

Trees 4 : LCA + Morris Inorder Traversal

Agenda

- K^{th} smallest element in BST
- Morris inorder traversal
- LCA in binary tree and BST
- Recover BST

Question

Given a BST, find K^{th} smallest element.

We know that, inorder traversal of BST is sorted.

Idea 1: do inorder traversal & store element in array, then return $(K-1)^{\text{th}}$ element.

$$TC = O(N)$$

$$SC = O(N)$$

Idea 2 : instead of storing elements, keep track of count of elements. When counter hits K, return that value.

code

```
count = 0
```

```
ans = INT_MIN
```

```
void inorder ( root , K ) {
```

```
    if (!root) return;
```

```
    inorder ( root->left , K );
```

```
    count++;
```

```
    if (count == K) {
```

```
        ans = root->data;
```

```
        return;
```

```
    }
```

```
    if ( ans == INT_MIN ) {
```

```
        inorder ( root->right , K );
```

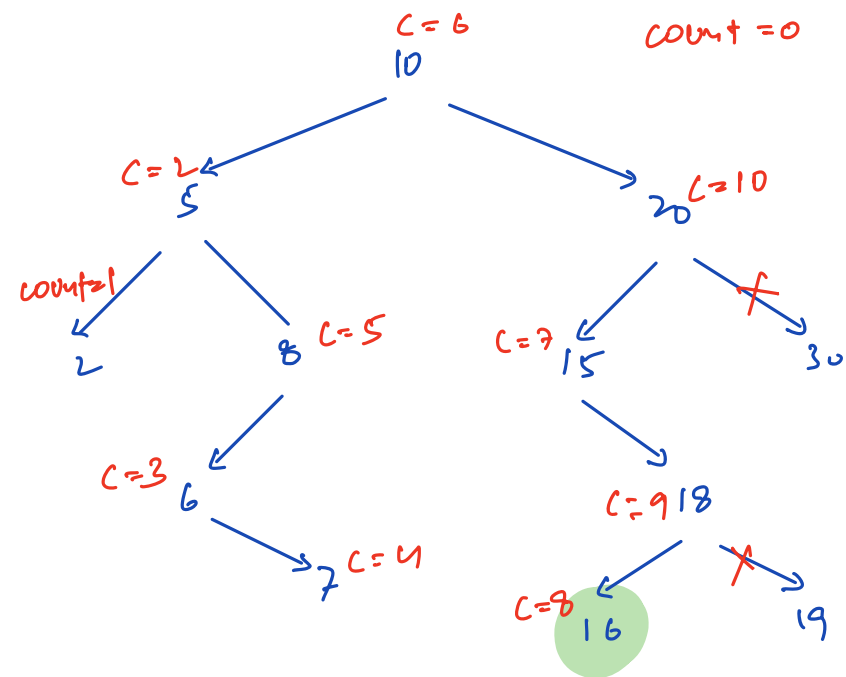
```
    }
```

```
}
```

TC = $O(N)$

SC = $O(\text{height})$

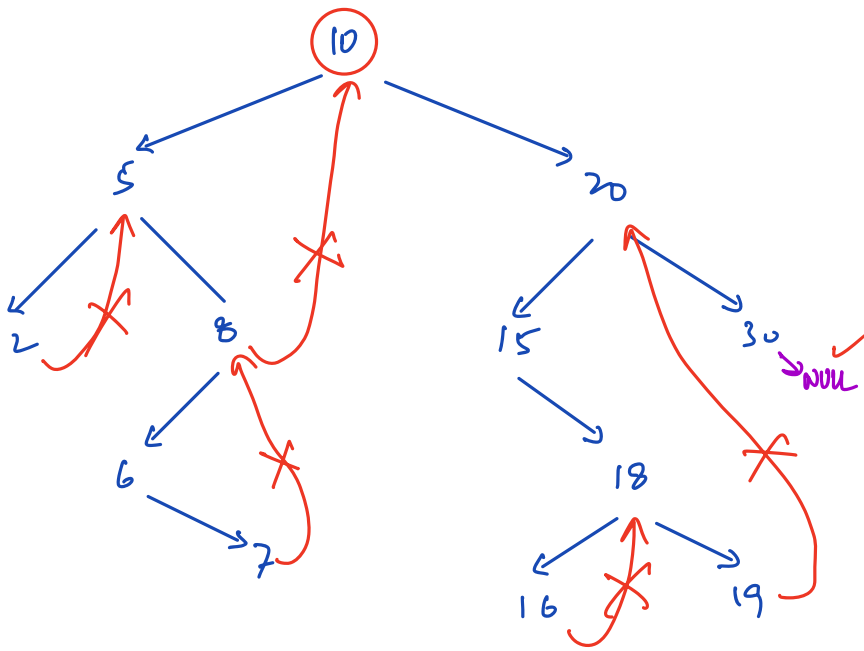
After inorder completes, "ans" will hold K^{th} smallest element in BST.



$K=8$

If I want to achieve $O(1)$ space?

Morris's Inorder Traversal



Where to store current node when we go left?

After which node, the current node is required?

Max element in left subtree

↙ inorder predecessor

right-most element
in left subtree

2 5 6 7 8 10 15 16 18 19 20 30

Code

```
curr = root
```

```
while (curr != null) {
```

```
    if (curr.left == null) {
```

```
        print(curr.data)
```

```
        curr = curr.right
```

```
    }
```

```
    else {
```

```
        pre = curr.left
```

```
while ( pre.right != null && pre.right != curr ) {
```

```
    pre = pre.right
```

```
}
```

```
if ( pre.right == null ) {
```

```
    pre.right = curr // create link
```

```
    curr = curr.left
```

```
}
```

```
else {
```

```
    pre.right = null // remove link
```

```
    print ( curr.data )
```

```
    curr = curr.right
```

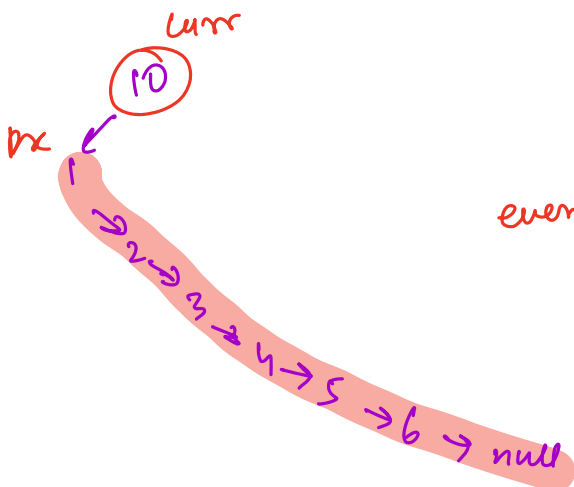
```
}
```

```
}
```

```
}
```

SC = $O(1)$

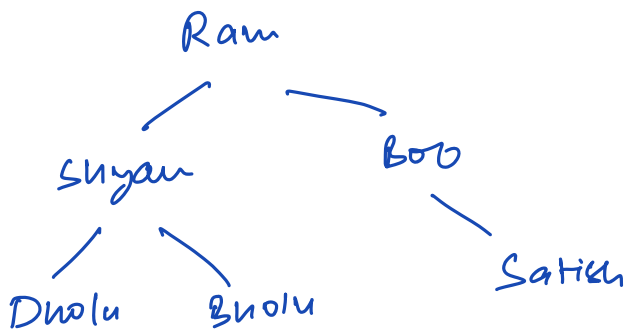
TC = $O(N)$



every node is visited 3 times

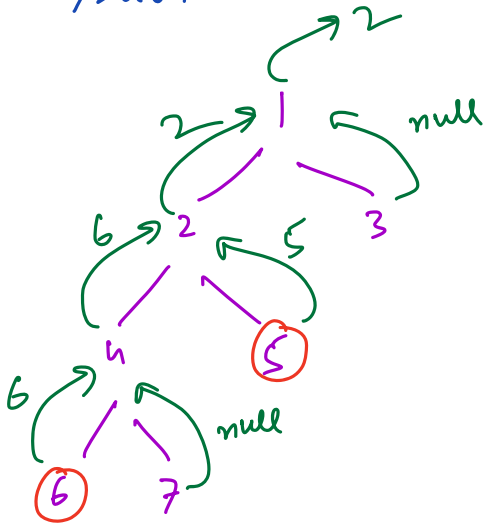
TC = $O(N)$

Common Ancestor



Lowest Common Ancestor (LCA)

LCA of 2 nodes is the deepest node in the tree where the two nodes lie in left & right subtree.



code

```
Node findLCA(root, node1, node2) {
```

```
    if (root == null || root == node1 || root == node2) {
```

```
        return root
```

```
    }
```

```
    leftLCA = findLCA(root.left, node1, node2)
```

```
    rightLCA = findLCA(root.right, node1, node2)
```

```
    if (leftLCA != null && rightLCA != null) {
```

```
        return root // current root is LCA
```

```
    }
```

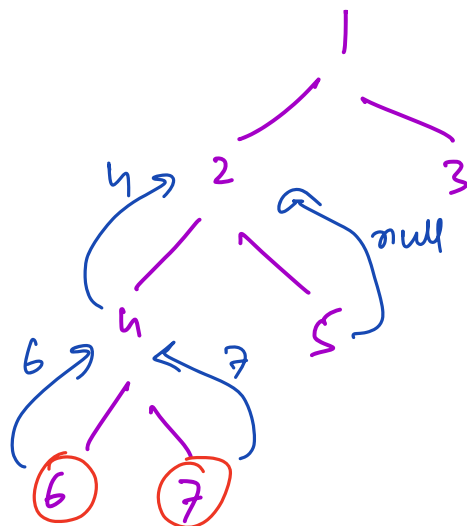
```
    if (leftLCA != null)
```

```
        return leftLCA
```

```
    else
```

```
        return rightLCA
```

```
}
```



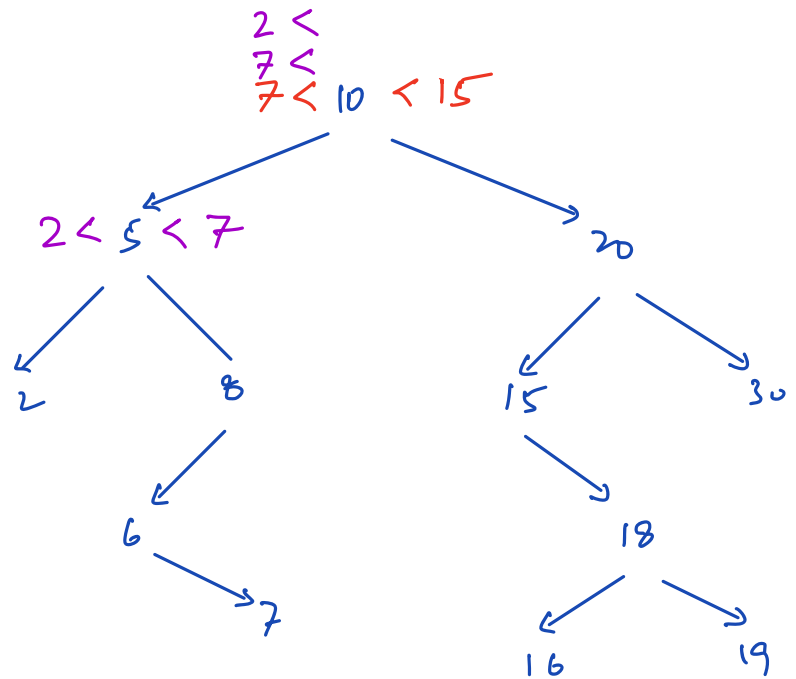
$T.C = O(N)$

$S.C = O(1)$

find LCA in BST

$$\text{LCA}(7, 15) = 10$$

$$\text{LCA}(2, 7) = 5$$



Code

curr = root

while (curr != null) {

if (x < curr.data && y < curr.data) {

curr = curr.left

}

else if (x > curr.data && y > curr.data) {

curr = curr.right

}

else {

return curr;

}

TC = O(h)

SC = O(1)

}

return null

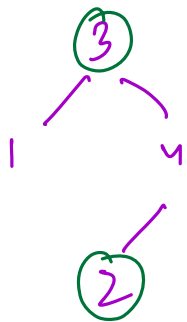
Question

In BST, inorder traversal is sorted.

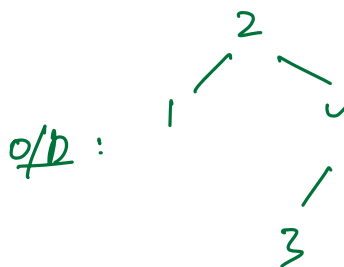
If 2 nodes are swapped by mistake, BST property is violated.

The goal is to recover the BST by swapping 2 misplaced nodes back to their correct position.

eg



inorder: 1 3 2 4

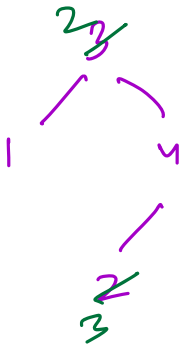


o/p:

→ 1 2 3 4

Idea 1:

1. Do inorder traversal & store the nodes in list
2. Sort the list
3. Perform inorder again & replace node values with the corresponding value in the sorted list.



inorder : 1 3 2 4

↓ sort

1 2 3 4

Code

```
ArrayList<int> vals;
```

```
void inorder (root) {
```

```
    if (!root) return
```

```
    inorder (root->left)
```

```
    vals.push (root->data)
```

```
    inorder (root->right)
```

```
}
```

Sort(vals)

```
void recover( root, index→0 ) {  
    if( !root ) return  
    recover( root->left, index )  
    root->data = vals[index]  
    index++  
    recover( root->right, index )  
}
```

3

$$TC = O(N + N \log N + N) = O(N \log N)$$

\downarrow \downarrow \downarrow
1st sort 2nd
inorder inorder

$$SC = O(H + N) \therefore O(N)$$

\downarrow
storing
data

Optimization

Since there is only 1 swapping happened,
there will be one or two violations in the
inorder sorted order.

Code

Node first = NULL

Node second = NULL

Node prev = NULL

bool a = false

if(a == ~~false~~) \Rightarrow if(!a)

void inorder(root) {

if(!root) return

inorder(root->left)

if(prev && prev->data > root->data) {

if(!first) first = prev

second = root

}

prev = root

inorder(root->right)

}

swap(first->data, second->data)

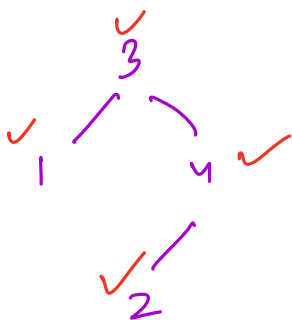
TC = $O(N)$

SC = $O(1)$

$O(1)$
 \downarrow

$O(1)$ using

Morris
inorder



prev = 1 \neq 2

first = 3

second = 2

prev = null 2 5 6 30 8 10 15 16
18 19 20

first = 30
second = 8 7

