# Projet Analyse de Credit Scoring 2 avec Data mining

Itaf Hamrouni Nour El Islem Nbiba Sarra Madani

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```
Project: Analyse Credit Scoring basée sur data mining
Charger Library
library("MASS")
## Warning: package 'MASS' was built under R version 3.4.3
library("FactoMineR")
## Warning: package 'FactoMineR' was built under R version 3.4.3
library(ggplot2)
Importation de base apres faire nettoyage et renommage
data= read.csv("C:/Users/user/Desktop/3eme/datamining/projet data mining/tp/CleanCreditScoring.csv", he
View(data)
dim(data)
## [1] 4446
str(data)
## 'data.frame':
                   4446 obs. of 27 variables:
             : Factor w/ 2 levels "bad", "good": 2 2 1 2 2 2 2 2 1 ...
## $ Seniority : int 9 17 10 0 0 1 29 9 0 0 ...
               : Factor w/ 6 levels "ignore", "other", ...: 6 6 3 6 6 3 3 4 3 4 ...
## $ Time
               : int 60 60 36 60 36 60 60 12 60 48 ...
## $ Age
               : int 30 58 46 24 26 36 44 27 32 41 ...
## $ Marital : Factor w/ 5 levels "divorced", "married",..: 2 5 2 4 4 2 2 4 2 2 ...
## $ Records
               : Factor w/ 2 levels "no_rec", "yes_rec": 1 1 2 1 1 1 1 1 1 1 ...
## $ Job
               : Factor w/ 4 levels "fixed", "freelance", ...: 2 1 2 1 1 1 1 1 2 4 ...
## $ Expenses : int 73 48 90 63 46 75 75 35 90 90 ...
                      129 131 200 182 107 214 125 80 107 80 ...
## $ Income
               : int
##
   $ Assets
               : int 0 0 3000 2500 0 3500 10000 0 15000 0 ...
## $ Debt
               : int 0000000000...
## $ Amount : int 800 1000 2000 900 310 650 1600 200 1200 1200 ...
               : int 846 1658 2985 1325 910 1645 1800 1093 1957 1468 ...
## $ Price
## $ Finrat
               : num 94.6 60.3 67 67.9 34.1 ...
## $ Savings
              : num 4.2 4.98 1.98 7.93 7.08 ...
## $ seniorityR: Factor w/ 5 levels "sen (-1,1]", "sen (1,3]",..: 5 3 5 1 1 1 3 5 1 1 ...
## $ timeR
               : Factor w/ 5 levels "time (0,12]",..: 5 5 3 5 3 5 5 1 5 4 ...
## $ ageR
                : Factor w/ 5 levels "age (0,25]", "age (25,30]",...: 2 5 4 1 2 3 4 2 3 4 ...
## $ expensesR : Factor w/ 5 levels "exp (0,40]", "exp (40,50]", ...: 4 2 5 4 2 4 4 1 5 5 ...
## $ incomeR : Factor w/ 5 levels "inc (0,80]", "inc (110,140]",..: 2 2 4 3 5 4 2 1 5 1 ...
## $ assetsR
               : Factor w/ 5 levels "asset (-1,0]",..: 1 1 2 2 1 3 5 1 5 1 ...
## $ debtR
               : Factor w/ 5 levels "debt (-1,0]",..: 1 1 1 1 1 1 1 1 1 1 ...
## $ amountR : Factor w/ 5 levels "am (0,600]", "am (1.1e+03,1.4e+03]",..: 4 5 3 4 1 4 3 1 2 2 ...
               : Factor w/ 5 levels "priz (0,1e+03]",...: 1 3 4 2 1 3 3 5 4 2 ...
## $ priceR
## $ finratR
               : Factor w/ 5 levels "finr (0,50]",..: 5 2 2 2 1 1 4 1 2 4 ...
```

```
## $ savingsR : Factor w/ 5 levels "sav (-99,0]",..: 4 4 2 5 5 5 2 3 2 1 ...
```

See what the data looks like: Summary

```
head(data)
```

```
Status Seniority Home Time Age Marital Records
                                                             Job Expenses
## 1
                    9 rent
                               60 30 married no_rec freelance
                                                                        73
       good
## 2
                                                                        48
       good
                   17
                       rent
                               60
                                   58
                                        widow
                                               no rec
                                                           fixed
## 3
                               36
                                  46 married yes_rec freelance
                                                                        90
        bad
                   10 owner
## 4
       good
                      rent
                               60
                                   24
                                       single no_rec
                                                           fixed
                                                                        63
## 5
                    0
                               36
                                   26
                                       single no rec
                                                                        46
       good
                       rent
                                                           fixed
## 6
       good
                    1 owner
                               60
                                   36 married no rec
                                                           fixed
                                                                        75
                                                  Savings
##
     Income Assets Debt Amount Price
                                        Finrat
                                                           seniorityR
## 1
                 0
                      0
                            800
                                  846 94.56265
                                                4.200000
                                                           sen (8,14]
        129
## 2
                                 1658 60.31363
                                                4.980000 sen (14,99]
        131
                 0
                      0
                           1000
## 3
        200
              3000
                      0
                           2000
                                 2985 67.00168
                                                1.980000
                                                           sen (8,14]
## 4
              2500
                      0
                            900
                                 1325 67.92453
        182
                                                7.933333
                                                           sen (-1,1]
## 5
        107
                 0
                      0
                            310
                                  910 34.06593 7.083871
                                                           sen (-1,1]
## 6
        214
              3500
                       0
                            650
                                 1645 39.51368 12.830769
                                                           sen (-1,1]
##
            timeR
                                    expensesR
                                                       incomeR
                          ageR
## 1 time (48,99] age (25,30]
                                  exp (60,80]
                                                 inc (110,140]
## 2 time (48,99] age (50,99]
                                  exp (40,50]
                                                 inc (110,140]
## 3 time (24,36] age (40,50] exp (80,1e+04] inc (190,1e+04]
## 4 time (48,99]
                  age (0,25]
                                  exp (60,80]
                                                 inc (140,190]
## 5 time (24,36] age (25,30]
                                  exp (40,50]
                                                  inc (80,110]
## 6 time (48,99] age (30,40]
                                  exp (60,80] inc (190,1e+04]
##
                 assetsR
                                debtR
                                                  amountR
## 1
            asset (-1,0] debt (-1,0]
                                            am (600,900]
                                        am (900,1.1e+03]
            asset (-1,0] debt (-1,0]
## 3
         asset (0,3e+03] debt (-1,0] am (1.4e+03,1e+05]
## 4
         asset (0,3e+03] debt (-1,0]
                                            am (600,900]
            asset (-1,0] debt (-1,0]
                                              am (0,600]
## 6 asset (3e+03,5e+03] debt (-1,0]
                                            am (600,900]
##
                      priceR
                                   finratR
                                             savingsR
             priz (0,1e+03] finr (90,100]
                                            sav (4,6]
## 2 priz (1.5e+03,1.8e+03]
                             finr (50,70]
                                            sav (4,6]
      priz (1.8e+03,1e+05]
                             finr (50,70]
                                            sav (0,2]
## 4 priz (1.3e+03,1.5e+03]
                             finr (50,70] sav (6,99]
                              finr (0,50] sav (6,99]
             priz (0,1e+03]
## 6 priz (1.5e+03,1.8e+03]
                               finr (0,50] sav (6,99]
```

#### summary(data)

```
##
     Status
                  Seniority
                                       Home
                                                       Time
    bad :1249
                Min.
                        : 0.000
                                  ignore :
                                             20
                                                  Min.
                                                         : 6.00
##
                1st Qu.: 2.000
                                                  1st Qu.:36.00
    good:3197
                                  other: 319
##
                Median : 5.000
                                  owner :2106
                                                  Median :48.00
                        : 7.991
##
                Mean
                                  parents: 782
                                                  Mean
                                                         :46.45
##
                3rd Qu.:12.000
                                  priv
                                          : 246
                                                  3rd Qu.:60.00
##
                Max.
                        :48.000
                                  rent
                                          : 973
                                                  Max.
                                                         :72.00
##
                          Marital
                                         Records
                                                              Inh
         Age
##
                                      no_rec :3677
    Min.
           :18.00
                    divorced:
                                 38
                                                      fixed
                                                                :2803
##
    1st Qu.:28.00
                    married :3238
                                      yes_rec: 769
                                                      freelance: 1021
   Median :36.00
                    separated: 130
                                                      others
                                                               : 171
## Mean
           :37.08
                    single
                             : 973
                                                      partime: 451
```

```
3rd Qu.:45.00
                    widow
           :68.00
##
    Max.
##
       Expenses
                         Income
                                         Assets
                                                            Debt
##
   Min.
          : 35.0
                           : 1.0
                                           :
                                                              :
                                                                    0.0
                    Min.
                                     Min.
                                                   0
                                                       Min.
##
    1st Qu.: 35.0
                    1st Qu.: 90.0
                                     1st Qu.:
                                                   0
                                                       1st Qu.:
                                                                    0.0
##
    Median: 51.0
                    Median :124.0
                                     Median:
                                               3000
                                                       Median:
                                                                    0.0
    Mean : 55.6
                    Mean :140.6
                                     Mean
                                           :
                                               5355
                                                       Mean
                                                                 342.3
    3rd Qu.: 72.0
##
                    3rd Qu.:170.0
                                     3rd Qu.:
                                               6000
                                                       3rd Qu.:
                                                                    0.0
##
    Max.
           :180.0
                    Max.
                            :959.0
                                     Max.
                                             :300000
                                                       Max.
                                                              :30000.0
##
        Amount
                       Price
                                        Finrat
                                                          Savings
    Min.
           : 100
                   Min.
                           : 105
                                    Min.
                                           : 6.702
                                                       Min.
                                                              :-8.160
                                    1st Qu.: 60.030
    1st Qu.: 700
                   1st Qu.: 1116
                                                       1st Qu.: 1.615
##
##
    Median:1000
                   Median: 1400
                                    Median: 77.097
                                                       Median : 3.120
                   Mean
                                                       Mean
##
    Mean
          :1039
                           : 1462
                                    Mean
                                           : 72.616
                                                             : 3.860
##
    3rd Qu.:1300
                   3rd Qu.: 1692
                                    3rd Qu.: 88.460
                                                       3rd Qu.: 5.196
##
    Max.
           :5000
                   Max.
                           :11140
                                    Max.
                                            :100.000
                                                       Max.
                                                              :33.250
##
                                 timeR
                                                      ageR
          seniorityR
                                            age (0,25] : 699
##
    sen (-1,1] :1042
                       time (0,12]: 180
                       time (12,24]: 441
##
    sen (1,3] : 789
                                            age (25,30]: 781
##
    sen (14,99]: 880
                       time (24,36]: 991
                                            age (30,40]:1415
##
    sen (3,8] : 978
                       time (36,48]:885
                                            age (40,50]: 900
##
    sen (8,14] : 757
                       time (48,99]:1949
                                            age (50,99]: 651
##
##
             expensesR
                                      incomeR
                                                                 assetsR
                                           :886
##
    \exp(0.40]
                   :1219
                           inc (0,80]
                                                  asset (-1,0]
                                                                      :1626
##
    exp (40,50]
                  : 999
                           inc (110,140]
                                          :866
                                                  asset (0,3e+03]
                                                                      : 626
##
    exp (50,60]
                  : 979
                           inc (140,190]
                                          :915
                                                  asset (3e+03,5e+03]: 937
                  : 798
##
    \exp (60,80]
                           inc (190,1e+04]:825
                                                  asset (5e+03,8e+03]: 538
##
    \exp (80,1e+04]: 451
                           inc (80,110]
                                          :954
                                                  asset (8e+03,1e+06]: 719
##
##
                        debtR
                                                    amountR
##
    debt (-1,0]
                           :3667
                                   am (0,600]
                                                        :895
##
    debt (0,500]
                           : 193
                                   am (1.1e+03,1.4e+03]:925
##
    debt (1.5e+03,2.5e+03]: 159
                                   am (1.4e+03,1e+05]
                                                       :770
##
    debt (2.5e+03,1e+06] : 197
                                   am (600,900]
                                                        :911
##
    debt (500,1.5e+03]
                                   am (900, 1.1e+03]
                                                        :945
                           : 230
##
##
                       priceR
                                            finratR
                                                               savingsR
##
    priz (0,1e+03]
                           : 821
                                   finr (0,50] :716
                                                        sav (-99,0]: 298
##
                                   finr (50,70] :954
    priz (1.3e+03,1.5e+03]: 801
                                                        sav (0,2]
                                                                  :1111
                                   finr (70,80] :821
   priz (1.5e+03,1.8e+03]:1028
                                                        sav (2,4]
                                                                   :1396
##
    priz (1.8e+03,1e+05] : 811
                                   finr (80,90] :995
                                                        sav (4,6]
                                                                   : 814
                                   finr (90,100]:960
##
    priz (1e+03,1.3e+03] : 985
                                                        sav (6,99] : 827
##
```

## #Partie Clustering#

select select categorized continuous variables

```
MCA
```

```
mca = MCA(datacat, ncp=40, quali.sup=12, graph=FALSE)
```

```
get the eigenvalues
```

```
eig = mca$eig
eigs=eig[,"eigenvalue"]
```

calculate significant dimension in MCA

```
dimmca = sum(eigs>1/length(eigs))
```

get factorial coordinates of individuals

```
coord = mca$ind$coord
```

K-means clustering on factorical coordinates from MCA results

The idea is to take the extracted dimensions

from the MCA in order to perform a k-means cluster analysis on them The first approach is to apply K-means on factorial coordinates Let's try k=5 groups

```
k1 = kmeans(coord, 5)
```

what does k1 contain?

```
attributes(k1)
```

```
## $names
## [1] "cluster" "centers" "totss" "withinss"
## [5] "tot.withinss" "betweenss" "size" "iter"
## [9] "ifault"
##
## $class
## [1] "kmeans"
```

examine the following

```
# size of clusters
```

k1\$size

```
## [1] 565 1476 1011 715 679
```

```
# within cluster variance
k1$withinss
```

## [1] 1940.754 5033.395 3468.125 2336.681 2519.399

```
# centers coordinates
```

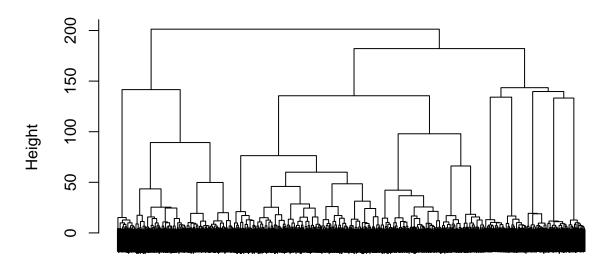
k1\$centers

```
##
         Dim 1
                    Dim 2
                               Dim 3
                                          Dim 4
                                                     Dim 5
## 1 0.41050363 0.29784120 0.14156136 -0.32930930 -0.31533970 0.22048379
## 2 0.08591084 -0.35271853 -0.18323668 0.08042069 -0.05139202 -0.04856248
## 3 -0.40773771
                0.04992065 -0.05997183 0.00980667 -0.19704363 0.10201872
## 4 0.41832313 -0.10860319 0.44820479
                                     0.04388507
                                                0.31378054 -0.15408231
## 5 -0.36173369
                0.55893044 -0.10214983
                                     0.03838946
                                                0.33708331 -0.06755109
##
         Dim 7
                   Dim 8
                              Dim 9
                                        Dim 10
                                                   Dim 11
                                                               Dim 12
## 1 -0.17648171
                0.1328949 -0.08776180 0.17282382 0.01340513
                                                          0.173048338
## 3 0.20117256 -0.2017906 0.12557979 0.07952246 -0.04085965 0.033854551
## 4 0.16195934 -0.2248877 0.03057247 0.03241203 0.11887595 -0.096742170
## 5 -0.16958304
                0.1825175 -0.06620536 -0.07300830 0.02562234 -0.071199227
##
                                 Dim 15
         Dim 13
                     Dim 14
                                              Dim 16
                                                         Dim 17
## 1 0.038531658 -0.008850204 -0.046170081 0.0065854002 0.020247642
```

```
## 2 -0.001054519 -0.043106649 0.061248172 0.0007085906 0.006936504
## 3 -0.110466987 0.038409500 -0.046179720 0.0217899489 -0.009469007
## 4 0.053954095 -0.002449406 -0.020981053 -0.0172216996 -0.040118774
## 5 0.077895478 0.046458175 -0.003869006 -0.0213295345 0.024418103
         Dim 18
                       Dim 19
                                   Dim 20
                                               Dim 21
## 1 -0.05042055 6.692696e-05 -0.04260641 -0.02342813 0.015872454
## 2 -0.01707266 1.939957e-02 -0.01735737 0.01866709 0.026996294
## 3 0.01557968 8.443794e-04 0.02524231 -0.02389661 -0.026501091
## 4 0.02669524 -1.981124e-02 -0.01211020 -0.01277295 -0.035588418
## 5 0.02775952 -2.262182e-02 0.04835186 0.02794758 0.005042496
         Dim 23
                      Dim 24
                                   Dim 25
                                                Dim 26
                                                             Dim 27
## 1 -0.03573093 -0.022993528 -0.005590173 0.004215240 -0.020057958
## 2 -0.03659032 -0.053301603 0.041428106 0.014322670 -0.053140395
## 3 0.02008987 0.076564741 0.007407082 -0.008155719 0.068801893
## 4 0.06284186 0.012720240 -0.017448018 -0.016032279 0.008566123
## 5 0.01318483 0.007603217 -0.078059887 -0.005616140
                                                        0.020742970
##
           Dim 28
                       Dim 29
                                    Dim 30
                                                Dim 31
                                                              Dim 32
## 1 -0.0706677255 -0.01632696 0.001772637 -0.02852486 6.166826e-02
## 2 0.0042930331 0.01225277 0.015512766 0.04997626 2.229776e-02
## 3 0.0172578190 0.04956408 0.005778219 -0.05506712 6.562681e-05
## 4 0.0227482265 -0.04445816 0.026688042 0.01930024 -2.804362e-02
## 5 -0.0001795126 -0.04003250 -0.071902962 -0.02323303 -7.035230e-02
##
                                                                     Dim 38
         Dim 33
                     Dim 34
                                 Dim 35
                                             Dim 36
                                                         Dim 37
## 1 -0.03511275 0.01234266 0.03940228 -0.01476452 0.01782357 -0.051920704
## 2 0.01652172 -0.00330396 0.03590698 -0.03867718 -0.02708309 0.002428777
## 3 -0.02166970 -0.04663777 0.05111587 -0.01940633 -0.01650596 0.014619143
## 4 -0.03275655 -0.03508175 -0.05081201 0.04359383 0.05141450 -0.002054473
## 5 0.06006134 0.10329495 -0.13344411 0.07935152 0.01447790 0.018320056
          Dim 39
##
                      Dim 40
## 1 0.057887164 0.03281676
## 2 -0.013502624 0.06057016
## 3 -0.003288366 -0.04693931
## 4 0.024355042 -0.14004791
## 5 -0.039566556 0.05839010
# between clusters sum of squares
sq = sum(rowSums(k1$centers^2) * k1$size)
sq
## [1] 2076.403
# within clusters sum of squares
Wss = sum(k1$withinss)
Wss
## [1] 15298.35
# total sum of squares
Tss = sum(rowSums(coord^2))
Tss
## [1] 17374.76
sq + Wss
## [1] 17374.76
```

```
# let's calculate the decomposition of inertia
Ib1 = 100 * sq / (sq + Wss)
Ib1
## [1] 11.95069
# let's repeat kmeans, again with k=5
k2 = kmeans(coord, 5)
# between clusters sum of squares
sq = sum(rowSums(k2$centers^2) * k2$size)
Wss = sum(k2\$withinss)
# total sum of squares
Tss = sum(rowSums(coord^2))
sq + Wss
           \# Tss = sq + Wss
## [1] 17374.76
# let's calculate the decomposition of inertia
Ib2 = 100 * sq / (sq + Wss)
## [1] 11.12723
# why are we obtaining different results? (Ib1 != Ib2)
\# you can keep playing with different values for k
# let's repeat kmeans, again with k=8
k3 = kmeans(coord, 8)
# between clusters sum of squares
sq = sum(rowSums(k3$centers^2) * k3$size)
Wss = sum(k3\$withinss)
# total sum of squares
Tss = sum(rowSums(coord^2))
          \# Tss = sq + Wss
sq + Wss
## [1] 17374.76
# let's calculate the decomposition of inertia
Ib3 = 100 * sq / (sq + Wss)
Ib3
## [1] 17.80674
Hierarchical clustering on factorical coordinates from MCA results
# Now, let's apply a hierarchical clustering
# first we calculate a distance matrix between individuals
idist = dist(coord)
# then we apply hclust with method="ward"
# notice the computation cost! (it takes a while to finish)
h1 = hclust(idist, method="ward")
## The "ward" method has been renamed to "ward.D"; note new "ward.D2"
# plot dendrogram
plot(h1, labels=FALSE)
```

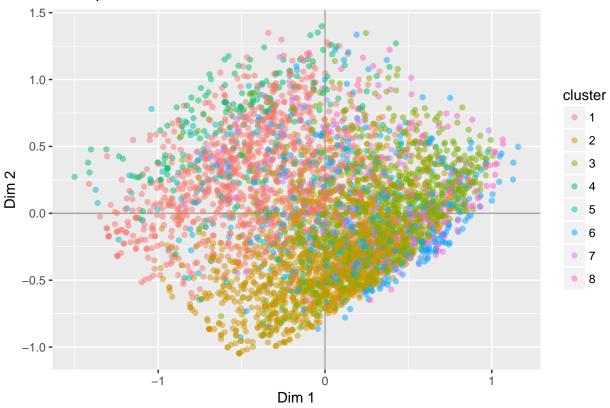
## **Cluster Dendrogram**



## idist hclust (\*, "ward.D")

```
# after checking the dendrogram, how many groups would you choose?
# where would you cut the dendrogram?
# let's try 8 clusters
nc = 8
# let's cut the tree and see the size of clusters
c1 = cutree(h1, nc)
table(c1)
## c1
##
      1
           2
                3
                     4
                          5
                               6
                                    7
                                         8
## 930 1402 994 170 206 361
                                 191 192
# prepare data frame for gaplot
df1 = data.frame(Status=data$Status, mca$ind$coord[,1:2], cluster=as.factor(c1))
# visualize clusters using the first two factorial coordinates
ggplot(data=df1, aes(x=Dim.1, y=Dim.2)) +
  geom_hline(yintercept=0, colour="gray65") +
  geom_vline(xintercept=0, colour="gray65") +
  geom_point(aes(colour=cluster), alpha=0.5) +
  labs(x="Dim 1", y="Dim 2") +
  ggtitle("MCA plot with clusters of individuals")
```

## MCA plot with clusters of individuals



```
# centers of gravity of the clusters
cog = aggregate(as.data.frame(coord), list(c1), mean)[,-1]

# what's the quality of the hierarchical partition?
sq = sum(rowSums(cog^2) * table(c1))
Ib4 = 100 * sq / Tss
Ib4
```

### ## [1] 16.37535

Combining k-means and hierarchical clustering with MCA results

```
# let's consolidate the partition
# we'll apply k-means using the cog's from the hierarchical clustering
k5 = kmeans(coord, center=cog)
k5$size

## [1] 1037 1705 569 178 224 350 190 193
sq = sum(rowSums(k5$centers^2) * k5$size)
Wss = sum(k5$withinss)
```

```
## [1] 17.68192
```

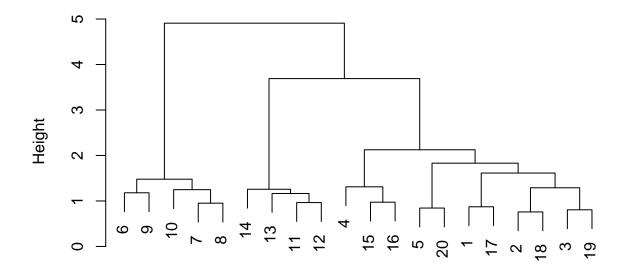
Ib5

Ib5 = 100 \* sq / (sq + Wss)

```
# clustering of large data sets # first 2 kmeans with k=14 n1 = 14
```

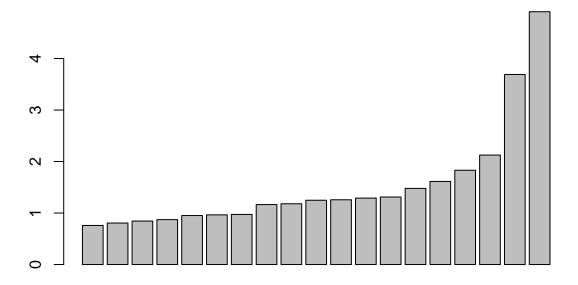
```
km1 = kmeans(coord, n1)
km2 = kmeans(coord, n1)
# what's the overlapping between clusters?
table(km2$cluster, km1$cluster)
##
##
          1
              2
                  3
                      4
                          5
                                  7
                                      8
                                          9 10
                                                 11
                                                     12
                                                         13 14
                              6
##
                  0
                          1
                                      5 141 192
                                                  1
                                                              0
##
       152
              0
                  0
                      0
                          0
                                          0
                                                  0
                                                              0
     2
                              0
                                  0
                                      0
                                              0
                                                      0
                                                          0
##
     3
              0 46 45
                         22
                             14
                                  0 29
                                         17
                                             48
                                                 36
                                                      0
                                                             31
          0
##
     4
          0
              0 139
                      0
                          0
                             38
                                  0 90
                                         11
                                             20
                                                 63
                                                      0
                                                          0
                                                             59
##
     5
          0
              0
                  8 193
                          0
                             63
                                  0 46
                                         25
                                             28
                                                 17
                                                      0
                                                          0
                                                             0
                 21
                                     21
                                         12
                                                             39
##
     6
          0
              1
                    58
                         14
                              5
                                  0
                                             10
                                                  6
                                                      0
                                                          6
     7
          0 178
                  0
                      0
                          0
                              0
                                  0
                                      0
                                         0
                                                  0
                                                      0
                                                          0
                                                             0
##
                                             0
##
              0 92
                      3
                          0
                             46
                                  0 115
                                        13
                                                 52
                                                      0
                                                             21
     8
          0
                                             43
                                                          0 300
##
     9
         0
             0
                 0 42
                          1
                             32
                                  0
                                      0
                                          0
                                              0
                                                  1
                                                      0
##
     10
        0 0
                  0
                     1
                          0
                             18
                                  0
                                      0
                                          0
                                              0
                                                 5
                                                      0 329
                                                              0
##
         0
              0
                  0
                      0
                          0
                              0 190
                                      0
                                          0
                                              0
                                                 0
                                                      0
                                                          0
                                                              0
     11
##
              0
                  3
                      0 341
                             13
                                      9 12
                                             63
                                                17
                                                      0
                                                              7
     12
         0
                                  0
##
     13
          0
              0
                  0
                      0
                          0
                              0
                                  0
                                      0
                                         0
                                             0
                                                  0 221
                                                          0
                                                              0
              0 128
                          0
                             46
                                             34 46
##
     14
                      0
                                  0 178 27
                                                      0
clas = (k2\$cluster - 1)*n1 + k1\$cluster
freq = table(clas)
freq[1:10]
## clas
         2
             3
                4 5 15 16 17 18 19
## 41 564 462 22 162 59 53
                                22 42 21
# what do we have in freq?
cogclas <- aggregate(as.data.frame(coord), list(clas), mean)[,2:(ncol(coord)+1)]</pre>
# perform a hierarchical clustering using cogclas
# compare the computational cost (this is way much faster!)
d2 = dist(cogclas)
h2 = hclust(d2, method="ward", members=freq)
## The "ward" method has been renamed to "ward.D"; note new "ward.D2"
# dendrogram
plot(h2)
```

# **Cluster Dendrogram**



d2 hclust (\*, "ward.D")

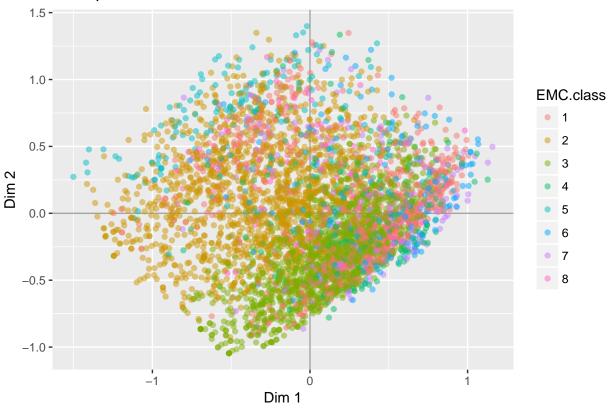
# barplot
barplot(h2\$height)



```
# cut tree in nc=8 groups
c2 <- cutree(h2, nc)
Probabilistic clustering on MCA results
# load package mclust
library(mclust)
## Warning: package 'mclust' was built under R version 3.4.3
## Package 'mclust' version 5.4
## Type 'citation("mclust")' for citing this R package in publications.
\# check the computational cost
emc <- Mclust(coord, G=7:9)</pre>
print(emc)
## 'Mclust' model object:
## best model: ellipsoidal, equal shape (VEV) with 8 components
attributes(emc)
## $names
##
  [1] "call"
                          "data"
                                            "modelName"
                                                              "n"
                          "G"
                                            "BIC"
                                                              "bic"
   [5] "d"
                          "df"
   [9] "loglik"
                                            "hypvol"
                                                              "parameters"
##
## [13] "z"
                          "classification" "uncertainty"
##
## $class
```

```
## [1] "Mclust"
# In this case, we have a probability for each individual
emc$z[1:10,]
                                         [,3] [,4] [,5] [,6] [,7] [,8]
##
              [,1]
                            [,2]
## 1 0.000000e+00 1.000000e+00 0.000000e+00
                                                           0
## 2 0.000000e+00 3.998893e-15 1.000000e+00
                                                           0
                                                                0
                                                                     0
                                                 0
                                                      0
     1.000000e+00 3.264870e-31 4.522799e-36
                                                      0
                                                           0
                                                                0
                                                                     0
## 4 0.000000e+00 1.000000e+00 6.092650e-19
                                                 0
                                                     0
                                                           0
                                                                0
## 5 0.000000e+00 1.000000e+00 0.000000e+00
                                                     0
                                                                0
                                                 0
## 6 0.000000e+00 1.000000e+00 0.000000e+00
                                                     0
                                                          0
                                                               0
                                                                     0
                                                 0
## 7 1.000000e+00 1.231278e-38 2.655344e-35
                                                 0
                                                     0
                                                          0
                                                               0
## 8 0.000000e+00 2.366643e-142 0.000000e+00
                                                     1
                                                          0
                                                               0
## 9 1.933187e-13 3.748554e-34 1.000000e+00
                                                 0
                                                     0
                                                           0
                                                               0
                                                                     0
## 10 0.000000e+00 1.000000e+00 0.000000e+00
                                                     0
                                                           0
                                                               0
# let's see the membership for every individual
emc$classification[1:10]
## 1 2 3 4 5 6 7 8 9 10
## 2 3 1 2 2 2 1 5 3 2
table(emc$classification)
##
          2
                               6
##
      1
               3
                    4
                          5
                                   7
                                         8
## 732 1417 1370 221 157 197 159 193
# what's the quality of the partition?
cog <- aggregate(as.data.frame(coord), list(emc$classification), mean)[,2:(ncol(coord)+1)]</pre>
sq <- sum(rowSums(cog^2)*as.numeric(table(c1)))</pre>
Ib7 <- 100*sq/Tss
Ib7
## [1] 19.75878
# adata emc classification to data frame
df1$EMC.class = as.factor(emc$classification)
# visualize clusters using the first two factorial coordinates
ggplot(data=df1, aes(x=Dim.1, y=Dim.2)) +
  geom_hline(yintercept=0, colour="gray65") +
  geom vline(xintercept=0, colour="gray65") +
 geom_point(aes(colour=EMC.class), alpha=0.5) +
 labs(x="Dim 1", y="Dim 2") +
  ggtitle("MCA plot with clusters of individuals")
```

## MCA plot with clusters of individuals



Apply Decision Trees Analysis

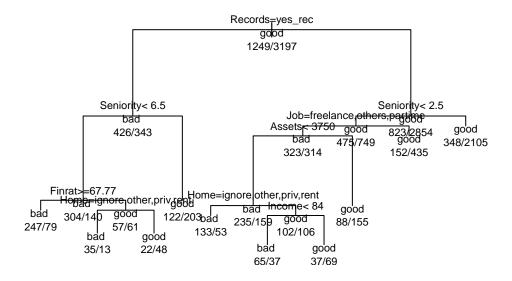
```
# load package FactoMineR and ggplot2
require(ggplot2)
require(rpart)
## Loading required package: rpart
# Let's obtain a decision tree with the function 'rpart'
# using all the variables (both continuous and categorical)
ct = rpart(Status ~ ., data=data)
# let's see how the output looks like
ct
## n= 4446
##
## node), split, n, loss, yval, (yprob)
##
        * denotes terminal node
##
   1) root 4446 1249 good (0.2809267 0.7190733)
##
##
     2) Records=yes_rec 769 343 bad (0.5539662 0.4460338)
##
       4) Seniority < 6.5 444 140 bad (0.6846847 0.3153153)
##
         8) Finrat>=67.77427 326
                                 79 bad (0.7576687 0.2423313) *
##
         9) Finrat< 67.77427 118
                                 57 good (0.4830508 0.5169492)
          ##
##
          19) Home=owner, parents 70 22 good (0.3142857 0.6857143) *
       5) Seniority>=6.5 325 122 good (0.3753846 0.6246154) *
##
     3) Records=no_rec 3677 823 good (0.2238238 0.7761762)
##
```

```
##
        6) Seniority< 2.5 1224 475 good (0.3880719 0.6119281)
##
         12) Job=freelance, others, partime 637 314 bad (0.5070644 0.4929356)
##
           24) Assets< 3750 394 159 bad (0.5964467 0.4035533)
             48) Home=ignore,other,priv,rent 186
                                                    53 bad (0.7150538 0.2849462) *
##
##
             49) Home=owner, parents 208 102 good (0.4903846 0.5096154)
               98) Income< 84 102
                                    37 bad (0.6372549 0.3627451) *
##
               99) Income>=84 106
##
                                    37 good (0.3490566 0.6509434) *
                                  88 good (0.3621399 0.6378601) *
##
           25) Assets>=3750 243
##
         13) Job=fixed 587 152 good (0.2589438 0.7410562) *
        7) Seniority>=2.5 2453 348 good (0.1418671 0.8581329) *
##
```

how to read the output? "node), split, n, loss, yval, (yprob)" node): indicates the node number split: indicates the split criterion n: indicates the number of individuals in the groupe loss: indicates the number of individuals misclassified yval: indicates the predicted value (yprob): indicates the probability of belonging to each class

```
# it's much easier to read a tree with a graphic
plot(ct, margin=0.05, compress=TRUE, main="Decision Tree")
text(ct, use.n=TRUE, pretty=1, all=TRUE, cex=0.7)
```

### **Decision Tree**



one of the goals is to obtain a tree in which the nodes are as much homogenous as possible, but also a tree with good prediction ability In order to improve our decision tree, we need to have 1) a train (aka learning) dataset 2) a test dataset let's keep 2/3 of the data for learning, and 1/3 for testing

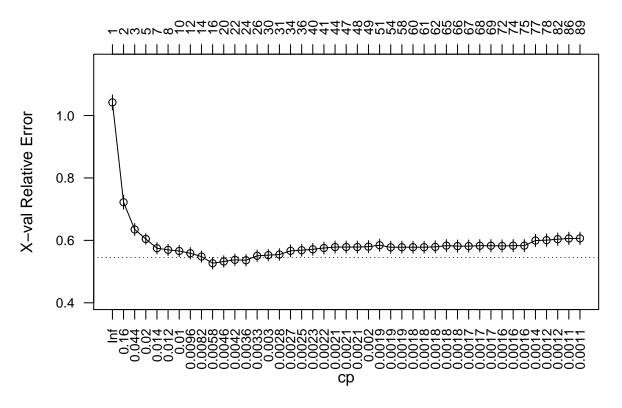
```
n = nrow(data)
learn = sample(1:n, size=round(0.67 * n))
nlearn = length(learn)
ntest = n - nlearn
```

```
CP nsplit rel error
                                      xerror
     0.277819456
                       0 1.0000000 1.0420286 0.02407896
     0.087297774
                       1 0.7221805 0.7221805 0.02228811
## 2
## 3
     0.022583574
                       2 0.6348828 0.6348828 0.01926025
## 4
     0.017029437
                       4 0.5897156 0.6044997 0.01701986
## 5
     0.012035729
                       6 0.5556567 0.5748011 0.01804697
                       7 0.5436210 0.5696093 0.01820245
## 6
     0.011135586
## 7
      0.009732978
                      9 0.5213498 0.5659240 0.01824133
## 8
     0.009493868
                      11 0.5018839 0.5586587 0.01819969
## 9 0.007138446
                      13 0.4828962 0.5481240 0.01814815
                      15 0.4686193 0.5267412 0.01818103
## 10 0.004670715
                      19 0.4488969 0.5322920 0.01836398
## 11 0.004489850
## 12 0.003968714
                      21 0.4399172 0.5377403 0.01845057
## 13 0.003346417
                      23 0.4319798 0.5362365 0.01835202
## 14 0.003163229
                      25 0.4252870 0.5504538 0.01857913
## 15 0.002904984
                      29 0.4112319 0.5527378 0.01853839
                      30 0.4083269 0.5546574 0.01859000
## 16 0.002749293
## 17 0.002567500
                      33 0.4000790 0.5664339 0.01891885
## 18 0.002385241
                      35 0.3949440 0.5684561 0.01906035
## 19 0.002284080
                      39 0.3821308 0.5713098 0.01911207
## 20 0.002151706
                      40 0.3798467 0.5754594 0.01927897
## 21 0.002101822
                      43 0.3728947 0.5785722 0.01935269
## 22 0.002076183
                      46 0.3653162 0.5785722 0.01935269
                      47 0.3632400 0.5785722 0.01935269
## 23 0.002024905
## 24 0.001945202
                      48 0.3612151 0.5797656 0.01937748
## 25 0.001868286
                      50 0.3573247 0.5844875 0.01943142
## 26 0.001868286
                      53 0.3517199 0.5778460 0.01932880
                      57 0.3433126 0.5780539 0.01930680
## 27 0.001841254
## 28 0.001817008
                      59 0.3396301 0.5780539 0.01930680
## 29 0.001817008
                      60 0.3378131 0.5780539 0.01930680
## 30 0.001791370
                      61 0.3359960 0.5790906 0.01939847
## 31 0.001762944
                      64 0.3299241 0.5830323 0.01958410
## 32 0.001762944
                      65 0.3281612 0.5815798 0.01953697
                      66 0.3263982 0.5815798 0.01953697
## 33 0.001711666
## 34 0.001711666
                      67 0.3246866 0.5828244 0.01960581
## 35 0.001658995
                      68 0.3229749 0.5828244 0.01960581
## 36 0.001634750
                      71 0.3169570 0.5820981 0.01958229
## 37 0.001609111
                      73 0.3136875 0.5830323 0.01958410
                      74 0.3120784 0.5830323 0.01958410
## 38 0.001505163
## 39 0.001244595
                      76 0.3090681 0.5994283 0.01985498
                      77 0.3078235 0.6006216 0.01987872
## 40 0.001219653
## 41 0.001158203
                      81 0.3029449 0.6037345 0.01994890
## 42 0.001141111
                      85 0.2976533 0.6060185 0.01990891
```

```
## 43 0.001000000 88 0.2942299 0.6064856 0.01990962
```

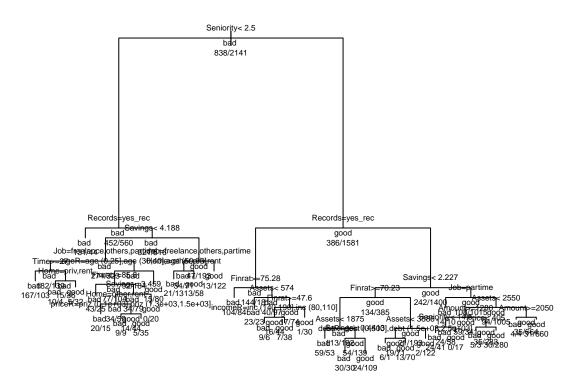
```
# we can use the function 'plotcp' to see the results
# the 'best' tree is the one with the lowest xerror
plotcp(ct1, las=2, cex.axis=0.8)
```

#### size of tree



```
# what is the minimum XERROR?
min(ct1$cptable[,4])
## [1] 0.5267412
min.xe = which(ct1$cptable[,4] == min(ct1$cptable[,4]))
# the optimal tree corresponds to a cp=0.003
ct1$cptable[min.xe,]
##
             CP
                      nsplit
                                rel error
                                                xerror
                                                                xstd
## 0.004670715 15.000000000 0.468619263 0.526741235 0.018181034
# Now that we know that the 'best' tree has cp=0.03
# we can plugin that information in the parameters
ct2 = rpart(Status ~ .,
            data = data[learn,],
            parms = list(prior=c(0.50, 0.50), split='gini'),
            control = rpart.control(cp=0.00285, xval=0, maxdepth=15))
# plot
par(mar = c(1,1,2,0.5))
plot(ct2, margin=0.05, compress=TRUE, main="Decision Tree")
text(ct2, use.n=TRUE, pretty=1, all=TRUE, cex=0.5)
```

## **Decision Tree**



#### summary(ct2)

```
## Call:
## rpart(formula = Status ~ ., data = data[learn, ], parms = list(prior = c(0.5,
       0.5), split = "gini"), control = rpart.control(cp = 0.00285,
       xval = 0, maxdepth = 15)
##
##
    n = 2979
##
##
               CP nsplit rel error
## 1 0.277819456
                       0 1.0000000
## 2
     0.087297774
                       1 0.7221805
## 3
     0.022583574
                       2 0.6348828
     0.017029437
                       4 0.5897156
     0.012035729
                       6 0.5556567
## 5
## 6
     0.011135586
                       7 0.5436210
## 7
     0.009732978
                       9 0.5213498
## 8 0.009493868
                      11 0.5018839
## 9 0.007138446
                      13 0.4828962
## 10 0.004670715
                      15 0.4686193
## 11 0.004489850
                      19 0.4488969
## 12 0.003968714
                      21 0.4399172
## 13 0.003346417
                      23 0.4319798
                      25 0.4252870
## 14 0.003163229
## 15 0.002904984
                      29 0.4112319
## 16 0.002850000
                     30 0.4083269
##
```

```
## Variable importance
   Seniority
                 {\tt Records\ seniority} {\tt R}
                                       Savings
                                                      Job
                                                            savingsR
##
           11
                       9
                           9
                                            8
                                                        7
##
                 finratR
                                                             assetsR
      Finrat
                               Home
                                        Assets
                                                   Income
##
           5
                       5
                                  5
                                             4
                                                        4
                                                                    4
##
                 incomeR
                                                             {\tt amountR}
       Amount
                               ageR
                                           Age
                                                     Time
##
            3
                       3
                                  3
                                             2
                                                        2
##
       Price
                 Marital
                              timeR
                                         debtR
                                                   priceR
##
            2
                       1
                                             1
##
## Node number 1: 2979 observations,
                                        complexity param=0.2778195
                           expected loss=0.5 P(node) =1
##
     predicted class=bad
       class counts: 838 2141
##
##
      probabilities: 0.500 0.500
##
     left son=2 (1012 obs) right son=3 (1967 obs)
##
     Primary splits:
##
                                to the left, improve=119.70850, (0 missing)
         Seniority < 2.5
         seniorityR splits as LLRRR, improve=110.00920, (0 missing)
##
##
                    splits as RL, improve=109.19100, (0 missing)
         Records
                                to the left, improve= 88.06506, (0 missing)
##
         Assets
                    < 2350
##
         Finrat
                    < 70.56687 to the right, improve= 87.37720, (0 missing)
##
     Surrogate splits:
         seniorityR splits as LLRRR, agree=0.926, adj=0.783, (0 split)
##
##
                    splits as RRLL, agree=0.740, adj=0.235, (0 split)
         Job
##
                                to the left, agree=0.703, adj=0.125, (0 split)
         Age
                    < 24.5
##
         ageR
                    splits as LRRRR, agree=0.702, adj=0.123, (0 split)
##
         Marital
                    splits as RRRLR, agree=0.685, adj=0.074, (0 split)
## Node number 2: 1012 observations,
                                        complexity param=0.01702944
                           expected loss=0.3265665 P(node) =0.4004697
##
     predicted class=bad
##
       class counts: 452
                             560
##
      probabilities: 0.673 0.327
     left son=4 (175 obs) right son=5 (837 obs)
##
##
     Primary splits:
         Records splits as RL, improve=29.92989, (0 missing)
##
##
         Savings < 4.204615 to the left, improve=27.13412, (0 missing)
##
                  splits as RLLL, improve=25.71396, (0 missing)
##
                  < 70.38018 to the right, improve=24.73849, (0 missing)
         savingsR splits as LLLRR, improve=24.54408, (0 missing)
##
##
     Surrogate splits:
##
         Price
                  < 2628
                              to the right, agree=0.834, adj=0.040, (0 split)
##
         Expenses < 144
                              to the right, agree=0.829, adj=0.011, (0 split)
                              to the right, agree=0.829, adj=0.011, (0 split)
##
         Amount < 2175
##
## Node number 3: 1967 observations,
                                        complexity param=0.08729777
     predicted class=good expected loss=0.3841512 P(node) =0.5995303
##
                     386 1581
##
       class counts:
##
     probabilities: 0.384 0.616
##
     left son=6 (325 obs) right son=7 (1642 obs)
##
     Primary splits:
##
         Records splits as RL, improve=79.51797, (0 missing)
##
         Assets < 1775
                            to the left, improve=52.50765, (0 missing)
         Finrat < 68.82601 to the right, improve=50.42371, (0 missing)
##
         finratR splits as RRLLL, improve=48.22299, (0 missing)
##
```

```
##
         assetsR splits as LLRRR, improve=43.70741, (0 missing)
##
     Surrogate splits:
         Amount < 3125
##
                            to the right, agree=0.835, adj=0.003, (0 split)
##
## Node number 4: 175 observations
     predicted class=bad
                           expected loss=0.1161897 P(node) =0.08843786
##
##
       class counts:
                       131
##
      probabilities: 0.884 0.116
##
## Node number 5: 837 observations,
                                       complexity param=0.01702944
     predicted class=bad
                           expected loss=0.3861927 P(node) =0.3120319
                             516
##
                       321
       class counts:
##
      probabilities: 0.614 0.386
     left son=10 (597 obs) right son=11 (240 obs)
##
##
     Primary splits:
##
         Savings < 4.188
                              to the left, improve=30.16554, (0 missing)
##
                  splits as RLLL, improve=30.14267, (0 missing)
         Job
##
         savingsR splits as LLLRR, improve=28.72795, (0 missing)
##
                 < 71.64577 to the right, improve=22.12857, (0 missing)
##
         finratR splits as RRLLL, improve=20.19856, (0 missing)
##
     Surrogate splits:
##
         savingsR splits as LLLRR, agree=0.977, adj=0.921, (0 split)
##
                 < 145.5
                             to the left, agree=0.849, adj=0.475, (0 split)
         Income
         incomeR splits as LLRRL, agree=0.843, adj=0.454, (0 split)
##
##
         Assets
                 < 1e+05
                              to the left, agree=0.716, adj=0.008, (0 split)
##
         Expenses < 111.5
                              to the left, agree=0.714, adj=0.004, (0 split)
##
                                       complexity param=0.007138446
## Node number 6: 325 observations,
                           expected loss=0.3297477 P(node) =0.1281888
     predicted class=bad
##
##
       class counts:
                       144
                             181
##
      probabilities: 0.670 0.330
##
     left son=12 (188 obs) right son=13 (137 obs)
##
     Primary splits:
##
         Finrat < 75.27964 to the right, improve=10.751960, (0 missing)
##
         finratR splits as RLLLL, improve= 8.639520, (0 missing)
##
                splits as RLRLLL, improve= 8.159015, (0 missing)
##
         Assets < 574
                             to the left, improve= 6.954906, (0 missing)
##
         Income < 109.5
                             to the left, improve= 6.481317, (0 missing)
##
     Surrogate splits:
##
         finratR splits as RRLLL, agree=0.923, adj=0.818, (0 split)
##
                            to the right, agree=0.751, adj=0.409, (0 split)
         Amount < 837.5
##
         amountR splits as RLLRL, agree=0.738, adj=0.380, (0 split)
                splits as RRLRL, agree=0.686, adj=0.255, (0 split)
##
         timeR
##
         Time
                 < 33
                             to the right, agree=0.677, adj=0.234, (0 split)
##
## Node number 7: 1642 observations,
                                        complexity param=0.02258357
     predicted class=good expected loss=0.3063414 P(node) =0.4713414
##
##
       class counts:
                       242 1400
##
      probabilities: 0.306 0.694
##
     left son=14 (519 obs) right son=15 (1123 obs)
##
     Primary splits:
##
         Savings < 2.227444 to the left, improve=42.73541, (0 missing)
##
                  < 70.23458 to the right, improve=38.59446, (0 missing)
##
         finratR splits as RRLLL, improve=37.49342, (0 missing)
```

```
##
         savingsR splits as LLRRR, improve=37.28172, (0 missing)
##
                              to the left, improve=37.05155, (0 missing)
         Assets
                 < 3586
##
     Surrogate splits:
##
         savingsR splits as LLRRR, agree=0.964, adj=0.886, (0 split)
##
         Income
                  < 97.5
                              to the left, agree=0.831, adj=0.466, (0 split)
         incomeR splits as LRRRL, agree=0.816, adj=0.418, (0 split)
##
                              to the left, agree=0.692, adj=0.027, (0 split)
##
         Time
                  < 15
                  splits as LRRRR, agree=0.692, adj=0.027, (0 split)
##
         timeR
##
## Node number 10: 597 observations,
                                        complexity param=0.009732978
##
     predicted class=bad
                           expected loss=0.3157255 P(node) =0.2389165
                             323
##
       class counts:
                       274
##
      probabilities: 0.684 0.316
     left son=20 (321 obs) right son=21 (276 obs)
##
##
     Primary splits:
##
         Job
                 splits as RLLL, improve=15.029720, (0 missing)
##
         Finrat < 71.64577 to the right, improve=14.406310, (0 missing)
##
         finratR splits as RRLLL, improve=11.887890, (0 missing)
##
                 splits as RRLLL, improve= 9.870686, (0 missing)
         timeR
                             to the right, improve= 9.870686, (0 missing)
##
         Time
                 < 27
##
     Surrogate splits:
##
         Seniority < 0.5
                                to the left, agree=0.645, adj=0.232, (0 split)
##
         seniorityR splits as LR---, agree=0.643, adj=0.228, (0 split)
                                to the left, agree=0.603, adj=0.141, (0 split)
##
         Income
                    < 85.5
##
         Savings
                    < 1.647958 to the left, agree=0.600, adj=0.134, (0 split)
##
         savingsR
                    splits as LLRL-, agree=0.598, adj=0.130, (0 split)
##
## Node number 11: 240 observations,
                                        complexity param=0.009493868
     predicted class=good expected loss=0.383544 P(node) =0.07311536
##
##
       class counts:
                        47
                             193
##
      probabilities: 0.384 0.616
##
     left son=22 (105 obs) right son=23 (135 obs)
##
     Primary splits:
##
         Job
                 splits as RLLL, improve=12.313570, (0 missing)
##
                 splits as
                           -LRRLL, improve= 8.991849, (0 missing)
##
         amountR splits as LLLRR, improve= 6.803730, (0 missing)
##
         Assets < 2250
                             to the left, improve= 5.963506, (0 missing)
##
         assetsR splits as LRRRR, improve= 5.827538, (0 missing)
##
     Surrogate splits:
##
                                to the left, agree=0.617, adj=0.124, (0 split)
         Seniority < 0.5
         seniorityR splits as LR---, agree=0.608, adj=0.105, (0 split)
##
##
                    < 21.5
                                to the left, agree=0.604, adj=0.095, (0 split)
         Age
                    < 4250
                                to the right, agree=0.604, adj=0.095, (0 split)
##
         Assets
##
                                to the left, agree=0.600, adj=0.086, (0 split)
         Time
                    < 33
##
## Node number 12: 188 observations
                           expected loss=0.2401998 P(node) =0.08166951
##
     predicted class=bad
##
       class counts:
                       104
                              84
##
      probabilities: 0.760 0.240
##
                                        complexity param=0.007138446
## Node number 13: 137 observations,
                           expected loss=0.4869583 P(node) =0.04651931
##
    predicted class=bad
##
      class counts:
                        40
                              97
##
     probabilities: 0.513 0.487
```

```
##
     left son=26 (46 obs) right son=27 (91 obs)
##
     Primary splits:
##
         Assets
                   < 574
                               to the left, improve=8.161677, (0 missing)
                              -LRLRL, improve=7.875192, (0 missing)
##
         Home
                   splits as
##
         assetsR
                  splits as LRRRR, improve=7.577441, (0 missing)
##
         Seniority < 11.5
                               to the left, improve=5.852244, (0 missing)
##
                   < 21
                               to the right, improve=4.819471, (0 missing)
         Time
##
     Surrogate splits:
##
         assetsR splits as LRRRR, agree=0.985, adj=0.957, (0 split)
##
                           -LRLRL, agree=0.920, adj=0.761, (0 split)
                 splits as
##
         Marital splits as -RLLR, agree=0.730, adj=0.196, (0 split)
##
                             to the left, agree=0.693, adj=0.087, (0 split)
                 < 27.5
         Age
         Finrat < 72.02305 to the right, agree=0.693, adj=0.087, (0 split)
##
##
## Node number 14: 519 observations,
                                        complexity param=0.02258357
##
     predicted class=good expected loss=0.4706853 P(node) =0.1698635
##
                             385
       class counts:
                     134
##
     probabilities: 0.471 0.529
##
     left son=28 (305 obs) right son=29 (214 obs)
##
     Primary splits:
##
        Finrat
                 < 70.23458 to the right, improve=33.28179, (0 missing)
##
         finratR splits as RRLLL, improve=31.98542, (0 missing)
                              to the left, improve=20.80176, (0 missing)
##
                  < 3586
         Assets
##
         assetsR splits as LLLRR, improve=18.70308, (0 missing)
##
                              to the right, improve=13.74221, (0 missing)
         Expenses < 81.5
##
     Surrogate splits:
##
         finratR splits as RRLLL, agree=0.994, adj=0.986, (0 split)
                             to the right, agree=0.730, adj=0.346, (0 split)
##
         Time
                 < 27
##
                 splits as RRLLL, agree=0.730, adj=0.346, (0 split)
         timeR
                             to the right, agree=0.728, adj=0.341, (0 split)
##
         Amount < 815
##
         amountR splits as RLLRL, agree=0.709, adj=0.294, (0 split)
##
## Node number 15: 1123 observations,
                                         complexity param=0.01203573
     predicted class=good expected loss=0.2137442 P(node) =0.3014779
##
##
       class counts:
                      108 1015
##
      probabilities: 0.214 0.786
     left son=30 (24 obs) right son=31 (1099 obs)
##
##
     Primary splits:
##
         Job
                 splits as RRRL, improve=21.28309, (0 missing)
##
         Assets < 2550
                             to the left, improve=17.58550, (0 missing)
##
        Finrat < 82.37497 to the right, improve=15.02562, (0 missing)
##
         assetsR splits as LLRRR, improve=13.87911, (0 missing)
         finratR splits as RRRLL, improve=13.66296, (0 missing)
##
##
## Node number 20: 321 observations,
                                        complexity param=0.00448985
                           expected loss=0.2301361 P(node) =0.1410534
##
     predicted class=bad
##
       class counts:
                     182
                             139
##
     probabilities: 0.770 0.230
##
     left son=40 (270 obs) right son=41 (51 obs)
##
     Primary splits:
##
         Time
                             to the right, improve=7.622062, (0 missing)
                 < 27
##
         timeR
                 splits as RRLLL, improve=7.622062, (0 missing)
##
         Finrat < 69.74764 to the right, improve=6.931061, (0 missing)
         finratR splits as RRLLL, improve=6.562940, (0 missing)
##
```

```
##
         Assets < 7250
                            to the left, improve=6.380556, (0 missing)
##
     Surrogate splits:
##
         Amount < 367.5
                             to the right, agree=0.875, adj=0.216, (0 split)
         Finrat < 35.32617 to the right, agree=0.875, adj=0.216, (0 split)
##
##
         Price
                 < 387.5
                             to the right, agree=0.850, adj=0.059, (0 split)
##
         finratR splits as RLLLL, agree=0.850, adj=0.059, (0 split)
                                        complexity param=0.009732978
## Node number 21: 276 observations,
##
     predicted class=bad
                           expected loss=0.4390883 P(node) =0.09786318
##
       class counts:
                        92
                             184
##
      probabilities: 0.561 0.439
##
     left son=42 (181 obs) right son=43 (95 obs)
##
     Primary splits:
                 splits as LRLRL, improve=12.88861, (0 missing)
##
         ageR
##
         Finrat < 79.83308 to the right, improve=11.53539, (0 missing)
##
                 splits as LLRRRL, improve=11.40421, (0 missing)
##
         amountR splits as RLLLR, improve=10.83089, (0 missing)
##
         finratR splits as RRRLL, improve= 9.32726, (0 missing)
##
     Surrogate splits:
##
         Age
                  < 40.5
                              to the left, agree=0.746, adj=0.263, (0 split)
##
         Savings < 3.905158 to the left, agree=0.670, adj=0.042, (0 split)
##
                              to the left, agree=0.667, adj=0.032, (0 split)
         Expenses < 89
##
         Marital splits as LLRLL, agree=0.663, adj=0.021, (0 split)
                              to the left, agree=0.663, adj=0.021, (0 split)
##
         Income < 177.5
##
## Node number 22: 105 observations,
                                        complexity param=0.009493868
     predicted class=bad
                           expected loss=0.4497475 P(node) =0.03686743
##
                              71
##
       class counts:
                        34
##
     probabilities: 0.550 0.450
##
     left son=44 (34 obs) right son=45 (71 obs)
##
     Primary splits:
##
         Home
                  splits as -LRRLL, improve=10.413170, (0 missing)
##
         Assets
                  < 2250
                              to the left, improve= 9.691406, (0 missing)
##
         assetsR splits as LRRRR, improve= 9.039795, (0 missing)
##
                  splits as LLRLR, improve= 5.459168, (0 missing)
         priceR
##
                              to the right, improve= 3.438065, (0 missing)
         Expenses < 46
##
     Surrogate splits:
##
         Expenses < 46
                               to the right, agree=0.743, adj=0.206, (0 split)
##
                   splits as RRLRR, agree=0.743, adj=0.206, (0 split)
         ageR
##
         expensesR splits as RRRLL, agree=0.743, adj=0.206, (0 split)
                               to the left, agree=0.724, adj=0.147, (0 split)
##
         Assets
                   < 1750
                   splits as LRRRR, agree=0.714, adj=0.118, (0 split)
##
         assetsR
##
## Node number 23: 135 observations
##
     predicted class=good expected loss=0.2139864 P(node) =0.03624792
##
       class counts:
                        13
                             122
##
      probabilities: 0.214 0.786
##
## Node number 26: 46 observations
##
     predicted class=bad
                           expected loss=0.2813025 P(node) =0.01909447
##
       class counts:
                        23
                              23
##
      probabilities: 0.719 0.281
##
## Node number 27: 91 observations,
                                       complexity param=0.003968714
```

```
##
     predicted class=good expected loss=0.3698544 P(node) =0.02742484
##
                        17
                              74
       class counts:
     probabilities: 0.370 0.630
##
##
     left son=54 (60 obs) right son=55 (31 obs)
##
     Primary splits:
##
        Finrat
                   < 47.60035 to the right, improve=5.320696, (0 missing)
##
         Time
                               to the right, improve=4.413863, (0 missing)
                   splits as RRLLL, improve=4.126937, (0 missing)
##
         timeR
##
         Seniority < 11.5
                               to the left, improve=2.586744, (0 missing)
##
         expensesR splits as LRRRL, improve=2.370883, (0 missing)
##
     Surrogate splits:
         finratR splits as RLL--, agree=0.967, adj=0.903, (0 split)
##
                             to the right, agree=0.802, adj=0.419, (0 split)
##
         Amount < 560
##
         amountR splits as RLLLL, agree=0.769, adj=0.323, (0 split)
##
                 < 33
                             to the right, agree=0.703, adj=0.129, (0 split)
         Time
##
         Age
                 < 27.5
                             to the right, agree=0.692, adj=0.097, (0 split)
##
## Node number 28: 305 observations,
                                        complexity param=0.01113559
     predicted class=bad
                           expected loss=0.3994151 P(node) =0.1122613
##
##
       class counts: 113
                             192
##
      probabilities: 0.601 0.399
##
     left son=56 (112 obs) right son=57 (193 obs)
##
     Primary splits:
##
         Assets
                               to the left, improve=9.544324, (0 missing)
                   < 1875
##
         Expenses < 88.5
                               to the right, improve=8.504675, (0 missing)
##
                  < 0.8863636 to the left, improve=7.668591, (0 missing)
##
         expensesR splits as RRRRL, improve=7.036196, (0 missing)
                  splits as LLLRR, improve=6.963943, (0 missing)
##
         assetsR
##
     Surrogate splits:
         assetsR splits as LRRRR, agree=0.967, adj=0.911, (0 split)
##
##
                 splits as
                           -LRLRL, agree=0.839, adj=0.562, (0 split)
##
         Marital splits as LRRLR, agree=0.682, adj=0.134, (0 split)
##
         Age
                 < 24.5
                             to the left, agree=0.662, adj=0.080, (0 split)
##
         Amount < 462.5
                             to the left, agree=0.652, adj=0.054, (0 split)
## Node number 29: 214 observations,
                                        complexity param=0.003346417
##
    predicted class=good expected loss=0.2175234 P(node) =0.05760223
##
       class counts:
                        21 193
##
     probabilities: 0.218 0.782
##
     left son=58 (90 obs) right son=59 (124 obs)
##
     Primary splits:
                             to the left, improve=11.474350, (0 missing)
##
         Assets < 3586
         assetsR splits as LLRRR, improve= 9.019293, (0 missing)
##
##
         debtR
                splits as RLRRR, improve= 8.873948, (0 missing)
                            to the left, improve= 7.795581, (0 missing)
##
         Age
                 < 36.5
                 splits as -LRRLR, improve= 7.430395, (0 missing)
##
         Home
##
     Surrogate splits:
##
         assetsR splits as LLRRR, agree=0.963, adj=0.911, (0 split)
##
         Home
                 splits as
                           -LRLLL, agree=0.794, adj=0.511, (0 split)
                            to the left, agree=0.692, adj=0.267, (0 split)
##
         Age
                 < 28.5
##
         Marital splits as RRRLR, agree=0.664, adj=0.200, (0 split)
                 splits as LLRRR, agree=0.664, adj=0.200, (0 split)
##
##
## Node number 30: 24 observations
```

```
##
                           expected loss=0.2184909 P(node) =0.01068858
     predicted class=bad
##
       class counts:
                        14
                              10
      probabilities: 0.782 0.218
##
##
## Node number 31: 1099 observations,
                                         complexity param=0.003163229
     predicted class=good expected loss=0.1928747 P(node) =0.2907893
##
       class counts:
                        94 1005
##
##
      probabilities: 0.193 0.807
##
     left son=62 (400 obs) right son=63 (699 obs)
##
     Primary splits:
                             to the left, improve=14.60992, (0 missing)
##
         Assets < 2550
         Finrat < 79.47655 to the right, improve=12.80257, (0 missing)
##
##
         assetsR splits as LRRRR, improve=12.14084, (0 missing)
##
                 splits as LLRLRL, improve=12.13259, (0 missing)
##
         finratR splits as RRRLL, improve=11.33896, (0 missing)
##
     Surrogate splits:
##
         assetsR splits as LLRRR, agree=0.938, adj=0.830, (0 split)
##
                 splits as RLRLRL, agree=0.878, adj=0.665, (0 split)
##
         Marital splits as RRLLR, agree=0.668, adj=0.087, (0 split)
##
         Age
                 < 26.5
                             to the left, agree=0.656, adj=0.055, (0 split)
##
         ageR
                 splits as LRRRR, agree=0.653, adj=0.047, (0 split)
##
## Node number 40: 270 observations
                           expected loss=0.1944618 P(node) =0.1236962
##
     predicted class=bad
##
       class counts:
                       167
                             103
##
      probabilities: 0.806 0.194
##
## Node number 41: 51 observations,
                                       complexity param=0.00448985
                           expected loss=0.4843697 P(node) =0.01735717
     predicted class=bad
##
##
       class counts:
                        15
                              36
##
      probabilities: 0.516 0.484
##
     left son=82 (14 obs) right son=83 (37 obs)
##
     Primary splits:
##
                 splits as RRRRLL, improve=8.312737, (0 missing)
         Home
##
         finratR splits as RLLRR, improve=6.401945, (0 missing)
##
         Finrat < 50.95748 to the right, improve=4.000770, (0 missing)
##
         Assets < 2250
                             to the left, improve=4.000770, (0 missing)
##
         Savings < 2.416667 to the left, improve=3.316496, (0 missing)
##
     Surrogate splits:
##
         Price
                               to the left, agree=0.784, adj=0.214, (0 split)
                   < 428
##
                   splits as RRLRR, agree=0.765, adj=0.143, (0 split)
         finratR
##
         Seniority < 1.5
                               to the right, agree=0.745, adj=0.071, (0 split)
                  splits as -RLR-, agree=0.745, adj=0.071, (0 split)
##
         Marital
##
         Assets
                               to the right, agree=0.745, adj=0.071, (0 split)
                   < 19000
##
## Node number 42: 181 observations,
                                        complexity param=0.004670715
                           expected loss=0.3458289 P(node) =0.07023044
##
     predicted class=bad
##
       class counts:
                        77
                             104
##
      probabilities: 0.654 0.346
##
     left son=84 (68 obs) right son=85 (113 obs)
##
     Primary splits:
         Finrat < 85.79927 to the right, improve=8.758754, (0 missing)
##
##
         finratR splits as RRRLL, improve=7.637574, (0 missing)
                 splits as LLRRRL, improve=6.878251, (0 missing)
##
         Home
```

```
##
         amountR splits as RLLLR, improve=5.189681, (0 missing)
##
         Assets < 1650
                            to the left, improve=4.853888, (0 missing)
     Surrogate splits:
##
##
         finratR splits as RRRRL, agree=0.884, adj=0.691, (0 split)
##
         Amount < 1330
                            to the right, agree=0.696, adj=0.191, (0 split)
         amountR splits as RRLRR, agree=0.674, adj=0.132, (0 split)
##
                            to the left, agree=0.652, adj=0.074, (0 split)
##
        Price
                < 1007
         priceR splits as LRRRR, agree=0.652, adj=0.074, (0 split)
##
##
## Node number 43: 95 observations
##
     predicted class=good expected loss=0.3238868 P(node) =0.02763274
       class counts:
##
                       15
##
      probabilities: 0.324 0.676
##
## Node number 44: 34 observations
##
     predicted class=bad
                         expected loss=0.1950407 P(node) =0.0155658
       class counts:
##
                       21
                              13
##
      probabilities: 0.805 0.195
##
## Node number 45: 71 observations
##
    predicted class=good expected loss=0.3641299 P(node) =0.02130164
##
      class counts:
                       13
                              58
##
     probabilities: 0.364 0.636
##
## Node number 54: 60 observations,
                                       complexity param=0.003968714
##
     predicted class=good expected loss=0.4816106 P(node) =0.01982211
##
      class counts:
                             44
                      16
##
      probabilities: 0.482 0.518
##
     left son=108 (15 obs) right son=109 (45 obs)
##
     Primary splits:
##
         incomeR
                   splits as RRLRL, improve=5.943565, (0 missing)
##
         timeR
                   splits as LRLLL, improve=3.249133, (0 missing)
##
                   < 110
                              to the left, improve=2.753481, (0 missing)
##
                   < 8.404286 to the left, improve=2.289904, (0 missing)
         Savings
##
         expensesR splits as LRRRL, improve=2.270408, (0 missing)
##
     Surrogate splits:
##
         Finrat < 48.48595 to the left, agree=0.783, adj=0.133, (0 split)
##
                 splits as -RRLRR, agree=0.767, adj=0.067, (0 split)
        Home
##
                            to the left, agree=0.767, adj=0.067, (0 split)
         Age
                 < 30.5
                 splits as -LRRR, agree=0.767, adj=0.067, (0 split)
##
         finratR splits as LRR--, agree=0.767, adj=0.067, (0 split)
##
##
## Node number 55: 31 observations
##
     predicted class=good expected loss=0.07847953 P(node) =0.007602731
##
       class counts:
                       1
##
      probabilities: 0.078 0.922
##
## Node number 56: 112 observations
##
     predicted class=bad
                           expected loss=0.2601372 P(node) =0.04758026
##
       class counts:
                       59
##
      probabilities: 0.740 0.260
##
## Node number 57: 193 observations,
                                        complexity param=0.01113559
    predicted class=good expected loss=0.4981301 P(node) =0.06468104
```

```
##
       class counts:
                        54
     probabilities: 0.498 0.502
##
##
     left son=114 (60 obs) right son=115 (133 obs)
##
     Primary splits:
##
         Savings
                   < 0.4413333 to the left, improve=11.739480, (0 missing)
##
                               to the right, improve= 9.522977, (0 missing)
         Expenses < 80
##
         expensesR splits as RRRRL, improve= 9.522977, (0 missing)
                   splits as RLLRL, improve= 7.042992, (0 missing)
##
         Marital
##
         Age
                   < 26.5
                               to the right, improve= 6.601569, (0 missing)
##
     Surrogate splits:
##
         savingsR splits as LRR--, agree=0.845, adj=0.500, (0 split)
                               to the left, agree=0.777, adj=0.283, (0 split)
##
         Income
                   < 68
##
         Expenses < 80
                               to the right, agree=0.725, adj=0.117, (0 split)
##
         expensesR splits as RRRRL, agree=0.725, adj=0.117, (0 split)
##
                   < 462.5
                               to the left, agree=0.705, adj=0.050, (0 split)
         Amount
##
## Node number 58: 90 observations,
                                       complexity param=0.003346417
     predicted class=good expected loss=0.4060713 P(node) =0.02791755
##
##
       class counts:
                        19
                              71
##
      probabilities: 0.406 0.594
##
     left son=116 (7 obs) right son=117 (83 obs)
##
     Primary splits:
##
         debtR
                   splits as RLL-R, improve=7.467203, (0 missing)
         Finrat
                   < 45.42485 to the right, improve=5.938332, (0 missing)
##
##
         Debt
                   < 0.5
                               to the right, improve=4.804710, (0 missing)
##
         expensesR splits as LLRRL, improve=4.059766, (0 missing)
##
                             -LRRLR, improve=4.002488, (0 missing)
                   splits as
##
     Surrogate splits:
##
         Debt < 0.5
                          to the right, agree=0.967, adj=0.571, (0 split)
         Home splits as -RRRLR, agree=0.933, adj=0.143, (0 split)
##
##
## Node number 59: 124 observations
##
     predicted class=good expected loss=0.04019978 P(node) =0.02968468
##
       class counts:
                         2
                             122
##
      probabilities: 0.040 0.960
##
## Node number 62: 400 observations,
                                        complexity param=0.003163229
##
     predicted class=good expected loss=0.3065422 P(node) =0.1148385
##
       class counts:
                        59
                             341
##
     probabilities: 0.307 0.693
     left son=124 (82 obs) right son=125 (318 obs)
##
##
     Primary splits:
         Amount < 1280
##
                             to the right, improve=9.425519, (0 missing)
##
         Job
                 splits as RLR-, improve=9.111476, (0 missing)
##
         Finrat < 73.75541 to the right, improve=8.027891, (0 missing)
         finratR splits as RRRLL, improve=6.924853, (0 missing)
##
##
         Price
                 < 405
                             to the left, improve=5.743579, (0 missing)
##
     Surrogate splits:
##
         amountR splits as RRLRR, agree=0.908, adj=0.549, (0 split)
##
         Price
                 < 1997.5
                             to the right, agree=0.828, adj=0.159, (0 split)
##
         priceR splits as RRRLR, agree=0.810, adj=0.073, (0 split)
##
         Debt
                             to the right, agree=0.802, adj=0.037, (0 split)
##
         debtR
                 splits as RRR-L, agree=0.802, adj=0.037, (0 split)
##
```

```
## Node number 63: 699 observations,
                                       complexity param=0.002904984
     predicted class=good expected loss=0.1186869 P(node) =0.1759508
##
##
       class counts:
                       35
                            664
##
     probabilities: 0.119 0.881
##
     left son=126 (8 obs) right son=127 (691 obs)
##
     Primary splits:
        Amount < 2050
                            to the right, improve=7.259942, (0 missing)
##
                            to the right, improve=5.080536, (0 missing)
                < 2744
##
        Price
##
        Finrat < 76.08052 to the right, improve=4.823086, (0 missing)
##
        Assets < 57500
                            to the right, improve=4.242301, (0 missing)
##
        finratR splits as RRRLL, improve=3.880929, (0 missing)
##
     Surrogate splits:
##
        Price < 4462
                           to the right, agree=0.991, adj=0.25, (0 split)
##
## Node number 82: 14 observations
##
     predicted class=bad expected loss=0.1353687 P(node) =0.00690073
##
       class counts:
                      10
##
      probabilities: 0.865 0.135
##
## Node number 83: 37 observations
##
     predicted class=good expected loss=0.2853069 P(node) =0.01045644
##
      class counts:
                      5 32
##
     probabilities: 0.285 0.715
##
## Node number 84: 68 observations
##
     predicted class=bad expected loss=0.1853769 P(node) =0.03149472
##
      class counts:
                       43
                              25
##
      probabilities: 0.815 0.185
##
## Node number 85: 113 observations,
                                      complexity param=0.004670715
##
     predicted class=bad
                          expected loss=0.4762871 P(node) =0.03873572
##
       class counts:
                       34
                             79
##
     probabilities: 0.524 0.476
##
     left son=170 (93 obs) right son=171 (20 obs)
##
     Primary splits:
##
        Savings < 3.458769 to the left, improve=8.679078, (0 missing)
##
        Assets < 1650
                            to the left, improve=6.605593, (0 missing)
##
         Income < 108.5
                            to the left, improve=6.589169, (0 missing)
##
         incomeR splits as LRR-L, improve=5.692712, (0 missing)
##
                splits as -LRRRL, improve=5.589621, (0 missing)
        Home
##
     Surrogate splits:
##
         Income < 141.5
                             to the left, agree=0.850, adj=0.15, (0 split)
##
        Finrat
                 < 85.35308 to the left, agree=0.841, adj=0.10, (0 split)
         incomeR splits as LLR-L, agree=0.841, adj=0.10, (0 split)
##
         savingsR splits as LLLR-, agree=0.841, adj=0.10, (0 split)
##
         Marital splits as LLLLR, agree=0.832, adj=0.05, (0 split)
##
## Node number 108: 15 observations
##
     predicted class=bad expected loss=0.2069391 P(node) =0.006771143
##
       class counts:
##
      probabilities: 0.793 0.207
##
## Node number 109: 45 observations
    predicted class=good expected loss=0.3200231 P(node) =0.01305097
```

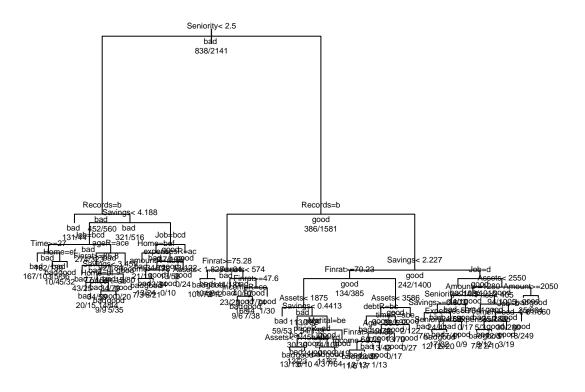
```
##
       class counts:
                       7
##
      probabilities: 0.320 0.680
##
## Node number 114: 60 observations
##
     predicted class=bad
                           expected loss=0.2813025 P(node) =0.02490583
##
      class counts:
                        30
                              30
##
     probabilities: 0.719 0.281
##
## Node number 115: 133 observations
##
     predicted class=good expected loss=0.3600185 P(node) =0.0397752
##
       class counts:
                        24
                             109
##
      probabilities: 0.360 0.640
##
## Node number 116: 7 observations
##
     predicted class=bad
                           expected loss=0.0612394 P(node) =0.003813488
##
       class counts:
##
      probabilities: 0.939 0.061
##
## Node number 117: 83 observations
     predicted class=good expected loss=0.3217948 P(node) =0.02410406
##
      class counts:
                        13
                              70
##
     probabilities: 0.322 0.678
##
                                        complexity param=0.003163229
## Node number 124: 82 observations,
                           expected loss=0.4860983 P(node) =0.02786488
##
     predicted class=bad
##
      class counts:
                        24
                              58
##
      probabilities: 0.514 0.486
##
     left son=248 (65 obs) right son=249 (17 obs)
##
     Primary splits:
##
         Seniority < 14.5
                                to the left, improve=7.284791, (0 missing)
##
         seniorityR splits as -LRLL, improve=7.284791, (0 missing)
##
         Savings
                    < 6.883761 to the right, improve=4.934247, (0 missing)
##
                    < 245.5
                               to the right, improve=4.130740, (0 missing)
##
                    splits as --RLL, improve=3.118667, (0 missing)
         savingsR
##
     Surrogate splits:
##
         Price < 1382.5
                           to the right, agree=0.841, adj=0.235, (0 split)
##
         debtR splits as LR--L, agree=0.805, adj=0.059, (0 split)
##
## Node number 125: 318 observations,
                                         complexity param=0.003163229
     predicted class=good expected loss=0.2401078 P(node) =0.08697367
##
##
       class counts:
                        35
                             283
##
      probabilities: 0.240 0.760
##
     left son=250 (8 obs) right son=251 (310 obs)
##
     Primary splits:
##
         Price < 405
                            to the left, improve=7.438997, (0 missing)
##
                splits as RLR-, improve=6.508769, (0 missing)
         Job
##
         Income < 113.5
                           to the left, improve=4.424561, (0 missing)
##
         Finrat < 61.81591 to the right, improve=3.724642, (0 missing)
##
         Age
               < 23.5
                           to the left, improve=3.473651, (0 missing)
##
## Node number 126: 8 observations
##
    predicted class=bad
                           expected loss=0.2813025 P(node) =0.003320778
##
      class counts:
                       4
                               4
##
     probabilities: 0.719 0.281
```

```
##
## Node number 127: 691 observations
##
     predicted class=good expected loss=0.1071449 P(node) =0.17263
##
       class counts:
                       31
                            660
##
      probabilities: 0.107 0.893
##
## Node number 170: 93 observations,
                                       complexity param=0.004670715
                          expected loss=0.4044799 P(node) =0.034065
##
     predicted class=bad
##
       class counts:
                        34
                             59
##
     probabilities: 0.596 0.404
##
     left son=340 (35 obs) right son=341 (58 obs)
##
     Primary splits:
##
        Home
                  splits as -LRRRL, improve=5.301208, (0 missing)
         Assets
##
                  < 1650
                              to the left, improve=4.889697, (0 missing)
##
                  < 55.36398 to the right, improve=4.817600, (0 missing)
        Finrat
##
                  < 1.155
                              to the left, improve=4.476099, (0 missing)
         Savings
##
         expensesR splits as RLRRL, improve=3.638053, (0 missing)
##
     Surrogate splits:
##
                              to the left, agree=0.796, adj=0.457, (0 split)
        Assets
                   < 750
##
         assetsR
                  splits as LRRRR, agree=0.796, adj=0.457, (0 split)
##
         expensesR splits as RLRLL, agree=0.677, adj=0.143, (0 split)
##
                 splits as RRRLR, agree=0.667, adj=0.114, (0 split)
                              to the left, agree=0.656, adj=0.086, (0 split)
##
        Seniority < 0.5
##
## Node number 171: 20 observations
##
     predicted class=good expected loss=0 P(node) =0.004670715
##
       class counts: 0
                             20
      probabilities: 0.000 1.000
##
##
## Node number 248: 65 observations
##
     predicted class=bad
                          expected loss=0.4007138 P(node) =0.02389477
##
       class counts:
                        24
                              41
##
     probabilities: 0.599 0.401
##
## Node number 249: 17 observations
    predicted class=good expected loss=0 P(node) =0.003970107
##
##
      class counts:
                        0
                             17
##
     probabilities: 0.000 1.000
##
## Node number 250: 8 observations
    predicted class=bad expected loss=0.1901808 P(node) =0.003683901
##
       class counts:
                        5
     probabilities: 0.810 0.190
##
##
## Node number 251: 310 observations
     predicted class=good expected loss=0.2149095 P(node) =0.08328977
##
##
       class counts:
                       30
                            280
##
      probabilities: 0.215 0.785
##
## Node number 340: 35 observations
    predicted class=bad expected loss=0.2269363 P(node) =0.01543621
##
##
      class counts:
                      20
##
     probabilities: 0.773 0.227
##
```

```
## Node number 341: 58 observations,
                                        complexity param=0.004670715
     predicted class=good expected loss=0.4484038 P(node) =0.01862879
##
##
       class counts:
                       14
                              44
##
      probabilities: 0.448 0.552
##
     left son=682 (18 obs) right son=683 (40 obs)
##
     Primary splits:
                  splits as LLRRR, improve=5.430383, (0 missing)
##
         priceR
                               to the left, improve=4.280187, (0 missing)
##
        Savings
                   < 1.125
##
         Income
                   < 63.5
                               to the left, improve=3.676496, (0 missing)
##
         timeR
                   splits as RLLRL, improve=3.569661, (0 missing)
##
         Seniority < 1.5
                              to the right, improve=2.937761, (0 missing)
##
     Surrogate splits:
##
        Price
                < 982
                             to the left, agree=0.793, adj=0.333, (0 split)
##
         Income < 67.5
                            to the left, agree=0.776, adj=0.278, (0 split)
##
         incomeR splits as LRR-R, agree=0.741, adj=0.167, (0 split)
##
         Finrat < 80.08016 to the right, agree=0.724, adj=0.111, (0 split)
##
         Savings < 3.210801 to the right, agree=0.724, adj=0.111, (0 split)
##
## Node number 682: 18 observations
    predicted class=bad expected loss=0.2813025 P(node) =0.00747175
##
       class counts:
                         9
##
     probabilities: 0.719 0.281
##
## Node number 683: 40 observations
    predicted class=good expected loss=0.267391 P(node) =0.01115704
       class counts:
                        5
##
      probabilities: 0.267 0.733
# calculate error rate in the learning sample
# (this will give a matrix)
ct2.learn = predict(ct2, data=data[learn,])
# create a vector with predicted status
ct2.learnp = rep("", nlearn)
ct2.learnp[ct2.learn[,1] < 0.5] = "pred_neg"
ct2.learnp[ct2.learn[,1] >= 0.5] = "pred_pos"
# let's make a table
status_learn = table(data$Status[learn], ct2.learnp)
# classification error
100 * sum(diag(status_learn)) / nlearn
## [1] 21.04733
# calculate error rate in the testing sample
# (this will give a matrix)
ct2.test = predict(ct2, newdata=data[-learn,])
# create a vector with predicted status
ct2.testp = rep("", ntest)
ct2.testp[ct2.test[,1] < 0.5] = "pred_neg"
ct2.testp[ct2.test[,1] >= 0.5] = "pred_pos"
# let's make a table
status_test = table(data$Status[-learn], ct2.testp)
# classification error
100 * sum(diag(status_test)) / ntest
```

## [1] 27.47103

## **Decision Tree**



```
# calculate error rate in the learning sample
# (this will give a matrix)
ct3.learn = predict(ct3, data=data[learn,])
# create a vector with predicted status
ct3.learnp = rep("", nlearn)
ct3.learnp[ct3.learn[,1] < 0.5] = "pred_neg"
ct3.learnp[ct3.learn[,1] >= 0.5] = "pred_pos"
# let's make a table
table(data$Status[learn], ct3.learnp)
##
         ct3.learnp
##
          pred_neg pred_pos
##
     bad
               125
                        713
              1687
                        454
##
     good
# classification error
100 * sum(diag(table(data$Status[learn], ct3.learnp))) / nlearn
```

```
## [1] 19.43605
# calculate error rate in the testing sample
# (this will give a matrix)
ct3.test = predict(ct3, newdata=data[-learn,])
# create a vector with predicted status
ct3.testp = rep("", ntest)
ct3.testp[ct3.test[,1] < 0.5] = "pred_neg"
ct3.testp[ct3.test[,1] \geq= 0.5] = "pred_pos"
# let's make a table
table(data$Status[-learn], ct3.testp)
##
         ct3.testp
##
          pred_neg pred_pos
##
               110
                        301
     bad
               760
                        296
##
     good
# classification error
100 * sum(diag(table(data$Status[-learn], ct3.testp))) / ntest
## [1] 27.67553
# concentration curve
# the positive predictions on the test sample
pred.test = ct2.test[,1]
# the number of individuals in each value
totn = table(-pred.test) / ntest
ac_totn = 100 * cumsum(as.numeric(totn))
# ranking the predictions
rank_pred.test = rank(pred.test)
# how many positive are in each leave?
Status.test = data$Status[-learn]
table(Status.test)
## Status.test
## bad good
## 411 1056
npos = table(Status.test)[1]
tapply(Status.test == "good", rank_pred.test, sum)
            45.5
                     80 253.5
                                   444 548.5 642.5
                                                      666.5
                                                                688
                                                                       720
                           316
##
       15
             54
                     12
                                    38
                                          144
                                                  21
                                                         17
                                                                12
                                                                        32
                                   952 992.5 1030.5
##
    760.5
             820
                    879
                           913
                                                       1099
                                                               1151 1160.5
                     23
                            23
##
       22
             69
                                    31
                                           18
                                                  27
                                                         45
                                                                  6
## 1170.5
            1189
                   1263
                          1325
                                  1345 1365.5
                                                1416
                                                       1466
##
              14
                     47
                             2
                                    24
ac true.pos = 100 * cumsum(rev(as.numeric(totn))) / npos
Description: Logistic Regression
# load package FactoMineR and ggplot2
require(FactoMineR)
require(ggplot2)
```

Apply logistic regression using all the variables

```
# let's keep 2/3 of the data for learning, and 1/3 for testing
n = nrow(data)
learn = sample(1:n, size=round(0.67 * n))
nlearn = length(learn)
ntest = n - nlearn
# "whole enchilada" logistic regression model
gl1 = glm(Status ~ ., data=data[learn,], family=binomial)
# use the 'summary' function to obtain more details on the logistic model
# (pay attention to the signicance of the coefficients)
summary(gl1)
##
## Call:
  glm(formula = Status ~ ., family = binomial, data = data[learn,
##
      ])
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -2.8385 -0.5349
                     0.3528
                              0.6427
                                       2.5235
## Coefficients:
                                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                1.223e+00 1.340e+00 0.913 0.361463
## Seniority
                                5.019e-02 2.614e-02 1.920 0.054905 .
## Homeother
                                6.303e-01 6.367e-01 0.990 0.322230
## Homeowner
                               1.083e+00 6.054e-01 1.789 0.073684 .
## Homeparents
                                1.400e+00 6.284e-01
                                                     2.228 0.025858 *
## Homepriv
                               5.232e-01 6.310e-01
                                                     0.829 0.406984
## Homerent
                               9.664e-01 6.240e-01
                                                     1.549 0.121424
## Time
                               -9.522e-02 4.925e-02 -1.933 0.053181
                               -1.302e-02 1.964e-02 -0.663 0.507316
## Age
## Maritalmarried
                               8.007e-01 5.182e-01
                                                      1.545 0.122303
                               -2.488e-01 5.787e-01 -0.430 0.667222
## Maritalseparated
                               5.318e-01 5.283e-01
                                                      1.007 0.314078
## Maritalsingle
## Maritalwidow
                               8.052e-02 6.536e-01
                                                       0.123 0.901959
## Recordsyes_rec
                               -1.644e+00 1.291e-01 -12.739 < 2e-16 ***
## Jobfreelance
                               -7.790e-01 1.325e-01 -5.880 4.10e-09 ***
## Jobothers
                               -4.124e-01 2.736e-01
                                                     -1.507 0.131715
## Jobpartime
                               -1.244e+00 1.637e-01 -7.601 2.93e-14 ***
## Expenses
                               -1.255e-02 1.060e-02 -1.183 0.236616
## Income
                               2.432e-03 1.730e-03
                                                     1.406 0.159801
                                7.172e-06 8.514e-06
## Assets
                                                     0.842 0.399599
                                3.094e-05 8.019e-05
## Debt.
                                                     0.386 0.699624
## Amount
                               -1.132e-03 5.521e-04 -2.051 0.040284 *
                                3.228e-04 3.498e-04
## Price
                                                      0.923 0.356043
## Finrat
                               -9.197e-03 1.354e-02 -0.680 0.496813
## Savings
                               -5.636e-02 3.871e-02 -1.456 0.145441
## seniorityRsen (1,3]
                                3.180e-01 1.540e-01
                                                     2.065 0.038877 *
## seniorityRsen (14,99]
                                7.157e-01 5.432e-01
                                                      1.318 0.187657
## seniorityRsen (3,8]
                                5.289e-01 2.014e-01
                                                       2.626 0.008629 **
## seniorityRsen (8,14]
                                6.737e-01 3.308e-01
                                                       2.036 0.041713 *
## timeRtime (12,24]
                                6.124e-01 7.061e-01 0.867 0.385768
```

```
## timeRtime (24,36]
                                 1.519e+00
                                           1.272e+00
                                                        1.195 0.232185
## timeRtime (36,48]
                                 2.625e+00 1.840e+00
                                                        1.426 0.153763
## timeRtime (48,99]
                                 3.990e+00 2.423e+00
                                                        1.647 0.099641
## ageRage (25,30]
                                 1.771e-01 2.003e-01
                                                        0.884 0.376669
## ageRage (30,40]
                                 2.093e-01
                                           2.901e-01
                                                        0.721 0.470690
## ageRage (40,50]
                                 4.261e-01 4.644e-01
                                                        0.918 0.358863
## ageRage (50,99]
                                 1.403e-01 6.659e-01
                                                        0.211 0.833075
## expensesRexp (40,50]
                                 5.272e-02
                                           2.086e-01
                                                        0.253 0.800455
## expensesRexp (50,60]
                                 2.245e-02 3.205e-01
                                                        0.070 0.944153
## expensesRexp (60,80]
                                 1.650e-01
                                           4.647e-01
                                                        0.355 0.722462
## expensesRexp (80,1e+04]
                                -1.453e-01 6.795e-01
                                                       -0.214 0.830644
## incomeRinc (110,140]
                                 6.594e-01 2.293e-01
                                                        2.876 0.004028 **
## incomeRinc (140,190]
                                 6.550e-01 2.860e-01
                                                        2.290 0.022019 *
## incomeRinc (190,1e+04]
                                 7.488e-01 3.913e-01
                                                       1.913 0.055686 .
## incomeRinc (80,110]
                                 1.546e-01 1.785e-01
                                                        0.866 0.386403
## assetsRasset (0,3e+03]
                                 3.495e-01
                                           2.043e-01
                                                        1.710 0.087184 .
## assetsRasset (3e+03,5e+03]
                                 7.916e-01 2.098e-01
                                                        3.773 0.000162 ***
## assetsRasset (5e+03,8e+03]
                                 1.033e+00 2.418e-01
                                                        4.273 1.93e-05 ***
## assetsRasset (8e+03,1e+06]
                                 1.144e+00 2.816e-01
                                                        4.063 4.85e-05 ***
## debtRdebt (0,500]
                                -3.119e-01 2.653e-01
                                                       -1.176 0.239723
## debtRdebt (1.5e+03,2.5e+03]
                                -8.940e-01 3.176e-01
                                                      -2.815 0.004877 **
## debtRdebt (2.5e+03,1e+06]
                                -1.071e+00 4.198e-01
                                                       -2.551 0.010733 *
## debtRdebt (500,1.5e+03]
                                -3.431e-01 2.601e-01
                                                       -1.319 0.187131
## amountRam (1.1e+03,1.4e+03]
                                 6.555e-02 3.771e-01
                                                        0.174 0.862012
## amountRam (1.4e+03,1e+05]
                                 3.245e-02 4.906e-01
                                                        0.066 0.947260
## amountRam (600,900]
                                 2.647e-01 2.298e-01
                                                        1.152 0.249416
## amountRam (900,1.1e+03]
                                 2.128e-01 3.054e-01
                                                        0.697 0.485975
## priceRpriz (1.3e+03,1.5e+03]
                                 5.617e-01 2.668e-01
                                                        2.105 0.035259 *
## priceRpriz (1.5e+03,1.8e+03]
                                 5.331e-01 2.984e-01
                                                       1.786 0.074043
## priceRpriz (1.8e+03,1e+05]
                                 1.726e-01 3.954e-01
                                                        0.437 0.662430
## priceRpriz (1e+03,1.3e+03]
                                 6.679e-01
                                           2.151e-01
                                                        3.105 0.001903 **
## finratRfinr (50,70]
                                 2.678e-01 3.384e-01
                                                        0.791 0.428741
## finratRfinr (70,80]
                                 5.593e-02 4.665e-01
                                                        0.120 0.904569
                                 2.482e-02 5.626e-01
## finratRfinr (80,90]
                                                        0.044 0.964805
## finratRfinr (90,100]
                                -1.792e-01
                                           6.785e-01
                                                       -0.264 0.791739
## savingsRsav (0,2]
                                 4.538e-01 2.345e-01
                                                        1.935 0.053003 .
## savingsRsav (2,4]
                                 7.983e-01 2.984e-01
                                                        2.675 0.007476 **
## savingsRsav (4,6]
                                 6.888e-01 3.666e-01
                                                        1.879 0.060223 .
## savingsRsav (6,99]
                                 1.115e+00 4.757e-01
                                                        2.344 0.019056 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 3528.8 on 2978 degrees of freedom
## Residual deviance: 2481.1 on 2910 degrees of freedom
## AIC: 2619.1
##
## Number of Fisher Scoring iterations: 5
# let's use the 'anova' function to get a sequential analysis of
# variance of the model fit (ie importance of variables in the model)
anova(gl1)
```

## Analysis of Deviance Table

```
##
## Model: binomial, link: logit
## Response: Status
## Terms added sequentially (first to last)
##
##
##
             Df Deviance Resid. Df Resid. Dev
## NULL
                               2978
                                        3528.8
## Seniority
              1 270.943
                               2977
                                        3257.9
                               2972
## Home
                 89.105
                                       3168.8
              5
                 21.795
## Time
              1
                               2971
                                        3147.0
## Age
              1 5.094
                               2970
                                       3141.9
## Marital
               4 11.576
                               2966
                                       3130.3
               1 185.783
## Records
                               2965
                                       2944.5
## Job
               3 138.118
                               2962
                                       2806.4
## Expenses
              1 10.920
                               2961
                                       2795.5
## Income
                 55.361
                               2960
                                       2740.1
              1
## Assets
                  6.971
                               2959
                                       2733.1
## Debt
              1
                  8.643
                               2958
                                       2724.5
## Amount
              1 56.274
                               2957
                                       2668.2
## Price
              1 45.543
                                       2622.7
                               2956
              1 10.241
## Finrat
                               2955
                                       2612.4
## Savings
                 0.497
                                       2611.9
               1
                               2954
## seniorityR 4
                 9.179
                               2950
                                       2602.8
## timeR
                   9.418
                               2946
                                       2593.3
## ageR
                   3.507
                               2942
                                        2589.8
## expensesR
                   3.140
                               2938
                                       2586.7
                 30.258
## incomeR
                                       2556.4
                               2934
                 20.713
## assetsR
               4
                               2930
                                       2535.7
## debtR
               4 12.499
                               2926
                                       2523.2
## amountR
               4 15.003
                               2922
                                       2508.2
                               2918
## priceR
               4 13.724
                                       2494.5
## finratR
               4
                   4.281
                               2914
                                        2490.2
## savingsR
              4
                   9.136
                               2910
                                        2481.1
# we can also use the 'step' function to perform model selection by
# applying a backward elimination method based on AIC (Akaike Info. Criterion)
step(gl1)
## Start: AIC=2619.08
## Status ~ Seniority + Home + Time + Age + Marital + Records +
       Job + Expenses + Income + Assets + Debt + Amount + Price +
      Finrat + Savings + seniorityR + timeR + ageR + expensesR +
##
##
       incomeR + assetsR + debtR + amountR + priceR + finratR +
##
       savingsR
##
##
                Df Deviance
                               AIC
## - expensesR
                     2483.6 2613.6
## - amountR
                     2483.9 2613.9
## - ageR
                     2485.1 2615.1
## - finratR
                 4
                     2485.8 2615.8
## - Debt
                 1
                     2481.2 2617.2
## - Age
                    2481.5 2617.5
```

```
2481.5 2617.5
## - Finrat
## - Assets
                     2481.9 2617.9
                 1
                     2482.1 2618.1
## - Price
## - Expenses
                     2482.4 2618.4
                 1
## - Income
                     2483.1 2619.1
## - Savings
                     2483.1 2619.1
## <none>
                     2481.1 2619.1
## - seniorityR 4
                     2490.2 2620.2
## - savingsR
                 4
                     2490.2 2620.2
## - Seniority
                 1
                     2485.1 2621.1
## - Time
                 1
                     2485.1 2621.1
                     2491.6 2621.6
## - debtR
                 4
                     2491.8 2621.8
## - incomeR
                 4
## - Amount
                     2486.2 2622.2
## - timeR
                 4
                     2493.8 2623.8
## - Marital
                 4
                     2496.9 2626.9
## - priceR
                 4
                     2497.2 2627.2
## - Home
                     2504.0 2632.0
## - assetsR
                     2506.9 2636.9
                 4
## - Job
                 3
                     2559.0 2691.0
## - Records
                 1
                     2650.0 2786.0
##
## Step: AIC=2613.6
## Status ~ Seniority + Home + Time + Age + Marital + Records +
##
       Job + Expenses + Income + Assets + Debt + Amount + Price +
       Finrat + Savings + seniorityR + timeR + ageR + incomeR +
##
       assetsR + debtR + amountR + priceR + finratR + savingsR
##
                Df Deviance
##
                               AIC
                     2486.4 2608.4
## - amountR
## - ageR
                 4
                     2487.9 2609.9
## - finratR
                 4
                     2488.4 2610.4
## - Debt
                     2483.7 2611.7
## - Finrat
                     2484.1 2612.1
                 1
## - Age
                 1
                     2484.2 2612.2
## - Assets
                     2484.5 2612.5
                 1
## - Price
                     2484.5 2612.5
## - Savings
                     2485.6 2613.6
                 1
## <none>
                     2483.6 2613.6
## - Income
                     2485.6 2613.6
                 1
## - savingsR
                     2492.6 2614.6
## - seniorityR 4
                     2492.7 2614.7
## - Time
                     2487.5 2615.5
                 1
## - Seniority
                     2487.7 2615.7
                 1
## - debtR
                     2493.8 2615.8
## - Amount
                     2488.4 2616.4
                 1
                     2494.6 2616.6
## - incomeR
## - timeR
                     2496.2 2618.2
## - priceR
                     2499.9 2621.9
                     2494.8 2622.8
## - Expenses
## - Marital
                     2502.0 2624.0
                 4
                     2506.0 2626.0
## - Home
                 5
## - assetsR
                 4
                     2509.4 2631.4
## - Job
                     2562.1 2686.1
```

```
2653.8 2781.8
## - Records
##
## Step: AIC=2608.45
## Status ~ Seniority + Home + Time + Age + Marital + Records +
       Job + Expenses + Income + Assets + Debt + Amount + Price +
##
       Finrat + Savings + seniorityR + timeR + ageR + incomeR +
##
       assetsR + debtR + priceR + finratR + savingsR
##
##
                Df Deviance
                               AIC
## - ageR
                     2490.7 2604.7
## - Debt
                 1
                     2486.5 2606.5
                     2486.6 2606.6
## - Finrat
                 1
                     2486.9 2606.9
## - Age
                 1
## - Assets
                     2487.3 2607.3
                 1
## - finratR
                    2493.4 2607.4
## <none>
                     2486.4 2608.4
## - Price
                     2488.6 2608.6
                 1
## - Savings
                 1
                     2488.9 2608.9
## - savingsR
                     2495.0 2609.0
                 4
## - Income
                     2489.0 2609.0
## - seniorityR 4
                     2495.3 2609.3
## - Time
                     2490.0 2610.0
## - Seniority
                     2490.5 2610.5
                 1
## - debtR
                 4
                     2497.0 2611.0
## - timeR
                 4
                     2498.2 2612.2
## - incomeR
                     2498.2 2612.2
## - Amount
                     2496.1 2616.1
                 1
## - Marital
                     2504.5 2618.5
                 4
                     2498.7 2618.7
## - Expenses
                 1
                     2509.2 2621.2
## - Home
                 5
                     2511.8 2625.8
## - assetsR
                 4
## - priceR
                 4
                     2512.6 2626.6
## - Job
                 3
                     2565.4 2681.4
## - Records
                     2657.7 2777.7
                 1
##
## Step: AIC=2604.7
## Status ~ Seniority + Home + Time + Age + Marital + Records +
##
       Job + Expenses + Income + Assets + Debt + Amount + Price +
##
       Finrat + Savings + seniorityR + timeR + incomeR + assetsR +
##
       debtR + priceR + finratR + savingsR
##
##
                Df Deviance
                               ATC
                     2490.8 2602.8
## - Debt
                 1
## - Finrat
                     2491.0 2603.0
                 1
## - finratR
                     2497.5 2603.5
## - Assets
                     2491.6 2603.6
                 1
                     2492.0 2604.0
## - Age
                 1
## - Price
                     2492.6 2604.6
## <none>
                     2490.7 2604.7
                     2499.0 2605.0
## - savingsR
                 4
## - Savings
                     2493.2 2605.2
                 1
## - Income
                 1
                     2493.4 2605.4
## - Seniority
                 1
                     2493.8 2605.8
## - Time
                    2494.0 2606.0
                 1
```

```
## - seniorityR 4
                     2501.1 2607.1
## - debtR
                 4
                     2501.5 2607.5
## - timeR
                    2502.1 2608.1
## - incomeR
                 4
                    2502.3 2608.3
## - Amount
                 1
                     2499.8 2611.8
## - Expenses
                    2501.2 2613.2
                1
## - Marital
                    2507.8 2613.8
## - Home
                     2512.9 2616.9
                 5
## - priceR
                 4
                     2516.0 2622.0
                 4
## - assetsR
                     2516.1 2622.1
## - Job
                 3
                     2569.2 2677.2
                     2660.1 2772.1
## - Records
                 1
##
## Step: AIC=2602.84
## Status ~ Seniority + Home + Time + Age + Marital + Records +
##
       Job + Expenses + Income + Assets + Amount + Price + Finrat +
##
       Savings + seniorityR + timeR + incomeR + assetsR + debtR +
##
      priceR + finratR + savingsR
##
##
                Df Deviance
## - Finrat
                1
                    2491.1 2601.1
## - finratR
                 4
                     2497.6 2601.6
## - Assets
                    2491.7 2601.7
                1
## - Age
                    2492.2 2602.2
                1
## - Price
                    2492.7 2602.7
                1
## <none>
                     2490.8 2602.8
## - savingsR
                 4
                     2499.0 2603.0
## - Savings
                 1
                     2493.4 2603.4
## - Income
                     2493.9 2603.9
                 1
## - Seniority
                     2493.9 2603.9
                 1
## - Time
                 1
                     2494.2 2604.2
## - seniorityR 4
                     2501.2 2605.2
                    2502.2 2606.2
## - timeR
## - incomeR
                    2502.6 2606.6
                 4
## - Amount
                 1
                     2500.0 2610.0
## - Expenses
                    2501.6 2611.6
                 1
## - Marital
                 4
                    2507.9 2611.9
## - debtR
                 4
                    2510.3 2614.3
## - Home
                 5
                     2513.0 2615.0
## - priceR
                 4
                     2516.1 2620.1
## - assetsR
                     2516.2 2620.2
## - Job
                 3
                     2569.6 2675.6
                     2660.8 2770.8
## - Records
##
## Step: AIC=2601.11
## Status ~ Seniority + Home + Time + Age + Marital + Records +
##
       Job + Expenses + Income + Assets + Amount + Price + Savings +
##
       seniorityR + timeR + incomeR + assetsR + debtR + priceR +
##
      finratR + savingsR
##
##
                Df Deviance
                               AIC
                    2492.0 2600.0
## - Assets
                1
## - Age
                 1
                     2492.5 2600.5
## <none>
                     2491.1 2601.1
```

```
## - savingsR
                     2499.4 2601.4
                     2493.5 2601.5
## - Savings
                 1
## - Income
                     2494.0 2602.0
                     2494.2 2602.2
## - Seniority
                 1
## - Price
                     2494.3 2602.3
## - Time
                     2494.6 2602.6
                 1
## - seniorityR 4
                     2501.5 2603.5
## - finratR
                     2501.7 2603.7
                 4
## - incomeR
                 4
                     2502.6 2604.6
## - timeR
                    2503.4 2605.4
## - Expenses
                 1
                     2501.7 2609.7
                     2508.2 2610.2
## - Marital
                 4
## - Amount
                 1
                     2504.4 2612.4
## - debtR
                    2510.5 2612.5
## - Home
                 5
                    2513.4 2613.4
## - assetsR
                 4
                     2516.4 2618.4
                 4
                    2516.8 2618.8
## - priceR
## - Job
                     2569.7 2673.7
## - Records
                     2660.8 2768.8
                 1
##
## Step: AIC=2599.98
## Status ~ Seniority + Home + Time + Age + Marital + Records +
##
       Job + Expenses + Income + Amount + Price + Savings + seniorityR +
##
       timeR + incomeR + assetsR + debtR + priceR + finratR + savingsR
##
                Df Deviance
                               AIC
## - Age
                    2493.4 2599.4
                1
                     2492.0 2600.0
## <none>
                     2500.3 2600.3
## - savingsR
## - Savings
                     2494.5 2600.5
                 1
## - Income
                 1
                     2495.1 2601.1
## - Seniority
                 1
                     2495.1 2601.1
## - Price
                     2495.4 2601.4
## - Time
                     2495.5 2601.5
                 1
## - seniorityR 4
                     2502.4 2602.4
## - finratR
                 4
                     2502.5 2602.5
## - incomeR
                    2503.6 2603.6
## - timeR
                 4
                     2504.6 2604.6
## - Expenses
                 1
                     2502.7 2608.7
## - Marital
                 4
                    2508.9 2608.9
## - debtR
                    2511.4 2611.4
## - Amount
                     2505.4 2611.4
                 1
## - Home
                     2514.3 2612.3
                 5
## - priceR
                 4
                     2517.6 2617.6
## - assetsR
                     2531.9 2631.9
## - Job
                     2570.1 2672.1
                 3
                     2661.8 2767.8
## - Records
##
## Step: AIC=2599.38
## Status ~ Seniority + Home + Time + Marital + Records + Job +
##
       Expenses + Income + Amount + Price + Savings + seniorityR +
##
       timeR + incomeR + assetsR + debtR + priceR + finratR + savingsR
##
##
                Df Deviance
                               AIC
```

```
2493.4 2599.4
## <none>
## - savingsR
                      2501.6 2599.6
## - Savings
                      2495.9 2599.9
## - Seniority
                      2496.0 2600.0
                  1
## - Income
                      2496.4 2600.4
## - Price
                  1
                      2496.8 2600.8
## - Time
                      2497.0 2601.0
## - finratR
                      2503.7 2601.7
## - seniorityR
                  4
                      2504.5 2602.5
## - incomeR
                      2504.9 2602.9
## - timeR
                      2506.4 2604.4
## - Marital
                      2510.4 2608.4
                  4
                      2504.6 2608.6
## - Expenses
                  1
## - debtR
                  4
                      2511.6 2609.6
## - Amount
                      2507.1 2611.1
                  1
                      2516.7 2612.7
## - Home
                  5
## - priceR
                  4
                      2519.0 2617.0
## - assetsR
                      2532.1 2630.1
## - Job
                  3
                      2571.9 2671.9
## - Records
                      2665.3 2769.3
                  1
##
   Call: glm(formula = Status ~ Seniority + Home + Time + Marital + Records +
##
       Job + Expenses + Income + Amount + Price + Savings + seniorityR +
##
       timeR + incomeR + assetsR + debtR + priceR + finratR + savingsR,
       family = binomial, data = data[learn, ])
##
##
   Coefficients:
##
##
                     (Intercept)
                                                       Seniority
##
                       0.5462050
                                                       0.0405282
##
                       Homeother
                                                       Homeowner
##
                       0.6098392
                                                       1.0768895
##
                     Homeparents
                                                       Homepriv
##
                       1.3718592
                                                       0.5160695
##
                        Homerent
                                                            Time
##
                       0.9292852
                                                      -0.0892810
##
                  Maritalmarried
                                               Maritalseparated
                       0.8337042
                                                      -0.1738908
##
                  Maritalsingle
                                                   Maritalwidow
                       0.5579600
                                                       0.0614361
##
##
                  Recordsyes rec
                                                   Jobfreelance
##
                      -1.6368653
                                                      -0.7776485
##
                       Jobothers
                                                      Jobpartime
##
                      -0.5630251
                                                      -1.2354969
##
                        Expenses
                                                          Income
##
                      -0.0134819
                                                       0.0029197
##
                          Amount
                                                           Price
##
                                                       0.0005319
                      -0.0014604
##
                                            seniorityRsen (1,3]
                         Savings
##
                      -0.0613866
                                                       0.3413326
##
          seniorityRsen (14,99]
                                            seniorityRsen (3,8]
##
                                                       0.5915305
                       0.8457011
##
           seniorityRsen (8,14]
                                              timeRtime (12,24]
                                                       0.5383464
##
                       0.7639826
```

```
##
              timeRtime (24,36]
                                              timeRtime (36,48]
                       1.3873974
                                                      2.4629163
##
##
              timeRtime (48,99]
                                           incomeRinc (110,140]
##
                       3.7601028
                                                      0.6805777
##
           incomeRinc (140,190]
                                         incomeRinc (190,1e+04]
                       0.7017612
##
                                                      0.7699443
            incomeRinc (80.110]
                                         assetsRasset (0.3e+03]
##
##
                       0.1767094
                                                      0.3531707
##
     assetsRasset (3e+03,5e+03]
                                    assetsRasset (5e+03,8e+03]
##
                       0.8108260
                                                       1.0407828
##
     assetsRasset (8e+03,1e+06]
                                              debtRdebt (0,500]
                                                     -0.2916967
##
                       1.2305642
##
    debtRdebt (1.5e+03,2.5e+03]
                                     debtRdebt (2.5e+03,1e+06]
                                                     -0.9177960
##
                      -0.8142196
##
        debtRdebt (500,1.5e+03]
                                  priceRpriz (1.3e+03,1.5e+03]
##
                      -0.2898358
                                                      0.5669796
##
   priceRpriz (1.5e+03,1.8e+03]
                                    priceRpriz (1.8e+03,1e+05]
##
                       0.5198064
                                                      0.1412146
##
     priceRpriz (1e+03,1.3e+03]
                                            finratRfinr (50,70]
##
                       0.7176613
                                                      0.2159518
##
            finratRfinr (70,80]
                                            finratRfinr (80,90]
##
                      -0.0828739
                                                     -0.1885193
           finratRfinr (90,100]
##
                                              savingsRsav (0,2]
                      -0.4588176
##
                                                      0.4392379
##
              savingsRsav (2,4]
                                              savingsRsav (4,6]
##
                       0.7427290
                                                      0.6278230
##
             savingsRsav (6,99]
                       1.0060084
##
## Degrees of Freedom: 2978 Total (i.e. Null); 2926 Residual
## Null Deviance:
                         3529
## Residual Deviance: 2493 AIC: 2599
Apply logistic regression after removing some variables
# new model
glf <- glm(formula = Status ~ Seniority + Age + Income + Debt + Amount + Finrat +</pre>
             seniorityR + expensesR + assetsR + priceR + savingsR + Home + Marital + Records +
             Job, family = binomial, data = data[learn, ])
# check summary
summary(glf)
## Call:
   glm(formula = Status ~ Seniority + Age + Income + Debt + Amount +
       Finrat + seniorityR + expensesR + assetsR + priceR + savingsR +
       Home + Marital + Records + Job, family = binomial, data = data[learn,
##
##
       ])
##
##
  Deviance Residuals:
       Min
                  10
                       Median
                                     3Q
                                             Max
   -3.0934 -0.5440
                       0.3667
                                0.6636
                                          2.6426
## Coefficients:
##
                                   Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept)
                                -1.420e-01 8.817e-01
                                                      -0.161 0.872022
## Seniority
                                 4.802e-02 2.603e-02
                                                        1.845 0.065096 .
## Age
                                -5.793e-03 6.294e-03
                                                       -0.920 0.357342
## Income
                                 3.129e-03 1.241e-03
                                                        2.521 0.011717 *
## Debt
                                -1.245e-04
                                           4.647e-05
                                                       -2.680 0.007361 **
## Amount
                                -6.345e-04 2.448e-04
                                                       -2.592 0.009534 **
## Finrat
                                -2.168e-02 4.346e-03
                                                       -4.989 6.07e-07 ***
## seniorityRsen (1,3]
                                 3.338e-01 1.517e-01
                                                        2.201 0.027755 *
## seniorityRsen (14,99]
                                 7.839e-01 5.400e-01
                                                        1.452 0.146566
## seniorityRsen (3,8]
                                 5.488e-01
                                           1.976e-01
                                                        2.777 0.005482 **
## seniorityRsen (8,14]
                                 6.692e-01 3.256e-01
                                                        2.055 0.039851 *
## expensesRexp (40,50]
                                -2.188e-02 1.727e-01
                                                       -0.127 0.899200
## expensesRexp (50,60]
                                -1.206e-01
                                           1.914e-01
                                                       -0.630 0.528531
                                                       -0.380 0.703729
## expensesRexp (60,80]
                                -8.100e-02 2.130e-01
## expensesRexp (80,1e+04]
                                -5.493e-01
                                            2.487e-01
                                                       -2.209 0.027202 *
## assetsRasset (0,3e+03]
                                 3.309e-01
                                            1.972e-01
                                                        1.678 0.093399
## assetsRasset (3e+03,5e+03]
                                 7.344e-01
                                            2.004e-01
                                                        3.664 0.000248 ***
## assetsRasset (5e+03,8e+03]
                                 1.004e+00 2.291e-01
                                                        4.383 1.17e-05 ***
## assetsRasset (8e+03,1e+06]
                                                        5.294 1.20e-07 ***
                                 1.217e+00 2.299e-01
## priceRpriz (1.3e+03,1.5e+03]
                                 5.625e-01
                                            2.027e-01
                                                        2.775 0.005521 **
## priceRpriz (1.5e+03,1.8e+03]
                                 5.244e-01
                                           2.235e-01
                                                        2.346 0.018966 *
## priceRpriz (1.8e+03,1e+05]
                                 2.189e-01
                                           3.185e-01
                                                        0.687 0.491873
## priceRpriz (1e+03,1.3e+03]
                                                        4.111 3.94e-05 ***
                                 7.179e-01
                                           1.746e-01
## savingsRsav (0,2]
                                 5.427e-01
                                           2.130e-01
                                                        2.548 0.010832 *
## savingsRsav (2,4]
                                 9.849e-01 2.339e-01
                                                        4.211 2.55e-05 ***
## savingsRsav (4,6]
                                 8.902e-01 2.709e-01
                                                        3.287 0.001014 **
## savingsRsav (6,99]
                                 1.041e+00 3.338e-01
                                                        3.118 0.001824 **
## Homeother
                                 7.020e-01
                                           6.440e-01
                                                        1.090 0.275674
## Homeowner
                                 1.100e+00 6.129e-01
                                                        1.795 0.072659
## Homeparents
                                 1.374e+00 6.358e-01
                                                        2.160 0.030741 *
## Homepriv
                                 5.455e-01
                                           6.372e-01
                                                        0.856 0.391944
## Homerent
                                 9.665e-01
                                           6.318e-01
                                                        1.530 0.126075
## Maritalmarried
                                 7.138e-01
                                           5.020e-01
                                                        1.422 0.155046
## Maritalseparated
                                -2.594e-01 5.610e-01
                                                       -0.462 0.643762
## Maritalsingle
                                 4.881e-01
                                            5.098e-01
                                                        0.957 0.338401
## Maritalwidow
                                 9.029e-02 6.351e-01
                                                        0.142 0.886957
## Recordsyes rec
                                -1.616e+00 1.262e-01 -12.808 < 2e-16 ***
## Jobfreelance
                                -7.512e-01
                                           1.284e-01
                                                       -5.849 4.94e-09 ***
                                            2.646e-01
                                                       -1.585 0.113034
## Jobothers
                                -4.194e-01
## Jobpartime
                                -1.254e+00 1.605e-01 -7.814 5.56e-15 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3528.8
                              on 2978
                                       degrees of freedom
## Residual deviance: 2534.5 on 2939
                                       degrees of freedom
## AIC: 2614.5
## Number of Fisher Scoring iterations: 5
# check coefficients
exp(glf$coefficients)
```

Seniority

(Intercept)

##

```
0.8675886
##
                                                      1.0491900
##
                                                          Income
                              Age
##
                       0.9942236
                                                      1.0031339
##
                                                          Amount
                            Debt.
##
                       0.9998755
                                                      0.9993657
                                            seniorityRsen (1,3]
##
                          Finrat
                       0.9785512
                                                      1.3962026
##
          seniorityRsen (14,99]
##
                                            seniorityRsen (3,8]
##
                       2.1900178
                                                      1.7312302
##
           seniorityRsen (8,14]
                                           expensesRexp (40,50]
##
                       1.9525967
                                                      0.9783588
##
           expensesRexp (50,60]
                                           expensesRexp (60,80]
##
                       0.8863639
                                                      0.9221950
##
        expensesRexp (80,1e+04]
                                        assetsRasset (0,3e+03]
##
                       0.5773446
                                                      1.3922042
##
     assetsRasset (3e+03,5e+03]
                                    assetsRasset (5e+03,8e+03]
##
                       2.0842009
                                                      2.7290361
##
     assetsRasset (8e+03,1e+06] priceRpriz (1.3e+03,1.5e+03]
##
                       3.3779624
                                                      1.7551040
   priceRpriz (1.5e+03,1.8e+03]
##
                                    priceRpriz (1.8e+03,1e+05]
##
                       1.6894056
                                                      1.2447248
##
     priceRpriz (1e+03,1.3e+03]
                                              savingsRsav (0,2]
                                                      1.7206446
##
                       2.0501524
                                              savingsRsav (4,6]
##
               savingsRsav (2,4]
##
                       2.6775392
                                                      2.4356302
             savingsRsav (6,99]
##
                                                      Homeother
##
                       2.8307267
                                                      2.0177890
##
                       Homeowner
                                                    Homeparents
                       3.0047064
##
                                                      3.9493960
##
                        Homepriv
                                                       Homerent
                                                      2.6288074
##
                       1.7254245
##
                  Maritalmarried
                                              Maritalseparated
##
                       2.0417095
                                                      0.7714918
##
                                                   Maritalwidow
                   Maritalsingle
##
                       1.6291861
                                                      1.0944900
##
                                                   Jobfreelance
                  Recordsyes_rec
##
                       0.1986371
                                                      0.4718103
##
                       Jobothers
                                                     Jobpartime
                       0.6574702
                                                      0.2853673
# re-expressed fitted values
glf$fitted.values = 1 - glf$fitted.values
# create vector for predictions
glfpred = rep(NA, length(glf$fitted.values))
glfpred[glf$fitted.values < 0.5] = 0</pre>
glfpred[glf$fitted.values >= 0.5] = 1
# how is the prediction? (confusion matrix)
table(data$Status[learn], glfpred)
##
         glfpred
##
             0
                   1
```

##

##

bad

400

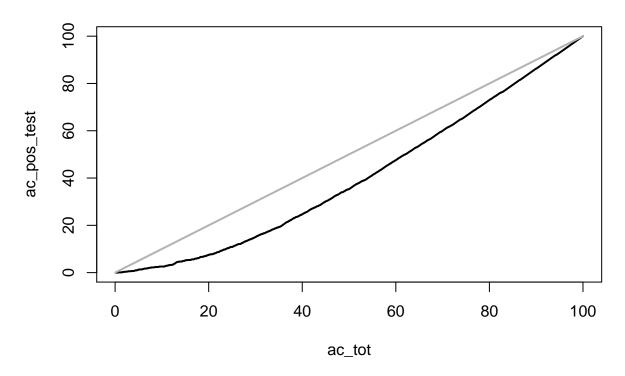
good 1958

432

189

```
# error rate
error_rate.learn = 100*sum(diag(table(data$Status[learn], glfpred))) / nlearn
error rate.learn
## [1] 19.77174
# let's use the test data to get predictions
glft = predict(glf, newdata=data[-learn,])
pt = 1 / (1 + exp(-glft))
pt = 1 - pt
# vector of predicted values
glftpred = rep(NA, length(pt))
glftpred[pt < 0.5] = 0
glftpred[pt >= 0.5] = 1
# confusion matrix
table(data$Status[-learn], glftpred)
##
         glftpred
##
            0 1
##
     bad 201 216
     good 971 79
error_rate.test = 100*sum(diag(table(data$Status[-learn], glftpred))) / ntest
error_rate.test
## [1] 19.08657
Concentration curve
ac_{tot} = 100*(1:ntest) / ntest
pt.ord = order(pt, decreasing=T)
Status_test = data$Status[-learn]
npos = table(Status_test)[2]
ac_pos_test = 100*cumsum(Status_test[pt.ord] == "good") / npos
plot(ac_tot, ac_pos_test, type="1", lwd=2,
    main="Concentration Curve")
lines(ac_tot, ac_tot, col="gray70", lwd=2)
```

## **Concentration Curve**



### ROC Curve

```
nneg = ntest - npos
ac_neg_test = 100*cumsum(Status_test[pt.ord] == "bad") / nneg
plot(ac_neg_test, ac_pos_test, type="l", lwd=2, main="ROC Curve", col="blue")
lines(ac_neg_test, ac_neg_test, col="grey70", lwd=2)
```

# **ROC Curve**

