Read Data

11/23/2021

```
library(foreign)
## Warning: package 'foreign' was built under R version 4.0.3
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.0.5
## -- Attaching packages ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5 v purrr 0.3.4
## v tibble 3.1.4 v dplyr 1.0.7
## v tidyr 1.1.3 v stringr 1.4.0
## v readr 2.0.1 v forcats 0.5.1
## Warning: package 'ggplot2' was built under R version 4.0.5
## Warning: package 'tibble' was built under R version 4.0.5
## Warning: package 'tidyr' was built under R version 4.0.4
## Warning: package 'readr' was built under R version 4.0.5
## Warning: package 'purrr' was built under R version 4.0.3
## Warning: package 'dplyr' was built under R version 4.0.5
## Warning: package 'stringr' was built under R version 4.0.4
## Warning: package 'forcats' was built under R version 4.0.4
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
library(e1071)
```

Warning: package 'e1071' was built under R version 4.0.5

```
library(tree)
## Warning: package 'tree' was built under R version 4.0.5
## Registered S3 method overwritten by 'tree':
##
    method
               from
    print.tree cli
##
library(gbm)
## Warning: package 'gbm' was built under R version 4.0.5
## Loaded gbm 2.1.8
library(randomForest)
## Warning: package 'randomForest' was built under R version 4.0.5
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
##
       combine
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(caret)
## Warning: package 'caret' was built under R version 4.0.5
## Loading required package: lattice
## Warning: package 'lattice' was built under R version 4.0.5
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
       lift
```

```
library(ggplot2)
library(dplyr)
library(tidyr)
library(tidyverse)
library(patchwork)
## Warning: package 'patchwork' was built under R version 4.0.5
library(UBL)
## Warning: package 'UBL' was built under R version 4.0.5
## Loading required package: MBA
## Warning: package 'MBA' was built under R version 4.0.5
## Loading required package: gstat
## Warning: package 'gstat' was built under R version 4.0.5
## Loading required package: automap
## Warning: package 'automap' was built under R version 4.0.5
## Loading required package: sp
## Warning: package 'sp' was built under R version 4.0.5
library(scales)
## Warning: package 'scales' was built under R version 4.0.4
##
## Attaching package: 'scales'
## The following object is masked from 'package:purrr':
##
##
       discard
## The following object is masked from 'package:readr':
##
##
       col_factor
```

```
sesame <- read.dta("sesame.dta")</pre>
sesame <- sesame %>%
  mutate(site=factor(site)) %>%
  mutate(bodyDiff = postbody - prebody,
         letDiff = postlet - prelet,
         formDiff = postform - preform,
         numbDiff = postnumb - prenumb,
         relatDiff = postrelat - prerelat,
         clasfDiff = postclasf - preclasf)
sesame.sd <- sesame%>%
  mutate(sd_pBod = scale(prebody, center = TRUE, scale = TRUE),
         sd_plet = scale(prelet, center = TRUE, scale = TRUE),
         sd_pform = scale(preform, center = TRUE, scale = TRUE),
         sd_pnumb = scale(prenumb, center = TRUE, scale = TRUE),
         sd_prelat = scale(prerelat, center = TRUE, scale = TRUE),
         sd_pclasf = scale(preclasf, center = TRUE, scale = TRUE),
         sd_peabody = scale(peabody, center = TRUE, scale = TRUE),
         sd_age = scale(age, center =TRUE, scale = TRUE),
         male=if_else(sex==1, 1, 0),
         female=if_else(sex==2, 1, 0))
```

Exploratory Data Analysis

```
head(sesame)
```

```
rownames id site sex age viewcat setting viewenc prebody prelet preform
## 1
             1 1
                      1
                           1
                              66
                                                 2
                                                                          23
                                                                                   12
                                        1
                                                          1
                                                                  16
                                                 2
             2 2
## 2
                           2
                              67
                                        3
                                                                  30
                                                                          26
                                                                                    9
## 3
             3 3
                              56
                                        3
                                                 2
                                                          2
                                                                  22
                                                                          14
                                                                                    9
                      1
                           1
             4 4
                                                 2
## 4
                      1
                           1
                              49
                                        1
                                                          2
                                                                  23
                                                                          11
                                                                                   10
## 5
             5 5
                      1
                           1
                              69
                                        4
                                                 2
                                                          2
                                                                  32
                                                                          47
                                                                                   15
             6
                6
                      1
                           2
                              54
                                        3
                                                 2
                                                          2
                                                                  29
                                                                          26
##
     prenumb prerelat preclasf postbody postlet postform postnumb postrelat
## 1
           40
                     14
                               20
                                         18
                                                  30
                                                            14
                                                                       44
                                                                                  14
## 2
           39
                     16
                               22
                                         30
                                                  37
                                                            17
                                                                       39
                                                                                  14
## 3
            9
                      9
                                8
                                         21
                                                  46
                                                            15
                                                                       40
                                                                                   9
                                                                                   8
## 4
           14
                      9
                               13
                                         21
                                                  14
                                                            13
                                                                       19
## 5
           51
                     17
                               22
                                         32
                                                  63
                                                            18
                                                                       54
                                                                                  14
## 6
                                         27
                                                  36
                                                                       39
           33
                     14
                               14
                                                            14
                                                                                  16
     postclasf peabody agecat encour _Isite_2 _Isite_3 _Isite_4 _Isite_5 regular
## 1
             23
                                                 0
                                                           0
                                                                      0
                                                                                0
                      62
                               1
                                       1
## 2
             22
                       8
                               1
                                                 0
                                                           0
                                                                      0
                                                                                0
                                                                                         1
                                       1
## 3
             19
                      32
                               1
                                                 0
                                                           0
                                                                      0
                                                                                0
                                                                                         1
## 4
             15
                      27
                               0
                                       0
                                                 0
                                                           0
                                                                      0
                                                                                0
                                                                                        0
             21
                      71
                                                 0
                                                           0
## 5
                               1
                                       0
                                                                      0
                                                                                0
                                                                                         1
## 6
             24
                      32
                               1
                                       0
                                                 0
                                                                                0
                                                                                         1
     bodyDiff letDiff formDiff numbDiff relatDiff clasfDiff
##
## 1
             2
                      7
                                2
                                                      0
                                          4
## 2
             0
                     11
                                8
                                          0
                                                     -2
                                                                 0
## 3
                     32
                                6
                                         31
                                                     0
                                                                11
            -1
## 4
            -2
                      3
                                3
                                          5
                                                     -1
                                                                 2
```

```
## 5 0 16 3 3 -3 -1
## 6 -2 10 4 6 2 10
```

Variables:

The ID refers to a subject's identification number. The site refers to the age and background information of the child. A site value of 1 indicates a 3-5 year old disadvantaged child from the inner city. A site value of 2 represents a 4 year old advantaged child from the suburbs. A value of 3 represents an advantaged rural child. A site value of 4 indicates a disadvantaged rural child. Lastly, a value of 5 represents a disadvantaged Spanish speaking child. For the sex, a value of 1 indicates male, and a value of 2 indicates female. The age category is the child's age in months. The viewcat column is the frequency of viewing Sesame Street (1 = rarely, 2 = once/twice per week, 3 = 3-5 times a week, 4 = more than 5 times per week). The setting is where Sesame Street was viewed; a value of 1 indicates home and a value of 2 indicates school. The viewenc column refers to if the child was encouraged to watch or not (1 = child not encouraged, 2 = child encouraged). Encour is the same variable but with values 0 and 1, respectively. Regular is an indicator variable representing if a child is a regular viewer (0 = rarely watched, 1 = watched once per week or greater).

The prebody, prelet, preform, prenumb, prerelat, and preclasf columns all decribe pretest scores on varying types of assessments (body parts, letters, forms, numbers, relational terms, and classification skills, respectively). The columns labelled postbody, postlet, postform, postnumb, postrelat, and postclasf are the children's respective posttest scores. Above, we created the following variables - bodydiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff - to represent the difference in posttest scores and pretest scores for each child. Lastly, peabody represents a score of "mental age" for vocabulary maturity from the Peabody Picture Vocabulary Test.

Our main focus will be on the new variables we created (bodyDiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff) and variables related to how often the children watch Sesame Street (namely, viewcat and regular). Lastly, we will look into the backgrounds of the children, including site, sex, and age.

Distributions:

For the purposes of our analysis, we will first look at the distributions of bodyDiff, letDiff, formDiff, numbDiff, relatDiff, and clasfDiff.

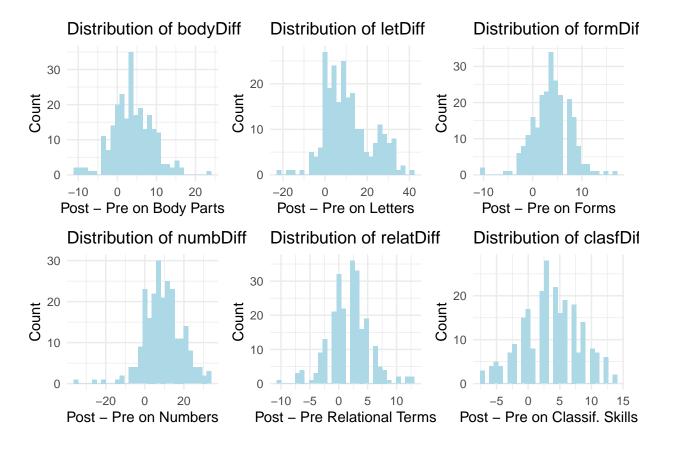
```
#want to visualize distributions of bodyDiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff
bodyDiffplot <- ggplot(sesame, aes(x = bodyDiff)) +</pre>
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of bodyDiff", x = "Post - Pre on Body Parts", y = "Count") +
  theme_minimal()
letDiffplot \leftarrow ggplot(sesame, aes(x = letDiff)) +
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of letDiff", x = "Post - Pre on Letters", y = "Count") +
  theme_minimal()
formDiffplot \leftarrow ggplot(sesame, aes(x = formDiff)) +
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of formDiff", x = "Post - Pre on Forms", y = "Count") +
  theme_minimal()
numbDiffplot <- ggplot(sesame, aes(x = numbDiff)) +</pre>
  geom histogram(fill = "lightblue") +
  labs(title = "Distribution of numbDiff", x = "Post - Pre on Numbers", y = "Count") +
```

```
theme_minimal()

relatDiffplot <- ggplot(sesame, aes(x = relatDiff)) +
    geom_histogram(fill = "lightblue") +
    labs(title = "Distribution of relatDiff", x = "Post - Pre Relational Terms", y = "Count") +
    theme_minimal()

clasfDiffplot <- ggplot(sesame, aes(x = clasfDiff)) +
    geom_histogram(fill = "lightblue") +
    labs(title = "Distribution of clasfDiff", x = "Post - Pre on Classif. Skills", y = "Count") +
    theme_minimal()

bodyDiffplot + letDiffplot + formDiffplot + numbDiffplot + relatDiffplot + clasfDiffplot</pre>
```



The six variables above were calculated by subtracting pre-test scores from post-test scores, so they are all numerical. The distributions of these six variables (bodyDiff, letDiff, formDiff, numbDiff, relatDiff, and clasfDiff) all appear to be roughly normal and unimodal. BodyDiff, letDiff, formDiff, relatDiff, and classDiff do not appear to have any obvious extreme outliers. Numbdiff, however, seems to be slightly left-skewed with outliers to the left -20. All of the six variables appear to have centers between 2 and 4.

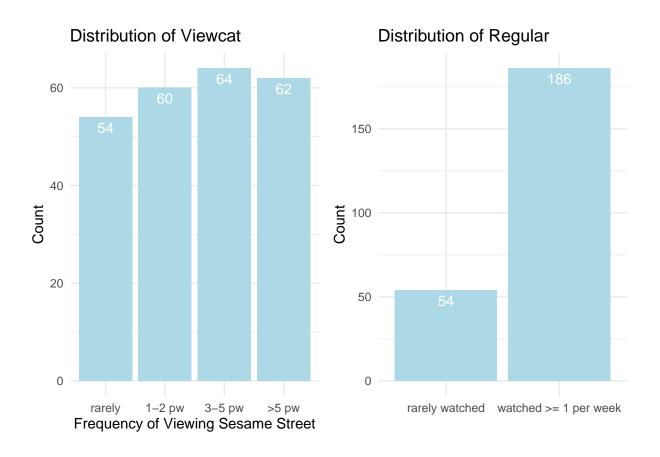
We will now examine the distributions of the variables related to how often children watch Sesame Street (namely, viewcat and regular).

 ${\it \# want \ to \ visualize \ distributions \ of \ viewcat \ and \ regular}$

```
viewcatplot <- ggplot(sesame, aes(x = factor(viewcat))) +
    geom_bar(fill = "lightblue") +
    labs(title = "Distribution of Viewcat", x = "Frequency of viewing Sesame Street", y = "Count") +
    scale_x_discrete("Frequency of Viewing Sesame Street", labels=c("rarely", "1-2 pw", "3-5 pw", ">5 pw"
    theme_minimal() +
    geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")

regularplot <- ggplot(sesame, aes(x = factor(regular))) +
    geom_bar(fill = "lightblue") +
    labs(title = "Distribution of Regular", y = "Count") +
    scale_x_discrete(labels=c("rarely watched", "watched >= 1 per week")) +
    theme_minimal() +
    theme(axis.title.x = element_blank()) +
    geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")

viewcatplot + regularplot
```

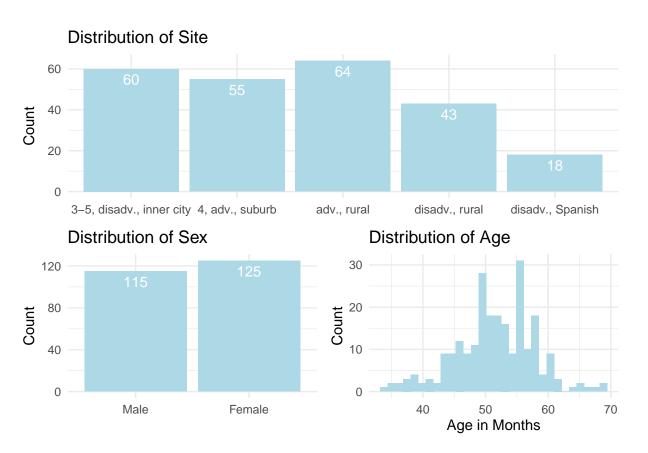


Both of these variables are categorical. On the left, viewcat appears to have a roughly uniform distribution, with "rarely" having the least amount of children and 3-5 times per week having the most (the range is only 10 children, so all of the bars are relatively close in height). For the variable regular, the category "watched once per week or greater" has far more observations than "rarely watched." The former category has more than triple the amount of the latter. We will be aware of this disparity in our analysis and continue with caution towards potential bias.

Lastly, we want to examine the distributions of site, sex, and age, all variables that relate to a child's

background.

```
# want to visualize distributions of site, sex, and age
siteplot \leftarrow ggplot(sesame, aes(x = factor(site))) +
  geom_bar(fill = "lightblue") +
  labs(title = "Distribution of Site", y = "Count") +
  scale_x_discrete(labels=c("3-5, disadv., inner city", "4, adv., suburb", "adv., rural", "disadv., rur
  theme minimal() +
  theme(axis.title.x = element_blank()) +
  geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")
sexplot \leftarrow ggplot(sesame, aes(x = factor(sex))) +
  geom_bar(fill = "lightblue") +
  labs(title = "Distribution of Sex", y = "Count") +
  scale_x_discrete(labels=c("Male", "Female")) +
  theme_minimal() +
  theme(axis.title.x = element_blank()) +
  geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")
ageplot \leftarrow ggplot(sesame, aes(x = age)) +
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of Age", x = "Age in Months", y = "Count") +
  theme_minimal()
siteplot / (sexplot + ageplot)
```



Site and Sex are both categorical variables. Distribution of Site has four categories with roughly the same amount of children (ranging from 43 to 64), but one category with far fewer observations (disadvantaged Spanish-speaking). This category has less than half of the observations as the next smallest category, which is a relatively large disparity. We will continue our analysis with caution towards this bias in the data. The distribution of sex is very even - the male category has 115 observations, while the female category has 125 observations. Age is a numerical variable that appears to be normal and bimodal, with two peaks around 50 and 56. There do not appear to be any extreme outliers in the distribution of age.

Q.1 Prediction Question: Can we use linear regression to predict the change in a child's test scores that occur after watching Sesame street (or in some instances, not watching Sesame street)?

Linear Regression Models

Here, I am fitting 6 linear regression models. Each of the models predicts a different difference in test score.

```
sesame.q1 <- sesame
sesame.q1$site <- as.factor(sesame.q1$site)
sesame.q1$sex <- as.factor(sesame.q1$sex)
sesame.q1$viewcat <- as.factor(sesame.q1$viewcat)
sesame.q1$setting <- as.factor(sesame.q1$setting)
sesame.q1$viewenc <- as.factor(sesame.q1$viewenc)</pre>
```

```
# Scaling Variables
sesame.q1$bodyDiff <- rescale(sesame.q1$bodyDiff, to = c(0, 30))
sesame.q1$letDiff <- rescale(sesame.q1$letDiff, to = c(0, 30))
sesame.q1$formDiff <- rescale(sesame.q1$formDiff, to = c(0, 30))
sesame.q1$numbDiff <- rescale(sesame.q1$numbDiff, to = c(0, 30))
sesame.q1$relatDiff <- rescale(sesame.q1$relatDiff, to = c(0, 30))
sesame.q1$relatDiff <- rescale(sesame.q1$relatDiff, to = c(0, 30))</pre>
```

```
# Test-Train Split
set.seed(1)
train <- sample(1:nrow(sesame.q1), nrow(sesame.q1)*0.7)
training = sesame.q1[train,]
testing = sesame.q1[-train,]</pre>
```

Firstly, we factored the following variables to encode them as categoricals: site, sex, viewcat, setting, viewenc.

One problem that we envisioned when evaluating the and comparing the different models is that the tests are scored on different scales. For example, the scores for the test on knowledge of body parts (noted by bodyDiff) range from 0-32, while those of the test on letters (noted by letDiff) range from 0-58. To be able to aptly compare the mean squared error (MSE) between models, we also decided to convert each response variable to the same range. More specifically, we scaled each variable to the arbitrary range [0, 30].

Lastly, we randomly split the data between testing and training, using 70% of the data for training and 30% of the data for testing.

```
lin.mod1.full <- lm(bodyDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod1.full)</pre>
```

```
##
## Call:
## lm(formula = bodyDiff ~ (site + sex + age + viewcat + setting +
       viewenc)^2, data = training)
##
## Residuals:
##
      Min
                                3Q
                1Q Median
                                       Max
## -8.0419 -2.3623 -0.0666 2.0079
                                   9.9599
##
## Coefficients: (2 not defined because of singularities)
                     Estimate Std. Error t value Pr(>|t|)
##
                     -5.21460
                                14.63930 -0.356
                                                   0.7224
## (Intercept)
## site2
                     -1.67860
                               13.72456 -0.122
                                                   0.9029
                                           0.130
## site3
                      1.18809
                                9.13599
                                                   0.8968
## site4
                     36.76705
                                16.49603
                                           2.229
                                                   0.0278 *
## site5
                      2.51268
                               17.41166
                                           0.144
                                                   0.8855
## sex2
                      2.67852
                                6.79950
                                           0.394
                                                   0.6944
                      0.30634
                                 0.26777
                                           1.144
                                                   0.2551
## age
                     11.62045
                                14.78702
                                           0.786
                                                   0.4336
## viewcat2
## viewcat3
                     12.46797
                                13.36691
                                           0.933
                                                   0.3530
## viewcat4
                     29.95220
                               14.54421
                                           2.059
                                                   0.0418 *
## setting2
                     -9.74959
                                         -1.069
                                                   0.2872
                                 9.11761
## viewenc2
                     19.16298
                               10.20959
                                          1.877
                                                   0.0631 .
## site2:sex2
                      3.01414
                                 2.22656
                                          1.354
                                                   0.1786
## site3:sex2
                     2.32383
                                 2.17020
                                          1.071
                                                   0.2866
## site4:sex2
                     0.53119
                                 2.63525
                                           0.202
                                                   0.8406
## site5:sex2
                     0.32139
                                 3.71691
                                           0.086
                                                   0.9312
## site2:age
                     0.04657
                                 0.24040
                                           0.194
                                                   0.8467
## site3:age
                     0.03300
                                 0.17150
                                           0.192
                                                   0.8477
## site4:age
                     -0.59988
                                 0.30613 -1.960
                                                   0.0525
## site5:age
                      0.01087
                                 0.33703
                                           0.032
                                                   0.9743
## site2:viewcat2
                      3.94606
                                 5.50815
                                           0.716
                                                   0.4752
## site3:viewcat2
                                           0.544
                      2.11625
                                 3.88814
                                                   0.5873
## site4:viewcat2
                      2.33983
                                 3.90246
                                           0.600
                                                   0.5500
## site5:viewcat2
                                 6.28877
                                           0.820
                     5.15446
                                                   0.4142
## site2:viewcat3
                     -4.60122
                                 5.15701
                                         -0.892
                                                   0.3742
                     -2.61690
                                          -0.714
## site3:viewcat3
                                 3.66597
                                                   0.4768
## site4:viewcat3
                     -4.29765
                                 4.15537
                                          -1.034
                                                   0.3033
## site5:viewcat3
                           NA
                                      NA
                                              NA
                                                       NA
## site2:viewcat4
                     -2.76550
                                 5.23768
                                          -0.528
                                                   0.5985
                    -2.14835
## site3:viewcat4
                                 3.84372
                                          -0.559
                                                   0.5773
## site4:viewcat4
                     -6.19787
                                 4.85958
                                          -1.275
                                                   0.2048
## site5:viewcat4
                    -3.85743
                                 6.63742 -0.581
                                                   0.5623
## site2:setting2
                     0.63008
                                 2.76440
                                           0.228
                                                   0.8201
## site3:setting2
                      0.14259
                                 3.16610
                                           0.045
                                                   0.9642
## site4:setting2
                      5.09348
                                 3.25326
                                           1.566
                                                   0.1203
## site5:setting2
                                      NA
                                              NA
                                                       NA
## site2:viewenc2
                                 2.60475
                                           0.342
                    0.89088
                                                   0.7330
## site3:viewenc2
                     -1.79090
                                 3.30478 -0.542
                                                   0.5890
## site4:viewenc2
                     -5.97857
                                 3.03298 -1.971
                                                   0.0512 .
```

```
## site5:viewenc2
                    -2.07853
                                7.09228 -0.293
                                                 0.7700
                               0.12653 -0.841
                    -0.10641
                                                 0.4022
## sex2:age
                    1.49879
## sex2:viewcat2
                                2.64935 0.566
                                                 0.5727
## sex2:viewcat3
                                         0.234
                    0.58754
                                2.51057
                                                 0.8154
## sex2:viewcat4
                    -1.20166
                                2.68241 -0.448
                                                 0.6550
                               1.70350 -0.903
## sex2:setting2
                   -1.53778
                                                 0.3686
## sex2:viewenc2
                               1.93998 0.622
                    1.20679
                                                 0.5352
                                0.26179 -1.048
## age:viewcat2
                    -0.27426
                                                 0.2971
## age:viewcat3
                    -0.15379
                               0.23654 -0.650
                                                 0.5169
## age:viewcat4
                    -0.46253
                                0.26054 -1.775
                                                 0.0786 .
## age:setting2
                     0.05401
                                0.15397
                                         0.351
                                                 0.7264
## age:viewenc2
                    -0.27988
                                0.18128 -1.544
                                                 0.1254
## viewcat2:setting2 5.64914
                                3.31141
                                        1.706
                                                 0.0908 .
## viewcat3:setting2 6.07677
                                3.20554
                                        1.896
                                                 0.0606 .
## viewcat4:setting2 6.21301
                                3.52866
                                        1.761
                                                 0.0810 .
## viewcat2:viewenc2 -7.71647
                                3.54437 -2.177
                                                 0.0316 *
## viewcat3:viewenc2 -6.24879
                                3.34488 -1.868
                                                 0.0644 .
## viewcat4:viewenc2 -7.65623
                                3.62444 -2.112
                                                 0.0369 *
## setting2:viewenc2 1.97122
                                2.32061 0.849
                                                 0.3974
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 4.226 on 112 degrees of freedom
## Multiple R-squared: 0.4033, Adjusted R-squared: 0.1103
## F-statistic: 1.377 on 55 and 112 DF, p-value: 0.07819
AIC(lin.mod1.full)
## [1] 1006.935
yhat <- predict(lin.mod1.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod1.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "bodyDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 32.44637
lin.mod2.full <- lm(letDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)</pre>
summary(lin.mod2.full)
##
## Call:
## lm(formula = letDiff ~ (site + sex + age + viewcat + setting +
      viewenc)^2, data = training)
##
##
## Residuals:
```

```
1Q
                        Median
                                      3Q
## -12.7462 -2.3134
                        0.0386
                                  2.3986 10.2234
##
## Coefficients: (2 not defined because of singularities)
                       Estimate Std. Error t value Pr(>|t|)
                                              1.236
## (Intercept)
                       19.20505
                                   15.54400
                                                       0.2192
## site2
                                             -0.518
                       -7.55435
                                   14.57273
                                                       0.6052
## site3
                        7.76205
                                    9.70058
                                              0.800
                                                       0.4253
## site4
                      -12.82246
                                   17.51547
                                             -0.732
                                                       0.4657
## site5
                        1.39944
                                   18.48769
                                              0.076
                                                       0.9398
## sex2
                       -7.03111
                                    7.21970
                                             -0.974
                                                       0.3322
                                             -0.480
## age
                       -0.13633
                                    0.28432
                                                       0.6325
## viewcat2
                      -20.28956
                                   15.70085
                                             -1.292
                                                       0.1989
## viewcat3
                       -0.74326
                                   14.19298
                                             -0.052
                                                       0.9583
                                              0.370
## viewcat4
                        5.71015
                                   15.44303
                                                       0.7123
## setting2
                       -0.93795
                                    9.68107
                                             -0.097
                                                       0.9230
                                             -0.500
## viewenc2
                       -5.41528
                                   10.84054
                                                       0.6184
## site2:sex2
                        1.20390
                                    2.36416
                                              0.509
                                                       0.6116
## site3:sex2
                                             -0.275
                       -0.63445
                                    2.30431
                                                       0.7836
## site4:sex2
                       -3.21100
                                    2.79810
                                             -1.148
                                                       0.2536
## site5:sex2
                       -1.80949
                                    3.94661
                                             -0.458
                                                       0.6475
## site2:age
                                    0.25526
                                              1.067
                                                       0.2881
                        0.27245
                                                       0.3328
                                             -0.973
## site3:age
                       -0.17713
                                    0.18209
## site4:age
                                              0.996
                        0.32387
                                    0.32505
                                                       0.3212
                                                       0.8474
## site5:age
                       -0.06901
                                    0.35786
                                             -0.193
## site2:viewcat2
                       -1.69100
                                    5.84855
                                             -0.289
                                                       0.7730
## site3:viewcat2
                        0.28314
                                    4.12842
                                              0.069
                                                       0.9454
## site4:viewcat2
                        3.57460
                                    4.14363
                                              0.863
                                                       0.3902
## site5:viewcat2
                        4.79038
                                    6.67741
                                              0.717
                                                       0.4746
## site2:viewcat3
                       -5.13072
                                    5.47571
                                             -0.937
                                                       0.3508
## site3:viewcat3
                       -1.48691
                                    3.89252
                                             -0.382
                                                       0.7032
## site4:viewcat3
                       -5.03691
                                    4.41217
                                             -1.142
                                                       0.2561
## site5:viewcat3
                             NA
                                         NA
                                                  NA
                                                           NA
                       -3.19663
                                             -0.575
                                                       0.5666
## site2:viewcat4
                                    5.56136
## site3:viewcat4
                       -0.93894
                                    4.08126
                                             -0.230
                                                       0.8185
## site4:viewcat4
                                             -1.162
                       -5.99748
                                    5.15990
                                                       0.2476
## site5:viewcat4
                       -0.21046
                                    7.04760
                                             -0.030
                                                       0.9762
## site2:setting2
                       -1.36444
                                    2.93524
                                             -0.465
                                                       0.6429
## site3:setting2
                       -1.30832
                                    3.36176
                                             -0.389
                                                       0.6979
                                    3.45430
## site4:setting2
                       -4.68028
                                             -1.355
                                                       0.1782
## site5:setting2
                             NA
                                         NA
                                                 NA
                                                           NA
## site2:viewenc2
                       -2.65415
                                    2.76572
                                             -0.960
                                                       0.3393
## site3:viewenc2
                        0.03940
                                    3.50901
                                              0.011
                                                       0.9911
## site4:viewenc2
                                             -0.019
                                                       0.9853
                       -0.05966
                                    3.22042
## site5:viewenc2
                        7.97522
                                    7.53058
                                              1.059
                                                       0.2919
                                                       0.2538
## sex2:age
                        0.15410
                                    0.13435
                                              1.147
## sex2:viewcat2
                        2.86176
                                    2.81308
                                              1.017
                                                       0.3112
## sex2:viewcat3
                       -0.20025
                                    2.66573
                                             -0.075
                                                       0.9403
## sex2:viewcat4
                       -0.45238
                                    2.84818
                                             -0.159
                                                       0.8741
## sex2:setting2
                       -1.93840
                                    1.80878
                                             -1.072
                                                       0.2862
                                              1.545
## sex2:viewenc2
                        3.18303
                                    2.05987
                                                       0.1251
## age:viewcat2
                        0.38696
                                    0.27796
                                              1.392
                                                       0.1666
## age:viewcat3
                        0.14608
                                    0.25116
                                              0.582
                                                       0.5620
## age:viewcat4
                        0.01779
                                    0.27664
                                              0.064
                                                       0.9488
```

```
## age:setting2
                    0.01359
                                0.16348
                                         0.083
                                                  0.9339
                                0.19248 0.108
                      0.02087
                                                  0.9139
## age:viewenc2
## viewcat2:setting2 2.59739
                                3.51606 0.739 0.4616
## viewcat3:setting2 4.02713
                                3.40364
                                         1.183
                                                  0.2392
## viewcat4:setting2 -0.78643
                                3.74673 -0.210
                                                  0.8341
## viewcat2:viewenc2 -3.47489 3.76341 -0.923
                                                  0.3578
## viewcat3:viewenc2 -1.80040 3.55159 -0.507
                                                  0.6132
## viewcat4:viewenc2 1.81492
                                3.84842
                                         0.472
                                                  0.6381
## setting2:viewenc2
                    4.70866
                                2.46403
                                         1.911
                                                  0.0586 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.488 on 112 degrees of freedom
## Multiple R-squared: 0.5727, Adjusted R-squared: 0.3628
## F-statistic: 2.729 on 55 and 112 DF, p-value: 3.56e-06
AIC(lin.mod2.full)
## [1] 1027.083
yhat <- predict(lin.mod2.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod2.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "letDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 24.44647
lin.mod3.full <- lm(formDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod3.full)
##
## Call:
## lm(formula = formDiff ~ (site + sex + age + viewcat + setting +
##
      viewenc)^2, data = training)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -8.9228 -1.8652 -0.0169 1.8737 12.7649
## Coefficients: (2 not defined because of singularities)
                      Estimate Std. Error t value Pr(>|t|)
                     29.944763 14.480042
## (Intercept)
                                          2.068
                                                   0.0409 *
## site2
                    12.327359 13.575252
                                          0.908
                                                   0.3658
## site3
                    -1.058753
                               9.036594 -0.117
                                                   0.9069
## site4
                     4.392580 16.316566 0.269
                                                  0.7883
                     4.356217 17.222238 0.253 0.8008
## site5
```

	sex2	3.675853	6.725528	0.547	0.5858
	age	-0.296259	0.264860	-1.119	0.2657
	viewcat2	-24.508158	14.626151	-1.676	0.0966 .
	viewcat3	-15.832596	13.221492	-1.197	0.2336
	viewcat4	-2.141958	14.385978	-0.149	0.8819
##	setting2	7.516078	9.018414	0.833	0.4064
	viewenc2	-15.197856	10.098523	-1.505	0.1351
##	site2:sex2	-3.772624	2.202334	-1.713	0.0895 .
##	site3:sex2	-4.100876	2.146588	-1.910	0.0586 .
##	site4:sex2	-5.714483	2.606577	-2.192	0.0304 *
##	site5:sex2	-4.513182	3.676472	-1.228	0.2222
##	site2:age	-0.271127	0.237788	-1.140	0.2566
##	site3:age	0.001186	0.169630	0.007	0.9944
##	site4:age	-0.031048	0.302804	-0.103	0.9185
##	site5:age	-0.082011	0.333365	-0.246	0.8061
##	site2:viewcat2	6.777720	5.448230	1.244	0.2161
##	site3:viewcat2	6.728359	3.845840	1.750	0.0829 .
##	site4:viewcat2	5.866619	3.860003	1.520	0.1314
##	site5:viewcat2	7.030391	6.220350	1.130	0.2608
##	site2:viewcat3	2.122722	5.100911	0.416	0.6781
##	site3:viewcat3	4.363483	3.626088	1.203	0.2314
##	site4:viewcat3	0.418813	4.110165	0.102	0.9190
##	site5:viewcat3	NA	NA	NA	NA
##	site2:viewcat4	1.747657	5.180694	0.337	0.7365
##	site3:viewcat4	5.788361	3.801908	1.522	0.1307
##	site4:viewcat4	-0.137820	4.806713	-0.029	0.9772
##	site5:viewcat4	1.851415	6.565206	0.282	0.7785
##	site2:setting2	1.586718	2.734325	0.580	0.5629
##	site3:setting2	-6.267179	3.131653	-2.001	0.0478 *
##	site4:setting2	1.393469	3.217863	0.433	0.6658
##	site5:setting2	NA	NA	NA	NA
##	site2:viewenc2	-0.253451	2.576413	-0.098	0.9218
##	site3:viewenc2	4.996265	3.268825	1.528	0.1292
##	site4:viewenc2	-4.076868	2.999986	-1.359	0.1769
##	site5:viewenc2	0.542663	7.015121	0.077	0.9385
##	sex2:age	0.040381	0.125154	0.323	0.7476
##	sex2:viewcat2	-2.039436	2.620528	-0.778	0.4381
##	sex2:viewcat3	0.317803	2.483262	0.128	0.8984
##	sex2:viewcat4	-0.544298	2.653230	-0.205	0.8378
##	sex2:setting2	-2.642309	1.684970	-1.568	0.1197
##	sex2:viewenc2	-2.157924	1.918879	-1.125	0.2632
##	age:viewcat2	0.364615	0.258937	1.408	0.1619
##	age:viewcat3	0.253258	0.233965	1.082	0.2814
##	age:viewcat4	0.017013	0.257708	0.066	0.9475
##	age:setting2	-0.094395	0.152294	-0.620	0.5366
	age:viewenc2	0.288927	0.179305	1.611	0.1099
	viewcat2:setting2	0.045540	3.275387	0.014	0.9889
	viewcat3:setting2	-0.916800	3.170671	-0.289	0.7730
	viewcat4:setting2	2.713885	3.490273	0.778	0.4385
	viewcat2:viewenc2	7.112277	3.505815	2.029	0.0449 *
	viewcat3:viewenc2	2.220835	3.308488	0.671	0.5034
	viewcat4:viewenc2	0.718803	3.585006	0.201	0.8415
	setting2:viewenc2	-1.590335	2.295369	-0.693	0.4898
		_ : = 0 0 0 0 0	5 0 0 0		
					

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.18 on 112 degrees of freedom
## Multiple R-squared: 0.3905, Adjusted R-squared: 0.09115
## F-statistic: 1.305 on 55 and 112 DF, p-value: 0.1189
AIC(lin.mod3.full)
## [1] 1003.259
yhat <- predict(lin.mod3.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod3.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "formDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 23.18844
lin.mod4.full <- lm(numbDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod4.full)
##
## Call:
## lm(formula = numbDiff ~ (site + sex + age + viewcat + setting +
      viewenc)^2, data = training)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   ЗQ
                                           Max
## -14.9731 -2.2530 -0.0413
                               2.4864
                                         9.4788
##
## Coefficients: (2 not defined because of singularities)
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     16.70541
                                15.13888
                                          1.103
                                                   0.2722
## site2
                     15.96399
                                14.19292
                                          1.125
                                                   0.2631
## site3
                      6.64629
                                 9.44776
                                          0.703
                                                   0.4832
                                 17.05897 -0.275
## site4
                     -4.69062
                                                   0.7838
                                18.00585
## site5
                      1.27560
                                           0.071
                                                   0.9436
## sex2
                     9.80788
                                 7.03154
                                          1.395
                                                   0.1658
                                 0.27691 -0.318
                                                   0.7513
## age
                     -0.08799
## viewcat2
                    -12.34222
                                15.29164 -0.807
                                                   0.4213
## viewcat3
                                13.82307 -0.808
                                                   0.4206
                    -11.17277
## viewcat4
                      3.28623
                                15.04054
                                          0.218
                                                   0.8274
                                          1.840
## setting2
                     17.35032
                                 9.42875
                                                   0.0684 .
## viewenc2
                     -7.37000
                                10.55800 -0.698
                                                   0.4866
## site2:sex2
                     -3.34924
                                 2.30254 -1.455
                                                   0.1486
## site3:sex2
                     -2.90207
                                 2.24426 -1.293
                                                   0.1986
## site4:sex2
                     -3.42395
                                 2.72518 -1.256
                                                  0.2116
```

```
## site5:sex2
                      -0.25383
                                   3.84375 -0.066
                                                     0.9475
## site2:age
                      -0.06976
                                   0.24861 -0.281
                                                     0.7795
## site3:age
                      -0.05208
                                   0.17735
                                           -0.294
                                                     0.7696
## site4:age
                                   0.31658
                                            0.858
                                                     0.3927
                       0.27163
## site5:age
                       0.05536
                                  0.34853
                                             0.159
                                                     0.8741
## site2:viewcat2
                      -6.50669
                                  5.69612
                                           -1.142
                                                     0.2558
                                           -0.465
## site3:viewcat2
                      -1.86918
                                   4.02083
                                                     0.6429
## site4:viewcat2
                      -4.52539
                                   4.03563
                                           -1.121
                                                     0.2645
## site5:viewcat2
                      -0.06176
                                   6.50337
                                           -0.009
                                                     0.9924
## site2:viewcat3
                      -6.54853
                                   5.33300
                                          -1.228
                                                     0.2220
## site3:viewcat3
                      0.37710
                                   3.79107
                                            0.099
                                                     0.9209
                                           -0.652
## site4:viewcat3
                      -2.80346
                                   4.29718
                                                     0.5155
## site5:viewcat3
                                                NA
                            NA
                                        NA
                                                         NA
## site2:viewcat4
                     -10.05730
                                   5.41641
                                            -1.857
                                                     0.0660
## site3:viewcat4
                                   3.97489
                      0.44685
                                             0.112
                                                     0.9107
## site4:viewcat4
                      -6.50503
                                   5.02542
                                            -1.294
                                                     0.1982
## site5:viewcat4
                      -5.38827
                                   6.86392
                                           -0.785
                                                     0.4341
## site2:setting2
                      -2.14597
                                   2.85874
                                           -0.751
                                                     0.4544
                                           -1.454
                                                     0.1488
## site3:setting2
                      -4.76023
                                   3.27414
## site4:setting2
                      -7.31658
                                   3.36428
                                            -2.175
                                                     0.0317 *
## site5:setting2
                            NA
                                        NA
                                                NA
                                                         NA
## site2:viewenc2
                      -2.72744
                                   2.69364
                                            -1.013
                                                     0.3135
## site3:viewenc2
                                            -0.397
                      -1.35549
                                   3.41756
                                                     0.6924
## site4:viewenc2
                      -1.50418
                                            -0.480
                                   3.13649
                                                     0.6325
## site5:viewenc2
                      6.83681
                                  7.33431
                                            0.932
                                                     0.3533
## sex2:age
                      -0.16226
                                  0.13085
                                           -1.240
                                                     0.2176
## sex2:viewcat2
                                             0.808
                                                     0.4208
                       2.21351
                                   2.73976
## sex2:viewcat3
                       2.04053
                                   2.59625
                                             0.786
                                                     0.4336
## sex2:viewcat4
                      -0.65653
                                  2.77395
                                           -0.237
                                                     0.8133
## sex2:setting2
                      -0.04353
                                            -0.025
                                                     0.9803
                                   1.76164
## sex2:viewenc2
                       1.03717
                                   2.00619
                                             0.517
                                                     0.6062
## age:viewcat2
                       0.29579
                                   0.27072
                                             1.093
                                                     0.2769
## age:viewcat3
                       0.28309
                                   0.24461
                                             1.157
                                                     0.2496
                                             0.312
## age:viewcat4
                                   0.26943
                                                     0.7552
                       0.08420
## age:setting2
                      -0.22758
                                  0.15922
                                            -1.429
                                                     0.1557
## age:viewenc2
                       0.12555
                                  0.18746
                                             0.670
                                                     0.5044
## viewcat2:setting2
                      -2.23219
                                   3.42442
                                           -0.652
                                                     0.5158
## viewcat3:setting2
                     -0.89840
                                   3.31494
                                            -0.271
                                                     0.7869
## viewcat4:setting2 -1.33874
                                            -0.367
                                                     0.7144
                                   3.64908
## viewcat2:viewenc2
                       3.29199
                                   3.66533
                                             0.898
                                                     0.3710
                                             0.318
## viewcat3:viewenc2
                       1.09871
                                   3.45902
                                                     0.7514
## viewcat4:viewenc2
                       2.49482
                                             0.666
                                                     0.5070
                                   3.74812
## setting2:viewenc2
                       0.59013
                                   2.39981
                                             0.246
                                                     0.8062
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.371 on 112 degrees of freedom
## Multiple R-squared: 0.3558, Adjusted R-squared: 0.03945
## F-statistic: 1.125 on 55 and 112 DF, p-value: 0.2971
```

AIC(lin.mod4.full)

[1] 1018.209

```
yhat <- predict(lin.mod4.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod4.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "numbDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 28.23554
lin.mod5.full <- lm(relatDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)</pre>
summary(lin.mod5.full)
##
## Call:
  lm(formula = relatDiff ~ (site + sex + age + viewcat + setting +
##
       viewenc)^2, data = training)
##
## Residuals:
##
        Min
                  10
                       Median
                                     30
                                             Max
## -10.1381 -2.1057 -0.0037
                                 1.9658 11.4625
## Coefficients: (2 not defined because of singularities)
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      17.06032
                                  14.42797
                                             1.182
                                                      0.2395
## site2
                      -4.32400
                                  13.52644 -0.320
                                                      0.7498
## site3
                       0.09709
                                   9.00410
                                             0.011
                                                      0.9914
## site4
                       8.82232
                                             0.543
                                                     0.5885
                                  16.25789
## site5
                      10.23066
                                  17.16031
                                             0.596
                                                      0.5523
                                             1.649
## sex2
                      11.05162
                                   6.70134
                                                     0.1019
                      -0.19817
                                   0.26391
                                           -0.751
                                                      0.4543
## age
## viewcat2
                     -12.06564
                                  14.57356
                                            -0.828
                                                      0.4095
## viewcat3
                      -1.76765
                                  13.17395
                                            -0.134
                                                      0.8935
## viewcat4
                      12.95777
                                  14.33425
                                             0.904
                                                      0.3679
                                             0.611
## setting2
                       5.49314
                                  8.98598
                                                      0.5422
## viewenc2
                       1.41758
                                  10.06221
                                             0.141
                                                      0.8882
                      -2.89712
## site2:sex2
                                   2.19441
                                           -1.320
                                                      0.1895
## site3:sex2
                      -1.50609
                                   2.13887
                                            -0.704
                                                      0.4828
## site4:sex2
                      -5.48305
                                   2.59720
                                            -2.111
                                                      0.0370 *
## site5:sex2
                      -2.72621
                                            -0.744
                                                      0.4583
                                   3.66325
                                             0.619
## site2:age
                       0.14657
                                   0.23693
                                                      0.5374
                                             0.553
## site3:age
                       0.09339
                                   0.16902
                                                      0.5817
                                   0.30171
                                             0.383
## site4:age
                       0.11553
                                                      0.7025
                                   0.33217 -0.380
## site5:age
                       -0.12613
                                                      0.7049
## site2:viewcat2
                                   5.42864
                                             0.257
                                                      0.7979
                       1.39325
## site3:viewcat2
                       0.58876
                                   3.83201
                                             0.154
                                                      0.8782
                                           -0.886
                                                      0.3773
## site4:viewcat2
                      -3.40928
                                   3.84612
## site5:viewcat2
                      -0.56097
                                   6.19798
                                            -0.091
                                                      0.9280
```

5.08257

site2:viewcat3

-0.72033

-0.142

0.8876

```
## site3:viewcat3
                     -0.90613
                                 3.61305 -0.251
                                                   0.8024
## site4:viewcat3
                     -7.73848
                                 4.09539
                                          -1.890
                                                   0.0614 .
## site5:viewcat3
                           NΑ
                                      NΑ
                                              NA
                                                       NΑ
## site2:viewcat4
                     -3.95053
                                 5.16206
                                          -0.765
                                                   0.4457
## site3:viewcat4
                     -1.08877
                                 3.78824
                                          -0.287
                                                   0.7743
## site4:viewcat4
                                 4.78943 -0.798
                     -3.82113
                                                   0.4267
                                 6.54160 -0.192
## site5:viewcat4
                    -1.25414
                                                   0.8483
## site2:setting2
                    -0.87824
                                 2.72449 -0.322
                                                   0.7478
## site3:setting2
                     -3.25960
                                 3.12039
                                          -1.045
                                                   0.2985
                                 3.20629 -2.095
## site4:setting2
                     -6.71576
                                                   0.0385 *
## site5:setting2
                           NA
                                      NA
                                              NA
                                                       NA
## site2:viewenc2
                      0.09165
                                 2.56715
                                           0.036
                                                   0.9716
## site3:viewenc2
                      0.08926
                                 3.25707
                                           0.027
                                                   0.9782
                                 2.98920 -1.899
## site4:viewenc2
                     -5.67745
                                                   0.0601 .
## site5:viewenc2
                                 6.98990 -0.226
                                                   0.8215
                     -1.58031
## sex2:age
                     -0.10161
                                 0.12470
                                          -0.815
                                                   0.4169
## sex2:viewcat2
                     -0.32485
                                 2.61110 -0.124
                                                   0.9012
## sex2:viewcat3
                     -0.81092
                                 2.47433 -0.328
                                                   0.7437
## sex2:viewcat4
                                 2.64369 -1.043
                                                   0.2992
                     -2.75732
## sex2:setting2
                     -3.19781
                                 1.67891 -1.905
                                                   0.0594
## sex2:viewenc2
                     -0.94590
                                 1.91198 -0.495
                                                   0.6218
## age:viewcat2
                      0.29068
                                 0.25801
                                          1.127
                                                   0.2623
## age:viewcat3
                                          0.407
                                                   0.6846
                      0.09494
                                 0.23312
## age:viewcat4
                                 0.25678 - 0.463
                                                   0.6443
                     -0.11889
## age:setting2
                     -0.01405
                                 0.15175 -0.093
                                                   0.9264
## age:viewenc2
                      0.06598
                                 0.17866
                                          0.369
                                                   0.7126
## viewcat2:setting2 -2.52471
                                 3.26361 -0.774
                                                   0.4408
## viewcat3:setting2 -0.09666
                                 3.15927 -0.031
                                                   0.9756
## viewcat4:setting2
                      2.70973
                                 3.47772
                                          0.779
                                                   0.4375
## viewcat2:viewenc2 -2.40402
                                 3.49321 -0.688
                                                   0.4928
## viewcat3:viewenc2 -1.85347
                                 3.29659
                                          -0.562
                                                   0.5751
## viewcat4:viewenc2 -2.73805
                                 3.57212 -0.767
                                                   0.4450
## setting2:viewenc2 -3.01217
                                 2.28711 -1.317
                                                   0.1905
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.165 on 112 degrees of freedom
## Multiple R-squared: 0.4263, Adjusted R-squared: 0.1446
## F-statistic: 1.513 on 55 and 112 DF, p-value: 0.03312
AIC(lin.mod5.full)
## [1] 1002.049
yhat <- predict(lin.mod5.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod5.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "relatDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
```

[1] 23.63526

```
summary(lin.mod6.full)
##
## Call:
## lm(formula = clasfDiff ~ (site + sex + age + viewcat + setting +
       viewenc)^2, data = training)
##
## Residuals:
##
        Min
                   1Q
                        Median
                                      3Q
                                              Max
## -11.6108 -3.1873
                        0.0668
                                 3.0854
                                         10.7635
##
## Coefficients: (2 not defined because of singularities)
##
                       Estimate Std. Error t value Pr(>|t|)
                       31.86932
                                  20.13470
                                              1.583
## (Intercept)
                                                      0.1163
## site2
                        5.71113
                                  18.87658
                                              0.303
                                                      0.7628
## site3
                      -11.78957
                                  12.56551
                                            -0.938
                                                      0.3501
## site4
                                            -1.571
                      -35.64786
                                  22.68842
                                                      0.1190
## site5
                      -56.84008
                                  23.94777
                                            -2.374
                                                      0.0193 *
## sex2
                      16.72781
                                   9.35194
                                              1.789
                                                      0.0764
                      -0.37531
                                   0.36829
                                            -1.019
                                                      0.3104
## age
## viewcat2
                      -33.62976
                                  20.33787
                                             -1.654
                                                      0.1010
                                            -1.849
## viewcat3
                      -33.98623
                                  18.38467
                                                      0.0672
## viewcat4
                      -12.80847
                                  20.00391
                                            -0.640
                                                      0.5233
## setting2
                      25.39476
                                  12.54023
                                              2.025
                                                      0.0452 *
## viewenc2
                       -9.74311
                                  14.04214
                                             -0.694
                                                      0.4892
## site2:sex2
                       -0.52039
                                   3.06238
                                            -0.170
                                                      0.8654
## site3:sex2
                       2.53032
                                   2.98486
                                              0.848
                                                      0.3984
## site4:sex2
                                            -0.930
                                                      0.3543
                       -3.37095
                                   3.62448
## site5:sex2
                                             -0.953
                       -4.87172
                                   5.11219
                                                      0.3427
## site2:age
                                   0.33065
                                              0.248
                                                      0.8045
                        0.08205
                                   0.23587
                                              0.692
                                                      0.4904
## site3:age
                        0.16320
                                              1.907
## site4:age
                        0.80312
                                   0.42105
                                                      0.0590
## site5:age
                        1.15008
                                   0.46355
                                              2.481
                                                      0.0146 *
                                            -0.387
                                                      0.6996
## site2:viewcat2
                       -2.93114
                                   7.57584
## site3:viewcat2
                        5.06294
                                   5.34770
                                              0.947
                                                      0.3458
## site4:viewcat2
                        3.68884
                                   5.36739
                                              0.687
                                                      0.4933
## site5:viewcat2
                                   8.64949
                                              0.646
                                                      0.5197
                        5.58665
## site2:viewcat3
                       -8.51958
                                   7.09289
                                            -1.201
                                                      0.2322
## site3:viewcat3
                        0.53577
                                   5.04213
                                              0.106
                                                      0.9156
## site4:viewcat3
                        1.94832
                                   5.71524
                                              0.341
                                                      0.7338
## site5:viewcat3
                             NA
                                        NA
                                                 NA
                                                          NA
## site2:viewcat4
                      -11.97418
                                   7.20383
                                             -1.662
                                                      0.0993
                                   5.28661
                                              1.262
## site3:viewcat4
                        6.67420
                                                      0.2094
## site4:viewcat4
                       -7.87519
                                   6.68380
                                             -1.178
                                                      0.2412
## site5:viewcat4
                                            -0.271
                      -2.47008
                                   9.12901
                                                      0.7872
                                              0.969
## site2:setting2
                        3.68492
                                   3.80212
                                                      0.3345
                                             -1.500
## site3:setting2
                       -6.53049
                                   4.35461
                                                      0.1365
                       -3.60393
                                   4.47448
                                             -0.805
                                                      0.4223
## site4:setting2
## site5:setting2
                                        NA
                             NA
                                                 NA
                                                          NA
                       -3.02265
                                   3.58254
                                             -0.844
                                                      0.4006
## site2:viewenc2
## site3:viewenc2
                        3.51672
                                   4.54535
                                              0.774
                                                      0.4407
```

lin.mod6.full <- lm(clasfDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)

```
## site4:viewenc2
                    1.12474
                                4.17152
                                          0.270
                                                  0.7879
                                         1.231
## site5:viewenc2
                                                  0.2209
                    12.00787
                                9.75463
                                                  0.1046
## sex2:age
                     -0.28474
                                0.17403 -1.636
## sex2:viewcat2
                                3.64388
                                         0.434
                                                  0.6651
                     1.58139
## sex2:viewcat3
                     1.22311
                                3.45301
                                         0.354
                                                  0.7238
## sex2:viewcat4
                                3.68935 -0.835
                     -3.07878
                                                  0.4058
## sex2:setting2
                                2.34297 -1.563
                                                  0.1210
                     -3.66101
## sex2:viewenc2
                     1.89995
                                2.66823
                                         0.712
                                                  0.4779
                      0.59861
## age:viewcat2
                                0.36006
                                         1.663
                                                  0.0992 .
## age:viewcat3
                     0.67510
                                0.32533
                                         2.075
                                                  0.0403 *
## age:viewcat4
                     0.32333
                                0.35835
                                          0.902
                                                  0.3688
## age:setting2
                                0.21177 - 1.527
                                                  0.1297
                     -0.32330
## age:viewenc2
                     -0.03592
                                0.24933 -0.144
                                                  0.8857
## viewcat2:setting2 -9.02471
                                4.55447 -1.982
                                                  0.0500 *
## viewcat3:setting2 -7.57750
                                4.40886 -1.719
                                                  0.0884 .
## viewcat4:setting2 -1.82366
                                4.85327 -0.376
                                                  0.7078
                                         2.169
                                                  0.0322 *
## viewcat2:viewenc2 10.57132
                                4.87489
## viewcat3:viewenc2 11.25111
                                4.60050
                                         2.446
                                                  0.0160 *
## viewcat4:viewenc2
                                4.98500
                                          1.391
                                                  0.1668
                    6.93655
## setting2:viewenc2
                    1.22748
                                3.19174
                                          0.385
                                                  0.7013
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 5.813 on 112 degrees of freedom
## Multiple R-squared: 0.4256, Adjusted R-squared: 0.1436
## F-statistic: 1.509 on 55 and 112 DF, p-value: 0.03404
AIC(lin.mod6.full)
## [1] 1114.029
yhat <- predict(lin.mod6.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod6.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "clasfDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
```

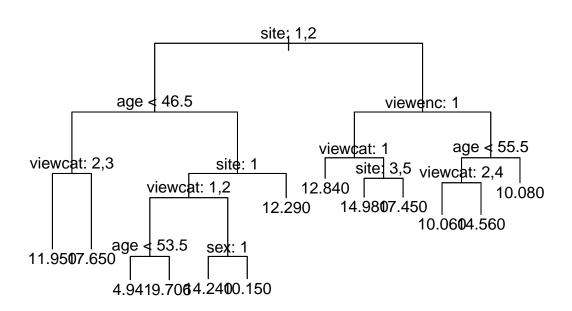
[1] 65.41

Regression Tree Models

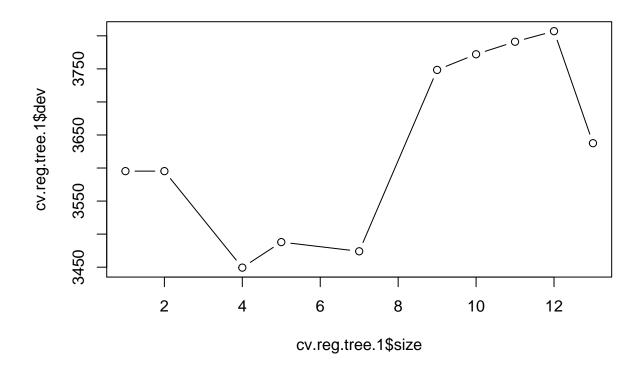
In the context of a regression tree, the deviance is simply the sum of the squared errors.

Model 1

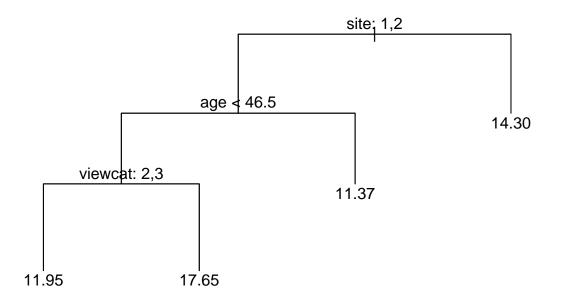
```
set.seed(1)
reg.tree.1 <- tree(bodyDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.1)
##
## Regression tree:
## tree(formula = bodyDiff ~ site + sex + age + viewcat + setting +
      viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "site"
                "age"
                          "viewcat" "sex"
                                            "viewenc"
## Number of terminal nodes: 13
## Residual mean deviance: 14.16 = 2194 / 155
## Distribution of residuals:
       Min. 1st Qu.
                        Median
                                     Mean
                                            3rd Qu.
                                                         Max.
## -11.08000 -2.45100 -0.06303 0.00000
                                            2.16900 12.55000
plot(reg.tree.1)
text(reg.tree.1, pretty = 0)
```



```
cv.reg.tree.1 <- cv.tree(reg.tree.1)
plot(cv.reg.tree.1$size, cv.reg.tree.1$dev, type = "b")</pre>
```



```
prune.reg.tree.1 <- prune.tree(reg.tree.1, best = 4)
plot(prune.reg.tree.1)
text(prune.reg.tree.1, pretty = 0)</pre>
```



```
yhat <- predict(prune.reg.tree.1, newdata = testing)
y.test <- testing[, "bodyDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

[1] 20.60159

Model 2

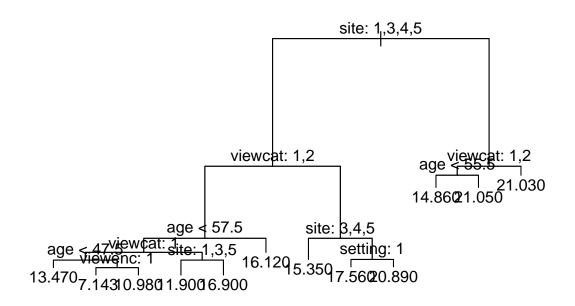
```
set.seed(1)
reg.tree.2 <- tree(letDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train)
summary(reg.tree.2)

##
## Regression tree:
## tree(formula = letDiff ~ site + sex + age + viewcat + setting +
## viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "site" "viewcat" "age" "viewenc" "setting"
## Number of terminal nodes: 12</pre>
```

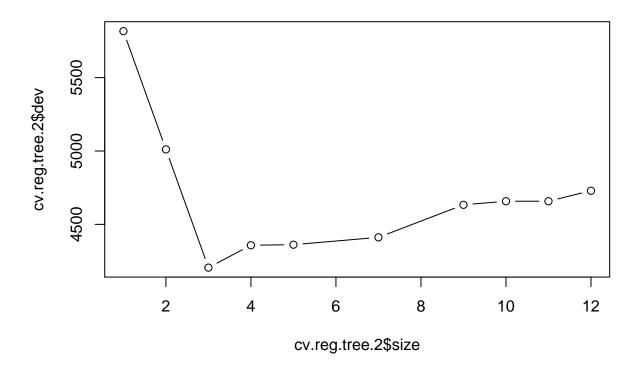
Residual mean deviance: 18.63 = 2906 / 156

```
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -17.560 -2.430 0.000 0.000 2.765 9.587

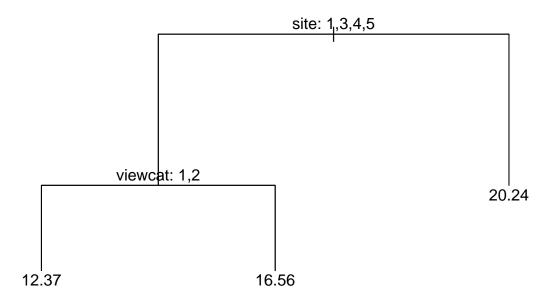
plot(reg.tree.2)
text(reg.tree.2, pretty = 0)
```



```
cv.reg.tree.2 <- cv.tree(reg.tree.2)
plot(cv.reg.tree.2$size, cv.reg.tree.2$dev, type = "b")</pre>
```



```
prune.reg.tree.2 <- prune.tree(reg.tree.2, best = 3)
plot(prune.reg.tree.2)
text(prune.reg.tree.2, pretty = 0)</pre>
```



```
yhat <- predict(prune.reg.tree.2, newdata = testing)
y.test <- testing[, "letDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

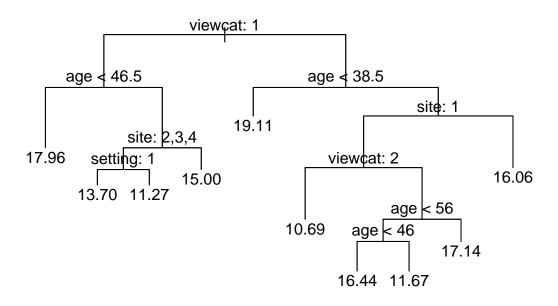
[1] 15.4124

Model 3

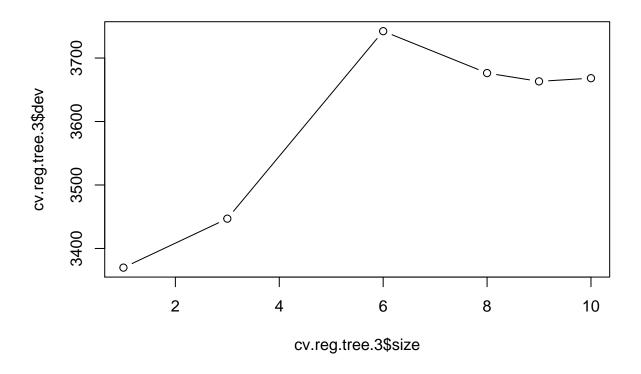
Residual mean deviance: 15.88 = 2509 / 158

```
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -11.610 -1.667 0.129 0.000 2.159 13.940

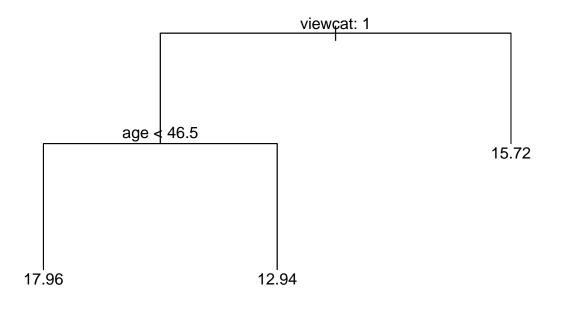
plot(reg.tree.3)
text(reg.tree.3, pretty = 0)
```



```
cv.reg.tree.3 <- cv.tree(reg.tree.3)
plot(cv.reg.tree.3$size, cv.reg.tree.3$dev, type = "b")</pre>
```



```
prune.reg.tree.3 <- prune.tree(reg.tree.3, best = 2)
plot(prune.reg.tree.3)
text(prune.reg.tree.3, pretty = 0)</pre>
```



```
yhat <- predict(prune.reg.tree.3, newdata = testing)
y.test <- testing[, "formDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

[1] 14.92273

-18.0900 -2.1210 0.2647 0.0000

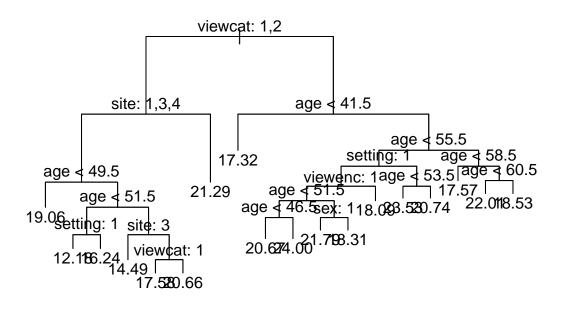
Model 4

```
set.seed(1)
reg.tree.4 <- tree(numbDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.4)

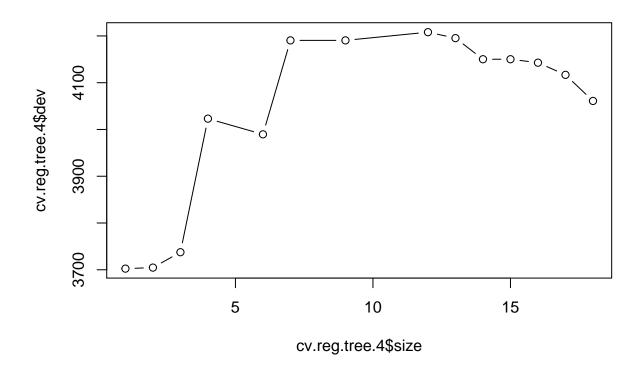
##
## Regression tree:
## tree(formula = numbDiff ~ site + sex + age + viewcat + setting +
## viewenc, data = sesame.q1, subset = train)
## Number of terminal nodes: 18
## Residual mean deviance: 13.64 = 2046 / 150
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.</pre>
```

2.1180 11.4700

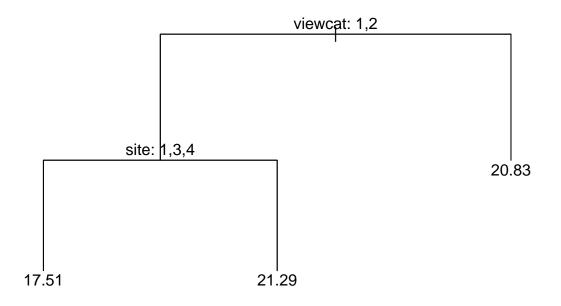
```
plot(reg.tree.4)
text(reg.tree.4, pretty = 0)
```



```
cv.reg.tree.4 <- cv.tree(reg.tree.4)
plot(cv.reg.tree.4$size, cv.reg.tree.4$dev, type = "b")</pre>
```



```
prune.reg.tree.4 <- prune.tree(reg.tree.4, best = 3)
plot(prune.reg.tree.4)
text(prune.reg.tree.4, pretty = 0)</pre>
```



```
yhat <- predict(prune.reg.tree.4, newdata = testing)
y.test <- testing[, "numbDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

Model 5

[1] "age"

[1] 15.90771

```
set.seed(1)
reg.tree.5 <- tree(relatDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = trainsummary(reg.tree.5)
##
## Regression tree:
## tree(formula = relatDiff ~ site + sex + age + viewcat + setting +</pre>
```

"viewcat" "setting" "sex"

viewenc, data = sesame.q1, subset = train)

Variables actually used in tree construction:

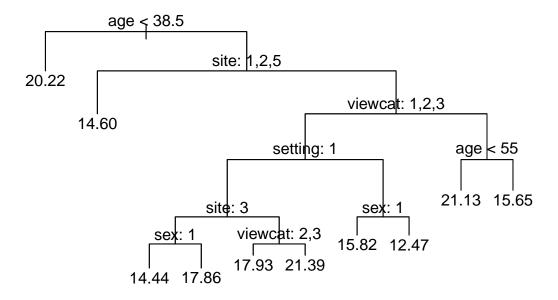
Residual mean deviance: 15.3 = 2418 / 158

"site"

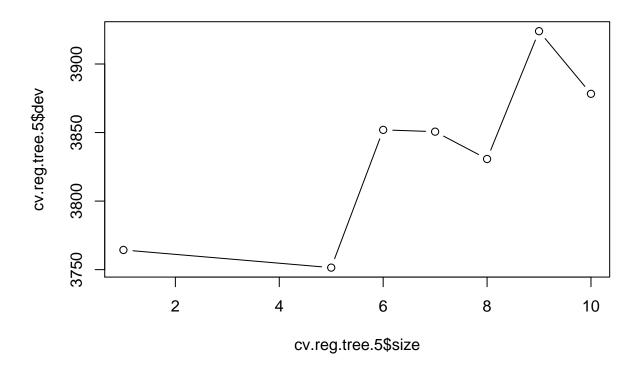
Number of terminal nodes: 10

```
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -10.6900 -1.5650 -0.2514 0.0000 1.8950 11.4900

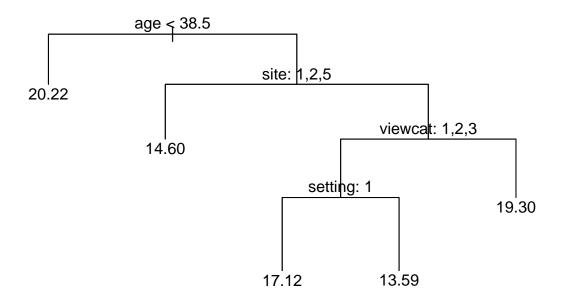
plot(reg.tree.5)
text(reg.tree.5, pretty = 0)
```



```
cv.reg.tree.5 <- cv.tree(reg.tree.5)
plot(cv.reg.tree.5$size, cv.reg.tree.5$dev, type = "b")</pre>
```



```
prune.reg.tree.5 <- prune.tree(reg.tree.5, best = 5)
plot(prune.reg.tree.5)
text(prune.reg.tree.5, pretty = 0)</pre>
```



```
yhat <- predict(prune.reg.tree.5, newdata = testing)
y.test <- testing[, "relatDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

[1] 19.88506

[1] "viewcat" "age"

Number of terminal nodes: 14

Model 6

```
set.seed(1)
reg.tree.6 <- tree(clasfDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.6)

##
## Regression tree:
## tree(formula = clasfDiff ~ site + sex + age + viewcat + setting +
##
## viewenc, data = sesame.q1, subset = train)</pre>
```

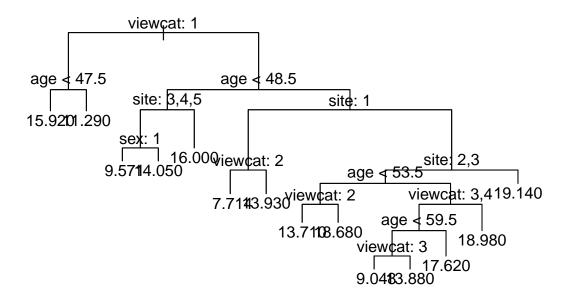
Variables actually used in tree construction:

Residual mean deviance: 29.66 = 4568 / 154

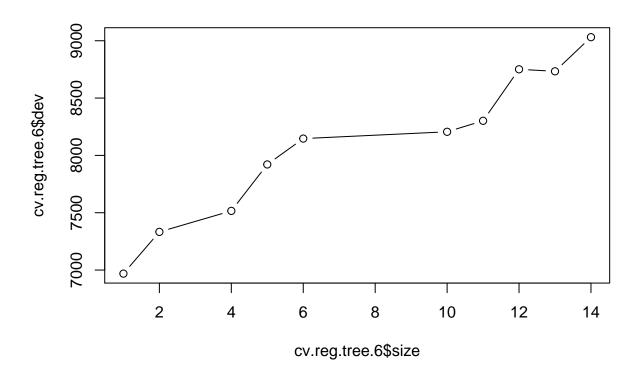
"site"

```
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -16.00000 -3.17300 0.01852 0.00000 3.71400 13.10000

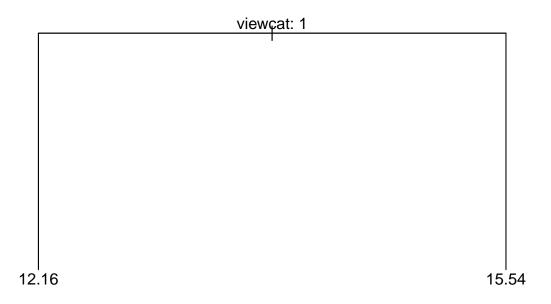
plot(reg.tree.6)
text(reg.tree.6, pretty = 0)
```



```
cv.reg.tree.6 <- cv.tree(reg.tree.6)
plot(cv.reg.tree.6$size, cv.reg.tree.6$dev, type = "b")</pre>
```



```
prune.reg.tree.6 <- prune.tree(reg.tree.6, best = 2)
plot(prune.reg.tree.6)
text(prune.reg.tree.6, pretty = 0)</pre>
```



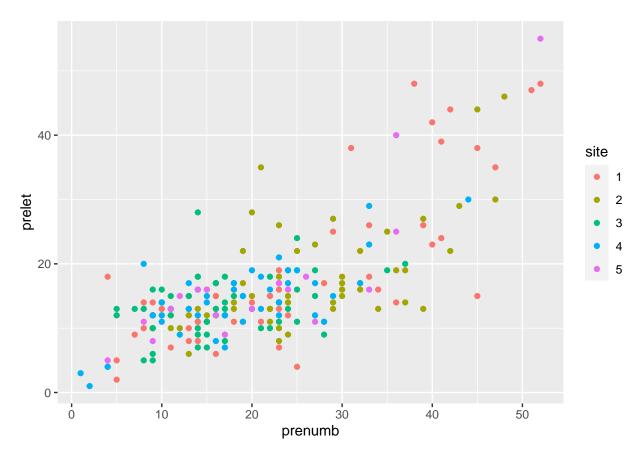
```
yhat <- predict(prune.reg.tree.6, newdata = testing)
y.test <- testing[, "clasfDiff"]

# Test MSE
mean((yhat-y.test)^2)</pre>
```

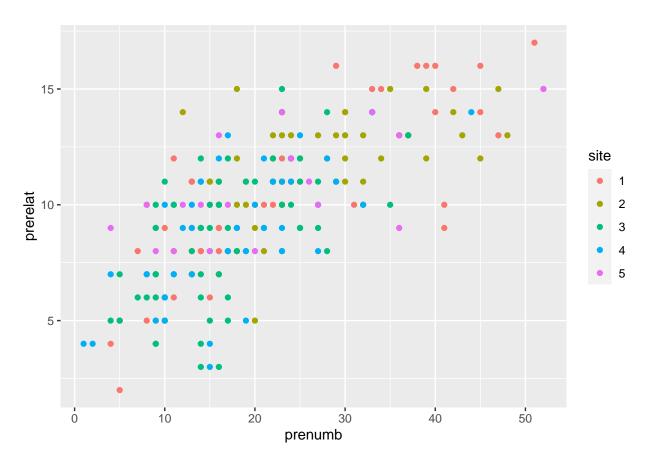
[1] 45.52784

Q.2 Classification Question: Can we use the pre-test scores and other demographic variables to predict which region the children came from?

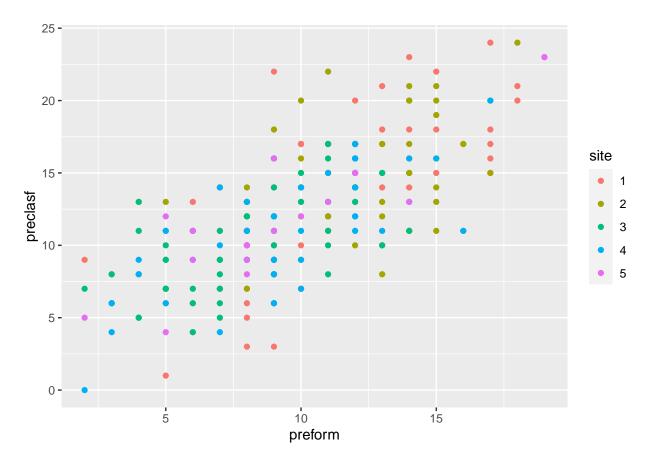
```
ggplot(data=sesame, aes(x=prenumb, y=prelet, color=site))+
  geom_point()
```



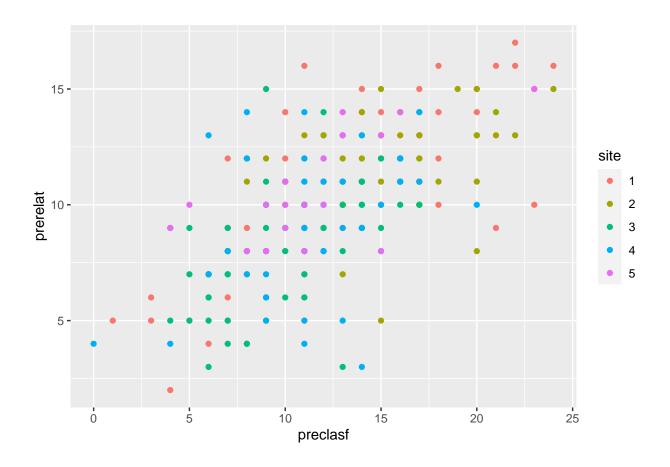
ggplot(data=sesame, aes(x=prenumb, y=prerelat, color=site))+
 geom_point()



ggplot(data=sesame, aes(x=preform, y=preclasf, color=site))+
 geom_point()



```
ggplot(data=sesame, aes(x=preclasf, y=prerelat, color=site))+
geom_point()
```



SVM

```
set.seed(3241)
n <- nrow(sesame)</pre>
train.index <- sample(1:n, size = floor(0.7*n), replace=FALSE)</pre>
train.data <- sesame.sd[train.index,]</pre>
test.data <- sesame.sd[-train.index,]</pre>
train.data %>%
count(site)
##
     site n
## 1
        1 40
## 2
        2 42
## 3
        3 48
        4 25
## 4
        5 13
## 5
#1 60
#2 55
#3 64
#4 43
```

```
#5 18
total.weight <- 60+55+64+43+18
weight.1 <- total.weight/(5*60)</pre>
weight.2 <- total.weight/(5*55)
weight.3 <- total.weight/(5*64)</pre>
weight.4 <- total.weight/(5*43)</pre>
weight.5 \leftarrow total.weight/(5*18)
weight.4 <- 1.5
weight.5 <- 3
# Response: site (categorical)
set.seed(315)
costs \leftarrow c(0.001, 0.01, 0.1, 1, 5, 10, 100)
# c(0.1, 0.2, 0.5, 0.7, 1, 2, 3, 4)
gammas \leftarrow seq(0, 4, by=0.1)
linear.tune <- tune(svm, site~female+ male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_pc
                     data=train.data, kernel="linear",
                     ranges=list(cost=costs),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5),
                     class.type="one.versus.one")
radial.tune <- tune(svm, site~female + male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_p
                     data=train.data, kernel="radial",
                     ranges=list(cost=costs,
                                 gamma=gammas),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5))
#radial.tune <- tune(sum, site~sex+age+prebody+prelet+preform+prenumb+prerelat+preclasf,</pre>
                      data=train.data, kernel="radial",
#
                      ranges=list(cost=costs,
#
                                   gamma=gammas))
sigmoid.tune <- tune(svm, site~female + male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_
                     data=train.data, kernel="sigmoid",
                     ranges=list(cost=costs,
                                 gamma=gammas),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5))
```

```
linear.conMatrix <- table(true=test.data[, "site"],</pre>
                         pred=predict(linear.tune$best.model, newdata=test.data))
radial.conMatrix <- table(true=test.data[, "site"],</pre>
                         pred=predict(radial.tune$best.model, newdata=test.data))
sigmoid.conMatrix <- table(true=test.data[, "site"],</pre>
                         pred=predict(sigmoid.tune$best.model, newdata=test.data))
confusionMatrix(linear.conMatrix)
## Confusion Matrix and Statistics
##
      pred
## true 1 2 3 4 5
##
     1 6 1 6
                 2 5
##
       1 7 1 1 3
##
     3 0 1 11 1 3
##
     4 3 3 9 3 0
##
     5 0 1 1 1 2
##
## Overall Statistics
##
##
                 Accuracy: 0.4028
##
                   95% CI: (0.2888, 0.525)
      No Information Rate: 0.3889
##
##
      P-Value [Acc > NIR] : 0.44844
##
##
                    Kappa: 0.2554
##
## Mcnemar's Test P-Value: 0.01728
## Statistics by Class:
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
##
## Sensitivity
                        0.60000 0.53846 0.3929 0.37500 0.15385
## Specificity
                        0.77419 0.89831 0.8864 0.76562 0.94915
## Pos Pred Value
                        0.30000 0.53846
                                         0.6875 0.16667
                                                          0.40000
## Neg Pred Value
                        0.92308 0.89831
                                          0.6964 0.90741
                                                          0.83582
## Prevalence
                        0.13889 0.18056
                                         0.3889 0.11111
                                                          0.18056
                                         0.1528 0.04167 0.02778
## Detection Rate
                        0.08333 0.09722
## Detection Prevalence 0.27778 0.18056
                                         0.2222 0.25000 0.06944
                        0.68710 0.71838
## Balanced Accuracy
                                         0.6396 0.57031 0.55150
confusionMatrix(radial.conMatrix)
## Confusion Matrix and Statistics
##
##
      pred
## true 1 2 3 4 5
     1 6 2 7 4 1
##
##
     2 4 4 3 0 2
```

##

3 1 1 11 3 0

```
##
     5 0 2 1 1 1
##
## Overall Statistics
##
##
                 Accuracy: 0.3611
##
                   95% CI: (0.2512, 0.4829)
      No Information Rate: 0.4306
##
##
      P-Value [Acc > NIR] : 0.9056
##
##
                    Kappa : 0.181
##
  Mcnemar's Test P-Value: 0.1807
##
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.46154 0.36364
                                         0.3548 0.33333 0.20000
## Specificity
                        0.76271 0.85246
                                          0.8780 0.76667
                                                           0.94030
## Pos Pred Value
                        0.30000 0.30769
                                          0.6875
                                                  0.22222
                                                           0.20000
## Neg Pred Value
                        0.86538 0.88136
                                          0.6429
                                                  0.85185
                                                           0.94030
## Prevalence
                        0.18056 0.15278
                                          0.4306
                                                  0.16667
                                                           0.06944
## Detection Rate
                        0.08333 0.05556
                                          0.1528
                                                  0.05556
                                                           0.01389
## Detection Prevalence 0.27778 0.18056
                                          0.2222 0.25000
                                                           0.06944
## Balanced Accuracy
                        0.61213 0.60805
                                           0.6164 0.55000 0.57015
confusionMatrix(sigmoid.conMatrix)
## Confusion Matrix and Statistics
##
##
      pred
##
  true 1 2
              3
                 4
                    5
##
     1
       1
          1 6 9 3
##
     2 1 3 4 5 0
     3 1 0 4 11 0
##
##
     4
       0
          0
              7 11
##
     5 0 0
              3 2 0
## Overall Statistics
##
##
                 Accuracy: 0.2639
##
                   95% CI: (0.167, 0.381)
##
      No Information Rate: 0.5278
      P-Value [Acc > NIR] : 1
##
##
##
                    Kappa: 0.0434
##
  Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.33333 0.75000 0.16667
                                                   0.2895 0.00000
## Specificity
                        0.72464 0.85294 0.75000 0.7941 0.92754
```

##

4 2 2 9 4 1

```
## Pos Pred Value
                         0.05000 0.23077
                                           0.25000
                                                     0.6111
                                                             0.00000
                         0.96154 0.98305
                                           0.64286
                                                     0.5000
                                                             0.95522
## Neg Pred Value
                                                     0.5278
## Prevalence
                         0.04167 0.05556
                                           0.33333
                                                             0.04167
## Detection Rate
                         0.01389
                                  0.04167
                                           0.05556
                                                     0.1528
                                                             0.00000
## Detection Prevalence
                         0.27778
                                 0.18056
                                           0.22222
                                                     0.2500
                                                             0.06944
                         0.52899
                                 0.80147
                                                     0.5418
## Balanced Accuracy
                                           0.45833
                                                             0.46377
```

predict(linear.tune\$best.model, newdata=test.data)

```
59
##
                       12
                            16
                                19
                                     22
                                         24
                                              25
                                                   29
                                                       38
                                                            42
                                                                 43
                                                                     46
                                                                          48
                                                                               54
                                                                                   56
                                                                                        57
##
     1
                   1
                        5
                             1
                                 1
                                      2
                                           5
                                               5
                                                    5
                                                         3
                                                             1
                                                                  4
                                                                       3
                                                                           3
                                                                                3
                                                                                    5
                                                                                              3
               1
##
    64
         82
             84
                  88
                       92
                            93
                                94
                                     98
                                         99 100 104 106 113 116 118 120 125 127 128 137
                             2
                                           5
     5
          1
               4
                   2
                        2
                                 2
                                      2
                                                    5
                                                                       3
                                                                           3
                                                                                3
                                                                                    5
##
                                               3
                                                         2
                                                             2
                                                                  4
                                                                                         3
   139 143 145 152 156 162 164 172 176 180 181 182 183 187 188 189 190 191 192 193
          2
                                           5
                                                                  2
                                                                       3
                                                                           3
                                                                                    3
##
     3
               3
                   3
                        5
                             3
                                 3
                                      3
                                               3
                                                    3
                                                         4
                                                             1
                                                                                4
                                                                                         3
## 196 202 207 208 212 221 222 225 226 227 234 235
                                           3
          2
               3
                   3
                        4
                             3
                                 1
                                      5
     1
## Levels: 1 2 3 4 5
```

predict(radial.tune\$best.model, newdata=test.data)

```
##
     6
              8
                      12
                           16
                               19
                                    22
                                        24
                                             25
                                                 29
                                                      38
                                                          42
                                                               43
                                                                    46
                                                                        48
                                                                             54
                                                                                 56
                                                                                      57
##
     3
          3
                   1
                       2
                            4
                                 4
                                     4
                                          3
                                              3
                                                   3
                                                       1
                                                            2
                                                                 1
                                                                     5
                                                                         3
                                                                              4
                                                                                  1
                      92
                                        99 100 104 106 113 116 118 120 125 127 128 137
##
    64
        82
             84
                  88
                           93
                               94
                                    98
                   2
                            2
                                     2
                                          5
          1
                       1
                                 5
                                              3
                                                   3
                                                       2
                                                            1
                                                                 1
                                                                         3
                                                                              3
##
  139 143 145 152 156 162 164 172 176 180 181 182 183 187 188 189 190 191 192 193
     3
          4
              3
                   3
                       3
                            3
                                 3
                                     3
                                          2
                                              3
                                                   3
                                                       3
                                                            3
                                                                2
                                                                     3
                                                                         3
                                                                              3
## 196 202 207 208 212 221 222 225 226 227 234 235
                   4
                       5
                            3
                                 4
                                     2
                                          3
                                                   5
          1
              1
## Levels: 1 2 3 4 5
```

predict(sigmoid.tune\$best.model, newdata=test.data)

```
7
              8
                   9
                      12
                           16
                                19
                                    22
                                         24
                                             25
                                                  29
                                                      38
                                                           42
                                                                43
                                                                    46
                                                                         48
                                                                             54
                                                                                  56
                                                                                       57
                                                                                           59
##
     6
     5
          3
              3
                   3
                                     2
                                          3
                                                   5
                                                            4
                                                                 4
                                                                      3
                                                                          4
                                                                               4
                                                                                   5
                                                                                        3
##
                            1
                                 4
                                               4
                                                        4
##
    64
        82
             84
                  88
                      92
                           93
                                94
                                    98
                                         99 100 104 106 113 116 118 120 125 127 128 137
##
          3
                   3
                        3
                            2
                                 1
                                     2
                                          4
                                               4
                                                   4
                                                        3
                                                            2
                                                                 4
                                                                      4
                                                                          3
                                                                               4
                                                                                   4
                                                                                        3
  139 143 145 152 156 162 164 172 176 180 181 182 183 187 188 189 190 191 192 193
          3
                            4
                                 3
                                     4
                                          4
                                                                                   3
              4
                   4
                        1
                                               4
                                                        4
                                                                 3
## 196 202 207 208 212 221 222 225 226 227 234 235
          4
              4
                   3
                        3
                            4
                                 3
                                     3
                                          4
## Levels: 1 2 3 4 5
```

test.data\$site

Radial kernel improves prediction on class 1.

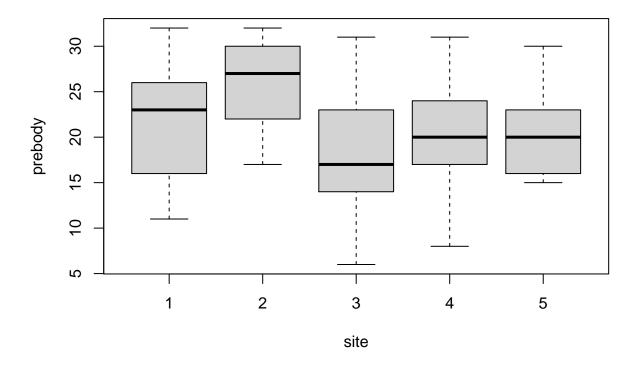
RBF slightly improved after standardizing? (it seems slightly more likely to predict on class 1.) thought, simpler models still retain the same performance (arguably better) sd_age+sd_pBod+sd_plet. But we are still not getting any prediction on class 4 & 5.

After assign class weights using this formula:

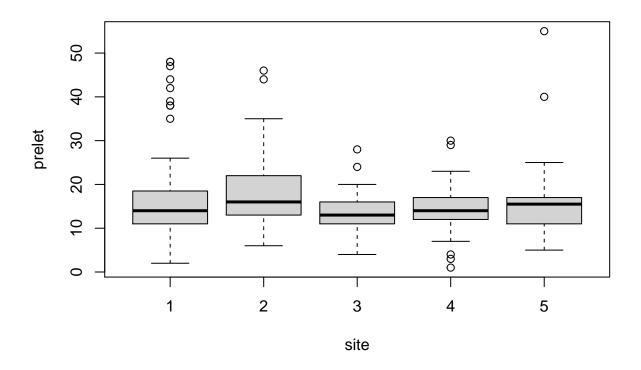
$$w_j = \frac{n}{kn_j}$$
, n is total number of data points, k is number of classes

Our model begins to make predictions on class 4 & class 5, though at the cost of overall accuracy. If we increase the weight for 4 & 5 to 1.5 and 3 respectively the performance of Radial SVM decreases but that of linear SVM increases to be comparable to Radial SVM's recorded highest accuracy (a little bit over 0.40).

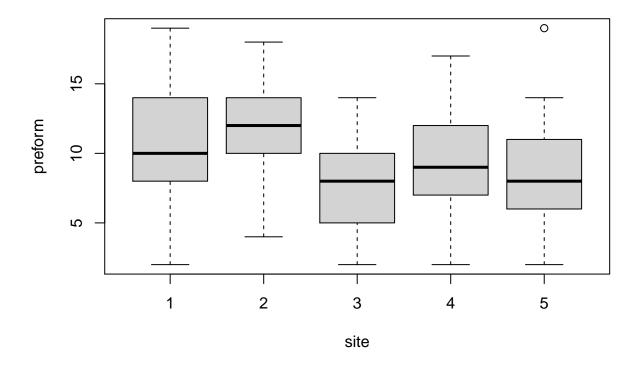
trying to do more EDA to see if anything explains why the data is not linearly separable
boxplot(prebody~site, data=sesame)



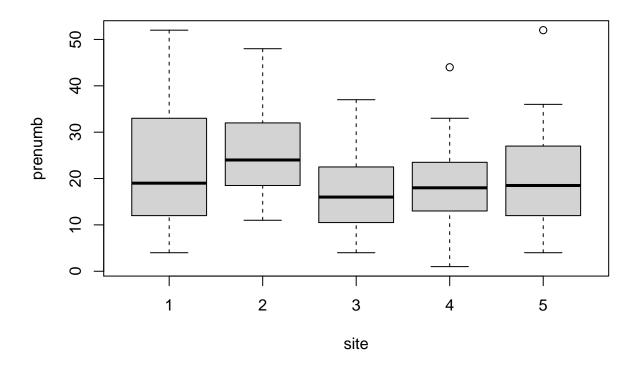
boxplot(prelet~site, data=sesame)



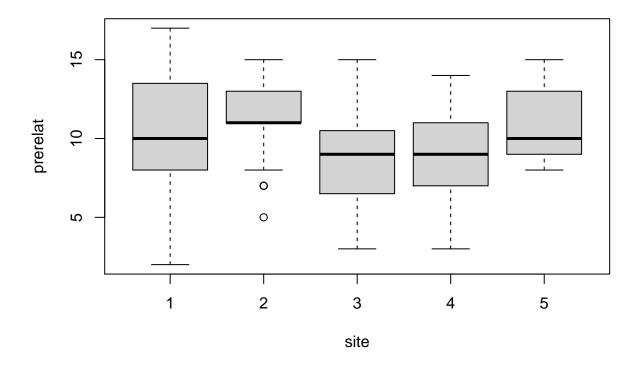
boxplot(preform~site, data=sesame)



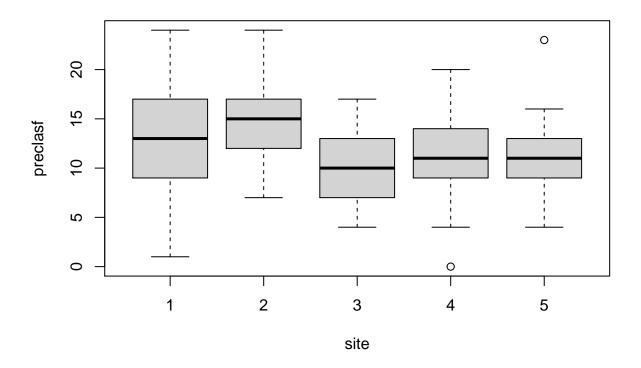
boxplot(prenumb~site, data=sesame)



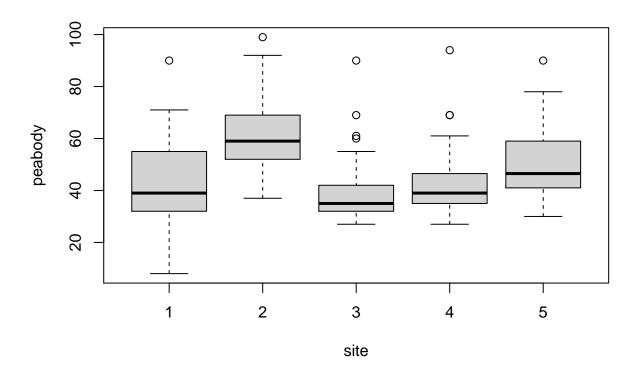
boxplot(prerelat~site, data=sesame)



boxplot(preclasf~site, data=sesame)



boxplot(peabody~site, data=sesame)



Trees

mtry=4, importance=TRUE)

importance(rf.tree) 5 MeanDecreaseAccuracy ## 1 3 4 ## age 16.071180 11.5639655 1.533526 10.24956 -12.646482 15.477245 ## viewcat 1.412544 8.8509648 4.714890 26.85440 -5.674656 19.084980 6.879913 ## setting 9.950184 0.7116516 11.570042 20.04012 22.690481 ## viewenc 1.061428 -1.4942151 6.283556 -2.36010 -3.154027 1.353554 MeanDecreaseGini ## ## age 67.80480 ## viewcat 24.57478 ## setting 10.77912 10.03605 ## viewenc rf.pred <- predict(rf.tree, newdata=test.data)</pre> tree.conMatrix <- table(true=test.data[,"site"],</pre> pred=rf.pred) confusionMatrix(tree.conMatrix) ## Confusion Matrix and Statistics ## ## pred ## true 1 2 3 4 5 1 10 2 3 3 0 ## ## 2 4 10 1 1 2 ## 3 2 3 11 3 0 ## 4 1 1 3 5 2 ## 5 0 1 3 0 1 ## ## Overall Statistics ## ## Accuracy: 0.5139 ## 95% CI : (0.3931, 0.6335) No Information Rate: 0.2917 ## ## P-Value [Acc > NIR] : 6.203e-05 ## ## Kappa: 0.3706 Mcnemar's Test P-Value : NA ## ## Statistics by Class: ## ## Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 0.5238 0.41667 0.20000 ## Sensitivity 0.5882 0.5882 0.8545 0.8545 ## Specificity 0.8431 0.88333 0.94030 ## Pos Pred Value 0.5556 0.5556 0.5789 0.41667 0.20000 ## Neg Pred Value 0.8113 0.88333 0.94030 0.8704 0.8704 ## Prevalence 0.2361 0.2361 0.2917 0.16667 0.06944 ## Detection Rate 0.1389 0.1389 0.1528 0.06944 0.01389 ## Detection Prevalence 0.2500 0.2500 0.2639 0.16667 0.06944

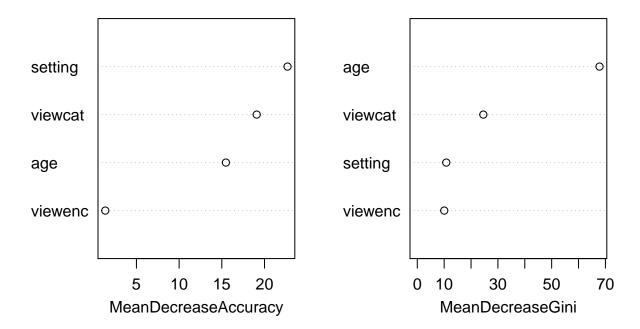
0.6835 0.65000

0.57015

0.7214 0.7214

Balanced Accuracy

rf.tree



0.42 - 0.5139 (but not including the test scores.) around 0.45 - 0.48, when including the pretest scores.

As seen in the table above, there is a notable discrepancy in the number of observations that lay in classes 4 and 5 for the variable site. More specifically, in the training data, there are just 25 observations with a value of 4 for the variable site and just 13 observations with a value of 5 for the variable site. In other words, there are less disadvantaged rural children and disadvantaged Spanish speaking children.

Consequently, when we initially ran our random forest model, our model was performing worse for test observations that take on the values 4 or 5 for the variable site.

To remedy this problem, we decided to use Synthetic Minority Oversampling Technique (SMOTE). SMOTE works by generating new samples in the classes of the response variable that are less represented. These new samples are generated using linear combinations of the "k" nearest neighbors in a given class. In this instance, we set k=5.

```
train.data$age <- as.numeric(train.data$age)
train.data$viewcat <- as.numeric(train.data$viewcat)
train.data$setting <- as.numeric(train.data$setting)
train.data$viewenc <- as.factor(train.data$viewenc)

test.data$age <- as.numeric(test.data$age)
test.data$viewcat <- as.numeric(test.data$viewcat)
test.data$setting <- as.numeric(test.data$setting)
test.data$viewenc <- as.factor(test.data$viewenc)</pre>
```

```
balanced.train.data <- SmoteClassif(site ~ ., train.data, k = 5, repl = FALSE, dist = "HEOM")
  # k --> represents the number of nearest neighbors (5) used to generate new examples of the minority
  # repl = FALSE --> cannot have repetition of examples when performing under-sampling by selecting amo
balanced.train.data %>%
 count(site)
     site n
## 1
       1 34
## 2
       2 34
## 3
       3 34
## 4
       4 33
## 5
       5 34
rf.tree<- randomForest(site~., data=balanced.train.data,</pre>
                       mtry=4, importance=TRUE)
importance(rf.tree)
##
                   1
                              2
                                       3
                                                            5 MeanDecreaseAccuracy
           15.112165 11.5044815 2.831522 12.2530454 12.35896
                                                                         24.534350
                                                                         32.088862
## viewcat 2.482319 12.5671060 5.114628 28.5410065 19.94849
## setting 14.672536  0.4233347  5.467389  22.8438707  32.97928
                                                                         34.377861
## viewenc 5.604315 -2.5081007 6.322412 0.1078161 12.91417
                                                                          9.960821
##
           MeanDecreaseGini
                 73.124641
## age
## viewcat
                  29.595993
## setting
                   9.359814
## viewenc
                   9.254742
rf.pred <- predict(rf.tree, newdata=test.data)</pre>
tree.conMatrix <- table(true=test.data[,"site"],</pre>
                         pred=rf.pred)
confusionMatrix(tree.conMatrix)
## Confusion Matrix and Statistics
##
##
       pred
## true 1 2 3 4 5
      1 7 4 3 2 2
##
      2 4 8 1 2 3
##
      3 3 4 9 2 1
##
##
      4 0 2 3 5 2
##
      5 0 2 2 0 1
##
## Overall Statistics
##
##
                  Accuracy : 0.4167
                    95% CI: (0.3015, 0.5389)
##
##
      No Information Rate: 0.2778
      P-Value [Acc > NIR] : 0.007741
##
```

```
##
##
                    Kappa: 0.2539
##
##
   Mcnemar's Test P-Value: 0.576888
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.50000
                                  0.4000
                                          0.5000 0.45455 0.11111
## Specificity
                        0.81034
                                 0.8077
                                           0.8148 0.88525
                                                           0.93651
## Pos Pred Value
                        0.38889 0.4444
                                          0.4737
                                                  0.41667
                                                           0.20000
## Neg Pred Value
                        0.87037 0.7778
                                           0.8302
                                                  0.90000
                                                           0.88060
## Prevalence
                        0.19444 0.2778
                                           0.2500
                                                  0.15278
                                                           0.12500
## Detection Rate
                        0.09722 0.1111
                                           0.1250
                                                  0.06944
                                                           0.01389
## Detection Prevalence 0.25000
                                 0.2500
                                           0.2639
                                                   0.16667
                                                           0.06944
## Balanced Accuracy
                        0.65517
                                  0.6038
                                           0.6574 0.66990
                                                           0.52381
```

While the SmoteClassif() function certainly did its job by balancing out the number of observations for each value of site in the training data, the new random forest model (fitted to this new data set) is less accurate and sees little improvement in the detection of site values of 4 and 5.

```
# set.seed(3215)
#
##, "prebody", "prelet", "preform", "prenumb", "prerelat", "preclasf", "postbody", "postlet", "postform
#
#
# features <- c("site", "age", "viewcat", "setting", "viewenc", "prebody", "prelet", "preform", "prenumb"
# tree.2 <- sesame[, features]</pre>
# train.2 <- tree.2[train.index,]</pre>
# test.2 <- tree.2[-train.index,]</pre>
#
# boost.tree <- gbm(site ~., data=train.2,</pre>
#
                     distribution="multinomial", n.trees=5000,
#
                     interaction.depth=1)
#
# #y.boost <- table(true=test.2[, "site"],
                     pred=predict(boost.tree, newdata=test.2))
# #
#
# boost.conMatrix <- table(true=test.2$site,</pre>
#
                            pred=predict(boost.tree, newdata=test.2))
# confusionMatrix(boost.conMatrix)
```

Questions for OH:

should we transform regular?

Both linear and radial kernels never output predictions for 4 & 5?

polynomial kernel? Which variables to give polynomial terms

use PCA to perform feature selection?

feature selections for SVM in general?

how to interpret the confusion matrix tables for SVM & Trees

How to interpret the imporatnce variance for multiclass classification

interpretations about the dataset, using the bad performance of the classifiers