Question 1. Show that the unit direction vector inclined equally to the coordi-

nate axes is
$$\begin{pmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{pmatrix}$$

Solution: Let **a** be the given unit vector such that $\mathbf{a} = (\mathbf{a}_x, \mathbf{a}_y, \mathbf{a}_z)$. The direction cosines of **a** are given as:

$$\cos \alpha = \frac{\mathbf{a}_x}{|a|}, \qquad \cos \beta = \frac{\mathbf{a}_y}{|a|} \qquad and \qquad \cos \gamma = \frac{\mathbf{a}_z}{|a|}$$
 (1)

As **a** is a unit vector, so |a| = 1 and also we are given is that **a** is inclined equally to the coordinate axis, thus we have by (1)

$$\cos \alpha = \cos \beta = \cos \gamma = \mathbf{a}_x = \mathbf{a}_y = \mathbf{a}_z \tag{2}$$

Using, (2) and

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$
$$3\cos^2 \alpha = 1$$
$$\cos \alpha = -\frac{1}{\sqrt{3}}$$

Thus, taking positive sign in above, we get

$$\mathbf{a}_x = \frac{1}{\sqrt{3}}, \quad \mathbf{a}_y = \frac{1}{\sqrt{3}} \quad and \quad \mathbf{a}_z = \frac{1}{\sqrt{3}}$$
 (3)

Thus, by (3) we have proved that the unit direction vector inclined equally to the coordinate axes is $\begin{pmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$.