponds to the NOR region [citation].

The average linkage disequilibrium R^2 for the population was XX... The MAGIC population also showed significant patterns of linkage disequilibrium between chromosomes. XX pairs of SNPs in the 600K genotype data that came from different chromosomes had R^2 values of greater than 0.7. The distribution of these regions of inter-chromosomal LD were ...

Simulation and Validation of Founder Probabilities

Using the package we created, *magicsim*, we simulated chromosome 10 for 1000 MAGIC DH lines following the crossing scheme used for the actual population. We then ran R/qt2 on these simulated lines to obtain founder probabilities and compared these probabilities to the known founder identities of the simulated lines. In total, for sites for which R/qt2 was able to assign founder probabilities, the maximum probability founder matched the actual founder for 99.8% of sites. This reinforced our confidence in the founder probabilities obtained from the actual data. The founder probabilities determined using R/qt2 were able to assign founders to the DH lines with high confidence (>0.90) for [percentage] of the 10 chromosomes of maize.

Identity-By-Descent and MAGIC Haplotypes

The results showed that a total of [bp][cM] of genome were in IBD between at least two different founders. The average size of an IBD segment between two founders was 140kb (0.51 cM) with a median of 122kb (0.46). Pairwise IBD segments sizes ranged from 8 kb (0.3 cM) to 673 kb (1.61 cM). The total percentage of IBD between two founders ranged from 0.0018% (F492 and VA85) to 4.3858% (B73 and A632), with an average of 0.06130%. There were no IBD segments found for 18 of 120 possible pairwise founder combinations. [Distribution across chromosomes]

Amount of IBD between the founders and the tester, MBS847...

Phenotype Data

The distribution of the six measured phenotypes were approximately normal (Figure 2).

QTL Mapping and Association Mapping

The three methods varied both in their ability to identify QTL. There was some difference in the resolution of those QTL between methods. A total of XX unique QTL were identified across all phenotypes and environments.

BLUPs performed better than individual environments, regardless of method used, identifying a total of XX unique QTL. There were, however, XX QTL that were environment-specific, and were not identified with BLUPs.

The vast majority of QTL ($n=40$) identified were found by all three methods. 7, 3, and 6 QTL were found uniquely by the $GWAS_S$, $GWAS_F$, and $GWAS_H$ methods, respectively. 10 QTL were found by both $GWAS_F$ and $GWAS_H$, but not by $GWAS_S$, while 1 QTL was found by both $GWAS_S$ and $GWAS_F$, but not by $GWAS_H$.

Resolution of QTL bounds differs significantly between methods in terms of physical size (Mb). The size of QTL bounds from the haplotype probabilities method were significantly smaller (p-value xx) than those from the 600K SNP GWAS by approximately XX Mb. There was no significant difference between the Founder

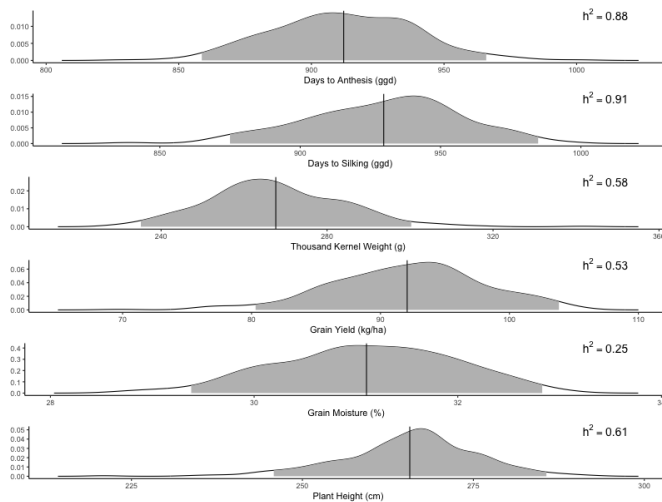


Figure 2 Distribution of phenotypes The density plots of the six measured phenotypes. The vertical bar represents the mean, and the grey shading shows two standard deviations. The heritability of each trait is shown on the right.

probabilities and the 600K SNPs or between the Founder probabilities and the Haplotype probabilities. The GWAS methods should be most powerful at identifying QTL for which the causal variant is biallelic and the tagged SNP is in tight LD with the causal variant. However, for multi-allelic QTL or QTL for which LD is low between tagged SNPs, this method begins to lose power. Founder probabilities increase the odds of detecting both QTL that are multi-allelic and QTL whose causal variant is not in tight LD with any one tagged SNP [Supplemental Figure?]. Lastly, haplotype probabilities potentially improve on the power of founder probabilities to detect QTL that meet the above criteria by reducing the number of tests. However, haplotype probabilities also may obscure the signal of some QTL if founders are called as being in IBD with one another when they actually differ for the causal variant. Due to the fact that the founder and haplotype probabilities take into account recent recombination events, whereas the GWAS method only uses historical recombination, we predicted that founder and haplotype mapping would result in higher resolution around QTL peaks. Higher resolution QTL are ideal in that it makes it easier to narrow down candidate genes and potential causal variants when the significant window is smaller.

Variation in Effect Sizes

The effect sizes of alleles within QTL bounds differed both across environments and between methods.

Variation around *vgt1*

A previously characterized QTL, *vgt1* is associated with variation in flowering time [citations]. An earlier flowering phenotype is strongly correlated with a MITE insertion about 70kb upstream of the flowering time regulator, *ZmRAP2.7*, an *APETALA*-like transcription factor [].

Evidence of epistasis around *vgt1*. Imperfect association between the presence of the MITE and the predicted effect size of the founder at *vgt1* (Figure 4)

Expression of *ZmRAP2.7*

Discussion

The results of using these three methods to identify QTL suggest that each has its own advantages and disadvantages in terms of how many and which QTL they can identify. If the goal of a study is to find as many QTL as possible, then it would be most useful to employ all three methods to maximize QTL identification. The lack of significant difference in the genetic size of support intervals for the QTL found in the three methods suggests that the differences in QTL detection ability is more a result of differences in statistical power than a difference in ability to account for recombination events (?).

vgt1

One benefit of using founder and haplotype approaches lies in the potential to dissect the effects of individual founders and/or haplotypes within QTL. This allowed us to look more closely at a well-characterized, large effect flowering time QTL, *vgt1* and observe an interesting pattern of effect sizes that deviated from our expectations based on previous research. This opens up new areas of inquiry for future studies.

another figure

This is a full size figure (Figure S1) just add stars to the figure

Acknowledgments

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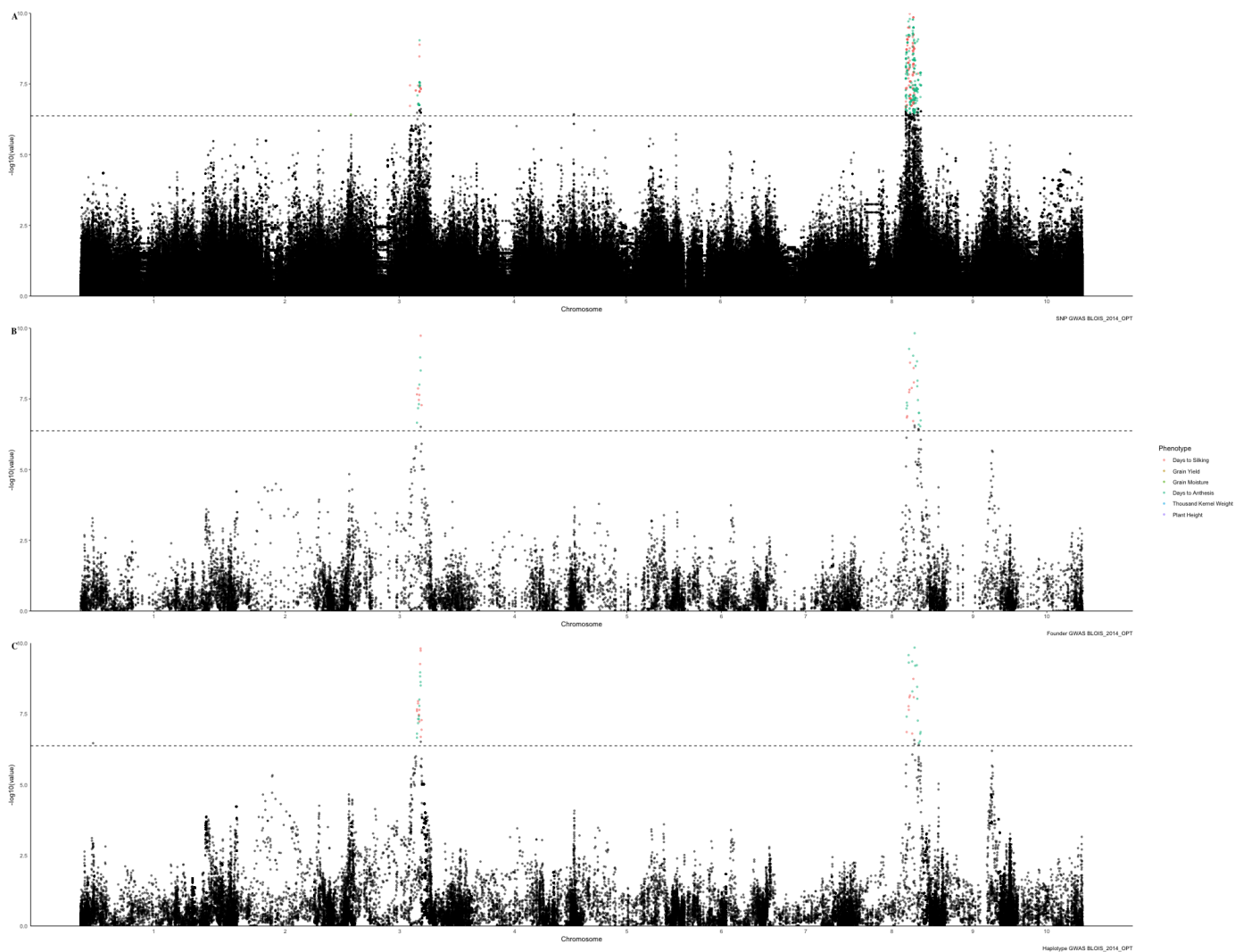


Figure 3 Results of three methods of QTL identification Colored points represent significant SNPs above the 5% significance threshold from 1000 random permutations **top** GWAS results using the 600K SNP array. **middle** Results from QTL mapping using founder probabilities **bottom** Results from QTL mapping using haplotype probabilities

Supplement

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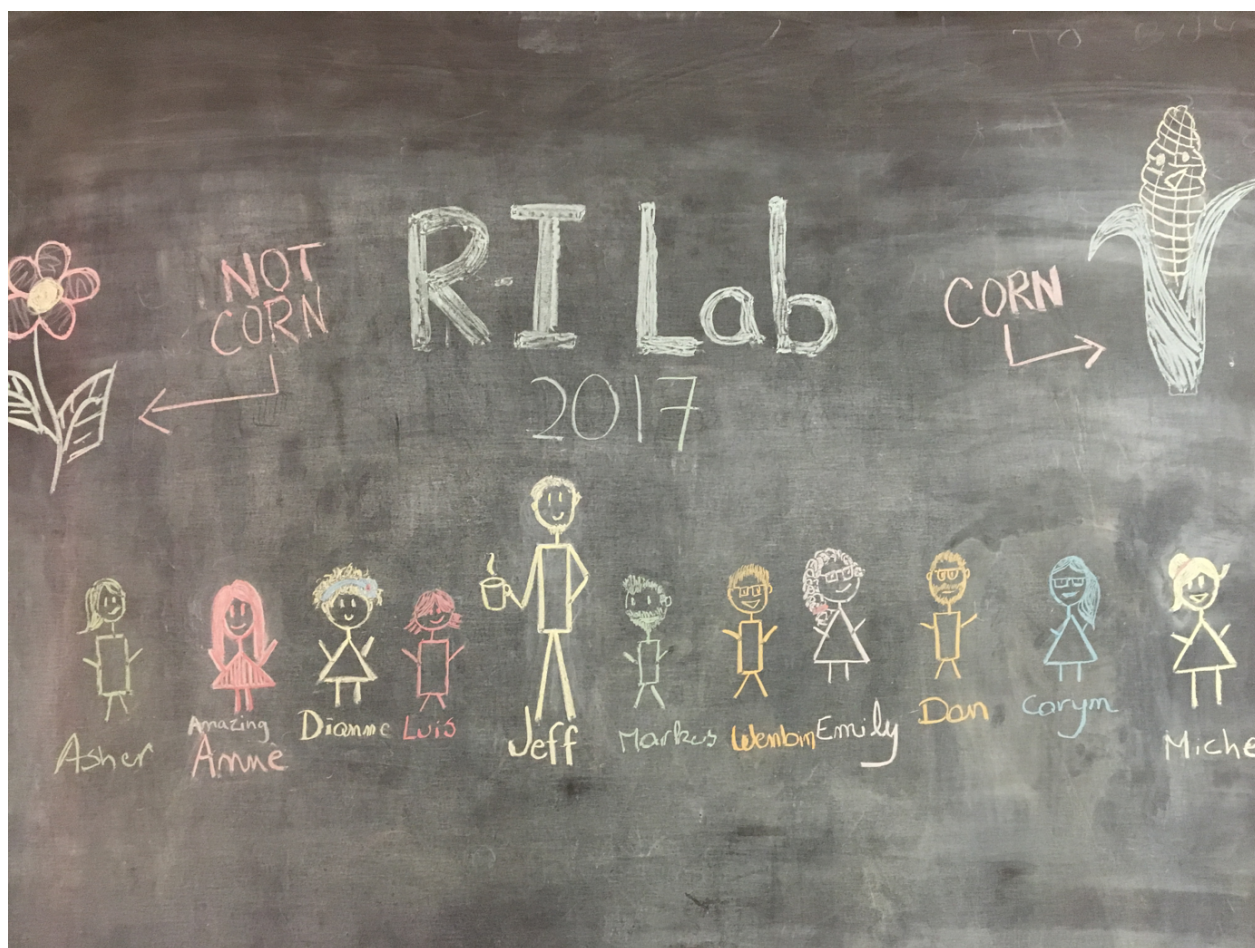


Figure S1 Supplemental figure Test test test

Table S1 Shrink a large table to fit the page

Parameter	Description
Adaptation	Trait related parameters
Time to optimum	Generations until new optimum is reached
Adaptation rate (haldane)	Adaptation rate until new optimum is reached. Calculated as $rate(h) = \frac{\frac{\ln(x_2)}{sd_{x12}} - \frac{\ln(x_1)}{sd_{x12}}}{t_2 - t_1}$
Final genetic variance	Genetic variance in the final generation
Fixations	Mutations that fix after the optimum shift
From new mutations (#)	Sum of fixed mutations in the final population that were already segregating before the optimum shift
From standing variation (#)	Sum of fixed mutations in the final population that arose after the optimum shift
Max. effect size	Maximal effect size of all fixations
Mean effect size	Mean effect size of all fixations
Mean effect size of negative fixations	Mean effect size of negative mutations
Mean effect size of positive fixations	Mean effect size of positive mutations
Mean emergence time	Mean generation when a mutation arose that fixed in the last 0.1 N generations
Mean fixation time	Mean generation in which a mutation fixed
Min. effect size	Minimal effect size of all fixations
Negative (#)	Sum of fixed mutations with negative effects in the final population
New/standing fixations	Ratio of mutations from new mutations vs. standing mutations
Proportion negative	Proportion of negative fixations from all mutations
Positive (#)	Sum of fixed mutations with positive effects in the final population
SD of effect sizes	Standard deviation of effect sizes of all fixations
SD of negative effect sizes	Standard deviation of effect sizes of negative fixations
SD of positive effect sizes	Standard deviation of effect sizes of positive fixations
Total (#)	Sum of fixed mutations in the final population
Sweeps	Mutations that fix faster than 99% of neutral fixations
Hard sweeps (#)	Sum of selective sweeps from new mutations
Proportion of hard sweeps	Porportion of hard selective sweeps of all selective sweeps
Proportion of sweeps from standing	Proportion of selective sweeps from ststanding variation of all selection sweeps
Sweeps (#)	Sum of selective sweeps
Sweeps from standing variation (#)	Sum of selective sweeps from mutations that were already segregating before the optimum shift
Sweeps/fixations	Ratio of sweeps vs. fixations
Segregating sites	Mutations that segregate in the final generation
Max. effect size	Maximal effect size of segregating sites
Mean effect size	Mean effect size of segregating sites
Mean effect size of negative sites	Mean effect size of segregating sites with negative effects
Mean effect size of positive sites	Mean effect size of segregating sites with positive effects
Mean frequency of all sites	Mean allele frequency of segregating sites
Mean frequency of negative sites	Mean allele frequency of segregating sites with negative effects
Mean frequency of positive sites	Mean allele frequency of segregating sites with positive effects
Min. effect size	Minimal effect size of segregating sites
Negative (#)	Sum of segregating sites with negative effect
Positive (#)	Sum of segregating sites with positive effect
Proportion of negative sites	Proportion of segregating sites with negative effect of all segregating sites
Standard deviation of effect sizes	Standard deviation of effect sizes of all segregating sites
Total (#)	Sum segregating sites in the final generation