Read Data

11/23/2021

```
library(foreign)
library(tidyverse)
## -- Attaching packages -----
                                                   ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5
                      v purrr
                                0.3.4
## v tibble 3.1.4
                      v dplyr
                               1.0.7
## v tidyr
           1.1.3
                      v stringr 1.4.0
## v readr
           2.0.1
                      v forcats 0.5.1
## -- Conflicts -----
                                             ## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
library(e1071)
library(tree)
## Registered S3 method overwritten by 'tree':
    method
               from
    print.tree cli
library(nnet)
library(gbm)
## Loaded gbm 2.1.8
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
##
      combine
## The following object is masked from 'package:ggplot2':
##
##
      margin
library(caret)
## Loading required package: lattice
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
```

```
##
       lift
library(ggplot2)
library(dplyr)
library(tidyr)
library(tidyverse)
library(patchwork)
library(UBL)
## Loading required package: MBA
## Loading required package: gstat
## Loading required package: automap
## Loading required package: sp
library(scales)
##
## Attaching package: 'scales'
## The following object is masked from 'package:purrr':
##
##
       discard
## The following object is masked from 'package:readr':
##
##
       col_factor
sesame <- read.dta("sesame.dta")</pre>
sesame <- sesame %>%
  mutate(site=factor(site)) %>%
  mutate(bodyDiff = postbody - prebody,
         letDiff = postlet - prelet,
         formDiff = postform - preform,
         numbDiff = postnumb - prenumb,
         relatDiff = postrelat - prerelat,
         clasfDiff = postclasf - preclasf)
sesame.sd <- sesame%>%
  mutate(sd_pBod = scale(prebody, center = TRUE, scale = TRUE),
         sd_plet = scale(prelet, center = TRUE, scale = TRUE),
         sd_pform = scale(preform, center = TRUE, scale = TRUE),
         sd_pnumb = scale(prenumb, center = TRUE, scale = TRUE),
         sd_prelat = scale(prerelat, center = TRUE, scale = TRUE),
         sd_pclasf = scale(preclasf, center = TRUE, scale = TRUE),
         sd_peabody = scale(peabody, center = TRUE, scale = TRUE),
         sd_age = scale(age, center =TRUE, scale = TRUE),
         male=if_else(sex==1, 1, 0),
         female=if_else(sex==2, 1, 0))
```

Exploratory Data Analysis

```
head(sesame)

## rownames id site sex age viewcat setting viewenc prebody prelet preform
```

```
## 1
                                             2
                                                                    23
                                                                            12
            1 1
                    1
                        1 66
                                     1
                                                     1
                                                            16
## 2
            2 2
                                             2
                    1
                        2 67
                                     3
                                                     1
                                                            30
                                                                    26
                                                                             9
```

##	વ	3	3 1	1 56	3	2	2	22	14	9
##	_	4	4 1	1 49	1	2	2	23	11	10
		=			_	_	2			
##	_	5	5 1	1 69	4	2	_	32	47	15
##	6	6	6 1	2 54	3	2	2	29	26	10
##		prenumb pr	rerelat	preclasf	postbody	postlet	_	postnumb	postrel	Lat
##	1	40	14	20	18	30	14	44		14
##	2	39	16	22	30	37	17	39		14
##	3	9	9	8	21	46	15	40		9
##	4	14	9	13	21	14	13	19		8
##	5	51	17	22	32	63	18	54		14
##	6	33	14	14	27	36	14	39		16
##		postclasf	peabody	agecat	encour I	site 2 I	site 3	Isite 4	Isite 5	regular
##	1	23	62	-	1	0	0	0	_0	0
##	2	22	8	1	1	0	0	0	0	1
##	3	19	32		0	0	0	0	0	1
##		15	27		0	0	0	0	0	0
##		21	71		0	0	0	0	0	1
##		24	32		0	0	0	0	0	1
##	Ü	bodyDiff 1			-	•	•	•	Ū	_
##	1	2	7	2		TCTGUDII	0	3		
##		0	11	8			-2	0		
	_	-				_	_	•		
##		-1	32	6			0	11		
##	_	-2	3	3	_		-1	2		
##	5	0	16	3	3	-	-3	-1		
##	6	-2	10	4	6		2	10		

Variables:

The ID refers to a subject's identification number. The site refers to the age and background information of the child. A site value of 1 indicates a 3-5 year old disadvantaged child from the inner city. A site value of 2 represents a 4 year old advantaged child from the suburbs. A value of 3 represents an advantaged rural child. A site value of 4 indicates a disadvantaged rural child. Lastly, a value of 5 represents a disadvantaged Spanish speaking child. For the sex, a value of 1 indicates male, and a value of 2 indicates female. The age category is the child's age in months. The viewcat column is the frequency of viewing Sesame Street (1 = rarely, 2 = once/twice per week, 3 = 3-5 times a week, 4 = more than 5 times per week). The setting is where Sesame Street was viewed; a value of 1 indicates home and a value of 2 indicates school. The viewenc column refers to if the child was encouraged to watch or not (1 = child not encouraged, 2 = child encouraged). Encour is the same variable but with values 0 and 1, respectively. Regular is an indicator variable representing if a child is a regular viewer (0 = rarely watched, 1 = watched once per week or greater).

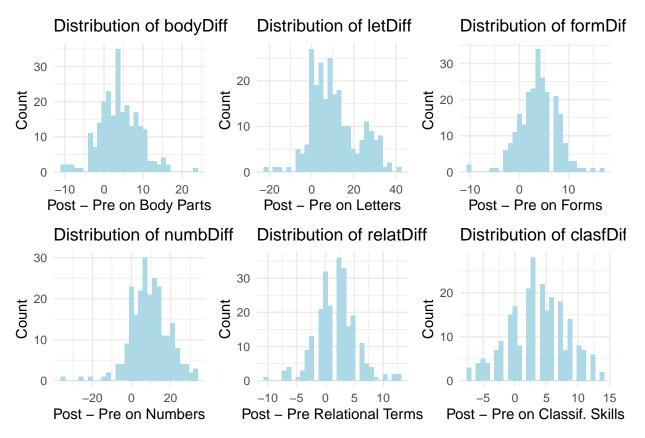
The prebody, prelet, preform, prenumb, prerelat, and preclasf columns all decribe pretest scores on varying types of assessments (body parts, letters, forms, numbers, relational terms, and classification skills, respectively). The columns labelled postbody, postlet, postform, postnumb, postrelat, and postclasf are the children's respective posttest scores. Above, we created the following variables - bodydiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff - to represent the difference in posttest scores and pretest scores for each child. Lastly, peabody represents a score of "mental age" for vocabulary maturity from the Peabody Picture Vocabulary Test.

Our main focus will be on the new variables we created (bodyDiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff) and variables related to how often the children watch Sesame Street (namely, viewcat and regular). Lastly, we will look into the backgrounds of the children, including site, sex, and age.

Distributions:

For the purposes of our analysis, we will first look at the distributions of bodyDiff, letDiff, formDiff, numbDiff, relatDiff, and clasfDiff.

```
#want to visualize distributions of bodyDiff, letDiff, formDiff, numbDiff, relatDiff, clasfDiff
bodyDiffplot \leftarrow ggplot(sesame, aes(x = bodyDiff)) +
  geom histogram(fill = "lightblue") +
  labs(title = "Distribution of bodyDiff", x = "Post - Pre on Body Parts", y = "Count") +
  theme_minimal()
letDiffplot \leftarrow ggplot(sesame, aes(x = letDiff)) +
  geom histogram(fill = "lightblue") +
  labs(title = "Distribution of letDiff", x = "Post - Pre on Letters", y = "Count") +
  theme_minimal()
formDiffplot <- ggplot(sesame, aes(x = formDiff)) +</pre>
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of formDiff", x = "Post - Pre on Forms", y = "Count") +
  theme minimal()
numbDiffplot \leftarrow ggplot(sesame, aes(x = numbDiff)) +
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of numbDiff", x = "Post - Pre on Numbers", y = "Count") +
  theme minimal()
relatDiffplot <- ggplot(sesame, aes(x = relatDiff)) +</pre>
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of relatDiff", x = "Post - Pre Relational Terms", y = "Count") +
  theme minimal()
clasfDiffplot <- ggplot(sesame, aes(x = clasfDiff)) +</pre>
  geom_histogram(fill = "lightblue") +
  labs(title = "Distribution of clasfDiff", x = "Post - Pre on Classif. Skills", y = "Count") +
  theme_minimal()
bodyDiffplot + letDiffplot + formDiffplot + numbDiffplot + relatDiffplot + clasfDiffplot
```



The six variables above were calculated by subtracting pre-test scores from post-test scores, so they are all numerical. The distributions of these six variables (bodyDiff, letDiff, formDiff, numbDiff, relatDiff, and clasfDiff) all appear to be roughly normal and unimodal. BodyDiff, letDiff, formDiff, relatDiff, and classDiff do not appear to have any obvious extreme outliers. Numbdiff, however, seems to be slightly left-skewed with outliers to the left -20. All of the six variables appear to have centers between 2 and 4.

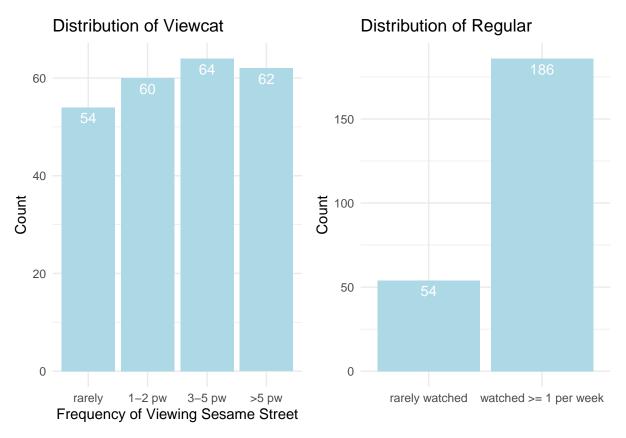
We will now examine the distributions of the variables related to how often children watch Sesame Street (namely, viewcat and regular).

```
# want to visualize distributions of viewcat and regular

viewcatplot <- ggplot(sesame, aes(x = factor(viewcat))) +
    geom_bar(fill = "lightblue") +
    labs(title = "Distribution of Viewcat", x = "Frequency of viewing Sesame Street", y = "Count") +
    scale_x_discrete("Frequency of Viewing Sesame Street", labels=c("rarely", "1-2 pw", "3-5 pw", ">5 pw"
    theme_minimal() +
    geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")

regularplot <- ggplot(sesame, aes(x = factor(regular))) +
    geom_bar(fill = "lightblue") +
    labs(title = "Distribution of Regular", y = "Count") +
    scale_x_discrete(labels=c("rarely watched", "watched >= 1 per week")) +
    theme_minimal() +
    theme_axis.title.x = element_blank()) +
    geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")

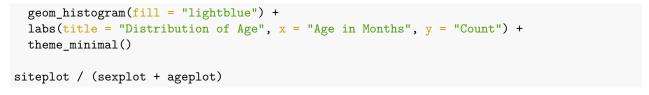
viewcatplot + regularplot
```

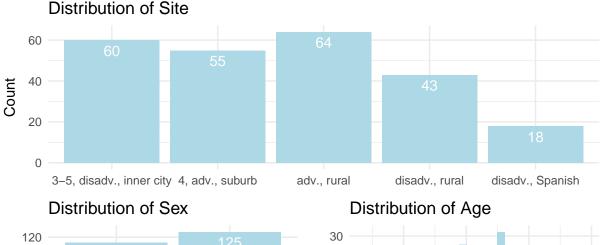


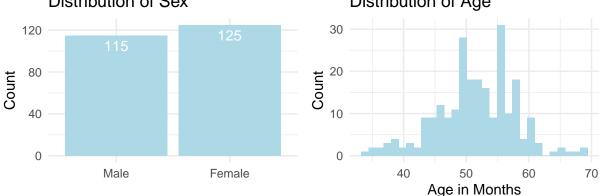
Both of these variables are categorical. On the left, viewcat appears to have a roughly uniform distribution, with "rarely" having the least amount of children and 3-5 times per week having the most (the range is only 10 children, so all of the bars are relatively close in height). For the variable regular, the category "watched once per week or greater" has far more observations than "rarely watched." The former category has more than triple the amount of the latter. We will be aware of this disparity in our analysis and continue with caution towards potential bias.

Lastly, we want to examine the distributions of site, sex, and age, all variables that relate to a child's background.

```
# want to visualize distributions of site, sex, and age
siteplot \leftarrow ggplot(sesame, aes(x = factor(site))) +
  geom_bar(fill = "lightblue") +
  labs(title = "Distribution of Site", y = "Count") +
  scale_x_discrete(labels=c("3-5, disadv., inner city", "4, adv., suburb", "adv., rural", "disadv., rur
  theme_minimal() +
  theme(axis.title.x = element_blank()) +
  geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")
sexplot \leftarrow ggplot(sesame, aes(x = factor(sex))) +
  geom_bar(fill = "lightblue") +
  labs(title = "Distribution of Sex", y = "Count") +
  scale_x_discrete(labels=c("Male", "Female")) +
  theme minimal() +
  theme(axis.title.x = element_blank()) +
  geom_text(aes(label = ..count..), stat = "count", vjust = 1.5, colour = "white")
ageplot \leftarrow ggplot(sesame, aes(x = age)) +
```







Site and Sex are both categorical variables. Distribution of Site has four categories with roughly the same amount of children (ranging from 43 to 64), but one category with far fewer observations (disadvantaged Spanish-speaking). This category has less than half of the observations as the next smallest category, which is a relatively large disparity. We will continue our analysis with caution towards this bias in the data. The distribution of sex is very even - the male category has 115 observations, while the female category has 125 observations. Age is a numerical variable that appears to be normal and bimodal, with two peaks around 50 and 56. There do not appear to be any extreme outliers in the distribution of age.

Q.1 Prediction Question: Can we use linear regression to predict the change in a child's test scores that occur after watching Sesame street (or in some instances, not watching Sesame street)?

Linear Regression Models

Here, I am fitting 6 linear regression models. Each of the models predicts a different difference in test score.

```
sesame.q1 <- sesame
sesame.q1$site <- as.factor(sesame.q1$site)
sesame.q1$sex <- as.factor(sesame.q1$sex)
sesame.q1$viewcat <- as.factor(sesame.q1$viewcat)
sesame.q1$setting <- as.factor(sesame.q1$setting)</pre>
```

```
sesame.q1$viewenc <- as.factor(sesame.q1$viewenc)

# Scaling Variables

sesame.q1$bodyDiff <- rescale(sesame.q1$bodyDiff, to = c(0, 30))
sesame.q1$letDiff <- rescale(sesame.q1$letDiff, to = c(0, 30))
sesame.q1$formDiff <- rescale(sesame.q1$formDiff, to = c(0, 30))
sesame.q1$numbDiff <- rescale(sesame.q1$numbDiff, to = c(0, 30))
sesame.q1$relatDiff <- rescale(sesame.q1$relatDiff, to = c(0, 30))
sesame.q1$clasfDiff <- rescale(sesame.q1$relatDiff, to = c(0, 30))
# Test-Train Split

set.seed(1)
train <- sample(1:nrow(sesame.q1), nrow(sesame.q1)*0.7)

training = sesame.q1[train,]
testing = sesame.q1[-train,]</pre>
```

Firstly, we factored the following variables to encode them as categoricals: site, sex, viewcat, setting, viewenc.

One problem that we envisioned when evaluating the and comparing the different models is that the tests are scored on different scales. For example, the scores for the test on knowledge of body parts (noted by bodyDiff) range from 0-32, while those of the test on letters (noted by letDiff) range from 0-58. To be able to aptly compare the mean squared error (MSE) between models, we also decided to convert each response variable to the same range. More specifically, we scaled each variable to the arbitrary range [0, 30].

Lastly, we randomly split the data between testing and training, using 70% of the data for training and 30% of the data for testing.

```
lin.mod1.full <- lm(bodyDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod1.full)
##
## Call:
## lm(formula = bodyDiff ~ (site + sex + age + viewcat + setting +
       viewenc)^2, data = training)
##
## Residuals:
##
                                3Q
       Min
                1Q Median
                                        Max
## -8.0419 -2.3623 -0.0666 2.0079 9.9599
##
## Coefficients: (2 not defined because of singularities)
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     -5.21460
                                14.63930 -0.356
                                                    0.7224
## site2
                     -1.67860
                                13.72456 -0.122
                                                    0.9029
## site3
                                            0.130
                                                    0.8968
                      1.18809
                                 9.13599
## site4
                     36.76705
                                16.49603
                                            2.229
                                                    0.0278 *
## site5
                                17.41166
                                            0.144
                                                    0.8855
                      2.51268
## sex2
                      2.67852
                                 6.79950
                                            0.394
                                                    0.6944
## age
                                            1.144
                      0.30634
                                 0.26777
                                                    0.2551
## viewcat2
                     11.62045
                                14.78702
                                            0.786
                                                    0.4336
## viewcat3
                     12.46797
                                13.36691
                                            0.933
                                                    0.3530
```

2.059

0.0418 *

0.2872

14.54421

9.11761 -1.069

viewcat4

setting2

29.95220

-9.74959

```
## viewenc2
                     19.16298
                                 10.20959
                                            1.877
                                                    0.0631 .
## site2:sex2
                                                    0.1786
                      3.01414
                                 2.22656
                                            1.354
                      2.32383
                                                    0.2866
## site3:sex2
                                  2.17020
                                            1.071
## site4:sex2
                      0.53119
                                  2.63525
                                            0.202
                                                    0.8406
## site5:sex2
                      0.32139
                                  3.71691
                                            0.086
                                                    0.9312
## site2:age
                      0.04657
                                 0.24040
                                            0.194
                                                    0.8467
## site3:age
                      0.03300
                                 0.17150
                                            0.192
                                                    0.8477
                                  0.30613 -1.960
## site4:age
                     -0.59988
                                                    0.0525 .
## site5:age
                      0.01087
                                  0.33703
                                            0.032
                                                    0.9743
## site2:viewcat2
                      3.94606
                                  5.50815
                                            0.716
                                                    0.4752
## site3:viewcat2
                      2.11625
                                  3.88814
                                            0.544
                                                    0.5873
                                  3.90246
                                            0.600
## site4:viewcat2
                      2.33983
                                                    0.5500
## site5:viewcat2
                      5.15446
                                  6.28877
                                            0.820
                                                    0.4142
## site2:viewcat3
                                                    0.3742
                     -4.60122
                                  5.15701
                                          -0.892
## site3:viewcat3
                     -2.61690
                                  3.66597
                                           -0.714
                                                    0.4768
## site4:viewcat3
                     -4.29765
                                  4.15537
                                           -1.034
                                                    0.3033
## site5:viewcat3
                           NA
                                       NA
                                               NA
                                                        NA
## site2:viewcat4
                     -2.76550
                                  5.23768
                                           -0.528
                                                    0.5985
## site3:viewcat4
                     -2.14835
                                  3.84372
                                           -0.559
                                                    0.5773
## site4:viewcat4
                     -6.19787
                                  4.85958
                                           -1.275
                                                    0.2048
## site5:viewcat4
                     -3.85743
                                  6.63742
                                          -0.581
                                                    0.5623
## site2:setting2
                      0.63008
                                  2.76440
                                            0.228
                                                    0.8201
                                            0.045
                                                    0.9642
## site3:setting2
                      0.14259
                                 3.16610
                      5.09348
                                  3.25326
                                            1.566
                                                    0.1203
## site4:setting2
## site5:setting2
                           NΑ
                                       NΑ
                                               NA
                                                        NΑ
## site2:viewenc2
                      0.89088
                                  2.60475
                                            0.342
                                                    0.7330
## site3:viewenc2
                     -1.79090
                                  3.30478
                                           -0.542
                                                    0.5890
## site4:viewenc2
                     -5.97857
                                  3.03298
                                           -1.971
                                                    0.0512
## site5:viewenc2
                     -2.07853
                                 7.09228
                                          -0.293
                                                    0.7700
## sex2:age
                     -0.10641
                                  0.12653
                                           -0.841
                                                    0.4022
## sex2:viewcat2
                      1.49879
                                  2.64935
                                            0.566
                                                    0.5727
## sex2:viewcat3
                      0.58754
                                  2.51057
                                            0.234
                                                    0.8154
## sex2:viewcat4
                     -1.20166
                                  2.68241
                                           -0.448
                                                    0.6550
                     -1.53778
                                           -0.903
## sex2:setting2
                                  1.70350
                                                    0.3686
## sex2:viewenc2
                      1.20679
                                  1.93998
                                            0.622
                                                    0.5352
## age:viewcat2
                     -0.27426
                                 0.26179
                                          -1.048
                                                    0.2971
## age:viewcat3
                     -0.15379
                                 0.23654
                                          -0.650
                                                    0.5169
## age:viewcat4
                     -0.46253
                                 0.26054
                                          -1.775
                                                    0.0786 .
## age:setting2
                      0.05401
                                  0.15397
                                            0.351
                                                    0.7264
                                          -1.544
## age:viewenc2
                     -0.27988
                                 0.18128
                                                    0.1254
## viewcat2:setting2 5.64914
                                  3.31141
                                            1.706
                                                    0.0908 .
## viewcat3:setting2 6.07677
                                  3.20554
                                            1.896
                                                    0.0606 .
## viewcat4:setting2 6.21301
                                  3.52866
                                            1.761
                                                    0.0810 .
## viewcat2:viewenc2 -7.71647
                                  3.54437
                                                    0.0316 *
                                          -2.177
## viewcat3:viewenc2 -6.24879
                                  3.34488 -1.868
                                                    0.0644 .
## viewcat4:viewenc2 -7.65623
                                  3.62444
                                           -2.112
                                                    0.0369 *
## setting2:viewenc2 1.97122
                                  2.32061
                                            0.849
                                                    0.3974
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.226 on 112 degrees of freedom
## Multiple R-squared: 0.4033, Adjusted R-squared: 0.1103
## F-statistic: 1.377 on 55 and 112 DF, p-value: 0.07819
```

```
AIC(lin.mod1.full)
## [1] 1006.935
yhat <- predict(lin.mod1.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod1.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "bodyDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 32.44637
lin.mod2.full <- lm(letDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)</pre>
summary(lin.mod2.full)
##
## Call:
## lm(formula = letDiff ~ (site + sex + age + viewcat + setting +
##
       viewenc)^2, data = training)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
                                2.3986 10.2234
## -12.7462 -2.3134
                       0.0386
## Coefficients: (2 not defined because of singularities)
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      19.20505
                                 15.54400
                                             1.236
                                                     0.2192
## site2
                      -7.55435
                                 14.57273
                                           -0.518
                                                     0.6052
## site3
                       7.76205
                                             0.800
                                                     0.4253
                                  9.70058
## site4
                     -12.82246
                                  17.51547
                                           -0.732
                                                     0.4657
## site5
                       1.39944
                                  18.48769
                                            0.076
                                                     0.9398
                                           -0.974
## sex2
                      -7.03111
                                  7.21970
                                                     0.3322
                                           -0.480
## age
                      -0.13633
                                  0.28432
                                                     0.6325
                                           -1.292
## viewcat2
                     -20.28956
                                 15.70085
                                                     0.1989
                                 14.19298 -0.052
                                                     0.9583
## viewcat3
                      -0.74326
## viewcat4
                      5.71015
                                 15.44303
                                            0.370
                                                     0.7123
                                           -0.097
## setting2
                      -0.93795
                                  9.68107
                                                     0.9230
## viewenc2
                      -5.41528
                                  10.84054 -0.500
                                                     0.6184
## site2:sex2
                       1.20390
                                  2.36416
                                            0.509
                                                     0.6116
## site3:sex2
                      -0.63445
                                  2.30431 -0.275
                                                     0.7836
## site4:sex2
                      -3.21100
                                   2.79810
                                           -1.148
                                                     0.2536
## site5:sex2
                      -1.80949
                                  3.94661
                                           -0.458
                                                     0.6475
## site2:age
                       0.27245
                                  0.25526
                                            1.067
                                                     0.2881
                                           -0.973
## site3:age
                      -0.17713
                                  0.18209
                                                     0.3328
## site4:age
                       0.32387
                                  0.32505
                                             0.996
                                                     0.3212
## site5:age
                      -0.06901
                                  0.35786
                                           -0.193
                                                     0.8474
                      -1.69100
                                           -0.289
## site2:viewcat2
                                   5.84855
                                                     0.7730
## site3:viewcat2
                       0.28314
                                   4.12842
                                            0.069
                                                     0.9454
                                             0.863
## site4:viewcat2
                       3.57460
                                   4.14363
                                                     0.3902
## site5:viewcat2
                       4.79038
                                   6.67741
                                             0.717
                                                     0.4746
## site2:viewcat3
                      -5.13072
                                   5.47571
                                           -0.937
                                                     0.3508
```

0.7032

3.89252 -0.382

site3:viewcat3

-1.48691

```
## site4:viewcat3
                      -5.03691
                                   4.41217 -1.142
                                                     0.2561
## site5:viewcat3
                            NΑ
                                        NA
                                                NA
                                                         NΑ
                                           -0.575
## site2:viewcat4
                      -3.19663
                                   5.56136
                                                     0.5666
## site3:viewcat4
                      -0.93894
                                   4.08126
                                           -0.230
                                                     0.8185
## site4:viewcat4
                      -5.99748
                                   5.15990
                                            -1.162
                                                     0.2476
## site5:viewcat4
                                           -0.030
                      -0.21046
                                  7.04760
                                                     0.9762
                                   2.93524 -0.465
## site2:setting2
                      -1.36444
                                                     0.6429
## site3:setting2
                      -1.30832
                                   3.36176
                                            -0.389
                                                     0.6979
## site4:setting2
                      -4.68028
                                   3.45430
                                           -1.355
                                                     0.1782
## site5:setting2
                            NA
                                        NA
                                                NA
                                                         NA
## site2:viewenc2
                      -2.65415
                                   2.76572
                                           -0.960
                                                     0.3393
## site3:viewenc2
                                   3.50901
                                             0.011
                                                     0.9911
                       0.03940
## site4:viewenc2
                      -0.05966
                                   3.22042
                                           -0.019
                                                     0.9853
                                            1.059
                                                     0.2919
## site5:viewenc2
                       7.97522
                                  7.53058
                                   0.13435
                                                     0.2538
## sex2:age
                       0.15410
                                             1.147
## sex2:viewcat2
                       2.86176
                                   2.81308
                                             1.017
                                                     0.3112
                                   2.66573 -0.075
## sex2:viewcat3
                      -0.20025
                                                     0.9403
## sex2:viewcat4
                      -0.45238
                                   2.84818
                                           -0.159
                                                     0.8741
                                          -1.072
                                                     0.2862
## sex2:setting2
                      -1.93840
                                   1.80878
## sex2:viewenc2
                       3.18303
                                   2.05987
                                             1.545
                                                     0.1251
## age:viewcat2
                       0.38696
                                  0.27796
                                             1.392
                                                     0.1666
## age:viewcat3
                                             0.582
                                                     0.5620
                       0.14608
                                  0.25116
                                             0.064
                                                     0.9488
## age:viewcat4
                       0.01779
                                   0.27664
                                             0.083
## age:setting2
                       0.01359
                                   0.16348
                                                     0.9339
## age:viewenc2
                       0.02087
                                  0.19248
                                             0.108
                                                     0.9139
## viewcat2:setting2
                       2.59739
                                   3.51606
                                             0.739
                                                     0.4616
                                             1.183
                                                     0.2392
## viewcat3:setting2
                       4.02713
                                   3.40364
## viewcat4:setting2
                      -0.78643
                                   3.74673
                                           -0.210
                                                     0.8341
                                           -0.923
## viewcat2:viewenc2
                      -3.47489
                                   3.76341
                                                     0.3578
## viewcat3:viewenc2 -1.80040
                                            -0.507
                                                     0.6132
                                   3.55159
## viewcat4:viewenc2
                       1.81492
                                   3.84842
                                             0.472
                                                     0.6381
## setting2:viewenc2
                       4.70866
                                   2.46403
                                             1.911
                                                     0.0586 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.488 on 112 degrees of freedom
## Multiple R-squared: 0.5727, Adjusted R-squared: 0.3628
## F-statistic: 2.729 on 55 and 112 DF, p-value: 3.56e-06
AIC(lin.mod2.full)
## [1] 1027.083
yhat <- predict(lin.mod2.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod2.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "letDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 24.44647
lin.mod3.full <- lm(formDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod3.full)
```

```
##
## Call:
## lm(formula = formDiff ~ (site + sex + age + viewcat + setting +
##
       viewenc)^2, data = training)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
  -8.9228 -1.8652 -0.0169 1.8737 12.7649
##
##
## Coefficients: (2 not defined because of singularities)
##
                        Estimate Std. Error t value Pr(>|t|)
                                               2.068
## (Intercept)
                       29.944763
                                  14.480042
                                                       0.0409 *
## site2
                       12.327359
                                  13.575252
                                               0.908
                                                        0.3658
## site3
                       -1.058753
                                   9.036594
                                              -0.117
                                                       0.9069
## site4
                        4.392580
                                  16.316566
                                               0.269
                                                       0.7883
## site5
                        4.356217
                                  17.222238
                                               0.253
                                                       0.8008
## sex2
                        3.675853
                                   6.725528
                                               0.547
                                                       0.5858
                       -0.296259
                                   0.264860
                                              -1.119
                                                       0.2657
## age
## viewcat2
                      -24.508158
                                  14.626151
                                              -1.676
                                                       0.0966 .
## viewcat3
                      -15.832596
                                  13.221492
                                              -1.197
                                                       0.2336
## viewcat4
                       -2.141958
                                  14.385978
                                              -0.149
                                                       0.8819
## setting2
                        7.516078
                                   9.018414
                                               0.833
                                                       0.4064
## viewenc2
                      -15.197856
                                  10.098523
                                              -1.505
                                                       0.1351
## site2:sex2
                       -3.772624
                                   2.202334
                                              -1.713
                                                        0.0895 .
## site3:sex2
                       -4.100876
                                   2.146588
                                              -1.910
                                                       0.0586 .
## site4:sex2
                       -5.714483
                                   2.606577
                                              -2.192
                                                        0.0304 *
## site5:sex2
                       -4.513182
                                   3.676472
                                              -1.228
                                                       0.2222
## site2:age
                       -0.271127
                                   0.237788
                                              -1.140
                                                        0.2566
                                               0.007
                                                       0.9944
## site3:age
                        0.001186
                                   0.169630
## site4:age
                       -0.031048
                                   0.302804
                                              -0.103
                                                       0.9185
## site5:age
                       -0.082011
                                   0.333365
                                              -0.246
                                                       0.8061
## site2:viewcat2
                        6.777720
                                   5.448230
                                               1.244
                                                        0.2161
                        6.728359
                                   3.845840
                                               1.750
                                                       0.0829 .
## site3:viewcat2
## site4:viewcat2
                        5.866619
                                   3.860003
                                               1.520
                                                        0.1314
## site5:viewcat2
                        7.030391
                                   6.220350
                                                       0.2608
                                               1.130
## site2:viewcat3
                        2.122722
                                   5.100911
                                               0.416
                                                       0.6781
                                                       0.2314
## site3:viewcat3
                        4.363483
                                   3.626088
                                               1.203
## site4:viewcat3
                        0.418813
                                   4.110165
                                               0.102
                                                       0.9190
## site5:viewcat3
                              NA
                                          NA
                                                  NA
                                                            NA
## site2:viewcat4
                        1.747657
                                   5.180694
                                               0.337
                                                       0.7365
## site3:viewcat4
                        5.788361
                                   3.801908
                                               1.522
                                                        0.1307
                                              -0.029
## site4:viewcat4
                       -0.137820
                                   4.806713
                                                        0.9772
## site5:viewcat4
                        1.851415
                                   6.565206
                                               0.282
                                                        0.7785
## site2:setting2
                        1.586718
                                   2.734325
                                               0.580
                                                        0.5629
## site3:setting2
                       -6.267179
                                   3.131653
                                              -2.001
                                                        0.0478 *
                        1.393469
                                   3.217863
                                               0.433
                                                        0.6658
## site4:setting2
## site5:setting2
                              NA
                                          NA
                                                  NA
                                                            NA
## site2:viewenc2
                       -0.253451
                                   2.576413
                                              -0.098
                                                        0.9218
## site3:viewenc2
                        4.996265
                                   3.268825
                                               1.528
                                                        0.1292
## site4:viewenc2
                                   2.999986
                                              -1.359
                       -4.076868
                                                        0.1769
## site5:viewenc2
                        0.542663
                                   7.015121
                                               0.077
                                                        0.9385
## sex2:age
                        0.040381
                                   0.125154
                                               0.323
                                                        0.7476
```

```
## sex2:viewcat2
                     -2.039436
                                 2.620528 -0.778
                                                    0.4381
## sex2:viewcat3
                                                    0.8984
                      0.317803
                                 2.483262
                                           0.128
## sex2:viewcat4
                                                    0.8378
                     -0.544298
                                 2.653230 -0.205
## sex2:setting2
                     -2.642309
                                 1.684970 -1.568
                                                    0.1197
                                 1.918879 -1.125
## sex2:viewenc2
                     -2.157924
                                                    0.2632
## age:viewcat2
                      0.364615
                                0.258937
                                           1.408
                                                    0.1619
## age:viewcat3
                      0.253258
                                0.233965
                                           1.082
                                                    0.2814
## age:viewcat4
                      0.017013
                                 0.257708
                                           0.066
                                                    0.9475
## age:setting2
                     -0.094395
                                 0.152294 -0.620
                                                    0.5366
## age:viewenc2
                      0.288927
                                 0.179305
                                           1.611
                                                    0.1099
## viewcat2:setting2
                      0.045540
                                 3.275387
                                            0.014
                                                    0.9889
                                 3.170671 -0.289
                                                    0.7730
## viewcat3:setting2 -0.916800
## viewcat4:setting2
                     2.713885
                                 3.490273
                                           0.778
                                                    0.4385
## viewcat2:viewenc2
                     7.112277
                                 3.505815
                                           2.029
                                                    0.0449 *
## viewcat3:viewenc2
                      2.220835
                                 3.308488
                                            0.671
                                                    0.5034
## viewcat4:viewenc2
                      0.718803
                                 3.585006
                                            0.201
                                                    0.8415
## setting2:viewenc2 -1.590335
                                 2.295369 -0.693
                                                    0.4898
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.18 on 112 degrees of freedom
## Multiple R-squared: 0.3905, Adjusted R-squared: 0.09115
## F-statistic: 1.305 on 55 and 112 DF, p-value: 0.1189
AIC(lin.mod3.full)
## [1] 1003.259
yhat <- predict(lin.mod3.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod3.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "formDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 23.18844
lin.mod4.full <- lm(numbDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)
summary(lin.mod4.full)
##
## Call:
## lm(formula = numbDiff ~ (site + sex + age + viewcat + setting +
##
       viewenc)^2, data = training)
##
## Residuals:
                 1Q
                      Median
                                   3Q
                                           Max
        Min
## -14.9731 -2.2530 -0.0413
                               2.4864
                                        9.4788
## Coefficients: (2 not defined because of singularities)
                     Estimate Std. Error t value Pr(>|t|)
                                          1.103
## (Intercept)
                     16.70541
                                15.13888
                                                   0.2722
## site2
                     15.96399
                                14.19292
                                          1.125
                                                   0.2631
## site3
                      6.64629
                                 9.44776
                                          0.703
                                                   0.4832
```

```
## site4
                       -4.69062
                                   17.05897
                                             -0.275
                                                       0.7838
## site5
                        1.27560
                                   18.00585
                                              0.071
                                                       0.9436
                        9.80788
## sex2
                                    7.03154
                                              1.395
                                                       0.1658
                       -0.08799
                                             -0.318
                                                       0.7513
## age
                                    0.27691
## viewcat2
                      -12.34222
                                   15.29164
                                             -0.807
                                                       0.4213
## viewcat3
                      -11.17277
                                   13.82307
                                             -0.808
                                                       0.4206
## viewcat4
                        3.28623
                                   15.04054
                                              0.218
                                                       0.8274
## setting2
                       17.35032
                                    9.42875
                                              1.840
                                                       0.0684
## viewenc2
                       -7.37000
                                   10.55800
                                             -0.698
                                                       0.4866
## site2:sex2
                       -3.34924
                                    2.30254
                                             -1.455
                                                       0.1486
## site3:sex2
                       -2.90207
                                    2.24426
                                             -1.293
                                                       0.1986
## site4:sex2
                       -3.42395
                                    2.72518
                                             -1.256
                                                       0.2116
## site5:sex2
                       -0.25383
                                    3.84375
                                             -0.066
                                                       0.9475
## site2:age
                                                       0.7795
                       -0.06976
                                    0.24861
                                             -0.281
                                             -0.294
## site3:age
                       -0.05208
                                    0.17735
                                                       0.7696
## site4:age
                        0.27163
                                    0.31658
                                              0.858
                                                       0.3927
## site5:age
                                              0.159
                                                       0.8741
                        0.05536
                                    0.34853
                       -6.50669
                                    5.69612
                                             -1.142
                                                       0.2558
## site2:viewcat2
                                             -0.465
## site3:viewcat2
                       -1.86918
                                    4.02083
                                                       0.6429
## site4:viewcat2
                       -4.52539
                                    4.03563
                                             -1.121
                                                       0.2645
## site5:viewcat2
                       -0.06176
                                    6.50337
                                             -0.009
                                                       0.9924
                                             -1.228
                                                       0.2220
## site2:viewcat3
                       -6.54853
                                    5.33300
## site3:viewcat3
                        0.37710
                                    3.79107
                                              0.099
                                                       0.9209
                                             -0.652
## site4:viewcat3
                       -2.80346
                                    4.29718
                                                       0.5155
## site5:viewcat3
                             NA
                                         NA
                                                  NΑ
                                                           NΑ
## site2:viewcat4
                      -10.05730
                                    5.41641
                                             -1.857
                                                       0.0660
## site3:viewcat4
                                    3.97489
                                                       0.9107
                        0.44685
                                              0.112
## site4:viewcat4
                       -6.50503
                                    5.02542
                                             -1.294
                                                       0.1982
## site5:viewcat4
                       -5.38827
                                    6.86392
                                             -0.785
                                                       0.4341
## site2:setting2
                       -2.14597
                                    2.85874
                                             -0.751
                                                       0.4544
## site3:setting2
                       -4.76023
                                    3.27414
                                             -1.454
                                                       0.1488
                                    3.36428
## site4:setting2
                       -7.31658
                                             -2.175
                                                       0.0317 *
## site5:setting2
                                         NA
                                                 NA
                                                           NA
                             NA
                       -2.72744
## site2:viewenc2
                                    2.69364
                                             -1.013
                                                       0.3135
## site3:viewenc2
                       -1.35549
                                    3.41756
                                             -0.397
                                                       0.6924
## site4:viewenc2
                                             -0.480
                       -1.50418
                                    3.13649
                                                       0.6325
## site5:viewenc2
                        6.83681
                                    7.33431
                                              0.932
                                                       0.3533
## sex2:age
                                             -1.240
                                                       0.2176
                       -0.16226
                                    0.13085
## sex2:viewcat2
                                              0.808
                                                       0.4208
                        2.21351
                                    2.73976
## sex2:viewcat3
                        2.04053
                                    2.59625
                                              0.786
                                                       0.4336
## sex2:viewcat4
                       -0.65653
                                    2.77395
                                             -0.237
                                                       0.8133
## sex2:setting2
                                             -0.025
                                                       0.9803
                       -0.04353
                                    1.76164
## sex2:viewenc2
                        1.03717
                                    2.00619
                                              0.517
                                                       0.6062
                                              1.093
## age:viewcat2
                        0.29579
                                    0.27072
                                                       0.2769
## age:viewcat3
                        0.28309
                                    0.24461
                                              1.157
                                                       0.2496
## age:viewcat4
                        0.08420
                                    0.26943
                                              0.312
                                                       0.7552
## age:setting2
                       -0.22758
                                    0.15922
                                             -1.429
                                                       0.1557
## age:viewenc2
                        0.12555
                                    0.18746
                                              0.670
                                                       0.5044
## viewcat2:setting2
                       -2.23219
                                    3.42442
                                             -0.652
                                                       0.5158
## viewcat3:setting2
                       -0.89840
                                    3.31494
                                             -0.271
                                                       0.7869
## viewcat4:setting2
                       -1.33874
                                    3.64908
                                             -0.367
                                                       0.7144
## viewcat2:viewenc2
                        3.29199
                                    3.66533
                                              0.898
                                                       0.3710
## viewcat3:viewenc2
                        1.09871
                                    3.45902
                                              0.318
                                                       0.7514
## viewcat4:viewenc2
                        2.49482
                                    3.74812
                                              0.666
                                                       0.5070
```

```
## setting2:viewenc2
                      0.59013
                                  2.39981
                                          0.246
                                                    0.8062
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.371 on 112 degrees of freedom
## Multiple R-squared: 0.3558, Adjusted R-squared: 0.03945
## F-statistic: 1.125 on 55 and 112 DF, p-value: 0.2971
AIC(lin.mod4.full)
## [1] 1018.209
yhat <- predict(lin.mod4.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod4.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "numbDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 28.23554
lin.mod5.full <- lm(relatDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)</pre>
summary(lin.mod5.full)
##
## Call:
## lm(formula = relatDiff ~ (site + sex + age + viewcat + setting +
##
       viewenc)^2, data = training)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                            Max
## -10.1381 -2.1057 -0.0037
                                1.9658 11.4625
##
## Coefficients: (2 not defined because of singularities)
##
                     Estimate Std. Error t value Pr(>|t|)
                     17.06032
                                14.42797
                                           1.182
## (Intercept)
                                                    0.2395
## site2
                     -4.32400
                               13.52644 -0.320
                                                    0.7498
## site3
                      0.09709
                                 9.00410
                                          0.011
                                                    0.9914
## site4
                                           0.543
                      8.82232
                                 16.25789
                                                    0.5885
## site5
                     10.23066
                                 17.16031
                                           0.596
                                                    0.5523
## sex2
                     11.05162
                                 6.70134
                                          1.649
                                                    0.1019
                     -0.19817
                                 0.26391 -0.751
                                                    0.4543
## age
## viewcat2
                     -12.06564
                                 14.57356 -0.828
                                                   0.4095
## viewcat3
                     -1.76765
                                 13.17395 -0.134
                                                    0.8935
## viewcat4
                     12.95777
                                 14.33425
                                          0.904
                                                    0.3679
                                           0.611
                                                    0.5422
## setting2
                      5.49314
                                 8.98598
## viewenc2
                      1.41758
                                 10.06221
                                           0.141
                                                    0.8882
## site2:sex2
                     -2.89712
                                 2.19441 -1.320
                                                    0.1895
## site3:sex2
                     -1.50609
                                  2.13887 -0.704
                                                    0.4828
## site4:sex2
                      -5.48305
                                  2.59720 -2.111
                                                    0.0370 *
## site5:sex2
                                  3.66325 -0.744
                     -2.72621
                                                    0.4583
## site2:age
                      0.14657
                                  0.23693
                                          0.619
                                                    0.5374
## site3:age
                                  0.16902
                                           0.553
                      0.09339
                                                    0.5817
```

0.30171

0.11553

site4:age

0.383

0.7025

```
## site5:age
                      -0.12613
                                   0.33217 -0.380
                                                     0.7049
## site2:viewcat2
                       1.39325
                                   5.42864
                                             0.257
                                                     0.7979
                                   3.83201
## site3:viewcat2
                       0.58876
                                             0.154
                                                     0.8782
## site4:viewcat2
                                            -0.886
                      -3.40928
                                   3.84612
                                                     0.3773
## site5:viewcat2
                      -0.56097
                                   6.19798
                                            -0.091
                                                     0.9280
## site2:viewcat3
                      -0.72033
                                   5.08257
                                            -0.142
                                                     0.8876
## site3:viewcat3
                      -0.90613
                                   3.61305
                                            -0.251
                                                     0.8024
## site4:viewcat3
                      -7.73848
                                   4.09539
                                            -1.890
                                                     0.0614
## site5:viewcat3
                            NA
                                        NA
                                                NA
                                                         NA
## site2:viewcat4
                      -3.95053
                                   5.16206
                                            -0.765
                                                     0.4457
## site3:viewcat4
                      -1.08877
                                   3.78824
                                            -0.287
                                                     0.7743
                                   4.78943
                                            -0.798
                                                     0.4267
## site4:viewcat4
                      -3.82113
## site5:viewcat4
                      -1.25414
                                   6.54160
                                            -0.192
                                                     0.8483
## site2:setting2
                      -0.87824
                                   2.72449
                                            -0.322
                                                     0.7478
                                   3.12039
                                            -1.045
                                                     0.2985
## site3:setting2
                      -3.25960
## site4:setting2
                      -6.71576
                                   3.20629
                                            -2.095
                                                     0.0385 *
## site5:setting2
                                                         NA
                            NA
                                        NA
                                                NA
## site2:viewenc2
                       0.09165
                                   2.56715
                                             0.036
                                                     0.9716
## site3:viewenc2
                                             0.027
                                                     0.9782
                       0.08926
                                   3.25707
## site4:viewenc2
                      -5.67745
                                   2.98920
                                            -1.899
                                                     0.0601
## site5:viewenc2
                      -1.58031
                                   6.98990
                                            -0.226
                                                     0.8215
## sex2:age
                                            -0.815
                                                     0.4169
                      -0.10161
                                   0.12470
                                            -0.124
## sex2:viewcat2
                      -0.32485
                                   2.61110
                                                     0.9012
                                            -0.328
## sex2:viewcat3
                      -0.81092
                                   2.47433
                                                     0.7437
## sex2:viewcat4
                      -2.75732
                                   2.64369
                                            -1.043
                                                     0.2992
## sex2:setting2
                      -3.19781
                                   1.67891
                                           -1.905
                                                     0.0594
## sex2:viewenc2
                                           -0.495
                                                     0.6218
                      -0.94590
                                   1.91198
## age:viewcat2
                       0.29068
                                   0.25801
                                             1.127
                                                     0.2623
                                             0.407
## age:viewcat3
                       0.09494
                                   0.23312
                                                     0.6846
## age:viewcat4
                                   0.25678
                                            -0.463
                                                     0.6443
                      -0.11889
## age:setting2
                      -0.01405
                                   0.15175
                                            -0.093
                                                     0.9264
## age:viewenc2
                       0.06598
                                   0.17866
                                             0.369
                                                     0.7126
## viewcat2:setting2
                      -2.52471
                                   3.26361
                                            -0.774
                                                     0.4408
                                            -0.031
## viewcat3:setting2
                      -0.09666
                                   3.15927
                                                     0.9756
## viewcat4:setting2
                       2.70973
                                   3.47772
                                             0.779
                                                     0.4375
## viewcat2:viewenc2
                      -2.40402
                                   3.49321
                                            -0.688
                                                     0.4928
## viewcat3:viewenc2
                      -1.85347
                                   3.29659
                                            -0.562
                                                     0.5751
## viewcat4:viewenc2
                      -2.73805
                                            -0.767
                                                     0.4450
                                   3.57212
                                   2.28711
                                                     0.1905
## setting2:viewenc2
                      -3.01217
                                            -1.317
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.165 on 112 degrees of freedom
## Multiple R-squared: 0.4263, Adjusted R-squared: 0.1446
## F-statistic: 1.513 on 55 and 112 DF, p-value: 0.03312
AIC(lin.mod5.full)
## [1] 1002.049
yhat <- predict(lin.mod5.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod5.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
```

```
y.test <- testing[, "relatDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
## [1] 23.63526
lin.mod6.full <- lm(clasfDiff ~ (site + sex + age + viewcat + setting + viewenc)^2, data = training)</pre>
summary(lin.mod6.full)
##
## Call:
## lm(formula = clasfDiff ~ (site + sex + age + viewcat + setting +
       viewenc)^2, data = training)
##
## Residuals:
        Min
                       Median
                                     30
                  1Q
                                             Max
## -11.6108 -3.1873
                       0.0668
                                 3.0854
                                        10.7635
## Coefficients: (2 not defined because of singularities)
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      31.86932
                                  20.13470
                                             1.583
                                                     0.1163
                                             0.303
## site2
                       5.71113
                                  18.87658
                                                     0.7628
## site3
                     -11.78957
                                  12.56551
                                            -0.938
                                                     0.3501
## site4
                                           -1.571
                     -35.64786
                                  22.68842
                                                     0.1190
## site5
                     -56.84008
                                  23.94777
                                           -2.374
                                                     0.0193 *
## sex2
                      16.72781
                                            1.789
                                                     0.0764 .
                                  9.35194
                                  0.36829
                                            -1.019
                                                     0.3104
## age
                      -0.37531
## viewcat2
                     -33.62976
                                  20.33787 -1.654
                                                     0.1010
                                  18.38467 -1.849
## viewcat3
                     -33.98623
                                                     0.0672
## viewcat4
                     -12.80847
                                  20.00391
                                           -0.640
                                                     0.5233
## setting2
                      25.39476
                                  12.54023
                                             2.025
                                                     0.0452 *
                                           -0.694
## viewenc2
                      -9.74311
                                  14.04214
                                                     0.4892
## site2:sex2
                      -0.52039
                                  3.06238
                                           -0.170
                                                     0.8654
## site3:sex2
                                             0.848
                       2.53032
                                   2.98486
                                                     0.3984
## site4:sex2
                      -3.37095
                                   3.62448 -0.930
                                                     0.3543
## site5:sex2
                      -4.87172
                                   5.11219
                                           -0.953
                                                     0.3427
## site2:age
                       0.08205
                                   0.33065
                                            0.248
                                                     0.8045
## site3:age
                       0.16320
                                   0.23587
                                             0.692
                                                     0.4904
## site4:age
                       0.80312
                                   0.42105
                                             1.907
                                                     0.0590
## site5:age
                       1.15008
                                   0.46355
                                             2.481
                                                     0.0146 *
## site2:viewcat2
                                           -0.387
                                                     0.6996
                      -2.93114
                                   7.57584
## site3:viewcat2
                       5.06294
                                   5.34770
                                             0.947
                                                     0.3458
## site4:viewcat2
                       3.68884
                                             0.687
                                                     0.4933
                                   5.36739
## site5:viewcat2
                       5.58665
                                   8.64949
                                             0.646
                                                     0.5197
                                   7.09289
                                           -1.201
## site2:viewcat3
                      -8.51958
                                                     0.2322
## site3:viewcat3
                       0.53577
                                   5.04213
                                             0.106
                                                     0.9156
                                                     0.7338
## site4:viewcat3
                       1.94832
                                   5.71524
                                             0.341
## site5:viewcat3
                            NΑ
                                        NΑ
                                                NA
                                                         NA
## site2:viewcat4
                     -11.97418
                                   7.20383
                                            -1.662
                                                     0.0993
## site3:viewcat4
                       6.67420
                                   5.28661
                                             1.262
                                                     0.2094
## site4:viewcat4
                      -7.87519
                                   6.68380
                                           -1.178
                                                     0.2412
## site5:viewcat4
                      -2.47008
                                   9.12901
                                           -0.271
                                                     0.7872
```

0.969

0.3345

3.80212

site2:setting2

3.68492

```
## site3:setting2
                      -6.53049
                                  4.35461
                                           -1.500
                                                    0.1365
                      -3.60393
                                                    0.4223
## site4:setting2
                                  4.47448 -0.805
## site5:setting2
                            NA
                                       NA
                                               NA
                                                        NA
## site2:viewenc2
                      -3.02265
                                  3.58254
                                           -0.844
                                                    0.4006
## site3:viewenc2
                       3.51672
                                  4.54535
                                            0.774
                                                    0.4407
## site4:viewenc2
                       1.12474
                                  4.17152
                                           0.270
                                                    0.7879
## site5:viewenc2
                      12.00787
                                  9.75463
                                           1.231
                                                    0.2209
## sex2:age
                      -0.28474
                                  0.17403 - 1.636
                                                    0.1046
## sex2:viewcat2
                       1.58139
                                  3.64388
                                            0.434
                                                    0.6651
## sex2:viewcat3
                      1.22311
                                  3.45301
                                            0.354
                                                    0.7238
## sex2:viewcat4
                      -3.07878
                                  3.68935
                                          -0.835
                                                    0.4058
                                           -1.563
## sex2:setting2
                      -3.66101
                                  2.34297
                                                    0.1210
## sex2:viewenc2
                       1.89995
                                  2.66823
                                            0.712
                                                    0.4779
                       0.59861
## age:viewcat2
                                  0.36006
                                            1.663
                                                    0.0992
                                  0.32533
                                            2.075
                                                    0.0403 *
## age:viewcat3
                       0.67510
## age:viewcat4
                       0.32333
                                  0.35835
                                            0.902
                                                    0.3688
                                  0.21177
                                          -1.527
## age:setting2
                                                    0.1297
                      -0.32330
## age:viewenc2
                      -0.03592
                                  0.24933
                                           -0.144
                                                    0.8857
                                           -1.982
## viewcat2:setting2 -9.02471
                                  4.55447
                                                    0.0500 *
## viewcat3:setting2 -7.57750
                                  4.40886
                                           -1.719
                                                    0.0884
## viewcat4:setting2 -1.82366
                                  4.85327
                                          -0.376
                                                    0.7078
## viewcat2:viewenc2 10.57132
                                  4.87489
                                           2.169
                                                    0.0322 *
## viewcat3:viewenc2 11.25111
                                            2.446
                                  4.60050
                                                    0.0160 *
                                            1.391
## viewcat4:viewenc2
                       6.93655
                                  4.98500
                                                    0.1668
## setting2:viewenc2
                       1.22748
                                  3.19174
                                            0.385
                                                    0.7013
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.813 on 112 degrees of freedom
## Multiple R-squared: 0.4256, Adjusted R-squared: 0.1436
## F-statistic: 1.509 on 55 and 112 DF, p-value: 0.03404
AIC(lin.mod6.full)
## [1] 1114.029
yhat <- predict(lin.mod6.full, newdata = testing)</pre>
## Warning in predict.lm(lin.mod6.full, newdata = testing): prediction from a rank-
## deficient fit may be misleading
y.test <- testing[, "clasfDiff"]</pre>
# Test MSE
mean((yhat-y.test)^2)
```

Regression Tree Models

In the context of a regression tree, the deviance is simply the sum of the squared errors.

Model 1

[1] 65.41

```
set.seed(1)
```

```
reg.tree.1 <- tree(bodyDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.1)
##
## Regression tree:
## tree(formula = bodyDiff ~ site + sex + age + viewcat + setting +
       viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "site"
                "age"
                         "viewcat" "sex"
                                              "viewenc"
## Number of terminal nodes: 13
## Residual mean deviance: 14.16 = 2194 / 155
## Distribution of residuals:
              1st Qu.
       Min.
                        Median
                                     Mean
                                            3rd Qu.
## -11.08000 -2.45100 -0.06303
                                            2.16900 12.55000
                                  0.00000
plot(reg.tree.1)
text(reg.tree.1, pretty = 0)
            age 4 46.5
                                                  viewenc: 1
                                                            age ₹ 55.5
                                         view¢at: 1
viewcat: 2,3
                                              site: 3,5 viewcat: 2,4
                                      12.840
                                                                  10.080
                                 12.290
                                            14.9807.450
```

```
cv.reg.tree.1 <- cv.tree(reg.tree.1)
plot(cv.reg.tree.1$size, cv.reg.tree.1$dev, type = "b")</pre>
```

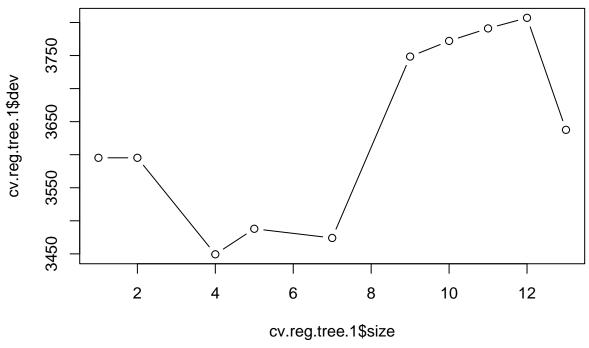
age < 53.5

11.9507.650

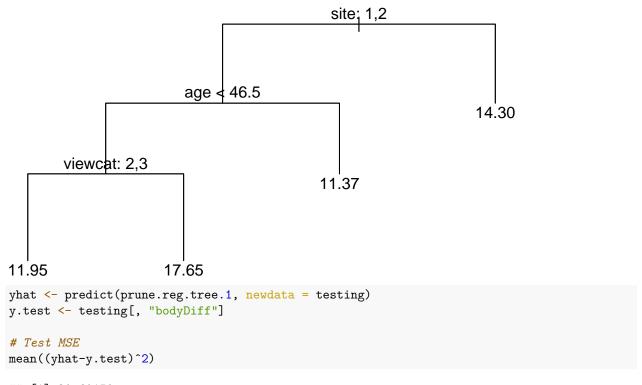
sex: 1

4.9419.7064.2400.150

10.0604.560

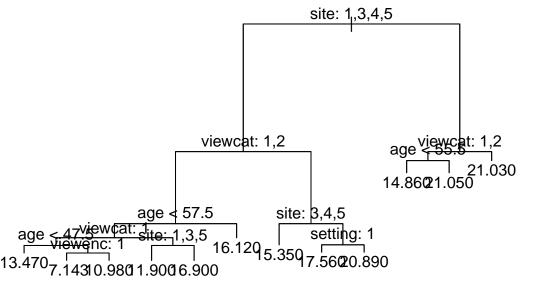


```
prune.reg.tree.1 <- prune.tree(reg.tree.1, best = 4)
plot(prune.reg.tree.1)
text(prune.reg.tree.1, pretty = 0)</pre>
```

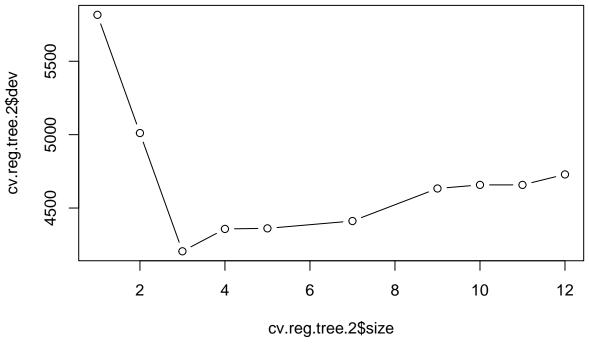


[1] 20.60159

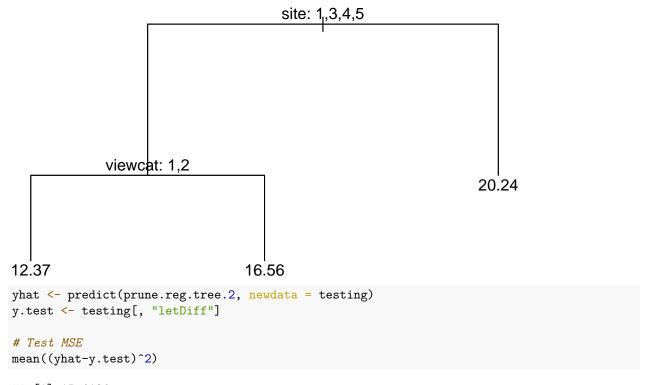
```
set.seed(1)
reg.tree.2 <- tree(letDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train)
summary(reg.tree.2)
##
## Regression tree:
## tree(formula = letDiff ~ site + sex + age + viewcat + setting +
##
      viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "site"
              "viewcat" "age"
                                   "viewenc" "setting"
## Number of terminal nodes: 12
## Residual mean deviance: 18.63 = 2906 / 156
## Distribution of residuals:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
## -17.560 -2.430
                   0.000
                            0.000
                                   2.765
                                            9.587
plot(reg.tree.2)
text(reg.tree.2, pretty = 0)
```



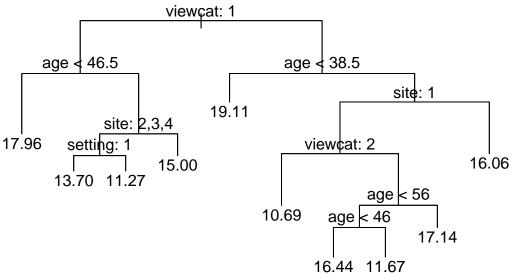
```
cv.reg.tree.2 <- cv.tree(reg.tree.2)
plot(cv.reg.tree.2$size, cv.reg.tree.2$dev, type = "b")</pre>
```



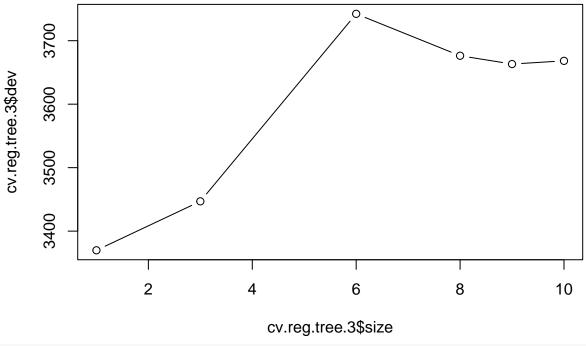
```
prune.reg.tree.2 <- prune.tree(reg.tree.2, best = 3)
plot(prune.reg.tree.2)
text(prune.reg.tree.2, pretty = 0)</pre>
```



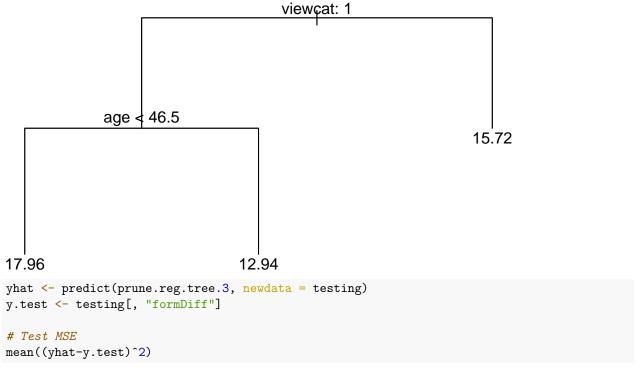
```
set.seed(1)
reg.tree.3 <- tree(formDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.3)
##
## Regression tree:
## tree(formula = formDiff ~ site + sex + age + viewcat + setting +
       viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "viewcat" "age"
                          "site"
                                     "setting"
## Number of terminal nodes: 10
## Residual mean deviance: 15.88 = 2509 / 158
## Distribution of residuals:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
## -11.610 -1.667
                            0.000
                   0.129
                                     2.159 13.940
plot(reg.tree.3)
text(reg.tree.3, pretty = 0)
```



```
cv.reg.tree.3 <- cv.tree(reg.tree.3)
plot(cv.reg.tree.3$size, cv.reg.tree.3$dev, type = "b")</pre>
```

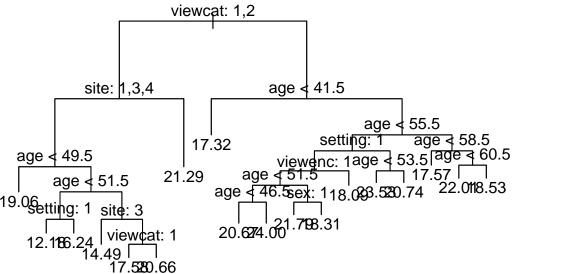


```
prune.reg.tree.3 <- prune.tree(reg.tree.3, best = 2)
plot(prune.reg.tree.3)
text(prune.reg.tree.3, pretty = 0)</pre>
```

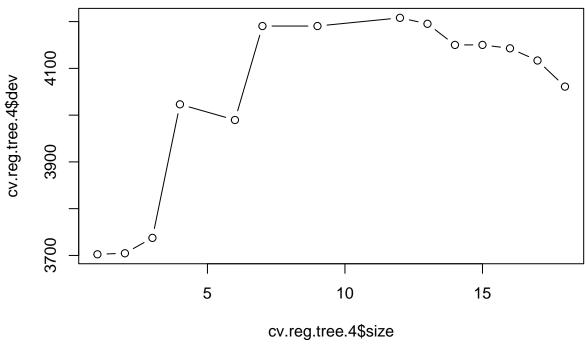


[1] 14.92273

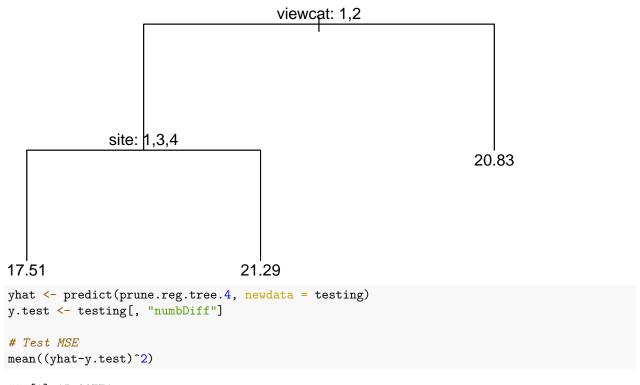
```
set.seed(1)
reg.tree.4 <- tree(numbDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.4)
##
## Regression tree:
## tree(formula = numbDiff ~ site + sex + age + viewcat + setting +
##
       viewenc, data = sesame.q1, subset = train)
## Number of terminal nodes: 18
## Residual mean deviance: 13.64 = 2046 / 150
## Distribution of residuals:
       Min. 1st Qu.
                     Median
                                 Mean 3rd Qu.
                                                    Max.
## -18.0900 -2.1210
                     0.2647
                                       2.1180 11.4700
                               0.0000
plot(reg.tree.4)
text(reg.tree.4, pretty = 0)
                        viewcat: 1,2
```



```
cv.reg.tree.4 <- cv.tree(reg.tree.4)
plot(cv.reg.tree.4$size, cv.reg.tree.4$dev, type = "b")</pre>
```



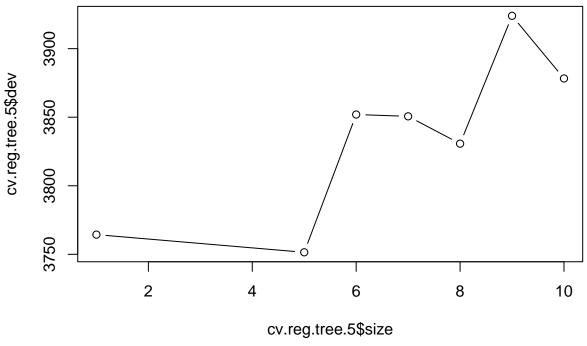
```
prune.reg.tree.4 <- prune.tree(reg.tree.4, best = 3)
plot(prune.reg.tree.4)
text(prune.reg.tree.4, pretty = 0)</pre>
```



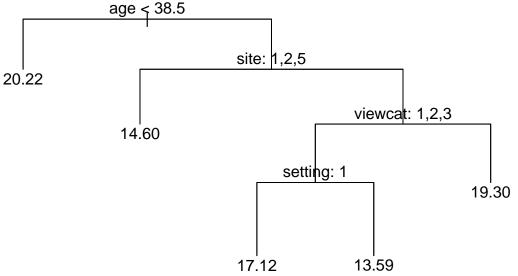
[1] 15.90771

```
set.seed(1)
reg.tree.5 <- tree(relatDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.5)
##
## Regression tree:
## tree(formula = relatDiff ~ site + sex + age + viewcat + setting +
       viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "age"
                 "site"
                          "viewcat" "setting" "sex"
## Number of terminal nodes: 10
## Residual mean deviance: 15.3 = 2418 / 158
## Distribution of residuals:
       Min. 1st Qu. Median
                                 Mean 3rd Qu.
                                                   Max.
## -10.6900 -1.5650 -0.2514 0.0000
                                       1.8950 11.4900
plot(reg.tree.5)
text(reg.tree.5, pretty = 0)
            age < 38.5
                          site: 1,2,5
20.22
                                              viewcalt: 1,2,3
       14.60
                                   setting: 1
                                                             age < 55
                                                           21.13 15.65
                         site: 3
                                                sex: 1
                              viewcat: 2,3
                                             15.82 12.47
                              17.93 21.39
```

```
cv.reg.tree.5 <- cv.tree(reg.tree.5)
plot(cv.reg.tree.5$size, cv.reg.tree.5$dev, type = "b")</pre>
```



```
prune.reg.tree.5 <- prune.tree(reg.tree.5, best = 5)
plot(prune.reg.tree.5)
text(prune.reg.tree.5, pretty = 0)</pre>
```

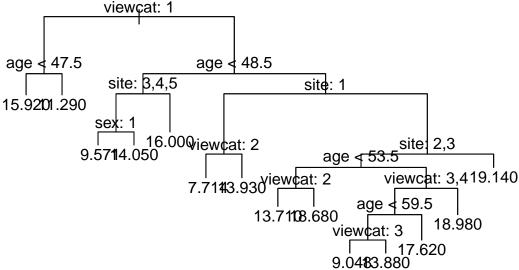


```
yhat <- predict(prune.reg.tree.5, newdata = testing)
y.test <- testing[, "relatDiff"]

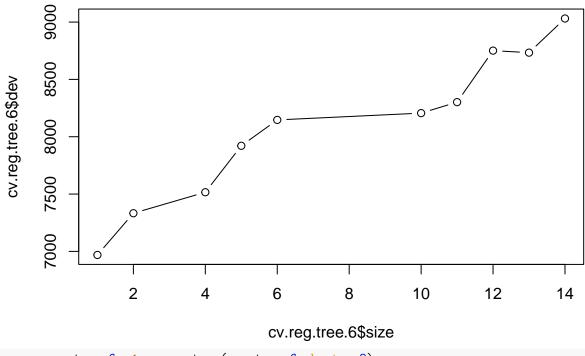
# Test MSE
mean((yhat-y.test)^2)</pre>
```

[1] 19.88506

```
set.seed(1)
reg.tree.6 <- tree(clasfDiff ~ site + sex + age + viewcat + setting + viewenc, sesame.q1, subset = train
summary(reg.tree.6)
##
## Regression tree:
## tree(formula = clasfDiff ~ site + sex + age + viewcat + setting +
       viewenc, data = sesame.q1, subset = train)
## Variables actually used in tree construction:
## [1] "viewcat" "age"
                          "site"
## Number of terminal nodes: 14
## Residual mean deviance: 29.66 = 4568 / 154
## Distribution of residuals:
       Min.
              1st Qu.
                         Median
                                      Mean
                                             3rd Qu.
                                                          Max.
## -16.00000 -3.17300 0.01852
                                             3.71400 13.10000
                                   0.00000
plot(reg.tree.6)
text(reg.tree.6, pretty = 0)
              viewçat: 1
```



```
cv.reg.tree.6 <- cv.tree(reg.tree.6)
plot(cv.reg.tree.6$size, cv.reg.tree.6$dev, type = "b")</pre>
```



```
prune.reg.tree.6 <- prune.tree(reg.tree.6, best = 2)
plot(prune.reg.tree.6)
text(prune.reg.tree.6, pretty = 0)</pre>
```

```
viewcat: 1

12.16

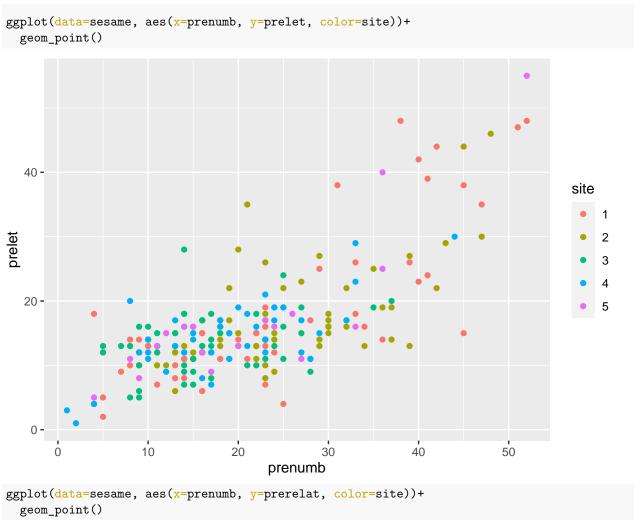
15.54

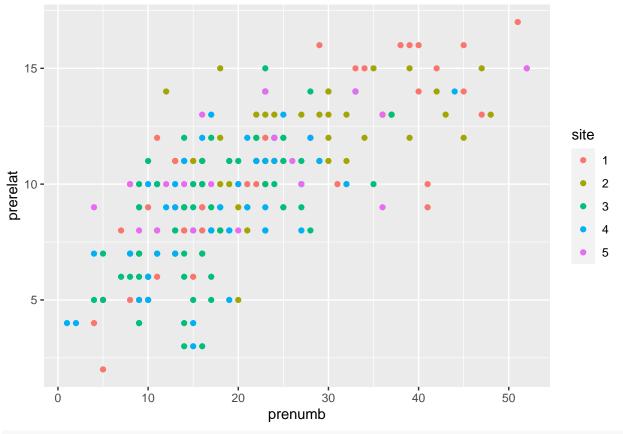
yhat <- predict(prune.reg.tree.6, newdata = testing)
y.test <- testing[, "clasfDiff"]

# Test MSE
mean((yhat-y.test)^2)
```

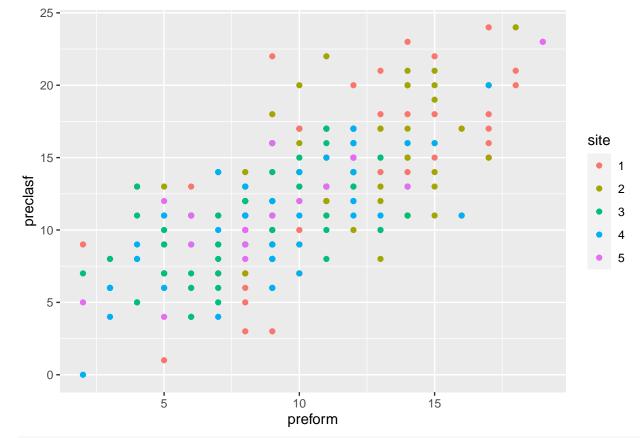
[1] 45.52784

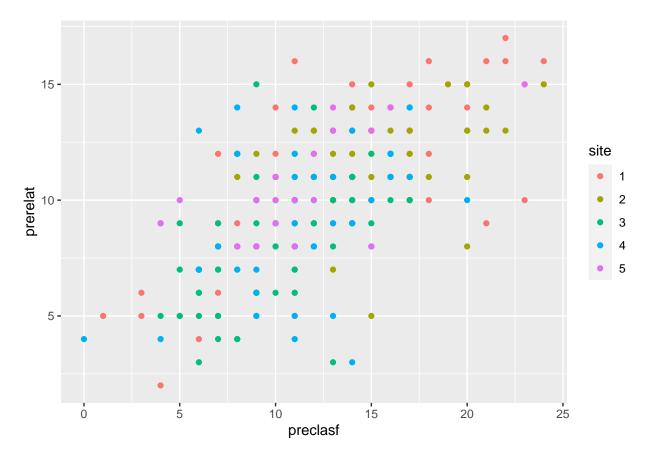
Q.2 Classification Question: Can we use the pre-test scores and other demographic variables to predict which region the children came from?





ggplot(data=sesame, aes(x=preform, y=preclasf, color=site))+
 geom_point()





SVM

```
set.seed(3241)
n <- nrow(sesame)</pre>
train.index <- sample(1:n, size = floor(0.7*n), replace=FALSE)</pre>
train.data <- sesame.sd[train.index,]</pre>
test.data <- sesame.sd[-train.index,]</pre>
train.data %>%
count(site)
##
     site n
## 1
        1 40
## 2
        2 42
## 3
        3 48
        4 25
## 4
## 5
        5 13
#1 60
#2 55
#3 64
#4 43
#5 18
total.weight <- 60+55+64+43+18
weight.1 <- total.weight/(5*60)</pre>
```

```
weight.2 <- total.weight/(5*55)</pre>
weight.3 <- total.weight/(5*64)</pre>
weight.4 <- total.weight/(5*43)</pre>
weight.5 <- total.weight/(5*18)</pre>
weight.4 <- 1.5
weight.5 <-3
# Response: site (categorical)
set.seed(315)
costs \leftarrow c(0.001, 0.01, 0.1, 1, 5, 10, 100)
# c(0.1, 0.2, 0.5, 0.7, 1, 2, 3, 4)
gammas \leftarrow seq(0, 4, by=0.1)
linear.tune <- tune(svm, site~female+ male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_pc
                     data=train.data, kernel="linear",
                     ranges=list(cost=costs),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5),
                     class.type="one.versus.one")
radial.tune <- tune(svm, site~female + male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_p
                     data=train.data, kernel="radial",
                     ranges=list(cost=costs,
                                  gamma=gammas),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5))
#radial.tune <- tune(sum, site~sex+age+prebody+prelet+preform+prenumb+prerelat+preclasf,
#
                      data=train.data, kernel="radial",
#
                      ranges=list(cost=costs,
#
                                  gamma=gammas))
sigmoid.tune <- tune(svm, site~female + male + sd_age+sd_pBod+sd_plet+sd_pform + sd_pnumb+sd_prelat+sd_
                     data=train.data, kernel="sigmoid",
                     ranges=list(cost=costs,
                                 gamma=gammas),
                     class.weights=c("1"=weight.1,
                                      "2"=weight.2,
                                      "3"=weight.3,
                                      "4"=weight.4,
                                      "5"=weight.5))
linear.conMatrix <- table(true=test.data[, "site"],</pre>
                           pred=predict(linear.tune$best.model, newdata=test.data))
radial.conMatrix <- table(true=test.data[, "site"],</pre>
                           pred=predict(radial.tune$best.model, newdata=test.data))
```

```
sigmoid.conMatrix <- table(true=test.data[, "site"],</pre>
                         pred=predict(sigmoid.tune$best.model, newdata=test.data))
confusionMatrix(linear.conMatrix)
## Confusion Matrix and Statistics
##
      pred
##
  true 1 2
              3
                 4
                   5
##
##
      1 6
           1 6 2 5
      2
        1
           7 1 1 3
##
##
     3 0 1 11 1 3
##
     4 3 3 9 3 0
##
     5 0 1 1 1 2
##
## Overall Statistics
##
##
                 Accuracy: 0.4028
##
                   95% CI: (0.2888, 0.525)
##
      No Information Rate: 0.3889
##
       P-Value [Acc > NIR] : 0.44844
##
##
                    Kappa: 0.2554
##
##
  Mcnemar's Test P-Value: 0.01728
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.60000 0.53846
                                          0.3929 0.37500 0.15385
                                           0.8864 0.76562 0.94915
## Specificity
                        0.77419 0.89831
## Pos Pred Value
                        0.30000 0.53846
                                           0.6875
                                                   0.16667
## Neg Pred Value
                        0.92308 0.89831
                                           0.6964
                                                   0.90741
                                                            0.83582
## Prevalence
                        0.13889 0.18056
                                           0.3889
                                                   0.11111
                                                            0.18056
## Detection Rate
                        0.08333 0.09722
                                           0.1528
                                                   0.04167
                                                            0.02778
## Detection Prevalence 0.27778 0.18056
                                           0.2222 0.25000
                                                            0.06944
## Balanced Accuracy
                        0.68710 0.71838
                                           0.6396 0.57031
                                                            0.55150
confusionMatrix(radial.conMatrix)
## Confusion Matrix and Statistics
##
      pred
##
## true 1
           2
              3
                 4
                    5
##
        6
           2
              7
                 4
        4
##
      2
           4 3
                 0 2
##
        1
                 3 0
           1 11
        2
           2
##
      4
              9
                 4
                    1
##
        0
           2
              1
##
## Overall Statistics
##
##
                 Accuracy : 0.3611
##
                   95% CI: (0.2512, 0.4829)
##
      No Information Rate: 0.4306
```

```
##
      P-Value [Acc > NIR] : 0.9056
##
                    Kappa: 0.181
##
##
##
   Mcnemar's Test P-Value: 0.1807
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.46154 0.36364
                                           0.3548 0.33333
                                                            0.20000
## Specificity
                        0.76271 0.85246
                                           0.8780
                                                   0.76667
                                                            0.94030
## Pos Pred Value
                        0.30000 0.30769
                                           0.6875
                                                   0.22222
                                                            0.20000
## Neg Pred Value
                        0.86538 0.88136
                                           0.6429
                                                   0.85185
                                                            0.94030
                                           0.4306
## Prevalence
                        0.18056 0.15278
                                                   0.16667
                                                            0.06944
## Detection Rate
                        0.08333 0.05556
                                           0.1528
                                                   0.05556
                                                            0.01389
## Detection Prevalence
                        0.27778 0.18056
                                           0.2222
                                                   0.25000
                                                            0.06944
## Balanced Accuracy
                        0.61213 0.60805
                                           0.6164 0.55000
                                                            0.57015
confusionMatrix(sigmoid.conMatrix)
## Confusion Matrix and Statistics
##
##
      pred
##
  true 1 2
              3
                 4
                    5
##
     1
       1 1 6 9 3
     2
##
        1
           3 4 5 0
##
     3
       1 0 4 11 0
##
     4 0 0 7 11 0
##
     5 0 0 3 2
##
## Overall Statistics
##
##
                 Accuracy: 0.2639
##
                   95% CI: (0.167, 0.381)
##
      No Information Rate: 0.5278
##
      P-Value [Acc > NIR] : 1
##
                    Kappa: 0.0434
##
##
   Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.33333 0.75000 0.16667
                                                    0.2895 0.00000
                        0.72464 0.85294 0.75000
## Specificity
                                                    0.7941
                                                            0.92754
## Pos Pred Value
                        0.05000 0.23077 0.25000
                                                    0.6111
                                                            0.00000
## Neg Pred Value
                        0.96154 0.98305
                                         0.64286
                                                    0.5000
                                                            0.95522
## Prevalence
                        0.04167
                                0.05556
                                          0.33333
                                                    0.5278
                                                            0.04167
## Detection Rate
                        0.01389 0.04167
                                          0.05556
                                                    0.1528
                                                            0.00000
## Detection Prevalence 0.27778 0.18056
                                          0.22222
                                                    0.2500
                                                            0.06944
## Balanced Accuracy
                        0.52899 0.80147
                                          0.45833
                                                    0.5418 0.46377
```

```
predict(linear.tune$best.model, newdata=test.data)
##
         7
             8
                 9
                    12
                        16
                            19
                                 22
                                     24
                                         25
                                             29
                                                 38
                                                     42
                                                         43
                                                              46
                                                                  48
                                                                      54
                                                                          56
                                                                              57
                                                                                  59
     6
                                  2
                                      5
                                          5
                                              5
                                                               3
                                                                   3
                                                                       3
                                                                           5
##
     1
         4
                 1
                     5
                         1
                              1
                                                  3
                                                      1
                                                           4
                                                                               3
                                                                                   3
                                                    113 116 118 120 125
                                                                        127
##
    64
        82
            84
                88
                    92
                        93
                            94
                                 98
                                     99 100
                                           104 106
                                                                             128
                                                                                 137
##
     5
         1
             4
                 2
                     2
                         2
                              2
                                  2
                                      5
                                          3
                                              5
                                                  2
                                                      2
                                                           4
                                                               3
                                                                   3
                                                                       3
                                                                           5
                                                                               3
                                                                                   3
   139
      143 145
               152 156 162 164
                               172 176 180 181 182 183 187
                                                            188
                                                                189
                                                                     190 191
                                                                             192 193
##
                              3
##
                 3
                         3
                                  3
                                      5
                                          3
                                              3
                                                               3
                                                                   3
##
  196 202 207 208 212 221 222 225 226 227
                                            234
                                                235
         2
             3
                 3
                         3
                              1
                                  5
                                      3
                                              5
## Levels: 1 2 3 4 5
predict(radial.tune$best.model, newdata=test.data)
##
     6
         7
             8
                    12
                        16
                             19
                                 22
                                     24
                                         25
                                             29
                                                 38
                                                     42
                                                         43
                                                              46
                                                                  48
                                                                      54
                                                                          56
                                                                              57
                                                                                  59
                                                      2
                     2
                                      3
                                              3
                                                               5
                                                                   3
                                                                       4
                                                                                   3
##
     3
         3
             1
                 1
                         4
                              4
                                  4
                                          3
                                                  1
                                                           1
                                                                           1
##
    64
        82
            84
                88
                    92
                        93
                            94
                                 98
                                     99 100 104
                                                106
                                                    113 116 118 120 125
                                                                        127
                                                                             128
                                                                                 137
                         2
##
     3
         1
             1
                 2
                     1
                              5
                                  2
                                      5
                                          3
                                              3
                                                  2
                                                           1
                                                                   3
                                                                       3
                                                                           3
  139 143 145 152 156 162 164 172
                                   176 180 181 182 183 187
                                                            188
                                                                189 190 191 192 193
##
                                                           2
                                                               3
##
         4
             3
                 3
                     3
                         3
                              3
                                  3
                                      2
                                          3
                                              3
                                                  3
                                                      3
                                                                   3
                                                                       3
                                                                           3
                                                                                   2
  196 202 207 208 212 221 222 225 226 227
##
                                            234
                                                235
                         3
                                      3
## Levels: 1 2 3 4 5
predict(sigmoid.tune$best.model, newdata=test.data)
##
                 9
                        16
                            19
                                 22
                                     24
                                         25
                                             29
                                                 38
                                                     42
                                                         43
                                                              46
                                                                  48
                                                                      54
                                                                          56
                                                                              57
                                                                                  59
             8
                    12
     5
         3
                 3
                                  2
                                      3
                                              5
                                                      4
                                                               3
                                                                           5
##
             3
                         1
                              4
                                          4
                                                  4
                                                           4
                                                                   4
                                                                       4
                                                                               3
##
    64
        82
                88
                    92
                        93
                            94
                                 98
                                     99 100 104 106 113 116 118 120 125
                                                                        127 128 137
            84
                         2
##
     4
         3
             4
                 3
                     3
                              1
                                  2
                                      4
                                          4
                                              4
                                                  3
                                                      2
                                                           4
                                                               4
                                                                   3
                                                                       4
##
   139
       143
           145
               152 156 162 164
                               172
                                    176
                                        180
                                            181
                                                182 183 187
                                                            188
                                                                189
                                                                     190
                                                                         191
                                                                             192 193
##
         3
             4
                         4
                              3
                                  4
                                      4
                                          4
                                              4
                                                           3
  196 202 207
               208 212 221 222 225 226 227
                                            234
                                                235
##
             4
                 3
                     3
                         4
                              3
                                  3
                                      4
                                          3
## Levels: 1 2 3 4 5
test.data$site
    ## Levels: 1 2 3 4 5
```

Radial kernel improves prediction on class 1.

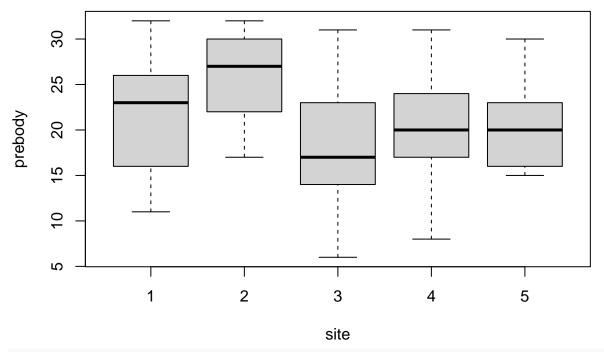
RBF slightly improved after standardizing? (it seems slightly more likely to predict on class 1.) thought, simpler models still retain the same performance (arguably better) sd_age+sd_pBod+sd_plet. But we are still not getting any prediction on class 4 & 5.

After assign class weights using this formula:

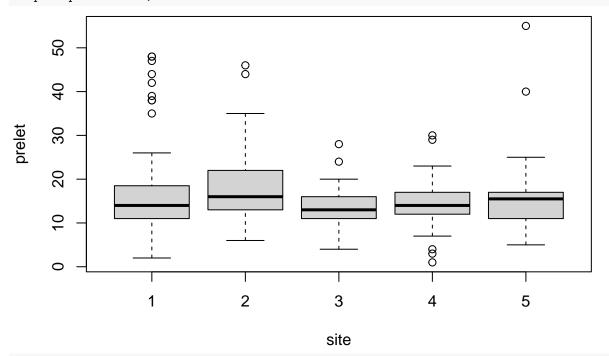
$$w_j = \frac{n}{kn_j}$$
, n is total number of data points, k is number of classes

Our model begins to make predictions on class 4 & class 5, though at the cost of overall accuracy. If we increase the weight for 4 & 5 to 1.5 and 3 respectively the performance of Radial SVM decreases but that of linear SVM increases to be comparable to Radial SVM's recorded highest accuracy (a little bit over 0.40).

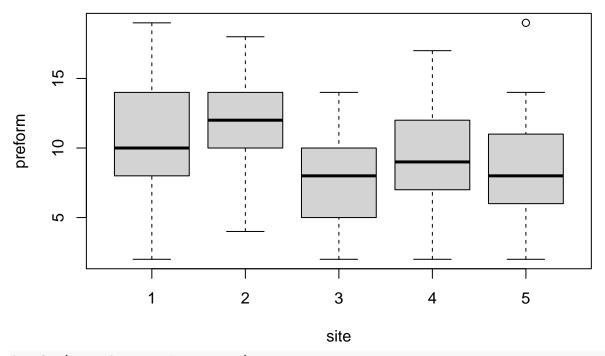
trying to do more EDA to see if anything explains why the data is not linearly separable boxplot(prebody~site, data=sesame)



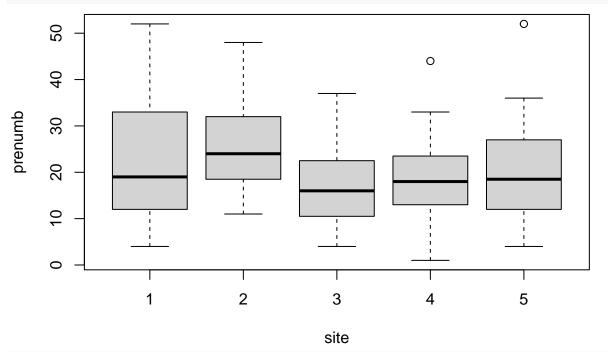
boxplot(prelet~site, data=sesame)



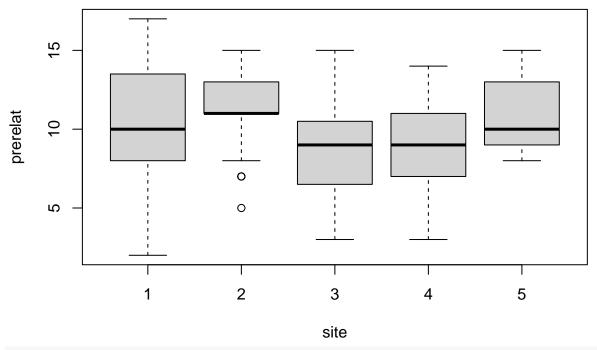
boxplot(preform~site, data=sesame)



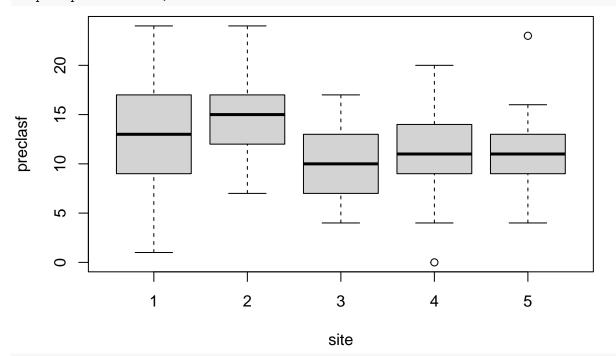
boxplot(prenumb~site, data=sesame)



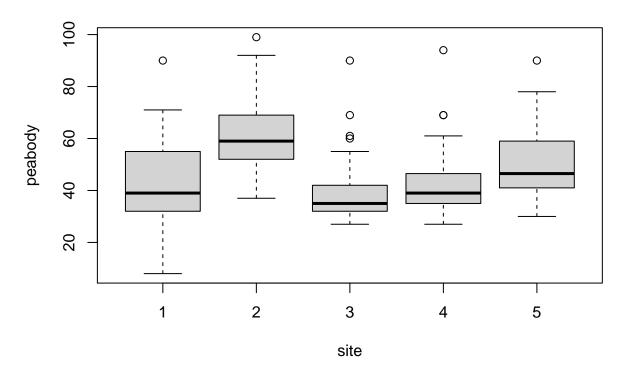
boxplot(prerelat~site, data=sesame)



boxplot(preclasf~site, data=sesame)



boxplot(peabody~site, data=sesame)

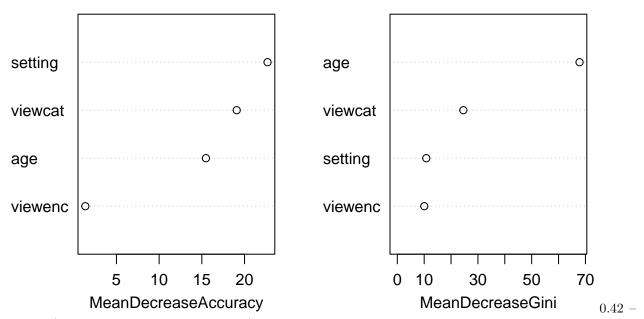


Trees

```
set.seed(3215)
#tree.data <- sesame %>%
# select(site, sex, age, viewcat, setting, viewenc, prebody, prelet, preform,
#
          prenumb, prerelat, preclasf)
n <- nrow(sesame)</pre>
train.index <- sample(1:n, size = floor(0.7*n), replace=FALSE)</pre>
#train.tree <- tree.data[train.index,]</pre>
#test.tree <- tree.data[-train.index,]</pre>
# "viewcat", "setting", "viewenc",
#, "prebody", "prelet", "preform", "prenumb", "prerelat", "preclasf", "postbody", "postlet", "postform",
tree.features <- c("site", "age", "viewcat", "setting", "viewenc")</pre>
tree.data <- sesame[, tree.features]</pre>
train.data <- tree.data[train.index,]</pre>
test.data <- tree.data[-train.index,]</pre>
rf.tree<- randomForest(site~., data=tree.data, subset=train.index,</pre>
                        mtry=4, importance=TRUE)
importance(rf.tree)
##
                                                               5 MeanDecreaseAccuracy
           16.071180 11.5639655 1.533526 10.24956 -12.646482
                                                                             15.477245
## viewcat 1.412544 8.8509648 4.714890 26.85440 -5.674656
                                                                             19.084980
## setting 9.950184 0.7116516 11.570042 20.04012
                                                                             22.690481
                                                        6.879913
## viewenc 1.061428 -1.4942151 6.283556 -2.36010 -3.154027
                                                                             1.353554
##
           MeanDecreaseGini
```

```
## age
                  67.80480
## viewcat
                  24.57478
## setting
                  10.77912
## viewenc
                  10.03605
rf.pred <- predict(rf.tree, newdata=test.data)</pre>
tree.conMatrix <- table(true=test.data[,"site"],</pre>
                        pred=rf.pred)
confusionMatrix(tree.conMatrix)
## Confusion Matrix and Statistics
##
##
      pred
## true 1 2 3 4 5
##
     1 10 2 3
                 3 0
##
     2 4 10 1 1 2
     3 2 3 11 3 0
##
     4 1 1 3 5 2
##
##
       0 1 3 0 1
##
## Overall Statistics
##
##
                 Accuracy : 0.5139
##
                   95% CI: (0.3931, 0.6335)
##
      No Information Rate: 0.2917
      P-Value [Acc > NIR] : 6.203e-05
##
##
##
                    Kappa: 0.3706
##
## Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
                       Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
##
## Sensitivity
                         0.5882   0.5882   0.5238   0.41667   0.20000
## Specificity
                         0.8545
                                  0.8545
                                           0.8431 0.88333 0.94030
## Pos Pred Value
                                  0.5556
                                           0.5789
                                                   0.41667
                                                            0.20000
                         0.5556
                                                            0.94030
## Neg Pred Value
                         0.8704 0.8704
                                           0.8113 0.88333
## Prevalence
                         0.2361
                                  0.2361
                                           0.2917
                                                   0.16667
                                                            0.06944
## Detection Rate
                         0.1389 0.1389
                                           0.1528
                                                   0.06944
                                                            0.01389
## Detection Prevalence
                         0.2500
                                  0.2500
                                           0.2639
                                                   0.16667
                                                            0.06944
## Balanced Accuracy
                         0.7214
                                  0.7214
                                           0.6835 0.65000
                                                            0.57015
varImpPlot(rf.tree)
```

rf.tree



0.5139 (but not including the test scores.) around 0.45-0.48, when including the pretest scores.

As seen in the table above, there is a notable discrepancy in the number of observations that lay in classes 4 and 5 for the variable site. More specifically, in the training data, there are just 25 observations with a value of 4 for the variable site and just 13 observations with a value of 5 for the variable site. In other words, there are less disadvantaged rural children and disadvantaged Spanish speaking children.

Consequently, when we initially ran our random forest model, our model was performing worse for test observations that take on the values 4 or 5 for the variable site.

To remedy this problem, we decided to use Synthetic Minority Oversampling Technique (SMOTE). SMOTE works by generating new samples in the classes of the response variable that are less represented. These new samples are generated using linear combinations of the "k" nearest neighbors in a given class. In this instance, we set k = 5.

```
train.data$age <- as.numeric(train.data$age)
train.data$viewcat <- as.numeric(train.data$viewcat)
train.data$setting <- as.numeric(train.data$setting)
train.data$viewenc <- as.factor(train.data$viewenc)

test.data$age <- as.numeric(test.data$age)
test.data$viewcat <- as.numeric(test.data$viewcat)
test.data$viewcat <- as.numeric(test.data$viewcat)
test.data$viewenc <- as.factor(test.data$viewenc)

balanced.train.data <- SmoteClassif(site ~ ., train.data, k = 5, repl = FALSE, dist = "HEOM")
    # k --> represents the number of nearest neighbors (5) used to generate new examples of the minority
    # repl = FALSE --> cannot have repetition of examples when performing under-sampling by selecting amo

balanced.train.data %>%
    count(site)
```

```
##
     site n
## 1
        1 34
## 2
        2 34
## 3
        3 34
## 4
        4 33
## 5
        5 34
rf.tree<- randomForest(site~., data=balanced.train.data,</pre>
                       mtry=4, importance=TRUE)
importance(rf.tree)
##
                                        3
                                                            5 MeanDecreaseAccuracy
## age
           15.112165 11.5044815 2.831522 12.2530454 12.35896
                                                                          24.534350
## viewcat 2.482319 12.5671060 5.114628 28.5410065 19.94849
                                                                          32.088862
## setting 14.672536  0.4233347  5.467389  22.8438707  32.97928
                                                                          34.377861
## viewenc 5.604315 -2.5081007 6.322412 0.1078161 12.91417
                                                                           9.960821
##
           MeanDecreaseGini
## age
                  73.124641
                  29.595993
## viewcat
                   9.359814
## setting
## viewenc
                   9.254742
rf.pred <- predict(rf.tree, newdata=test.data)</pre>
tree.conMatrix <- table(true=test.data[,"site"],</pre>
                         pred=rf.pred)
confusionMatrix(tree.conMatrix)
## Confusion Matrix and Statistics
##
##
       pred
## true 1 2 3 4 5
      1 7 4 3 2 2
##
      2 4 8 1 2 3
      3 3 4 9 2 1
##
      4 0 2 3 5 2
##
##
      5 0 2 2 0 1
##
## Overall Statistics
##
##
                  Accuracy : 0.4167
##
                    95% CI: (0.3015, 0.5389)
##
       No Information Rate: 0.2778
##
       P-Value [Acc > NIR] : 0.007741
##
##
                     Kappa: 0.2539
##
##
  Mcnemar's Test P-Value: 0.576888
##
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                         0.50000 0.4000 0.5000 0.45455 0.11111
## Specificity
                         0.81034
                                    0.8077
                                             0.8148 0.88525 0.93651
```

```
## Pos Pred Value
                        0.38889
                                 0.4444
                                          0.4737 0.41667
                                                           0.20000
## Neg Pred Value
                        0.87037 0.7778
                                          0.8302 0.90000
                                                           0.88060
## Prevalence
                        0.19444 0.2778
                                          0.2500 0.15278
                                                           0.12500
## Detection Rate
                        0.09722
                                 0.1111
                                           0.1250
                                                  0.06944
                                                           0.01389
## Detection Prevalence
                        0.25000
                                  0.2500
                                           0.2639
                                                  0.16667
                                                           0.06944
## Balanced Accuracy
                        0.65517
                                  0.6038
                                          0.6574 0.66990 0.52381
```

While the SmoteClassif() function certainly did its job by balancing out the number of observations for each value of site in the training data, the new random forest model (fitted to this new data set) is less accurate and sees little improvement in the detection of site values of 4 and 5.

```
# set.seed(3215)
##, "prebody", "prelet", "preform", "prenumb", "prerelat", "preclasf", "postbody", "postlet", "postform
#
#
# features <- c("site", "age", "viewcat", "setting", "viewenc", "prebody", "prelet", "preform", "prenumb"
# tree.2 <- sesame[, features]</pre>
# train.2 <- tree.2[train.index,]</pre>
# test.2 <- tree.2[-train.index,]</pre>
# boost.tree <- gbm(site ~., data=train.2,
#
                     distribution="multinomial", n.trees=5000,
#
                     interaction.depth=1)
#
# #y.boost <- table(true=test.2[, "site"],
# #
                     pred=predict(boost.tree, newdata=test.2))
#
# boost.conMatrix <- table(true=test.2$site,</pre>
                            pred=predict(boost.tree, newdata=test.2))
# confusionMatrix(boost.conMatrix)
```

Logistic Regression

iter 40 value 186.948903 ## iter 50 value 186.213534 ## iter 60 value 186.148958 ## iter 70 value 186.146812

```
# ,"prebody", "prelet","preform", "prenumb", "prerelat", "preclasf", "postbody", "postlet", "postform",
tree.features <- c("site", "age", "viewcat", "setting", "viewenc","prebody", "prelet","preform", "prenume tree.log <- sesame[, tree.features]
train.log <- tree.log[train.index,]
test.log <- tree.log[-train.index,]
multinom.log <- multinom(factor(site)~., data=train.log)

## weights: 60 (44 variable)
## initial value 270.385569
## iter 10 value 224.661284
## iter 20 value 205.001057
## iter 30 value 193.994082</pre>
```

```
## iter 70 value 186.146811
## iter 70 value 186.146811
## final value 186.146811
## converged
summary(multinom.log)
## Call:
## multinom(formula = factor(site) ~ ., data = train.log)
## Coefficients:
##
   (Intercept)
                     age viewcat
                                     setting
                                                 viewenc
## 2 -2.33155723 -0.02851059 0.1671689 -0.1723663 -0.4205104 0.18169812
## 3 0.05755516 0.20107446 0.0726002 -1.4396594 -1.5937567 -0.10132305
## 4 0.52070488 0.14041265 -1.1560807 -0.2744569 -1.3458286 -0.08902983
prelet
                   preform
                                prenumb
                                          prerelat
                                                    preclasf
## 2 -0.021574850 -0.12985947 -0.0781747329 0.16740257 0.10875790
## 3 -0.009618286 -0.32080214 -0.0307718697 0.05942666 -0.08062801
## 5 0.149877507 -0.31580541 -0.1020246788 0.34854595 -0.12639855
##
## Std. Errors:
    (Intercept)
                     age viewcat
                                   setting
                                            viewenc
                                                      prebody
## 2
      2.539808 0.05877122 0.2735599 0.6038785 0.6013929 0.07166225 0.03755288
      2.552263 0.06296057 0.2800905 0.6392345 0.6272709 0.07157933 0.05105309
## 3
      2.743404 0.06311748 0.3228949 0.6489907 0.6712331 0.07501958 0.04404500
## 5
    2.206224 0.08353394 0.4579698 2.2063318 0.9368912 0.09992158 0.07033801
               prenumb prerelat
      preform
                                preclasf
## 2 0.1144522 0.05108224 0.1361291 0.08630272
## 3 0.1256428 0.05602075 0.1440701 0.09338212
## 4 0.1173569 0.05356710 0.1389164 0.09183664
## 5 0.1771026 0.08446858 0.2087433 0.14707062
## Residual Deviance: 372.2936
## AIC: 460.2936
tabs <- table(true=test.log[, "site"],</pre>
            pred=predict(multinom.log,newdata=test.log))
confusionMatrix(tabs)
## Confusion Matrix and Statistics
##
##
      pred
## true 1 2 3 4 5
     1 3 4 8 3 0
##
##
     2 8 7 2 1 0
     3 2 3 12 2 0
##
     4 0 1 4
##
##
     5 0 0 2 1 2
## Overall Statistics
##
##
                Accuracy : 0.4167
##
                 95% CI: (0.3015, 0.5389)
```

```
##
      No Information Rate: 0.3889
##
      P-Value [Acc > NIR] : 0.3557
##
##
                    Kappa: 0.2396
##
##
  Mcnemar's Test P-Value : NA
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.23077 0.46667
                                           0.4286 0.46154 0.66667
## Specificity
                        0.74576 0.80702
                                           0.8409
                                                   0.89831
                                                            0.95652
## Pos Pred Value
                        0.16667 0.38889
                                           0.6316
                                                   0.50000
                                                            0.40000
## Neg Pred Value
                                                   0.88333
                        0.81481 0.85185
                                           0.6981
                                                            0.98507
## Prevalence
                        0.18056 0.20833
                                           0.3889
                                                   0.18056
                                                            0.04167
## Detection Rate
                        0.04167 0.09722
                                           0.1667
                                                   0.08333
                                                            0.02778
## Detection Prevalence 0.25000 0.25000
                                           0.2639
                                                   0.16667
                                                            0.06944
## Balanced Accuracy
                        0.48827 0.63684
                                           0.6347
                                                   0.67992
                                                            0.81159
##forward selection
log.tune <- train(site~(.)^2, data=train.log, method="multinom", direction="forward",
                 k = log(3562)
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 223.009710
## iter 20 value 185.817438
## iter 30 value 164.746276
## iter 40 value 142.208692
## iter 50 value 114.120976
## iter 60 value 105.061057
## iter 70 value 96.136366
## iter 80 value 86.279565
## iter 90 value 68.226344
## iter 100 value 56.986576
## final value 56.986576
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 223.009765
## iter 20 value 185.818463
## iter 30 value 164.749701
## iter 40 value 142.227179
## iter 50 value 114.217355
## iter 60 value 105.233432
## iter 70 value 96.390732
## iter 80 value 85.327276
## iter 90 value 70.002063
## iter 100 value 59.270525
## final value 59.270525
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 223.009710
```

iter 20 value 185.817439

```
## iter 30 value 164.746280
## iter 40 value 142.208711
## iter 50 value 114.121072
## iter 60 value 105.061229
## iter 70 value 96.136613
## iter 80 value 86.280792
## iter 90 value 68.229713
## iter 100 value 56.993283
## final value 56.993283
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 173.938475
## iter 20 value 138.721492
## iter 30 value 121.837401
## iter 40 value 102.694977
## iter 50 value 87.793408
## iter 60 value 78.834826
## iter 70 value 69.705169
## iter 80 value 60.078338
## iter 90 value 49.433061
## iter 100 value 30.412960
## final value 30.412960
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 173.938525
## iter 20 value 138.722238
## iter 30 value 121.840535
## iter 40 value 102.713762
## iter 50 value 87.856776
## iter 60 value 78.916581
## iter 70 value 71.245467
## iter 80 value 61.578500
## iter 90 value 49.020816
## iter 100 value 35.855958
## final value 35.855958
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 173.938475
## iter 20 value 138.721493
## iter 30 value 121.837404
## iter 40 value 102.694996
## iter 50 value 87.793471
## iter 60 value 78.834899
## iter 70 value 69.705169
## iter 80 value 60.081440
## iter 90 value 49.429589
## iter 100 value 30.613095
## final value 30.613095
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
```

```
## iter 10 value 196.128288
## iter 20 value 152.338821
## iter 30 value 134.098144
## iter 40 value 120.528256
## iter 50 value 107.006267
## iter 60 value 97.433053
## iter 70 value 91.319595
## iter 80 value 80.124846
## iter 90 value 66.699682
## iter 100 value 51.368028
## final value 51.368028
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 196.128329
## iter 20 value 152.339603
## iter 30 value 134.101185
## iter 40 value 120.542755
## iter 50 value 107.075877
## iter 60 value 97.622659
## iter 70 value 90.390179
## iter 80 value 79.683704
## iter 90 value 68.002823
## iter 100 value 53.884570
## final value 53.884570
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 196.128288
## iter 20 value 152.338822
## iter 30 value 134.098147
## iter
       40 value 120.528271
## iter 50 value 107.006336
## iter 60 value 97.433244
## iter 70 value 91.320015
## iter 80 value 80.124455
## iter 90 value 66.695323
## iter 100 value 52.559315
## final value 52.559315
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 189.587833
## iter 20 value 163.400377
## iter 30 value 149.397008
## iter 40 value 130.865745
## iter 50 value 118.037225
## iter
       60 value 102.868952
## iter 70 value 92.450294
## iter 80 value 81.333564
## iter 90 value 66.847399
## iter 100 value 54.770259
## final value 54.770259
## stopped after 100 iterations
```

```
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 189.587869
## iter 20 value 163.400999
## iter 30 value 149.399651
## iter 40 value 130.879708
## iter 50 value 118.074280
## iter 60 value 103.060569
## iter 70 value 92.686823
## iter 80 value 82.398605
## iter 90 value 70.243125
## iter 100 value 56.884732
## final value 56.884732
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 189.587833
## iter 20 value 163.400378
## iter 30 value 149.397010
## iter 40 value 130.865759
## iter 50 value 118.037262
## iter 60 value 102.869143
## iter 70 value 92.450438
## iter 80 value 81.335289
## iter 90 value 66.849983
## iter 100 value 54.773938
## final value 54.773938
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 218.066994
## iter 20 value 166.160778
## iter 30 value 147.813821
## iter 40 value 126.512571
## iter 50 value 105.678336
## iter 60 value 92.005056
## iter 70 value 76.732392
## iter 80 value 65.655736
## iter 90 value 52.831643
## iter 100 value 41.316977
## final value 41.316977
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 218.067049
## iter 20 value 166.161877
## iter 30 value 147.817302
## iter
       40 value 126.532313
## iter 50 value 106.035090
## iter 60 value 92.573822
## iter 70 value 77.440839
## iter 80 value 66.671660
## iter 90 value 57.517909
## iter 100 value 46.862520
```

```
## final value 46.862520
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 218.066994
## iter 20 value 166.160780
## iter 30 value 147.813825
## iter 40 value 126.512591
## iter 50 value 105.678677
## iter 60 value 92.005568
## iter 70 value 76.732185
## iter 80 value 65.656811
## iter 90 value 52.829713
## iter 100 value 41.436199
## final value 41.436199
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 187.347617
## iter 20 value 167.486745
## iter 30 value 154.146359
## iter 40 value 139.480057
## iter 50 value 122.619656
## iter 60 value 110.529375
## iter 70 value 102.625116
## iter 80 value 90.421158
## iter 90 value 74.054788
## iter 100 value 57.909803
## final value 57.909803
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 187.347643
## iter 20 value 167.487082
## iter 30 value 154.148036
## iter 40 value 139.492855
## iter 50 value 122.826896
## iter 60 value 110.867861
## iter 70 value 102.854835
## iter 80 value 92.576101
## iter 90 value 77.396820
## iter 100 value 64.941930
## final value 64.941930
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 187.347617
## iter 20 value 167.486745
## iter 30 value 154.146360
## iter 40 value 139.480070
## iter 50 value 122.619857
## iter 60 value 110.529704
## iter 70 value 102.625311
## iter 80 value 90.422822
```

```
## iter 90 value 74.054983
## iter 100 value 57.934475
## final value 57.934475
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 208.590047
## iter 20 value 174.245490
## iter 30 value 157.555386
## iter 40 value 129.021489
## iter 50 value 109.837072
## iter 60 value 93.512606
## iter 70 value 81.991673
## iter 80 value 74.052179
## iter 90 value 60.298671
## iter 100 value 48.252392
## final value 48.252392
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 208.590094
## iter 20 value 174.246094
## iter 30 value 157.557920
## iter 40 value 129.041017
## iter 50 value 110.099794
## iter 60 value 95.257380
## iter 70 value 84.712232
## iter 80 value 76.674761
## iter 90 value 63.088355
## iter 100 value 48.790899
## final value 48.790899
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 208.590047
## iter 20 value 174.245490
## iter 30 value 157.555389
## iter 40 value 129.021509
## iter 50 value 109.837330
## iter 60 value 93.513161
## iter 70 value 81.992850
## iter 80 value 74.053951
## iter 90 value 60.302615
## iter 100 value 48.251118
## final value 48.251118
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 198.318184
## iter 20 value 175.950870
## iter 30 value 165.501135
## iter 40 value 147.679228
## iter 50 value 135.519155
## iter 60 value 124.002190
```

```
## iter 70 value 113.636452
## iter 80 value 99.187196
## iter 90 value 80.973452
## iter 100 value 67.940819
## final value 67.940819
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 198.318211
## iter 20 value 175.951353
## iter 30 value 165.503279
## iter 40 value 147.694380
## iter 50 value 135.553180
## iter 60 value 124.189654
## iter 70 value 114.073441
## iter 80 value 100.694573
## iter 90 value 84.427530
## iter 100 value 69.210273
## final value 69.210273
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 198.318184
## iter 20 value 175.950870
## iter 30 value 165.501137
## iter 40 value 147.679243
## iter 50 value 135.519189
## iter 60 value 124.002378
## iter 70 value 113.636894
## iter 80 value 99.188748
## iter 90 value 80.977323
## iter 100 value 67.968767
## final value 67.968767
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.878402
## iter 20 value 160.411948
## iter 30 value 146.293438
## iter 40 value 132.445684
## iter 50 value 121.735515
## iter 60 value 110.913748
## iter 70 value 101.797034
## iter 80 value 89.943451
## iter 90 value 76.345444
## iter 100 value 66.319285
## final value 66.319285
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.878435
## iter 20 value 160.412633
## iter 30 value 146.295768
## iter 40 value 132.456699
```

```
## iter 50 value 121.753991
## iter 60 value 111.068167
## iter 70 value 101.725838
## iter 80 value 91.901527
## iter 90 value 79.790681
## iter 100 value 67.956986
## final value 67.956986
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.878402
## iter 20 value 160.411948
## iter 30 value 146.293441
## iter 40 value 132.445695
## iter 50 value 121.735534
## iter 60 value 110.913903
## iter 70 value 101.797552
## iter 80 value 89.944796
## iter 90 value 76.348390
## iter 100 value 66.328651
## final value 66.328651
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.507155
## iter 20 value 168.008151
## iter 30 value 154.351529
## iter 40 value 139.161429
## iter 50 value 126.127147
## iter 60 value 115.398471
## iter 70 value 107.554452
## iter 80 value 97.821720
## iter 90 value 79.668626
## iter 100 value 66.257381
## final value 66.257381
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.507174
## iter 20 value 168.008683
## iter 30 value 154.353641
## iter 40 value 139.169359
## iter 50 value 126.120865
## iter 60 value 115.561001
## iter 70 value 107.881745
## iter 80 value 98.577837
## iter 90 value 81.756531
## iter 100 value 68.196680
## final value 68.196680
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 195.507155
## iter 20 value 168.008152
```

```
## iter 30 value 154.351531
## iter 40 value 139.161437
## iter 50 value 126.127140
## iter 60 value 115.398638
## iter 70 value 107.554789
## iter 80 value 97.822265
## iter 90 value 79.670619
## iter 100 value 66.258275
## final value 66.258275
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 216.166446
## iter 20 value 185.522611
## iter 30 value 173.564102
## iter 40 value 155.099978
## iter 50 value 139.144040
## iter 60 value 129.027054
## iter 70 value 119.722624
## iter 80 value 107.450564
## iter 90 value 91.208985
## iter 100 value 78.111012
## final value 78.111012
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 216.166467
## iter 20 value 185.523132
## iter 30 value 173.566575
## iter 40 value 155.113493
## iter 50 value 139.192277
## iter 60 value 128.900937
## iter 70 value 119.118226
## iter 80 value 107.573476
## iter 90 value 94.029691
## iter 100 value 82.140576
## final value 82.140576
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 216.166446
## iter 20 value 185.522611
## iter 30 value 173.564105
## iter 40 value 155.099991
## iter 50 value 139.144087
## iter 60 value 129.026928
## iter 70 value 119.723323
## iter 80 value 107.451068
## iter 90 value 91.210481
## iter 100 value 78.142450
## final value 78.142450
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
```

```
## iter 10 value 205.902789
## iter 20 value 154.466750
## iter 30 value 139.653249
## iter 40 value 119.238914
## iter 50 value 105.406380
## iter 60 value 88.117632
## iter 70 value 81.629122
## iter 80 value 67.715729
## iter 90 value 50.488608
## iter 100 value 41.579569
## final value 41.579569
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 205.902819
## iter 20 value 154.467845
## iter 30 value 139.654432
## iter 40 value 119.255897
## iter 50 value 105.473859
## iter 60 value 88.376053
## iter 70 value 81.017059
## iter 80 value 67.879342
## iter 90 value 53.401341
## iter 100 value 44.545720
## final value 44.545720
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 205.902789
## iter 20 value 154.466751
## iter 30 value 139.653250
## iter 40 value 119.238931
## iter 50 value 105.406448
## iter 60 value 88.117893
## iter 70 value 81.629666
## iter 80 value 67.717719
## iter 90 value 50.492750
## iter 100 value 41.591961
## final value 41.591961
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 207.828724
## iter 20 value 176.130978
## iter 30 value 150.697453
## iter 40 value 133.751248
## iter 50 value 116.398121
## iter
       60 value 103.381280
## iter 70 value 93.375389
## iter 80 value 83.585598
## iter 90 value 68.466643
## iter 100 value 57.109246
## final value 57.109246
## stopped after 100 iterations
```

```
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 207.828758
## iter 20 value 176.131477
## iter 30 value 150.702178
## iter 40 value 133.771356
## iter 50 value 116.447071
## iter 60 value 103.577894
## iter 70 value 94.171941
## iter 80 value 84.466346
## iter 90 value 69.755066
## iter 100 value 59.272430
## final value 59.272430
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 207.828724
## iter 20 value 176.130978
## iter 30 value 150.697458
## iter 40 value 133.751268
## iter 50 value 116.398170
## iter 60 value 103.381476
## iter 70 value 93.376113
## iter 80 value 83.586754
## iter 90 value 68.469243
## iter 100 value 57.171046
## final value 57.171046
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 197.459887
## iter 20 value 171.807460
## iter 30 value 162.216908
## iter 40 value 145.682362
## iter 50 value 131.191764
## iter 60 value 116.528722
## iter 70 value 99.801864
## iter 80 value 87.048354
## iter 90 value 71.433299
## iter 100 value 62.605663
## final value 62.605663
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 197.459939
## iter 20 value 171.808111
## iter 30 value 162.218561
## iter
       40 value 145.695424
## iter 50 value 131.200207
## iter 60 value 117.099548
## iter 70 value 100.169194
## iter 80 value 87.031378
## iter 90 value 72.315875
## iter 100 value 65.278252
```

```
## final value 65.278252
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 197.459888
## iter 20 value 171.807461
## iter 30 value 162.216910
## iter 40 value 145.682375
## iter 50 value 131.191771
## iter 60 value 116.529329
## iter 70 value 99.791086
## iter 80 value 87.059637
## iter 90 value 71.418633
## iter 100 value 61.334669
## final value 61.334669
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.702743
## iter 20 value 159.830659
## iter 30 value 139.978162
## iter 40 value 118.274196
## iter 50 value 100.017759
## iter 60 value 88.746993
## iter 70 value 83.800188
## iter 80 value 71.801326
## iter 90 value 59.118625
## iter 100 value 44.540729
## final value 44.540729
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.702828
## iter 20 value 159.831649
## iter 30 value 139.981279
## iter 40 value 118.291279
## iter 50 value 100.096491
## iter 60 value 88.961493
## iter 70 value 84.107769
## iter 80 value 73.071035
## iter 90 value 62.452530
## iter 100 value 50.377832
## final value 50.377832
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.702743
## iter 20 value 159.830660
## iter 30 value 139.978165
## iter 40 value 118.274213
## iter 50 value 100.017838
## iter 60 value 88.747209
## iter 70 value 83.800488
## iter 80 value 71.802620
```

```
## iter 90 value 59.120887
## iter 100 value 44.563505
## final value 44.563505
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.431157
## iter 20 value 175.359213
## iter 30 value 160.382800
## iter 40 value 140.003843
## iter 50 value 124.504878
## iter 60 value 111.647835
## iter 70 value 99.352902
## iter 80 value 87.131942
## iter 90 value 70.093546
## iter 100 value 56.313191
## final value 56.313191
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.431192
## iter 20 value 175.359877
## iter 30 value 160.385404
## iter 40 value 140.021855
## iter 50 value 124.572136
## iter 60 value 111.845314
## iter 70 value 99.830156
## iter 80 value 86.696368
## iter 90 value 71.285501
## iter 100 value 59.652946
## final value 59.652946
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.431157
## iter 20 value 175.359214
## iter 30 value 160.382803
## iter 40 value 140.003861
## iter 50 value 124.504945
## iter 60 value 111.648030
## iter 70 value 99.353384
## iter 80 value 87.135619
## iter 90 value 70.097516
## iter 100 value 56.327647
## final value 56.327647
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 201.371805
## iter 20 value 166.031971
## iter 30 value 150.075932
## iter 40 value 135.132305
## iter 50 value 120.592996
## iter 60 value 104.861049
```

```
## iter 70 value 94.760756
## iter 80 value 86.209075
## iter 90 value 70.479690
## iter 100 value 59.293584
## final value 59.293584
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 201.371834
## iter 20 value 166.032587
## iter 30 value 150.078439
## iter 40 value 135.145979
## iter 50 value 120.647244
## iter 60 value 105.100395
## iter 70 value 95.630193
## iter 80 value 86.629358
## iter 90 value 73.769241
## iter 100 value 62.418038
## final value 62.418038
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 201.371805
## iter 20 value 166.031971
## iter 30 value 150.075934
## iter 40 value 135.132319
## iter 50 value 120.593051
## iter 60 value 104.861290
## iter 70 value 94.761635
## iter 80 value 86.204322
## iter 90 value 70.477907
## iter 100 value 59.380211
## final value 59.380211
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 193.758552
## iter 20 value 161.466052
## iter 30 value 143.149426
## iter 40 value 119.906737
## iter 50 value 105.972213
## iter 60 value 94.038716
## iter 70 value 86.611103
## iter 80 value 76.999325
## iter 90 value 64.304604
## iter 100 value 49.108594
## final value 49.108594
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 193.758575
## iter 20 value 161.466759
## iter 30 value 143.152818
## iter 40 value 119.925067
```

```
## iter 50 value 106.063601
## iter 60 value 94.476557
## iter 70 value 88.125313
## iter 80 value 79.353741
## iter 90 value 68.383917
## iter 100 value 55.778427
## final value 55.778427
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 193.758552
## iter 20 value 161.466053
## iter 30 value 143.149429
## iter 40 value 119.906755
## iter 50 value 105.972298
## iter 60 value 94.039119
## iter 70 value 86.612063
## iter 80 value 77.024634
## iter 90 value 64.294496
## iter 100 value 48.946694
## final value 48.946694
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 205.700241
## iter 20 value 172.245031
## iter 30 value 161.350362
## iter 40 value 145.949562
## iter 50 value 134.646862
## iter 60 value 123.431117
## iter 70 value 115.427646
## iter 80 value 107.575646
## iter 90 value 93.359323
## iter 100 value 78.496595
## final value 78.496595
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 205.700275
## iter 20 value 172.245662
## iter 30 value 161.352088
## iter 40 value 145.960485
## iter 50 value 134.688955
## iter 60 value 123.574379
## iter 70 value 115.743901
## iter 80 value 108.252481
## iter 90 value 95.287892
## iter 100 value 84.379872
## final value 84.379872
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 205.700241
## iter 20 value 172.245032
```

```
## iter 30 value 161.350363
## iter 40 value 145.949573
## iter 50 value 134.646905
## iter 60 value 123.431261
## iter 70 value 115.427971
## iter 80 value 107.576296
## iter 90 value 93.361320
## iter 100 value 78.502007
## final value 78.502007
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 219.760490
## iter 20 value 187.124426
## iter 30 value 169.999087
## iter 40 value 150.988583
## iter 50 value 138.413835
## iter 60 value 123.009829
## iter 70 value 109.478001
## iter 80 value 93.806014
## iter 90 value 75.758745
## iter 100 value 58.395941
## final value 58.395941
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 219.760529
## iter 20 value 187.125144
## iter 30 value 170.001985
## iter 40 value 151.002233
## iter 50 value 138.477224
## iter 60 value 123.272620
## iter 70 value 111.151892
## iter 80 value 92.955032
## iter 90 value 77.276762
## iter 100 value 64.227998
## final value 64.227998
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 219.760490
## iter 20 value 187.124427
## iter 30 value 169.999090
## iter 40 value 150.988596
## iter 50 value 138.413899
## iter 60 value 123.010094
## iter 70 value 109.478646
## iter 80 value 93.807518
## iter 90 value 75.762081
## iter 100 value 58.410349
## final value 58.410349
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
```

```
## iter 10 value 202.083849
## iter 20 value 171.218444
## iter 30 value 148.002738
## iter 40 value 131.483341
## iter 50 value 119.899625
## iter 60 value 101.885103
## iter 70 value 88.167837
## iter 80 value 77.579263
## iter 90 value 67.403824
## iter 100 value 54.845992
## final value 54.845992
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.083917
## iter 20 value 171.219158
## iter 30 value 148.006594
## iter 40 value 131.494731
## iter 50 value 119.947547
## iter 60 value 102.164080
## iter 70 value 88.909884
## iter 80 value 80.246572
## iter 90 value 70.884610
## iter 100 value 62.437067
## final value 62.437067
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 202.083849
## iter 20 value 171.218445
## iter 30 value 148.002742
## iter
       40 value 131.483352
## iter 50 value 119.899672
## iter 60 value 101.885379
## iter 70 value 88.168693
## iter 80 value 77.580997
## iter 90 value 67.407609
## iter 100 value 54.896169
## final value 54.896169
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 210.893574
## iter 20 value 176.968481
## iter 30 value 157.621487
## iter 40 value 142.056823
## iter 50 value 121.819529
## iter
       60 value 111.531475
## iter 70 value 100.966866
## iter 80 value 88.183437
## iter 90 value 73.319758
## iter 100 value 58.907600
## final value 58.907600
## stopped after 100 iterations
```

```
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 210.893616
## iter 20 value 176.969104
## iter 30 value 157.624217
## iter 40 value 142.070829
## iter 50 value 121.894347
## iter 60 value 111.706223
## iter 70 value 101.934582
## iter 80 value 88.907037
## iter 90 value 74.853558
## iter 100 value 62.676623
## final value 62.676623
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 210.893574
## iter 20 value 176.968482
## iter 30 value 157.621490
## iter 40 value 142.056837
## iter 50 value 121.819604
## iter 60 value 111.531651
## iter 70 value 100.967339
## iter 80 value 88.182492
## iter 90 value 73.321790
## iter 100 value 58.923957
## final value 58.923957
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 215.234341
## iter 20 value 187.495648
## iter 30 value 156.884090
## iter 40 value 126.627495
## iter 50 value 108.092316
## iter 60 value 93.655427
## iter 70 value 82.956918
## iter 80 value 70.727103
## iter 90 value 54.497157
## iter 100 value 38.707756
## final value 38.707756
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 215.234405
## iter 20 value 187.496165
## iter 30 value 156.890467
## iter
       40 value 126.670853
## iter 50 value 108.136155
## iter 60 value 93.903580
## iter 70 value 82.571252
## iter 80 value 71.747868
## iter 90 value 60.863267
## iter 100 value 46.666754
```

```
## final value 46.666754
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 215.234341
## iter 20 value 187.495649
## iter 30 value 156.884096
## iter 40 value 126.627538
## iter 50 value 108.092360
## iter 60 value 93.655673
## iter 70 value 82.958070
## iter 80 value 70.733975
## iter 90 value 54.499717
## iter 100 value 38.186024
## final value 38.186024
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 206.360036
## iter 20 value 172.487861
## iter 30 value 155.021658
## iter 40 value 136.335948
## iter 50 value 119.177256
## iter 60 value 110.476952
## iter 70 value 103.090165
## iter 80 value 95.068108
## iter 90 value 79.645467
## iter 100 value 66.656328
## final value 66.656328
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 206.360068
## iter 20 value 172.488629
## iter 30 value 155.023441
## iter 40 value 136.350067
## iter 50 value 119.240533
## iter 60 value 110.611543
## iter 70 value 103.346467
## iter 80 value 95.453720
## iter 90 value 81.089286
## iter 100 value 71.797990
## final value 71.797990
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 206.360036
## iter 20 value 172.487862
## iter 30 value 155.021660
## iter 40 value 136.335963
## iter 50 value 119.177320
## iter 60 value 110.477087
## iter 70 value 103.090422
## iter 80 value 95.067651
```

```
## iter 90 value 79.646829
## iter 100 value 66.657618
## final value 66.657618
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 220.183939
## iter 20 value 185.813346
## iter 30 value 166.002072
## iter 40 value 145.689793
## iter 50 value 129.203808
## iter 60 value 112.779371
## iter 70 value 101.156987
## iter 80 value 89.181144
## iter 90 value 71.341174
## iter 100 value 60.270997
## final value 60.270997
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 220.183976
## iter 20 value 185.813893
## iter 30 value 166.005036
## iter 40 value 145.706838
## iter 50 value 129.260881
## iter 60 value 113.034823
## iter 70 value 101.614811
## iter 80 value 90.462165
## iter 90 value 74.152421
## iter 100 value 64.434659
## final value 64.434659
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 220.183939
## iter 20 value 185.813346
## iter 30 value 166.002075
## iter 40 value 145.689810
## iter 50 value 129.203865
## iter 60 value 112.779628
## iter 70 value 101.157452
## iter 80 value 89.182589
## iter 90 value 71.344062
## iter 100 value 60.255059
## final value 60.255059
## stopped after 100 iterations
## # weights: 285 (224 variable)
## initial value 270.385569
## iter 10 value 213.786480
## iter 20 value 183.820116
## iter 30 value 175.610350
## iter 40 value 166.416809
## iter 50 value 156.687239
## iter 60 value 150.770066
```

```
## iter 70 value 141.604223
## iter 80 value 132.373761
## iter 90 value 117.371155
## iter 100 value 107.188847
## final value 107.188847
## stopped after 100 iterations
summary(log.tune)
## Call:
## nnet::multinom(formula = .outcome ~ ., data = dat, decay = param$decay,
       direction = "forward", k = ..2)
##
## Coefficients:
##
     (Intercept)
                       age
                               viewcat
                                            setting
                                                        viewenc
                                                                   prebody
## 2 -0.10430024 0.2129859 -0.34982789 0.04138759 -0.09653652 -0.3325268
## 3 0.06293638 0.5017950 -0.86594527 0.17242433 0.34030478 -1.5850149
## 4 -0.11348294 0.1084882 -0.09580164 -0.05144057 -0.28198446 -0.2926012
## 5 -0.04232544 0.1268965 -0.00157604 -0.04201233 -0.16079544
                                                                 0.2624026
##
          prelet
                     preform
                                prenumb
                                            prerelat
                                                       preclasf `age:viewcat`
     1.07548218 -1.19154198 -0.1355582 0.01218500 -0.8281805
                                                                   0.01101840
## 3 -0.09390197 -0.31628259 0.9186298 0.31343738 -0.5633445
                                                                  -0.02328669
## 4 -0.30935254 0.01800312 -0.2184987 -0.26198492 0.9754936
                                                                   0.08728599
    0.02435272  0.22175132  -0.6841873  0.08376244  0.2796019
                                                                   0.01044005
     `age:setting` `age:viewenc` `age:prebody` `age:prelet`
                                                            `age:preform`
## 2
        -0.1950952
                      0.15083709 -0.015740783 0.003796499
                                                                0.03454772
## 3
        -0.2402140
                      0.05406668
                                  0.006006701 0.002664593
                                                                0.04427898
## 4
        0.0370847
                      0.03283911 -0.013181506 0.011476032
                                                                0.01067502
## 5
        -0.1834337
                      0.06846291 -0.011654324 0.010500400
                                                                0.00502330
      age:prenumb` `age:prerelat` `age:preclasf` `viewcat:setting`
                                                         -0.7157048
## 2
       0.002748548
                      0.017421552
                                     -0.03449594
     -0.021179041
                      0.006862094
                                     -0.02046393
                                                          1.9296577
## 4
       0.005381244
                      0.002834208
                                     -0.03462003
                                                         -1.3304799
       0.004025159
                      0.021167701
## 5
                                     -0.01529625
                                                         -0.6193439
##
     'viewcat:viewenc` `viewcat:prebody` `viewcat:prelet` `viewcat:preform`
## 2
            -0.6267928
                              0.14158801
                                               -0.18278208
                                                                 -0.33356833
## 3
            -0.6451057
                                               -0.19113344
                                                                 -0.19616855
                              0.15032040
## 4
            -0.7600318
                              0.02100516
                                               -0.06168443
                                                                 -0.09204344
## 5
            -0.7298604
                             -0.01705615
                                               -0.08760215
                                                                 -0.00448432
      viewcat:prenumb` `viewcat:prerelat`
                                          `viewcat:preclasf` `setting:viewenc`
## 2
           0.036088877
                               0.14586964
                                                   0.23145567
                                                                     0.07630395
## 3
           0.021174552
                               0.31836093
                                                  -0.07370337
                                                                     0.86832568
## 4
           0.003855981
                               0.07887976
                                                  -0.10100460
                                                                    -0.63499806
## 5
           0.087689197
                               0.24193609
                                                  -0.07174626
                                                                     0.37153187
     `setting:prebody` `setting:prelet` `setting:preform` `setting:prenumb`
## 2
           0.469099240
                             -0.4122878
                                              -0.13051934
                                                                  0.05284150
## 3
           0.135607010
                                               0.01884259
                                                                  0.05295298
                             -0.1971371
## 4
          -0.006161835
                             -0.2960129
                                               -0.10589631
                                                                  0.26263062
## 5
           0.421579113
                             -0.2513299
                                               0.15172993
                                                                  0.04497442
##
      setting:prerelat` `setting:preclasf` `viewenc:prebody` `viewenc:prelet`
## 2
              0.9158782
                               -0.20327566
                                               -0.1732281310
                                                                   -0.15753436
## 3
                                                -0.1003194116
                                                                    0.22031347
             -0.6874554
                                0.77873656
## 4
              0.2901539
                               -0.09297208
                                                 0.0008472878
                                                                    0.10954771
## 5
              0.1997050
                               -0.02496983
                                               -0.4660637394
                                                                    0.08286859
     `viewenc:preform` `viewenc:prenumb` `viewenc:prerelat` `viewenc:preclasf'
```

```
## 2
           -0.56985394
                              0.03247080
                                                  -1.3095372
                                                                       1.4372910
## 3
           -0.78356022
                                                  -0.8061659
                                                                       0.8328746
                              0.06169254
           -0.01496193
                             -0.09635533
## 4
                                                  -0.2666694
                                                                       0.3122020
## 5
           -0.17168716
                               0.20628325
                                                  -0.4768000
                                                                       0.5294078
##
      prebody:prelet` `prebody:preform` `prebody:prenumb` `prebody:prerelat`
         -0.026728574
                                              -0.004690487
## 2
                             0.02310599
                                                                    0.06567582
          0.008919958
                            -0.07757222
                                               0.004168160
                                                                    0.08221147
## 4
                            -0.06621870
          0.002594866
                                              -0.005876983
                                                                    0.08031019
## 5
         -0.018649963
                             -0.05937411
                                              -0.031267621
                                                                    0.12347594
     `prebody:preclasf` `prelet:preform` `prelet:prenumb` `prelet:prerelat`
## 2
             0.01621294
                             0.053767578
                                              -0.024222497
                                                                  0.010990911
             0.04294225
                             0.037711752
## 3
                                              -0.028066953
                                                                  0.054014235
## 4
             0.07572520
                             0.003193047
                                              -0.011355172
                                                                 -0.003240511
## 5
             0.04845629
                             0.023606964
                                               0.002600023
                                                                 -0.039934799
     `prelet:preclasf` `preform:prenumb`
                                          `preform:prerelat` `preform:preclasf`
## 2
           0.040880193
                             -0.06146975
                                                0.0001794691
                                                                     0.072813219
## 3
          -0.006339726
                               0.02589022
                                               -0.0338563962
                                                                    -0.005385365
## 4
           0.029870629
                               0.01796772
                                                0.0091114656
                                                                     0.046634386
                                                                     0.036711837
## 5
           0.028841972
                               0.03215846
                                               -0.0931836916
      prenumb:prerelat` `prenumb:preclasf`
                                            `prerelat:preclasf`
## 2
           0.0347272942
                                0.034704048
                                                     -0.2159680
## 3
          -0.0023133262
                                0.006896269
                                                     -0.1384417
          -0.0002585178
## 4
                               -0.019663447
                                                     -0.1506193
           0.0255919064
                               -0.001445600
                                                     -0.2108050
## 5
##
## Std. Errors:
     (Intercept)
                                           setting
##
                       age
                               viewcat
                                                      viewenc
                                                                 prebody
     0.01769491 0.2281321 0.04463296 0.017978327 0.02743229 0.2795415 0.2451148
    0.02272730 0.1783334 0.06424362 0.029933348 0.03521339 0.2644438 0.4033421
     0.02199825 0.1887900 0.06092779 0.024090342 0.03376304 0.3572217 0.4088392
## 5
     0.01018045 0.2010834 0.03038656 0.009964914 0.01420608 0.1814051 0.2567150
##
        preform
                  prenumb
                             prerelat
                                        preclasf `age:viewcat` `age:setting`
## 2 0.11178013 0.3364181 0.09881117 0.13663278
                                                    0.05635717
                                                                   0.09530280
                                                                   0.09138367
## 3 0.13921911 0.3950844 0.09883397 0.14861756
                                                    0.05043176
## 4 0.13220239 0.3274458 0.11556801 0.14712060
                                                    0.04885287
                                                                   0.08840051
  5 0.09857628 0.1968719 0.07393768 0.09452461
                                                    0.06297351
                                                                   0.11500433
     `age:viewenc` `age:prebody` `age:prelet` `age:preform` `age:prenumb`
## 2
        0.11304152
                      0.01433104
                                   0.01356935
                                                  0.02786496
                                                                 0.01497572
## 3
        0.09915620
                      0.01349342
                                    0.01315086
                                                  0.02339626
                                                                 0.01438330
                                    0.01221907
## 4
        0.09331245
                      0.01429374
                                                  0.02392057
                                                                 0.01476449
        0.13061367
                      0.01728838
                                    0.01324726
                                                  0.02935786
                                                                 0.01581603
     `age:prerelat`
                    `age:preclasf` `viewcat:setting`
                                                      `viewcat:viewenc`
##
## 2
         0.02584354
                        0.02741556
                                            0.2490771
                                                               0.3332642
## 3
         0.02480077
                        0.02372367
                                            0.2847775
                                                               0.2908848
         0.02586148
                        0.02541847
                                            0.3029041
                                                               0.4216808
                                            0.1607059
                                                               0.1494858
## 5
         0.02754718
                        0.02878072
     `viewcat:prebody` `viewcat:prelet` `viewcat:preform` `viewcat:prenumb`
## 2
             0.1108576
                             0.11755013
                                                 0.2010431
                                                                   0.09697412
## 3
             0.1219053
                             0.11054466
                                                 0.1733514
                                                                   0.09255908
## 4
             0.1107068
                             0.09731512
                                                 0.1698175
                                                                   0.08853306
## 5
             0.1380371
                             0.12158710
                                                 0.2223183
                                                                   0.11578095
     `viewcat:prerelat` `viewcat:preclasf` `setting:viewenc` `setting:prebody`
                                 0.1629227
## 2
              0.2751360
                                                   0.08493856
                                                                       0.2330639
## 3
              0.2601977
                                  0.1541121
                                                   0.07712831
                                                                       0.2437100
```

```
## 4
              0.2304470
                                  0.1370595
                                                   0.13297704
                                                                       0.2560144
## 5
              0.2974449
                                  0.2124611
                                                   0.06689098
                                                                       0.3039591
     `setting:prelet` `setting:preform` `setting:prenumb` `setting:prerelat`
## 2
            0.2149093
                               0.3573498
                                                 0.2038061
                                                                     0.3706735
## 3
            0.2632529
                               0.3247801
                                                 0.2250007
                                                                     0.3562895
## 4
            0.2180408
                               0.3425432
                                                 0.2068494
                                                                     0.3963333
            0.2570749
                               0.3889281
                                                 0.2517049
                                                                     0.2415947
     `setting:preclasf` `viewenc:prebody` `viewenc:prelet` `viewenc:preform`
##
## 2
              0.3342676
                                 0.2457295
                                                  0.1839863
                                                                     0.3807850
## 3
              0.3125047
                                 0.2560498
                                                  0.1967347
                                                                     0.3360116
## 4
              0.3433573
                                 0.2228863
                                                  0.1694260
                                                                     0.3106407
## 5
              0.3701965
                                 0.3151663
                                                  0.2098595
                                                                     0.4171969
     viewenc:prenumb` `viewenc:prerelat` `viewenc:preclasf` `prebody:prelet`
##
## 2
             0.1837119
                                 0.4035093
                                                    0.3503429
                                                                     0.02038602
## 3
             0.2189024
                                 0.3392222
                                                                     0.02341377
                                                     0.3549874
## 4
             0.1679850
                                 0.4089991
                                                     0.3004770
                                                                     0.01934844
## 5
             0.2426103
                                 0.3200753
                                                    0.3722014
                                                                     0.02845440
     `prebody:preform` `prebody:prenumb` `prebody:prerelat` `prebody:preclasf`
## 2
            0.05337533
                               0.02326317
                                                  0.06436399
                                                                      0.05175746
## 3
            0.05680423
                               0.02309044
                                                  0.06277950
                                                                      0.04906464
## 4
            0.05059798
                               0.02129793
                                                  0.06010049
                                                                      0.04585516
## 5
            0.06802325
                               0.02925413
                                                  0.07559607
                                                                      0.05945588
     prelet:preform` `prelet:prenumb` `prelet:prerelat` `prelet:preclasf`
##
           0.04333995
                             0.01443954
                                               0.04451862
                                                                  0.03412912
## 2
## 3
                                                                  0.03562827
           0.04561577
                             0.01585042
                                               0.04955802
## 4
           0.04016587
                             0.01239328
                                               0.04068016
                                                                  0.02845603
## 5
           0.04602906
                             0.01454398
                                               0.05396960
                                                                  0.03432086
##
     preform:prenumb`
                        `preform:prerelat` `preform:preclasf` `prenumb:prerelat`
## 2
            0.04078930
                                0.10960277
                                                   0.07055708
                                                                       0.04544892
## 3
            0.04170952
                                0.10147248
                                                   0.06993119
                                                                       0.04374414
## 4
            0.03378745
                                0.08337231
                                                   0.05951540
                                                                       0.04023916
## 5
            0.04886538
                                0.11943772
                                                   0.08905010
                                                                       0.05140125
     `prenumb:preclasf` `prerelat:preclasf`
## 2
             0.03153069
                                  0.10242770
## 3
             0.02978874
                                  0.09538739
## 4
             0.03086232
                                  0.09338443
## 5
             0.04096462
                                  0.11263783
##
## Residual Deviance: 214.3777
## AIC: 662.3777
tabs2 <- table(true=test.log[, "site"],</pre>
              pred=predict(log.tune,newdata=test.log))
confusionMatrix(tabs2)
## Confusion Matrix and Statistics
##
##
       pred
  true 1 2 3
##
##
      1
        4
           1 5 4 4
##
      2
        3
           6 7
                  1 1
##
      3 3 0 16 0
##
      4 0 1 6 4 1
##
      5
        1
            1
               3
                  0
##
```

```
## Overall Statistics
##
##
                 Accuracy : 0.4167
##
                   95% CI: (0.3015, 0.5389)
##
      No Information Rate: 0.5139
##
      P-Value [Acc > NIR] : 0.961676
##
                    Kappa: 0.2408
##
##
   Mcnemar's Test P-Value: 0.006843
##
## Statistics by Class:
##
##
                        Class: 1 Class: 2 Class: 3 Class: 4 Class: 5
## Sensitivity
                        0.36364 0.66667
                                           0.4324 0.44444
                                                            0.00000
## Specificity
                        0.77049 0.80952
                                           0.9143
                                                   0.87302
                                                            0.92424
## Pos Pred Value
                        0.22222 0.33333
                                           0.8421
                                                   0.33333
                                                            0.00000
## Neg Pred Value
                        0.87037 0.94444
                                           0.6038
                                                   0.91667
                                                            0.91045
                                                   0.12500
## Prevalence
                        0.15278 0.12500
                                           0.5139
                                                            0.08333
## Detection Rate
                        0.05556 0.08333
                                           0.2222
                                                   0.05556
                                                            0.00000
## Detection Prevalence 0.25000 0.25000
                                           0.2639
                                                   0.16667
                                                            0.06944
## Balanced Accuracy
                        0.56706 0.73810
                                           0.6734 0.65873 0.46212
```

Questions for OH:

should we transform regular?

Both linear and radial kernels never output predictions for 4 & 5? polynomial kernel? Which variables to give polynomial terms use PCA to perform feature selection?

feature selections for SVM in general?

how to interpret the confusion matrix tables for SVM & Trees

How to interpret the imporatnce variance for multiclass classification

interpretations about the dataset, using the bad performance of the classifiers