

# Hashing I : Introduction

Radisson Hotel

5 rooms only

Register

1 Yes

no technology

2 No

3 Yes

4 No

5 No

5 rooms  $\rightarrow$  1000 rooms  $[1, 1000]$

bool room[1001]

$\Rightarrow$  room[i] = true

if  $i^{\text{th}}$  room is occupied

$\Rightarrow$  room[i] = false else

After Pandemic,

1000 room  $\rightarrow [1 - 10^9]$  room no.

bool room  $[10^9 + 1]$

SC =  $O(10^9)$

$\rightarrow$  Issues: huge space wastage

$\rightarrow$  Advantage: TC =  $O(1)$

HashMap : stores  $\langle \text{key}, \text{value} \rangle$  pair

$\langle 10015, \text{occupied} \rangle$   
 $\langle 3, \text{free} \rangle$   
 $\langle 1007, \text{occupied} \rangle$

}  $\rightarrow$  check in 1007?  
 $\rightarrow$  occupied in O(1) TC

TC : O(1) to search

SC : O(N) to store  $\underline{N}$  room entries  
 $\hookrightarrow 1000$  in our ex.

$\text{HashMap} \langle \text{int}, \text{bool} \rangle$

Note : keys are unique  
value can be anything

Quiz 1 Store population of every country

key : country name  $\rightarrow$  string  
value : population  $\rightarrow$  int/long

$\text{HashMap} \langle \text{String}, \text{Long} \rangle$  hm

Quiz No. of states of every country

Key: country name → string

value: # of states → int

HashMap<String, int>

Quiz Name of all states of every country

Key: country name → string

value: all state names → List<String>

C++: vector

java: ArrayList

<India, UP>

<India, MP> X Keys have to be unique

HashMap<String, List<String>> hm

Quiz Population of each state in every country

Key: country name → string

value: population of each state ] → HashMap<String, long>

↑  
state  
name

↑  
population

HashMap<String, HashMap<String, long>> hm

we observe 2 things:

1. value can be anything

2. Key can only be primitive datatype

✓  
int / long / float / double / string / char

HashSet <Key>

→ it only store keys

→ keys have to be unique

→ only be primitive datatype

HashMap functionality

Size: {# keys present}

insert(key, value)

search(key)

delete(key)

update(key, value)

HashSet functionality

size: {# keys present}

insert(key)

search(key) {present or not}

delete(key)

All operations are  $O(1)$

→ Hashing libraries name in diff. languages

Pseudo code	Java	C++	Python	JS	C#
HashMap	HashMap	unordered_map	dict	map	dictionary
HashSet	HashSet	unordered_set	set	set	HashSet

## Question 1

Given  $N$  array elements &  $Q$  queries.

for each query, find the frequency of given element in array.

$a[11] = \{ 2, 6, 3, 8, 2, 8, 2, 3, 8, 10, 6 \}$

$Q = 4$

freq

2

3

8

3

3

2

constraints

$N \leq 10^5$

$Q \leq 10^5$

$(1 \leq a_i) \leq 10^9$

5

0

Bruteforce : for every query, iterate & get count

$$TC = O(Q \times N)$$

$$SC = O(1)$$

not  
feasible

Optimize

Store freq. in hashmap

Key : array element  $\rightarrow$  int

value : freq. of element  $\rightarrow$  int

HashMap < int, int >

{ 2 6 3 8 2 8 2 3 8 10 6 }

<2, 3>

<3, 2>

<6, 2>

<8, 3>

<10, 1>

Code

```
HashMap<int, int> hm
for (i=0 to n-1) {    → N iterations
    if ( hm.search(ai) == true ) {
        // ai is present
        hm[ai] ++      // update +1
    }
    else {
        hm.insert(ai, 1)
    }
}

for ( i=0 to Q-1 ) {    → Q iterations
    if ( hm.search(query[i]) == true ) {
        print( hm[query[i]] )
    }
    else {
        print(0)
    }
}

}
```

$$TC = O(N+Q)$$

$$SC = O(N)$$

## Question 2

Given N elements, find no. of distinct elements.

$a[5] = \{ \overset{\checkmark}{3} \overset{\checkmark}{5} \overset{\checkmark}{6} 5 \overset{\checkmark}{4} \}$        $ans = 4$

Insert everything in hashset & print its size.

Hashset will not  
insert duplicate entries.

code

```
HashSet<int> hs
```

```
for (i=0 to n-1) {
```

```
    hs.insert(a[i])
```

```
}
```

```
print (hs.size)
```

TC:  $O(N)$

SC:  $O(N)$



### Question 3

Given a string  $s$ , find the length of the longest substring without repeating chars.

$s = "abcabcbb"$        $ans = 3$

$s = "bbbb"$        $ans = 1$

Bruteforce      Check all substrings for uniqueness &  
Keep track of max. length.

substrings  $\rightarrow O(N^2)$       # total substrings

for each substring  $\rightarrow O(N)$  (insert everything in  
hashset &

if hashset.size = substring  
size

then unique)

$TC = O(N^3)$

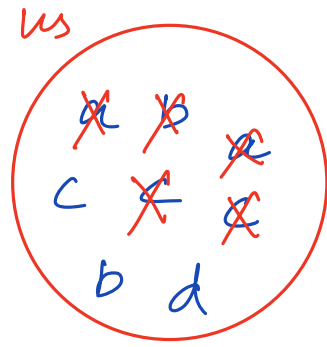
$SC = O(N)$

"a b c a c b d c"

↑ start

↑

ans = 1 2 3 4



Code

```
int longestUniqueSubstring ( s ) {
```

```
    int start = 0
```

```
    int maxLength = 0
```

```
    unordered_set<char> us
```

```
    for ( end = 0 to n-1 ) {
```

```
        while ( us.search ( a[end] ) == true ) {
```

```
            us.delete ( a[start] )
```

```
            start++
```

```
        }
```

```
        us.insert ( a[end] )
```

```
        maxLength = max ( maxLength , end - start + 1 )
```

```
    }
```

TC = O(N)

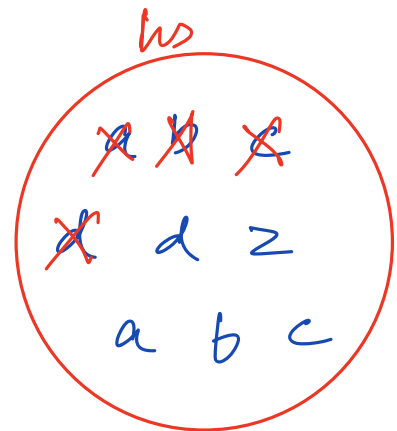
SC = O(N)

or us.size()

return max length

eg a b c d d z a b c  
                    ↑  
                    start

ans = 1 2 3 4 5



TC Analysis

we are inserting every char max 1 time

⇒ total N insertions

⇒ we can only delete total N times

total TC =  $O(N)$

eg "a a a a a a a"  
                    ↑

end = 0

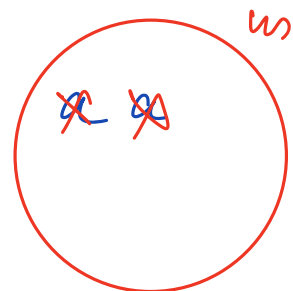
while → 0 times

end = 1

while → 1 time

22

→ 1 times



$n-1$

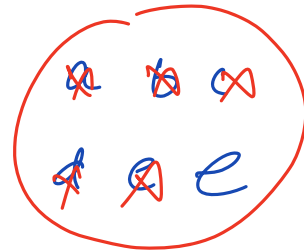
→ 1 time

total N times

eg a b c d e e

↑

us



end=0

while → 0 time

=1

→ 0 time

=2

0

=3

0

=4

0

=5

5 times

total N times

i	j
0	0
1	0
⋮	⋮
N-1	N

(N)