

## Trees 5: Problems on trees

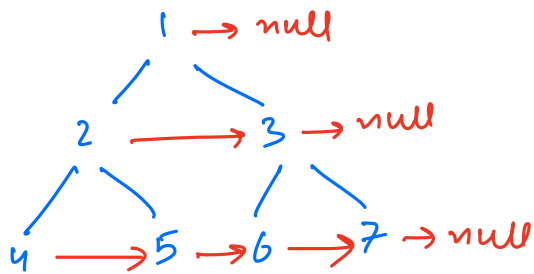
### Question 1

(all levels completely filled)

Given a perfect binary tree with next pointer in

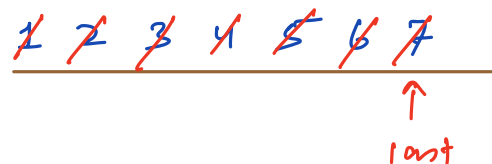
all nodes initially pointing to null.

update the next pointer to point to next node in same level of nodes.



level order traversal

queue



Code

last = root

q.enqueue(root)

while (!q.isEmpty()) {

    x = q.dequeue()

    if (x.left != null) q.enqueue(x.left)

```
if (x.right != null) q.enqueue(x.right)
```

```
if (x != last) {
```

```
    x.next = q.front()
```

```
}
```

```
else {
```

```
    if (!q.isEmpty()) last = q.rear()
```

```
}
```

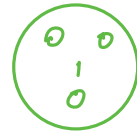
```
}
```

TC =  $O(N)$

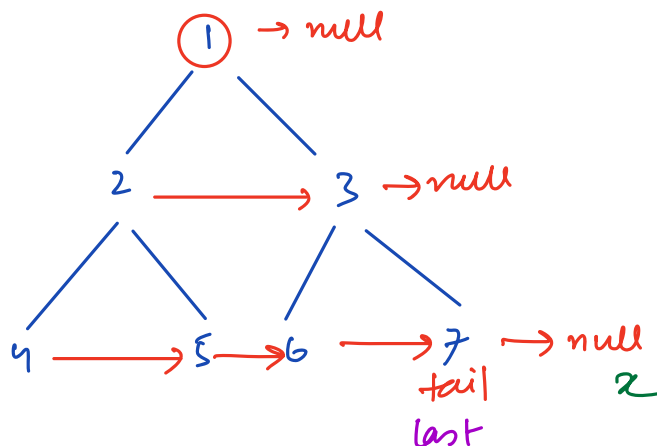
SC =  $O(N)$

~~queue~~ →

OU ?



queue → linked list



Code

tail = root

last = root

x = root

while ( x != null ) {

if ( x.left != null ) {

tail.next = x.left

tail = tail.next

}

if ( x.right != null ) {

tail.next = x.right

tail = tail.next

}

if ( x != last ) x = x.next

else {

x = x.next

last.next = null

last = tail

}

}

TC = O(N)

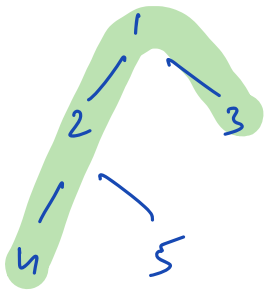
SC = O(1)

## Question 2

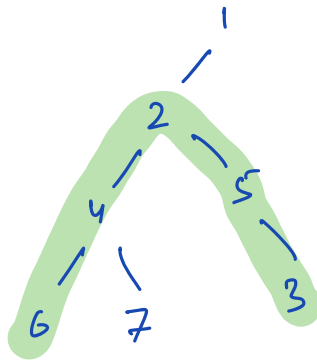
Given a binary tree, find the length of the longest path b/w any 2 nodes in the tree.

The path may or may not pass through the root.

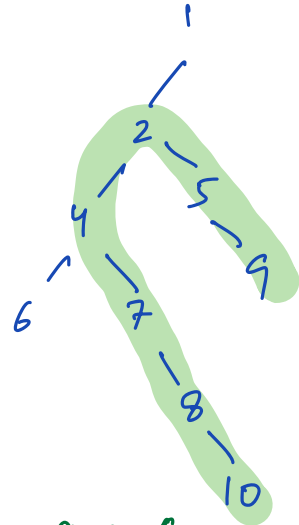
Diameter of binary tree : # edges in the longest path b/w any 2 leaf nodes.



am = 3



am = 4



am = 6

Code

am = 0

```
int height (root) {  
    if (root == null)  
        return 0  
    L = height (root->left)
```

$R = \text{height (root-right)}$

$am = \max(am, L+R)$

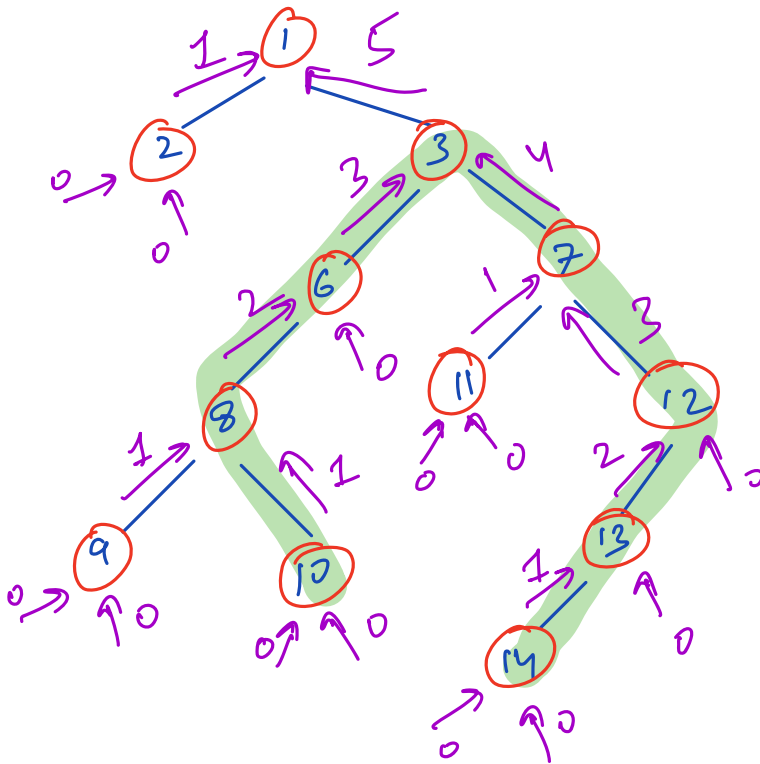
$\text{return } \max(L, R) + 1$

$TC = O(N)$

$SC = O(1)$

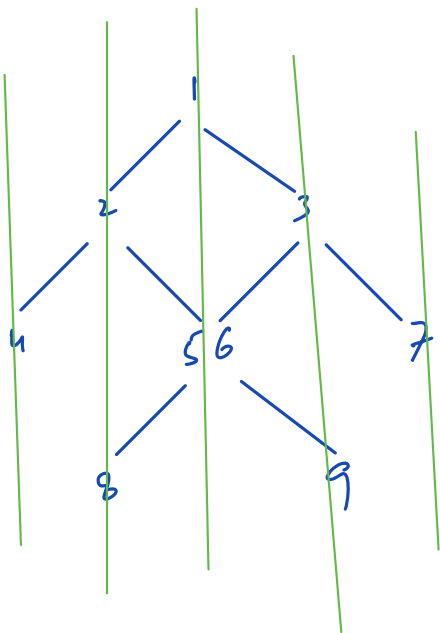
3

$am = 0 \neq 417$

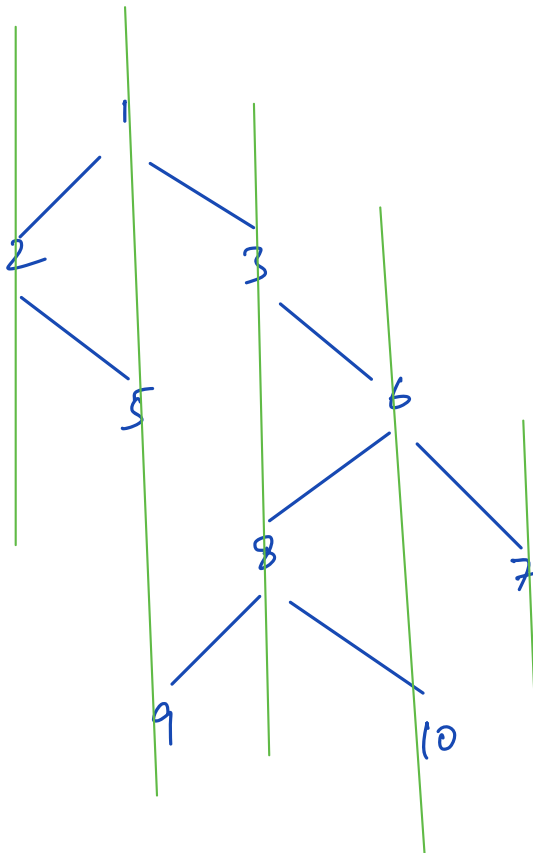


### Question 3

Print vertical order traversal

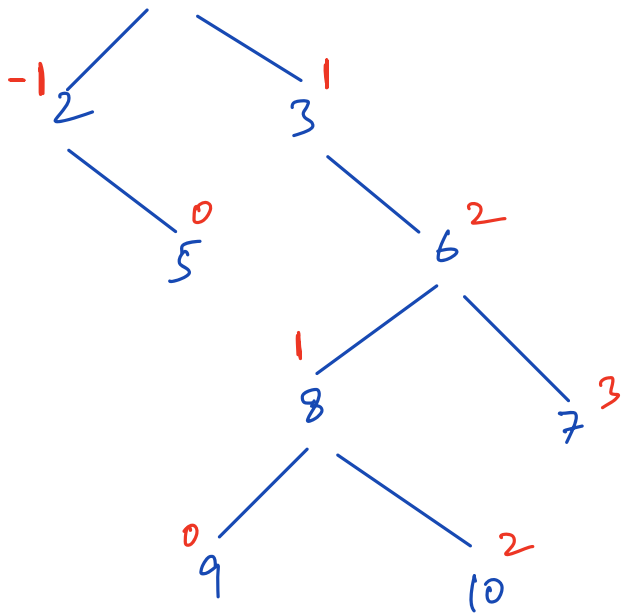


o/p →  
4  
2 8  
1 5 6  
3 9  
7



o/p → 2 1 5 9 3 8  
6 10 7

horizontal  
distance 0



Create hashmap with

key  $\rightarrow$  horizontal distance

value  $\rightarrow$  list of nodes

code

```
HashMap<int, list<int>> hm
```

```
Queue<pair<Node, int>> q;
```

```
q.enqueue(<root, 0>);
```

```
mind = 0, maxd = 0
```

```
while(! q.isEmpty()) {
```

```
    x, d = q.dequeue();
```

```
    mind = min(mind, d)
```

```
    maxd = max(maxd, d)
```

```
    hm[d].add(x.data)
```

```
if (x.left != null) {
```

```
    q.enqueue(<x.left, d+1>)
```

```
}
```

```
if (x.right != null) {
```

```
    q.enqueue(<x.right, d+1>)
```

```
}
```

```
}
```

```
for (i = mind to maxd) {
```

```
    for (val in hm[i])
```

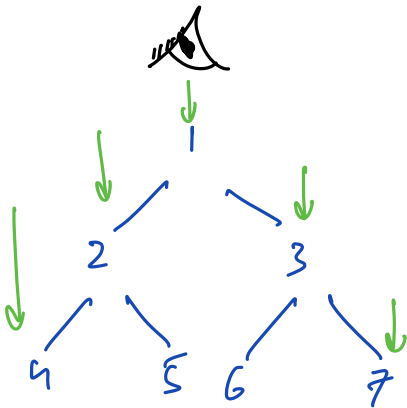
```
        print(val)
```

```
}
```

TC =  $O(N)$

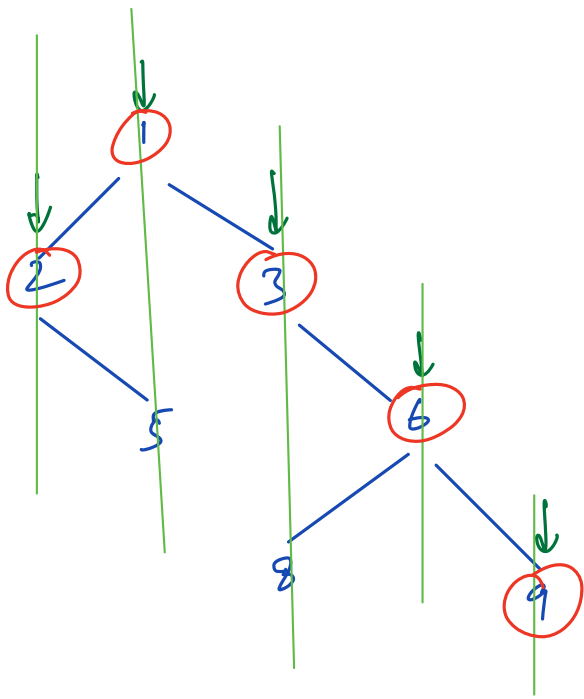
SC =  $O(N)$

Question 4 Print top view



o/p: 4 2 1 3 7





o/p : 2 1 3 6 9

Observation : first element of each vertical in the vertical order traversal is answer.

code

```

HashMap < int, int > hm
Queue < pair < Node, int > > q;
q.enqueue(< root, 0 >);
mind = 0 , maxd = 0
while( ! q.isEmpty() ) {
    x, d = q.dequeue()
    mind = min(mind, d)
    maxd = max(maxd, d)
}

```

```
if (!hm.containsKey(d)) {
```

```
    hm[d] = x.data  
}
```

```
if (x.left != null) {
```

```
    q.enqueue(<x.left, d-1>)
```

```
}
```

```
if (x.right != null) {
```

```
    q.enqueue(<x.right, d+1>)
```

```
}
```

```
for (i = mind to maxd) {
```

```
    print(hm[i])
```

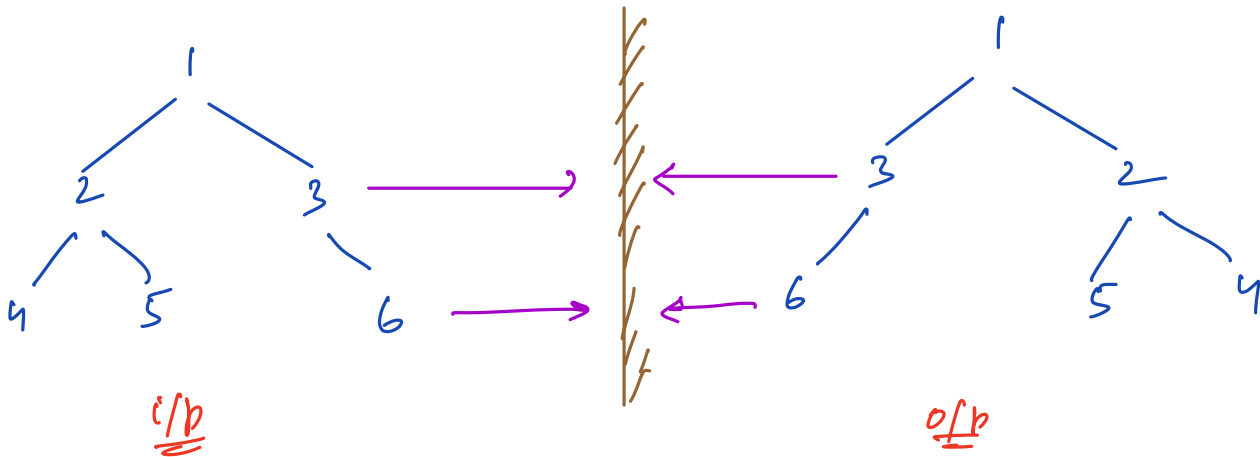
```
}
```

$TC = O(N)$

$SC = O(N)$

## Question 5

Invert the given binary tree



Solution : if nodes, swap left & right child

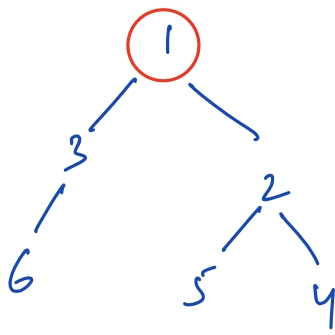
## Code

```
Node invert(root) {  
    if(!root) return null  
    inverted-left = invert(root-right)  
    inverted-right = invert(root-left)  
    root-left = inverted-right  
    root-right = inverted-left  
    return root  
}
```

}

TC =  $O(N)$

SC =  $O(1)$



X  $\left\{ \begin{array}{l} \text{root.left} = \text{invert}(\text{root.right}) \\ \text{root.right} = \text{invert}(\text{root.left}) \end{array} \right.$

✓  $\left\{ \begin{array}{l} \text{temp} = \text{invert}(\text{root.right}) \\ \text{root.right} = \text{invert}(\text{root.left}) \\ \text{root.left} = \text{temp} \end{array} \right.$